SCIENTIFIC REPORTS

OPEN

Chemical Partition of the Radiative Decay Rate of Luminescence of Europium Complexes

Nathalia B. D. Lima¹, José Diogo L. Dutra^{1,2}, Simone M. C. Gonçalves¹, Ricardo O. Freire² & Alfredo M. Simas¹

Received: 04 November 2015

Accepted: 15 January 2016

Published: 19 February 2016

The spontaneous emission coefficient, A_{rad} , a global molecular property, is one of the most important quantities related to the luminescence of complexes of lanthanide ions. In this work, by suitable algebraic transformations of the matrices involved, we introduce a partition that allows us to compute, for the first time, the individual effects of each ligand on A_{rad} , a property of the molecule as a whole. Such a chemical partition thus opens possibilities for the comprehension of the role of each of the ligands and their interactions on the luminescence of europium coordination compounds. As an example, we applied the chemical partition to the case of repeating non-ionic ligand ternary complexes of europium(III) with DBM, TTA, and BTFA, showing that it allowed us to correctly order, in an *a priori* manner, the non-obvious pair combinations of non-ionic ligands that led to mixed-ligand compounds with larger values of A_{rad} .

Almost 40 years ago, systems containing lanthanide ions started attracting the interest of many research groups around the world^{1,2} due to their very peculiar luminescence properties. Such properties make these ions, such as trivalent europium, essential for the development of photo and electroluminescent devices^{3,4}. Since intra-ion f-f transitions are Laporte forbidden, the light absorption capability of the lanthanide ions is poor and therefore luminescence cannot be generated from direct excitation. However, when the lanthanide ion is surrounded by coordinating ligands who can effectively absorb radiation and subsequently transfer the energy, in an intramolecular manner, to the coordinated lanthanide ion – a process known as the antenna effect⁵ – then something entirely different happens. Asymmetries in the ligand field, asymmetries due to different spatial arrangement of the ligands around the lanthanide ion, asymmetries due to mixed ligands coordination⁶, asymmetries due to thermal vibrations, etc, all make the intra-ion f-f decay less forbidden, and, as a result, strong luminescence ensues. Nevertheless, this strong luminescence is still a result of an almost forbidden intra-ion f-f transition, which therefore both exhibits long lifetimes and high color purity. Indeed, the exhibited luminescence is essentially monochromatic. Moreover, since the lanthanide trication 4f orbitals belong to an inner shell which is shielded by the outer 5s²5p⁶ shell, this luminescence displays a high degree of insensitivity to environmental quenching, and is of value for applications in sensors⁷, displays³, fluoroimmunoassays⁸, fluorescence microscopy⁹, etc.

The rapid technological development of the last decades^{10,11} has contributed to escalating the interest in lanthanide complexes. So much so, that, currently, there are about one thousand articles published every year on the subject¹². However, less than 5% of the studies involving lanthanide ions make use of theoretical tools¹². Even though, it is possible to verify an increase in the use of theoretical tools assisting the experimental studies in their quest to design increasingly more efficient luminescent systems^{13–16}. Hence, the extant theoretical tools and techniques are slowly becoming increasingly popular, such as the Sparkle Models^{17–21} and RM1 for lanthanides^{22–25}, which are fully available in the MOPAC software²⁶, as well as the new lanthanide luminescence software package LUMPAC (www.lumpac.pro.br)¹², the first and only software dedicated to the study of the luminescence properties of systems containing europium ions.

Recently, we showed that the charge factors of the simple overlap model and the polarizabilities of Judd-Ofelt theory can be uniquely modeled by perturbation theory on the semiempirical electronic wavefunction of the complex²⁷. Consequently, the terms of the intensity parameters related to dynamic coupling and electric dipole mechanisms are made unique, leading to a unique set of intensity parameters per complex.

¹Departamento de Química Fundamental, CCEN, UFPE, 50590-470, Recife, PE, Brazil. ²Pople Computational Chemistry Laboratory, Departamento de Química, CCET, UFS, 49100-000, São Cristóvão, SE, Brazil. Correspondence and requests for materials should be addressed to A.M.S. (email: simas@ufpe.br)

Luminescence of europium complexes is a phenomenon entirely dependent on the chemical nature of the ligands and on the fine details of their geometric arrangements, as they are coordinated to the central metal ion. Nevertheless, luminescence is still a property of the complex as a whole. Hence, the emission spectrum of the complex conceals a profusion of ligand contributions to the luminescence phenomenon. For example, by examining the luminescence properties, it is not always entirely clear which ligand should replace another, in a given compound, in order to design a novel and more luminescent complex.

In the present article, we are advancing a novel formalism for a partition of the radiative decay rate of luminescence of europium complexes into ligand contributions. Such a chemical partition scheme is shown to be general, and applicable to any europium complex. Finally, we exemplify the usage of this novel chemical partition for the choice of the best couple of non-ionic ligands for the design of mixed ligand complexes with boosted luminescence.

Intensity parameters from experiment

Luminescence in europium complexes is a process by which ultraviolet light is converted into visible light, mostly in the red-orange region of the spectrum. The first step of this light conversion is the absorption of the ultra-violet light by high-absorbance ligands. Then, the absorbed energy is transferred to the central trivalent europium ion that, as a result, is placed in its 5D_0 excited state. From that excited state, two types of processes occur: radiative decays to the low-lying 7F_J states and nonradiative decays to the ground state. This final step of the luminescence phenomenon is expressed mathematically in terms of the emission efficiency $\eta = A_{\text{rad}}/(A_{\text{rad}} + A_{\text{nr}})$, where A_{rad} and A_{nr} are, respectively, the radiative and nonradiative total decay rates.

The radiative decay rate A_{rad} is the sum of all radiative decay rates from the 5D_0 excited state to each of the 7F_J states, with $J = 0, 1, 2, 3, 4, 5, 6$, whereas the non-radiative rate, A_{nr} , is actually a bundle of non-radiative processes. Since we are not interested in non-radiative decays, there is no need to identify any of their terms.

The experimental radiative decay rate, $A_{\text{rad}}^{\text{exp}}$, is the sum of the radiative decay rates of each of the possible transitions $^5D_0 \rightarrow ^7F_J$ with J ranging from 0–6:

$$A_{\text{rad}}^{\text{exp}} = \sum_{J=0}^6 A_{\text{rad}}^{\text{exp}} [^5D_0 \rightarrow ^7F_J] \quad (1)$$

The transition $^5D_0 \rightarrow ^7F_J$ is governed by a magnetic dipole mechanism and is therefore insensitive to electric dipole contributions. This transition is thus regarded as insensitive to the essentially static electric fields produced by the ligands and can be determined through the expression²⁸ $A_{\text{rad}}^{\text{exp}} [^5D_0 \rightarrow ^7F_J] = (0.31 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}) n^3 \nu [^5D_0 \rightarrow ^7F_J]^3$, where n is the refractive index of the medium, and $\nu [^5D_0 \rightarrow ^7F_J]$ is the barycenter, the weighted mean of the frequencies in cm^{-1} , corresponding to the $^5D_0 \rightarrow ^7F_J$ transition. From this value, we can now compute the other radiative decay rates, with J from 0–6:

$$A_{\text{rad}}^{\text{exp}} [^5D_0 \rightarrow ^7F_J] = \frac{\nu [^5D_0 \rightarrow ^7F_J] S [^5D_0 \rightarrow ^7F_J]}{\nu [^5D_0 \rightarrow ^7F_J] S [^5D_0 \rightarrow ^7F_J]} A_{\text{rad}}^{\text{exp}} [^5D_0 \rightarrow ^7F_J] \quad (2)$$

where $\nu [^5D_0 \rightarrow ^7F_J]$ are the energies of the barycenters of the respective transitions; and $S [^5D_0 \rightarrow ^7F_J]$ are the areas under the spectra corresponding to the respective transitions. Finally, the experimental intensity parameters can be calculated from²⁸:

$$\Omega_{\lambda}^{\text{exp}} = \frac{3\hbar A_{\text{rad}}^{\text{exp}} [^5D_0 \rightarrow ^7F_J]}{32e^2\pi^3\chi\nu [^5D_0 \rightarrow ^7F_J]^3 |\langle ^5D_0 || U^{(\lambda)} || ^7F_J \rangle|^2} \quad (3)$$

where $\hbar$ is Planck-Dirac constant, e is the fundamental electric charge, $\nu [^5D_0 \rightarrow ^7F_J]$ is the frequency of the transition in wavenumbers, χ is the Lorentz local-field correction term given by $\chi = n(n^2 + 2)^2/9$, and $|\langle ^5D_0 || U^{(\lambda)} || ^7F_J \rangle|^2$ are the square reduced matrix elements whose values are 0.0032, 0.0023, and 0.0002 for $\lambda = 2, 4$, and 6, and $J = \lambda$ in the case of europium²⁹.

Another way of obtaining the $\Omega_{\lambda}^{\text{exp}}$ is from absorption spectra³⁰. In such a procedure, the $\Omega_{\lambda}^{\text{exp}}$ are obtained by parameterization so that the calculated oscillator strengths match the experimental ones from the absorption spectra, and the parameterization error propagates to the intensity parameters. Besides, further errors may derive from uncertainties in the choice of theoretical transitions to relate to the experimental ones. Indeed, when Judd-Ofelt parameters are estimated from absorption spectra in this manner, errors are of the order of 10–20%³⁰ and that is why, in this article, we chose to evaluate them from emission spectra instead.

Theoretical intensity parameters

The theoretical radiative decay rate for the forced electric dipole and magnetic dipole governed transitions, $A_{\text{rad}}^{\text{ed,md}}$, is given by $A_{\text{rad}}^{\text{ed,md}} = A_{\text{rad}}^{\text{ed}} + A_{\text{rad}}^{\text{md}}$, where, for europium,

$$A_{\text{rad}}^{\text{ed}} = \frac{32e^2\pi^3\chi}{3\hbar(2J+1)} \sum_{\lambda=2,4,6} \nu [^5D_0 \rightarrow ^7F_{J=\lambda}]^3 \Omega_{\lambda} |\langle ^5D_0 || U^{(\lambda)} || ^7F_{J=\lambda} \rangle|^2 \quad (4)$$

and $A_{\text{rad}}^{\text{md}}$ is equal to

$$A_{rad}^{md} = \frac{32\pi^3 n^3 \nu [{}^5D_0 \rightarrow {}^7F_1]^3}{3\hbar} S_{md} \quad (5)$$

where e is the elementary charge; $2J + 1$ is the degeneracy of the initial state, in this case 5D_0 , and therefore $J = 0$. Transitions ${}^5D_0 \rightarrow {}^7F_1$ with $J = 0, 3$, and 5 depend on contributions from both electric and magnetic dipole mechanisms and thus are not as easy to calculate. Fortunately, their intensities are very low and, thus, they can be safely disregarded. Transition ${}^5D_0 \rightarrow {}^7F_1$ is the only one which does not have an electric dipole contribution, therefore, is not sensitive to the presence of the ligands around the europium ion, and is relatively small: its magnetic dipole strength is theoretically evaluated as being $S_{md} = 96 \times 10^{-42} \text{ esu}^2 \text{ cm}^2$ ³¹. Therefore, for the purpose of this work, we define $A_{rad}^{ed} = A_{rad}^{ed} \cong A_{rad}^{ed,md}$, restricted to the chemically interesting transitions ${}^5D_0 \rightarrow {}^7F_1$ with $J = 2, 4$, and 6 . Their corresponding theoretical intensity parameters Ω_λ ($\lambda = 2, 4, 6$) emerge from the Judd-Ofelt theory^{32,33}, depend on the coordination interaction between the lanthanide cation and the ligands, and are given by the following expression:

$$\Omega_\lambda = (2\lambda + 1) \sum_{t=\lambda-1}^{\lambda+1} \sum_{p=-t}^t \frac{|B_{\lambda,t,p}|^2}{(2t + 1)} \quad (6)$$

The $B_{\lambda,t,p}$ terms in eq. (6) are given by the following expression:

$$B_{\lambda,t,p} = B_{\lambda,t,p}^{ed} + B_{\lambda,t,p}^{dc} \quad (7)$$

where $B_{\lambda,t,p}^{ed}$ corresponds to the forced electric dipole contribution and $B_{\lambda,t,p}^{dc}$ corresponds to the dynamic coupling contribution, respectively given by:

$$B_{\lambda,t,p}^{ed} = \frac{2}{\Delta E} \langle r^{t+1} \rangle \theta(t, \lambda) \gamma_p^t \quad (8)$$

$$B_{\lambda,t,p}^{dc} = - \left[\frac{(\lambda + 1)(2\lambda + 3)}{2\lambda + 1} \right]^{\frac{1}{2}} \langle r^\lambda \rangle (1 - \sigma_\lambda) \langle f \| C^{(\lambda)} \| f \rangle \Gamma_p^t \delta_{t,\lambda+1} \quad (9)$$

where ΔE is a constant, approximately given by the energy difference between the barycenters of the ground $4f^N$ and first opposite parity excited state of configuration $4f^{(N-1)}5d$ of the europium ion; $\langle r^2 \rangle = 2.567541 \times 10^{-17} \text{ cm}^2$ and $\langle r^4 \rangle = 1.58188 \times 10^{-33} \text{ cm}^4$ are radial integrals, pre-defined for the europium ion³⁴; $\theta(t, \lambda)$ are numerical factors for a given lanthanide, estimated by Malta *et al.*³⁵ from Hartree-Fock calculations of the radial integrals as being: $\theta(1,2) = -0.17$; $\theta(3,2) = 0.345$; $\theta(3,4) = 0.18$, $\theta(5,4) = -0.24$, $\theta(5,6) = -0.24$, $\theta(7,6) = 0.24$; γ_p^t are the odd-rank ligand field parameters; $(1 - \sigma_\lambda)$ is a shielding factor due to the filled $5s$ and $5p$ sub-shells of the lanthanide ion³⁵, with σ_2 , σ_4 , and σ_6 being, respectively, 0.6 , 0.139 , and 0.100 for Eu(III) , as previously calculated by Malta and Silva³⁶; $\langle f \| C^{(\lambda)} \| f \rangle$ is a Racah tensor operator of rank λ whose values for $\lambda = 2, 4, 6$, are -1.3660 , 1.128 , and -1.270 , respectively, for any lanthanide; Γ_p^t is also a sum over coordinating atoms which further reflects the chemical environment; finally, $\delta_{t,\lambda+1}$ is a Kronecker delta symbol. All these pre-defined parameters are taken as constants for all europium complexes.

The odd rank ligand field parameters are, in turn, given by:

$$\gamma_p^t = \left(\frac{4\pi}{2t + 1} \right)^{\frac{1}{2}} e^2 \sum_i \rho_i (2\beta_i)^{t+1} \frac{g_i}{R_i^{t+1}} Y_p^{t*}(\theta_i, \phi_i) \quad (10)$$

where the term $\rho_i (2\beta_i)^{t+1}$, according to the Simple Overlap Model (SOM)^{37,38}, introduces a correction to the crystal field parameters of the point charge electrostatic model (PCEM)³⁹, $\gamma_p^t(\text{PCEM})$, such that $\gamma_{p,i}^t(\text{SOM}) = \rho_i (2\beta_i)^{t+1} \gamma_{p,i}^t(\text{PCEM})$, which confers a degree of covalency to the point charge model through the inclusion of parameter ρ , since PCEM only treats the metal-ligand atom bonds as a purely electrostatic phenomenon; g_i is the charge factor associated to the lanthanide-ligand atom bond; R_i is the lanthanide-ligand atom bond distance; and $Y_i^{t*}(\theta_i, \phi_i)$ are complex conjugate spherical harmonics.

The other odd-rank parameter Γ_p^t , which further reflects the chemical environment is given by:

$$\Gamma_p^t = \left(\frac{4\pi}{2t + 1} \right)^{\frac{1}{2}} \sum_i \frac{\alpha_i}{R_i^{t+1}} Y_p^{t*}(\theta_i, \phi_i) \quad (11)$$

where α_i is the polarizability associated to the lanthanide-ligand atom bond.

In a recent article²⁷, we introduced a protocol to model the charge factors g_i of the simple overlap model by electron densities, and the polarizabilities α_i of Judd-Ofelt theory by superdelocalizabilities, all obtained by perturbation theory on the semiempirical electronic wavefunction of the complex. A fitting of the theoretical intensity parameters Ω_λ is then carried out, which reproduces the experimentally obtained $\Omega_\lambda^{\text{exp}}$ using only three adjustable constants: Q , D , and C , which must obey the acceptance criterion $D/C > 1$ leading to a unique adjustment. Whenever $D/C \leq 1$, it was shown that the presumed geometry of the coordination polyhedron is not

seemingly compatible with the experimental intensity parameters and requires improvement, either via calculation by another theoretical model, such as another Sparkle Model^{17–21} or RM1 model for lanthanides²², or via X-ray crystallographic measurements, etc. The importance of this previous work is that all derived quantities become also uniquely determined for a given complex geometry²⁷, including the chemical partition that is being advanced in this article.

Results and Discussion

Partitioning A_{rad} into ligand terms. According to the theory, $A_{\text{rad}} = A_{\text{rad}}^{\text{ed}} + A_{\text{rad}}^{\text{md}}$. The first term, $A_{\text{rad}}^{\text{ed}}$, with even J , is mainly driven by electric dipole transitions. The second term, $A_{\text{rad}}^{\text{md}}$, with odd J , is mainly driven by magnetic dipole transitions. Besides, recall that the strengths of the transitions $^5D_0 \rightarrow ^7F_J$ with $J = 0, 3$, and 5 are set at zero because of their low values. Likewise, the magnetic dipole driven transition $^5D_0 \rightarrow ^7F_1$ is not sensitive to the ligands and, as a result, is not directly relevant from a chemical point of view. Therefore, the partition will focus on the electric dipole driven transitions with $J = 2, 4, 6$. Accordingly, we will partition a subset of A_{rad} , we call $A_{\text{rad}}^{\text{exp}}$, defined by:

$$A_{\text{rad}}^{\text{exp}} = \sum_{J=2,4,6} A_{\text{rad}}^{\text{exp}} [^5D_0 \rightarrow ^7F_J] \quad (12)$$

the most significant term being the decay rate of the so-called hypersensitive transition $^5D_0 \rightarrow ^7F_2$, which is highly susceptible to the presence of the ligands.

Now, let us turn to compute the $B_{\lambda,t,p}$ terms from eqs (8–11).

$$\begin{aligned} B_{\lambda,t,p} = & \frac{2}{\Delta E} \langle r^{t+1} \rangle \theta(t, \lambda) \left(\frac{4\pi}{2t+1} \right)^{\frac{1}{2}} e^2 \sum_i \rho_i (2\beta_i)^{t+1} \frac{g_i}{R_i^{t+1}} Y_p^{t*}(\theta_i, \phi_i) \\ & - \left[\frac{(\lambda+1)(2\lambda+3)}{2\lambda+1} \right]^{\frac{1}{2}} \langle r^\lambda \rangle (1 - \sigma_\lambda) \langle f \| C^{(\lambda)} \| f \rangle \\ & \times \left(\frac{4\pi}{2t+1} \right)^{\frac{1}{2}} \sum_i \frac{\alpha_i}{R_i^{t+1}} Y_p^{t*}(\theta_i, \phi_i) \delta_{t,\lambda+1} \end{aligned} \quad (13)$$

which can be rewritten as,

$$\begin{aligned} B_{\lambda,t,p} = & \sum_i \left(\frac{4\pi}{2t+1} \right)^{\frac{1}{2}} \left\{ \frac{2}{\Delta E} \langle r^{t+1} \rangle \theta(t, \lambda) e^2 \rho_i (2\beta_i)^{t+1} \frac{g_i}{R_i^{t+1}} \right. \\ & \left. - \left[\frac{(\lambda+1)(2\lambda+3)}{2\lambda+1} \right]^{\frac{1}{2}} \langle r^\lambda \rangle (1 - \sigma_\lambda) \langle f \| C^{(\lambda)} \| f \rangle \frac{\alpha_i}{R_i^{t+1}} \delta_{t,\lambda+1} \right\} Y_p^{t*}(\theta_i, \phi_i) \end{aligned} \quad (14)$$

Accordingly, $B_{\lambda,t,p}$ are obtained by sums over all coordinating atoms of the ligands of the product of a term, $K_{\lambda,t,p}(i)$, defined below, which depends only on the lanthanide ion and on the particular coordinating bond as previously described, with a complex conjugate spherical harmonic.

$$\begin{aligned} K_{\lambda,t,p}(i) = & \left(\frac{4\pi}{2t+1} \right)^{\frac{1}{2}} \left\{ \frac{2}{\Delta E} \langle r^{t+1} \rangle \theta(t, \lambda) e^2 \rho_i (2\beta_i)^{t+1} \frac{g_i}{R_i^{t+1}} \right. \\ & \left. - \left[\frac{(\lambda+1)(2\lambda+3)}{2\lambda+1} \right]^{\frac{1}{2}} \langle r^\lambda \rangle (1 - \sigma_\lambda) \langle f \| C^{(\lambda)} \| f \rangle \frac{\alpha_i}{R_i^{t+1}} \delta_{t,\lambda+1} \right\} \end{aligned} \quad (15)$$

Therefore,

$$B_{\lambda,t,p} = \sum_i K_{\lambda,t,p}(i) Y_p^{t*}(\theta_i, \phi_i) \quad (16)$$

and we can define an auxiliary matrix, $Q_{\lambda,t,p}(i, i')$, which is a function of only the coordinating atoms of the complex as

$$Q_{\lambda,t,p}(i, i') = K_{\lambda,t,p}(i) Y_p^{t*}(\theta_i, \phi_i) K_{\lambda,t,p}(i') Y_p^t(\theta_{i'}, \phi_{i'}) \quad (17)$$

Note that all diagonal elements $Q_{\lambda,t,p}(i, i) \geq 0$. Besides, $Q_{\lambda,t,p}(i, i')$ is an Hermitian matrix because $Q_{\lambda,t,p}(i, i') = Q_{\lambda,t,p}(i', i)^*$. Therefore, its eigenvalues are all real numbers. Moreover, we will show that $Q_{\lambda,t,p}(i, i')$ is a positive semi-definite matrix and therefore all its eigenvalues are, not only real, but also equal to or greater

than zero. Q is said to be positive semi-definite if $t^T Q t$ is non-negative for every non-zero column vector t of n real numbers. Here t^T denotes the transpose of t .

As such,

$$t^T Q t = \sum_{i,j} t_i t_j Q_{i,j} \quad (18)$$

Replacing Q by its expression,

$$\begin{aligned} t^T Q t &= \sum_{i,j} [t_i K_{\lambda,t,p}(i) Y_p^t(\theta_i, \varphi_i)] [t_j K_{\lambda,t,p}(j) Y_p^{t*}(\theta_j, \varphi_j)] \\ &= \sum_{i,j} [t_i K_{\lambda,t,p}(i) Y_p^t(\theta_i, \varphi_i)] [t_j K_{\lambda,t,p}(j) Y_p^t(\theta_j, \varphi_j)]^* \\ &= \left(\sum_i t_i K_{\lambda,t,p}(i) Y_p^t(\theta_i, \varphi_i) \right) \left(\sum_j t_j K_{\lambda,t,p}(j) Y_p^{t*}(\theta_j, \varphi_j) \right) \\ &= \left(\sum_i t_i K_{\lambda,t,p}(i) Y_p^t(\theta_i, \varphi_i) \right) \left(\sum_j t_j K_{\lambda,t,p}(j) Y_p^t(\theta_j, \varphi_j) \right)^* \\ &= \left| \sum_i t_i K_{\lambda,t,p}(i) Y_p^t(\theta_i, \varphi_i) \right|^2 \geq 0 \end{aligned} \quad (19)$$

That is, $t^T Q t \geq 0$. Therefore, Q is positive semi-definite.

The $B_{\lambda,t,p}$ terms of eq. (16) can now be computed in terms of the directly coordinating atoms as:

$$|B_{\lambda,t,p}|^2 = \sum_i \sum_{i'} Q_{\lambda,t,p}(i, i') \quad (20)$$

then,

$$\begin{aligned} \Omega_\lambda &= (2\lambda + 1) \sum_{t=\lambda-1}^{\lambda+1} \sum_{p=-t}^t \frac{\sum_i \sum_{i'} Q_{\lambda,t,p}(i, i')}{(2t + 1)} \\ &= \sum_i \sum_{i'} (2\lambda + 1) \sum_{t=\lambda-1}^{\lambda+1} \sum_{p=-t}^t \frac{Q_{\lambda,t,p}(i, i')}{(2t + 1)} \end{aligned} \quad (21)$$

Likewise, we can define the efficacy of luminescence matrix $A(i, i')$ as

$$A(i, i') = \frac{64\pi^4 e^2 \chi}{3h} \sum_{\lambda=2,4,6} (2\lambda + 1) \nu_\lambda^3 |\langle {}^5D_0 \| U^{(\lambda)} \| {}^7F_{J=\lambda} \rangle|^2 \sum_{t=\lambda-1}^{\lambda+1} \sum_{p=-t}^t \frac{Q_{\lambda,t,p}(i, i')}{(2t + 1)} \quad (22)$$

where ν_λ is the frequency (in cm^{-1}) corresponding to the energy gap between the initial 5D_0 and final 7F_J states.

Note that $A(i, i')$ is a real symmetric positive semi-definite matrix, since $Q_{\lambda,t,p}(i, i')$ is also a real symmetric positive semi-definite matrix and the coefficients multiplying $Q_{\lambda,t,p}(i, i')$ in eq. (22) are all positive. The diagonal terms $A(i, i)$ are coordinating atom contributions, and the off diagonal terms $A(i, i')$ with $i \neq i'$, are the coordinated atom pair contributions to $A_{\text{rad}}[{}^5D_0 \rightarrow {}^7F_J]$, and, ultimately, indirect contributions to the emission efficiency. As a result,

$$A_{\text{rad}} = \sum_i \sum_{i'} A(i, i') \quad (23)$$

From the point of view of coordination chemistry, it is more useful to aggregate all contributions from each ligand in the complex and define the ligand contributions to the radiative decay rate by matrix $A_L(L, L)$, in terms of summations over the coordinating atoms k of ligand L as:

$$A_L(L, L) = \sum_k \sum_{k'} A(k, k') \quad (24)$$

Likewise, we can define the ligand pair contribution to the radiative decay rate by matrix $A_L(L, L')$, which is a measure of how well the ligands interact to enhance the radiative decay rate, in terms of summations over the coordinating atoms k and m , of ligands L and L' , respectively, as:

$$A_L(L, L') = \sum_k \sum_m A(k, m) \quad (25)$$

Note that the ligand-pair contributions do not contain any atomic contributions, since, by being different ligands, L and L' do not share any directly coordinating atom.

Finally,

$$A_{rad'} = \sum_L \sum_{L'} A_l(L, L') \quad (26)$$

We will use the efficacies of luminescence, or simply efficacies $A(i, i')$ and $A_l(L, L')$ in order to interpret, from a chemical point of view, the various influences of the ligands and of their atoms, together with their pair influences, directly on $A_{rad'}$. The elements of both efficacy matrices A and A_l are partial decay rates (see eqs (23) and (26)), being expressed in units of a decay rate, usually s^{-1} . So, in order to obtain the total decay rate in s^{-1} , just add all elements of either matrix, that is, their grand sums $Su(A)$ or $Su(A_l)$ defined as $Su(A) = \vec{1}^T A \vec{1}$ and $Su(A_l) = \vec{1}^T A_l \vec{1}$, where $\vec{1}$ is a column vector with all elements equal to unity.

The chemical partition of $A_{rad'}$. The elements of the efficacy matrices A and A_l are often negative, which require an interpretation, which may sometimes be useful, but is certainly less chemically intuitive, of the partition of $A_{rad'}$. For example, if a given complex displays a very low luminescence, that is an $A_{rad'}$ close to zero, it is possible that the contribution A_l from one of its ligands be $+800 s^{-1}$ and the A_l of another ligand be $-800 s^{-1}$. Such a situation in which one contribution annihilates the other, renders the role of each of the ligands on the luminescence phenomenon somewhat indiscernible, especially when they are chemically identical.

A chemically more intuitive partition would require only coordinated atom or ligand contributions, always positive, and hence, whenever $A_{rad'}$ is zero, they all should be zero.

In order to define such a partition, we start by recognizing that matrix Q is Hermitian and positive semi-definite, and, as a consequence, matrix $A(i, i')$ is also Hermitian and positive semi-definite. That implies that their eigenvalues are not only all real, but they are all greater than or equal to zero. Now, define the orthonormal eigenvectors of $A(i, i')$ as $U_1, U_2, \dots, U_n$. Let $c_i = \langle \vec{1}, U_i \rangle$, where $\langle \cdot, \cdot \rangle$ denotes an inner product. Then, $\vec{1} = c_1 U_1 + \dots + c_n U_n$. Let the eigenvalues associated to the eigenvectors $U_1 \dots U_n$ be, respectively, $\lambda_1, \dots, \lambda_n$. Thus, $Su(A) = c_1^2 \lambda_1 + \dots + c_n^2 \lambda_n$. In fact,

$$Su(A) = \vec{1}^T A \vec{1} = (c_1 U_1 + \dots + c_n U_n)^T A (c_1 U_1 + \dots + c_n U_n) \quad (27)$$

$$Su(A) = \sum_{j=1}^n \sum_{k=1}^n c_j c_k U_j^T A U_k = \sum_{j=1}^n \sum_{k=1}^n c_j c_k \lambda_k U_j^T U_k = \sum_{j=1}^n c_j^2 \lambda_j \quad (28)$$

Let,

$$\begin{aligned} U_1 &= (U_{11}, U_{12}, \dots, U_{1n})^T; \\ U_2 &= (U_{21}, U_{22}, \dots, U_{2n})^T; \\ &\dots \\ U_n &= (U_{n1}, U_{n2}, \dots, U_{nn})^T; \end{aligned} \quad (29)$$

Observe that

$$\lambda_i = \lambda_i U_i^T U_i = U_i^T A U_i = \sum_{j=1}^n U_{ij} [A U_i]_j \quad (30)$$

So, we define the relative contribution of the coordinated atom j to the eigenvalue λ_i as

$$\frac{1}{\lambda_i} U_{ij} [A U_i]_j \quad (31)$$

We will now obtain a nicer expression for this relative contribution. Since $A U_i = \lambda_i U_i$, we have $[A U_i]_j = \lambda_i U_{ij}$, thus $U_{ij} [A U_i]_j = \lambda_i U_{ij}^2$. Finally, $\frac{1}{\lambda_i} U_{ij} [A U_i]_j = U_{ij}^2$. Thus, U_{ij}^2 is the relative contribution of the coordinated atom j to eigenvalue λ_i because these relative contributions are non-negative and sum 1, and thus can be viewed as proportions as we intended. We can now define the vectors with the ligand contributions to the eigenvectors:

$$\begin{aligned} U^{(1)} &= (U_{11}^2, U_{21}^2, \dots, U_{n1}^2)^T \\ U^{(2)} &= (U_{12}^2, U_{22}^2, \dots, U_{n2}^2)^T \\ &\dots \\ U^{(n)} &= (U_{1n}^2, U_{2n}^2, \dots, U_{nn}^2)^T \end{aligned} \quad (32)$$

In a similar manner, we can define the absolute contribution of coordinated atom j to $c_i^2 \lambda_i$ as $c_i^2 \lambda_i$ times the relative contribution of coordinated atom j to the eigenvalue λ_i , i.e. $c_i^2 \lambda_i U_{ij}^2$. Finally, we can define the absolute contribution of coordinated atom j to $Su(A)$, Λ_j , as the sum of the contributions of coordinated atom j over all values $c_i^2 \lambda_i$, with $i = 1 \dots n$. Let $V = (c_1^2 \lambda_1, \dots, c_n^2 \lambda_n)$. Then, the contribution of coordinated atom j to $Su(A)$, Λ_j , is given by

$$\Lambda_j = VU^{(j)} \quad (33)$$

due to the definition above, $\Lambda_1 + \Lambda_2 + \Lambda_3 + \dots + \Lambda_n = Su(A)$, with $\Lambda_i \geq 0$.

The set of coefficients Λ_j thus constitutes a partition of $A_{rad'}$ in n terms, all positive, each corresponding to each of the n coordinated atoms. These terms reflect how each coordinated atom contributed to make the $^5D_0 \rightarrow ^7F_1$ less forbidden.

As before, we can aggregate all contributions from each ligand in the complex and define the ligand contributions to $A_{rad'}$ in terms of summations over the coordinating atoms k of ligand L as:

$$\Lambda^L = \sum_k \Lambda_k \quad (34)$$

Of course,

$$A_{rad'} = \sum_L \Lambda^L \quad (35)$$

In summary, the chemical partitions we introduce in this article, $A(i, i)$, $A(i, i')$, $A_L(L, L)$, $A_L(L, L')$, Λ_j , and Λ^L , are from now on available, ready to be interpreted from a myriad of chemical perspectives depending on the system of interest, subject to the creativity of the researcher.

LUMPAC chemical partition implementation. The luminescent software package LUMPAC¹², since 2013 freely available from <http://www.lumpac.pro.br/>, is the first state of the art complete software to treat europium luminescence from a theoretical point of view. Recently, the unique adjustment of theoretical intensity parameters developed by our group²⁷ was implemented in LUMPAC. Now, the chemical partition being advanced in this article has also been implemented and is already available to all users of LUMPAC.

From eqs (10) and (11), clearly geometry makes a profound impact on the calculation of the theoretical intensity parameters Ω_2 , Ω_4 and Ω_6 , and, by extension makes an impact on our partition scheme. Therefore, users must first determine the most stable geometry of the complex of interest via either RM1²² or any of the Sparkle Models^{17–21} in such a manner as to satisfy the binary outcome acceptance conditions for the unique adjustment of theoretical intensity parameters as described in the “LUMPAC implementation” section of ref. 27. Once the adjustment is considered accepted, calculation of the chemical partition follows in a seamless manner.

The partition is first computed per directly coordinated atom, and then subsequently aggregated per ligand by summing up the terms of the directly coordinated atoms of each ligand. It has been proven useful to further aggregate the terms of the ligands into terms for classes of ligands, such as the terms of all ionic ligands and those of all non-ionic ligands.

Interpretation of the chemical partition ligand terms. Interpretation of the ligand terms requires an understanding of the fact that, according to Laporte rule, the electronic f-f transitions in lanthanide complexes should be forbidden in centrosymmetric molecules, since they conserve parity with respect to the inversion center where the metal is located. In this sense, luminescence happens because the centrosymmetry can be broken by ligands coordinating the lanthanide ion. Since luminescence happens in the europium ion, not at the ligands, the ligand terms of the $A_{rad'}$ chemical partition cannot possibly be regarded as ligand contributions to $A_{rad'}$, but rather as measures of the relaxation of the forbidding character of the $^5D_0 \rightarrow ^7F_1$ transitions ($J = 2, 4, 6$), conferred by each of the respective ligands to the europium ion. Note that each ligand term of the chemical partition is defined within the distinctive chemical ambience of the particular complex, and cannot be expected to be transferable from complex to complex.

Sensitivity of the chemical partition to complex geometry. We now turn to exemplify aspects of our partition scheme by first studying three specific complexes of the general formula $\text{Eu}(\beta\text{-diketonate})_3(\text{TPPO})_2$, where TPPO is the non-ionic ligand triphenylphosphine oxide and β -diketonate stands for one of the ionic ligands TTA, 1-(2-thenoyl)-3,3,3-trifluoroacetone, BTFA, 4,4,4-trifluoro-1-phenyl-2,4-butanedione, or DBM, 1,3-diphenylpropane-1,3-dione.

A complex of this general formula $\text{Eu}(\beta\text{-diketonate})_3(\text{TPPO})_2$ may display two possible ligand arrangements: both TPPOs are either adjacent or opposite to each other. All structural data have been computed by either RM1²², or, in a single case, by the Sparkle/PM3¹⁸ method. The choice of method followed the QDC acceptance criterion²⁷ defined in a previous article on the unique adjustment of theoretical intensity parameters²⁷. We will now examine the impact of these different geometric arrangements on the chemical partition of $A_{rad'}$. However, since the emission spectra, A_{rad} , Ω_2 and Ω_4 have been measured for these complexes in the opposite TPPO configuration^{6,40}, we will use these same values to arrive at the chemical partition for each of the two possible geometrical arrangements for enlightening purposes only. Tables S1 and S2 of the Supplementary Information contain information on the adjustments of the theoretical intensity parameters, unique for each of the geometrical arrangements, and the partition results, aggregated by ligand, for all three complexes considered.

Figure 1 shows the chemical partition of the radiative decay rate $A_{rad'}$ for each of the ligands coordinated to the metal ion for both cases of adjacent and opposite non-ionic ligands for all three TPPO complexes considered.

Figure 1 evidences the chemical nature of the partition because, now, $A_{rad'}$ has been sliced into ligand terms that depend on the chemical nature of the ligands, as well as on their collective arrangements around the europium ion.

Figure 1. Chemical partition of A_{rad} per ligand for two conformations of complexes of the type $\text{Eu}(\beta\text{-diketonate})_3(\text{TPPO})_2$: one with the two TPPOs non-adjacent, and the other with the two TPPOs adjacent to each other.

In an environment with three other identical ionic ligands, adjacent non-ionic ligands are less centrosymmetric than opposite ones. So, one would expect that adjacent same ligands should contribute more to the relaxation of the forbidding character of the $^5\text{D}_0 \rightarrow ^7\text{F}_j$ transitions ($J = 2, 4, 6$) than opposite ones. That is indeed the case for $\text{Eu}(\text{TTA})_3(\text{TPPO})_2$, where the sum of terms of the adjacent TPPOs is 382 s^{-1} , whereas for opposite TPPOs it is 122 s^{-1} . Equivalent numbers for $\text{Eu}(\text{BTFA})_3(\text{TPPO})_2$ are 422 s^{-1} and 160 s^{-1} , and for $\text{Eu}(\text{DBM})_3(\text{TPPO})_2$, they are 96 s^{-1} and 102 s^{-1} , a more balanced situation which arises seemingly due to the more symmetric and bulky nature of DBM.

Conversely, the β -diketonate ligands are more centrosymmetric when the TPPOs are adjacent (two of them tend to occupy opposite axial-like positions) and therefore they should contribute less to the relaxation of the forbidding character of the $^5\text{D}_0 \rightarrow ^7\text{F}_j$ transitions ($J = 2, 4, 6$). On the other hand, the β -diketonate ligands are less centrosymmetric when the TPPOs are opposite, because in this case they tend to occupy planar trigonal-like positions, in which case they should contribute more to the relaxation of the forbidding character of the $^5\text{D}_0 \rightarrow ^7\text{F}_j$ transitions ($J = 2, 4, 6$). For $\text{Eu}(\text{TTA})_3(\text{TPPO})_2$, the sum of the three β -diketonate terms for opposite TPPOs is 636 s^{-1} , whereas for adjacent TPPOs it is 374 s^{-1} . Equivalent numbers for $\text{Eu}(\text{BTFA})_3(\text{TPPO})_2$ are 635 s^{-1} and 454 s^{-1} . For $\text{Eu}(\text{DBM})_3(\text{TPPO})_2$ the numbers are 190 s^{-1} and 233 s^{-1} , which we again attribute to the bulky nature of DBM which is in itself the most symmetric of the β -diketonates used and makes the whole complex overall more centrosymmetric, severely reducing the value of A_{rad} to 335 s^{-1} when compared to the other two, which average 858 s^{-1} .

Applications of the chemical partition. Complexes $\text{Eu}(\text{TTA})_3(\text{TPPO})_2$ and $\text{Eu}(\text{BTFA})_3(\text{TPPO})_2$ had their geometries determined by crystallography and deposited in the Cambridge Structural Database, CSD^{41–43}, with refcodes SABHIM and WIFWIR, respectively. In both cases, the non-ionic ligands appear opposite to each other. Recently, a theoretical determination of the thermodynamic properties of $\text{Eu}(\text{DBM})_3(\text{TPPO})_2$ also indicated that the opposite TPPO configuration should be the preferred one⁴⁰. This study further extended the analysis for other non-ionic ligands and predicted that $\text{Eu}(\text{DBM})_3(\text{DBSO})_2$ and $\text{Eu}(\text{DBM})_3(\text{PTSO})_2$ should also display opposite non-ionic ligand configurations, where DBSO is dibenzyl sulfoxide and PTSO is p-tolyl sulfoxide. As a consequence, in the present article we assume that all complexes of the general formula $\text{Eu}(\beta\text{-diketonate})_3(\text{L})_2$ where L is a non-ionic ligand, will adopt opposite non-ionic ligand configurations. As before, all structural data have been computed by either RM1²², or, in a single case, by the Sparkle/PM3¹⁸ method - the choice of method followed the QDC acceptance criterion²⁷.

Table 1 presents luminescence results for 9 different complexes of the general formula $\text{Eu}(\beta\text{-diketonate})_3(\text{L})_2$, radiative decay rates, both experimental ($A_{\text{rad}}^{\text{exp}}$) and calculated, ($A_{\text{rad}}^{\text{calc}}$), the latter one partitioned by ligands and summed up into ionic ligand ($A_{\text{rad}}^{\text{ionic}}$) and non-ionic ligand ($A_{\text{rad}}^{\text{non-ionic}}$) terms. Please remember that ($A_{\text{rad}}^{\text{exp}}$) will always be larger than ($A_{\text{rad}}^{\text{calc}}$) because $A_{\text{rad}}^{\text{exp}}$ refers to all $^5\text{D}_0 \rightarrow ^7\text{F}_j$ transitions, while $A_{\text{rad}}^{\text{calc}}$ only adds up those with $j = 2, 4, 6$.

Examination of the average values in Table 1 reveals that the contribution of the non-ionic ligands to the triggering of luminescence decay by the excited europium trivalent ion is much smaller, in average 120 s^{-1} , than the corresponding contribution of the ionic ligands, 544 s^{-1} . That could lead to a misunderstanding that the non-ionic ligands, in these cases, are not too relevant to the luminescence phenomenon. However, their modest contribution to ($A_{\text{rad}}^{\text{calc}}$) is seemingly due to that fact that they are opposite to each other, and, therefore, in a symmetric configuration with respect to the europium ion, which does not help to relax the Laporte's rule.

Recently, our group introduced a simple strategy to boost three important luminescence properties of complexes of the general formula $\text{Eu}(\beta\text{-diketonate})_3(\text{L})_2$: the quantum yield, Φ , the emission efficiency η , and $A_{\text{rad}}^{\text{exp}}$, which was mathematically translated into the following conjecture⁶:

$$P[\text{Eu}(\beta\text{-diketonate})_3(\text{L}, \text{L}')_2] \geq \frac{P[\text{Eu}(\beta\text{-diketonate})_3(\text{L})_2] + P[\text{Eu}(\beta\text{-diketonate})_3(\text{L}')_2]}{2} \quad (36)$$

where P stands for either Φ , η , or $A_{\text{rad}}^{\text{exp}}$ and L and L' are different non-ionic ligands. This conjecture states that mixed non-ionic ligand complexes, $\text{Eu}(\beta\text{-diketonate})_3(\text{L}, \text{L}')_2$, should display larger luminescence properties when compared to the average of the same properties for repeating ligand complexes, $\text{Eu}(\beta\text{-diketonate})_3(\text{L})_2$ and $\text{Eu}(\beta\text{-diketonate})_3(\text{L}')_2$. This conjecture has already been proven experimentally for all combinations of the non-ionic ligands DBSO, TPPO, and PTSO, for all ternary europium complexes of TTA, BTFA, and DBM.

Table 2 displays $A_{\text{rad}}^{\text{exp}}$, $A_{\text{rad}}^{\text{calc}}$, $A_{\text{rad}}^{\text{ionic}}$ and $A_{\text{rad}}^{\text{non-ionic}}$ for the complexes with mixed non-ionic ligands. The role of the non-ionic ligands in the mixed-ligand complexes becomes clearer. Indeed, now the contribution of both different non-ionic ligands, to the triggering of luminescence decay, becomes accentuated to an average of 302 s^{-1} , up from the average of 120 s^{-1} in the repeating non-ionic ligand complexes of Table 1. Once again, this behavior can be rationalized in terms of symmetry: the different non-ionic ligands are opposite to each other, rendering the situation considerably more asymmetric, thus much more capable of triggering the luminescent decay of the excited europium ion. On the other hand, the role of the ionic ligands remains, in average, unaffected. Indeed, the average of $A_{\text{rad}}^{\text{ionic}}$ for the mixed non-ionic ligand complexes is 552 s^{-1} , whereas in the repeating non-ionic ligand complexes it is 544 s^{-1} , thus reinforcing the protagonist role of the non-ionic ligands in the luminescence boost.

Complex	$A_{\text{rad}}^{\text{exp}} (\text{s}^{-1})$	$A_{\text{rad}}^{\text{calc}} (\text{s}^{-1})$	$A_{\text{rad}}^{\text{ionic}} (\text{s}^{-1})$	$A_{\text{rad}}^{\text{non-ionic}} (\text{s}^{-1})$
$\text{Eu}(\text{TTA})_3(\text{DBSO})_2$	846	806	721	86
$\text{Eu}(\text{TTA})_3(\text{TPPO})_2$	796	757	635	122
$\text{Eu}(\text{TTA})_3(\text{PTSO})_2$	752	718	709	8
$\text{Eu}(\text{BTFA})_3(\text{DBSO})_2$	827	792	651	141
$\text{Eu}(\text{BTFA})_3(\text{TPPO})_2$	919	795	635	160
$\text{Eu}(\text{BTFA})_3(\text{PTSO})_2$	956	919	550	370
$\text{Eu}(\text{DBM})_3(\text{DBSO})_2$	522	477	418	59
$\text{Eu}(\text{DBM})_3(\text{TPPO})_2^a$	335	292	190	102
$\text{Eu}(\text{DBM})_3(\text{PTSO})_2$	459	413	383	29
Averages	712	663	544	120

Table 1. Radiative decay rates $A_{\text{rad}}^{\text{exp}}$ and $A_{\text{rad}}^{\text{calc}}$ as well as the ionic and non-ionic partitions of $A_{\text{rad}}^{\text{calc}}$: $A_{\text{rad}}^{\text{ionic}}$ and $A_{\text{rad}}^{\text{non-ionic}}$. $A_{\text{rad}}^{\text{calc}}$ corresponds to the transitions from $^5\text{D}_0$ to $^7\text{F}_2$, $^7\text{F}_4$, and $^7\text{F}_6$, and is therefore always smaller than $A_{\text{rad}}^{\text{exp}}$ which, in addition, also includes the transitions to $^7\text{F}_0$, $^7\text{F}_1$, $^7\text{F}_3$, and $^7\text{F}_5$. The $A_{\text{rad}}^{\text{ionic}}$ partition comprises the terms for each of the three identical β -diketonates. The $A_{\text{rad}}^{\text{non-ionic}}$ partition comprises the terms for each of the two identical non-ionic ligands. Geometries were optimized and the chemical partitions were calculated with the RM1 model (except where otherwise indicated). ^aGeometry was optimized and the chemical partition was calculated with Sparkle/PM3.

Figure 2. Choice (represented by the arrows) of pairs of non-ionic ligands (in parenthesis) from the values (in red) of $A_{rad'}^{non-ionic}$ of the repeating non-ionic ligand complexes (inside the rectangles), perfectly orders all mixed non-ionic ligand complexes in terms of their A_{rad}^{exp} values (in blue).

Complex	A_{rad}^{exp} (s ⁻¹)	$A_{rad'}$ (s ⁻¹)	$A_{rad'}^{ionic}$ (s ⁻¹)	$A_{rad'}^{non-ionic}$ (s ⁻¹)
Eu(TTA) ₃ (DBSO,TPPO)	1100	1061	926	135
Eu(TTA) ₃ (PTSO,TPPO)	1072	1023	459	564
Eu(TTA) ₃ (DBSO,PTSO)	1038	1004	626	379
Eu(BTFA) ₃ (DBSO,TPPO) ^a	983	949	440	509
Eu(BTFA) ₃ (PTSO,TPPO)	1050	1036	927	108
Eu(BTFA) ₃ (DBSO,PTSO)	1011	980	219	761
Eu(DBM) ₃ (DBSO,TPPO)	652	609	566	43
Eu(DBM) ₃ (PTSO,TPPO)	572	528	410	117
Eu(DBM) ₃ (DBSO,PTSO)	540	496	391	105
Averages	891	854	552	302

Table 2. Radiative decay rates A_{rad}^{exp} and $A_{rad'}$ as well as the ionic and non-ionic partitions of $A_{rad'}$: $A_{rad'}^{ionic}$ and $A_{rad'}^{non-ionic}$. $A_{rad'}$ corresponds to the transitions from 5D_0 to 7F_2 , 7F_4 , and 7F_6 , and is therefore always smaller than A_{rad}^{exp} which, in addition, also includes the transitions to 7F_0 , 7F_1 , 7F_3 , and 7F_5 . The $A_{rad'}^{ionic}$ partition comprises the terms for each of the three identical β -diketonates. The $A_{rad'}^{non-ionic}$ partition comprises the terms for each of the two non-ionic ligands. Geometries were optimized and the chemical partitions were calculated with the RM1 model (except where otherwise indicated). ^aGeometry was optimized and the chemical partition was calculated with Sparkle/RM1.

So far, we have argued the usefulness of our chemical partition in terms of averages across complexes, which helped us understand some global aspects of the luminescence phenomenon.

We now turn to examine the usefulness of the chemical partition per complex. The conjecture, eq. (36), indicates that in order to obtain a more luminescent complex, of the type Eu(β -diketonate)₃(L,L'), one should synthesize complexes of the type Eu(β -diketonate)₃(L,L'). However, the conjecture does not provide a hint of which pair combination of non-ionic ligands L,L' one must choose to obtain the mixed non-ionic ligand complex of maximum A_{rad}^{exp} . Actually, this is by no means trivial as exemplified by the case of Eu(DBM)₃(L,L'). Which pair of non-ionic ligands L,L' will lead to the complex Eu(DBM)₃(L,L') with the largest A_{rad}^{exp} ? If one naively decides to choose in terms of A_{rad}^{exp} of Table 1, by picking the non-ionic ligands of the two complexes with the highest values of A_{rad}^{exp} : Eu(DBM)₃(DBSO)₂ and Eu(DBM)₃(PTSO)₂, one would synthesize complex Eu(DBM)₃(DBSO,PTSO) and would be left with the mixed non-ionic DBM ternary complex with the smallest A_{rad}^{exp} . On the other hand, for the case of TTA ternary complexes, such a choice would lead to the correct complex, that is, to Eu(TTA)₃(DBSO,TPPO). Clearly, choosing mixed non-ionic ligand combinations from A_{rad}^{exp} of repeating non-ionic ligand complexes is not correct, as extraneous factors seem to be playing a role in the different ligands synergy, factors that, as will be shown below, the chemical partition seems to unveil.

Since what one needs to choose is one pair of non-ionic ligands which will lead to the mixed ligand complex with the highest value of A_{rad}^{exp} , one must therefore simply look, instead, at the non-ionic ligand term $A_{rad'}^{non-ionic}$ in the corresponding repeating ligand complexes in Table 1. Thus, for the before mentioned case of DBM ternary complexes, one would choose the two non-ionic ligands L and L', whose corresponding repeating non-ionic ligand complexes display the largest values of $A_{rad'}^{non-ionic}$: Eu(DBM)₃(TPPO)₂ and Eu(DBM)₃(DBSO)₂, respec-

tively, 102 s^{-1} , and 59 s^{-1} , leading to complex $\text{Eu}(\text{DBM})_3(\text{DBSO}, \text{TPPO})$. Indeed, this complex has the largest $A_{\text{rad}}^{\text{exp}}$ of 652 s^{-1} . Furthermore, one can use the same reasoning to arrive at the DBM ternary complex with the next larger $A_{\text{rad}}^{\text{exp}}$, where two possibilities exist: $\text{Eu}(\text{DBM})_3(\text{PTSO}, \text{TPPO})$ and $\text{Eu}(\text{DBM})_3(\text{DBSO}, \text{PTSO})$. The corresponding pair of largest $A_{\text{rad}}^{\text{non-ionic}}$ that are left are 102 s^{-1} for $\text{Eu}(\text{DBM})_3(\text{TPPO})_2$ and 29 s^{-1} for $\text{Eu}(\text{DBM})_3(\text{PTSO})_2$, leading to complex $\text{Eu}(\text{DBM})_3(\text{PTSO}, \text{TPPO})$, which, indeed, is the next best complex, with an $A_{\text{rad}}^{\text{exp}}$ of 572 s^{-1} . Finally, the last one left is complex $\text{Eu}(\text{DBM})_3(\text{DBSO}, \text{PTSO})$, with an $A_{\text{rad}}^{\text{exp}}$ of 540 s^{-1} .

Undoubtedly, for the case of ternary complexes of DBM, usage of the chemical partition allowed us to perfectly order, in an *a priori* way, the pair combinations of non-ionic ligands in terms of their $A_{\text{rad}}^{\text{exp}}$, a single outcome out of six possibilities.

Let us now apply the same strategy to the other ternary complexes of TTA and BTFA. The overall situation is present in pictorial format in Fig. 2, which shows that choosing non-ionic ligands by their $A_{\text{rad}}^{\text{non-ionic}}$ terms in non-ionic repeating ligand complexes also perfectly orders all mixed non-ionic ligand complexes in terms of their $A_{\text{rad}}^{\text{exp}}$ values for the remaining cases of TTA and BTFA ternary complexes.

Overall, the chemical partition predicted, in an *a priori* manner, a single joint outcome out of 216 possibilities, which, if it were by chance, would have a probability of only 0.46% of occurrence.

Conclusions

For the first time, a molecular global property related to luminescence, the radiative decay rate of europium complexes, is partitioned into ligand contributions. Such a novel approach gives rise to possible chemical interpretations of the effect of each ligand and their interactions on the luminescence phenomenon, allowing for the design of cutting edge compounds with enhanced brightness upon ultra-violet illumination.

As a demonstration of an application made only possible with the chemical partition, we address the case of repeating non-ionic ligand ternary complexes of europium(III) with DBM, TTA, and BTFA. We show that the chemical partition allows us to perfectly order, in an *a priori* way, the non-obvious pair combinations of non-ionic ligands that led to mixed-ligand compounds with larger values of A_{rad} .

Our new chemical partition has been implemented in the LUMPAC software, which is freely available¹².

References

- Horrocks, W. D. & Sudnick, D. R. Lanthanide ion luminescence probes of the structure of biological macromolecules. *Acc. Chem. Res.* **14**, 384–392 (1981).
- Sabbatini, N., Guardigli, M. & Lehn, J. M. Luminescent Lanthanide Complexes as Photochemical Supramolecular Devices. *Coord. Chem. Rev.* **123**, 201–228 (1993).
- Thejokalyani, N. & Dhoble, S. J. Novel approaches for energy efficient solid state lighting by RGB organic light emitting diodes—A review. *Renew. Sust. Energ. Rev.* **32**, 448–467 (2014).
- Kalyani, N. T. & Dhoble, S. J. Organic light emitting diodes: Energy saving lighting technology—A review. *Renew. Sust. Energ. Rev.* **16**, 2696–2723 (2012).
- Lehn, J. M. Perspectives in Supramolecular Chemistry - from Molecular Recognition Towards Molecular Information-Processing and Self-Organization. *Angew. Chem.-Int. Edit. Engl.* **29**, 1304–1319 (1990).
- Lima, N. B. D., Gonçalves, S. M. C., Júnior, S. A. & Simas, A. M. A Comprehensive Strategy to Boost the Quantum Yield of Luminescence of Europium Complexes. *Sci. Rep.* **3**, 2395 (2013).
- Diniz, J. R. *et al.* Water-Soluble Tb^{3+} and Eu^{3+} Complexes with Ionophilic (Ionically Tagged) Ligands as Fluorescence Imaging Probes. *Inorg. Chem.* **52**, 10199–10205 (2013).
- Hagan, A. K. & Zuchner, T. Lanthanide-based time-resolved luminescence immunoassays. *Anal. Bioanal. Chem.* **400**, 2847–2864 (2011).
- Kimura, H. *et al.* Quantitative evaluation of time-resolved fluorescence microscopy using a new europium label: Application to immunofluorescence imaging of nitrotyrosine in kidneys. *Anal. Biochem.* **372**, 119–121 (2008).
- Bunzli, J. C. G. & Piguet, C. Taking advantage of luminescent lanthanide ions. *Chem. Soc. Rev.* **34**, 1048–1077 (2005).
- Armélao, L. *et al.* Design of luminescent lanthanide complexes: From molecules to highly efficient photo-emitting materials. *Coord. Chem. Rev.* **254**, 487–505 (2010).
- Dutra, J. D. L., Bispo, T. D. & Freire, R. O. LUMPAC lanthanide luminescence software: Efficient and user friendly. *J. Comput. Chem.* **35**, 772–775 (2014).
- Albuquerque, R. Q., Da Costa, N. B. & Freire, R. O. Design of new highly luminescent Tb^{3+} complexes using theoretical combinatorial chemistry. *J. Lumin.* **131**, 2487–2491 (2011).
- Dutra, J. D. L., Gimenez, I. F., da Costa, N. B. & Freire, R. O. Theoretical design of highly luminescent europium (III) complexes: A factorial study. *J. Photoch. Photobiol. A* **217**, 389–394 (2011).
- Freire, R. O., Silva, F. R. G. E., Rodrigues, M. O., de Mesquita, M. E. & Junior, N. B. D. Design of europium(III) complexes with high quantum yield. *J. Mol. Model.* **12**, 16–23 (2005).
- Freire, R. O., Albuquerque, R. Q., Junior, S. A., Rocha, G. B. & de Mesquita, M. E. On the use of combinatory chemistry to the design of new luminescent Eu^{3+} complexes. *Chem. Phys. Lett.* **405**, 123–126 (2005).
- Freire, R. O., Rocha, G. B. & Simas, A. M. Sparkle model for the calculation of lanthanide complexes: AM1 parameters for $\text{Eu}(\text{III})$, $\text{Gd}(\text{III})$, and $\text{Tb}(\text{III})$. *Inorg. Chem.* **44**, 3299–3310 (2005).
- Freire, R. O., Rocha, G. B. & Simas, A. M. Sparkle/PM3 for the Modeling of Europium(III), Gadolinium(III), and Terbium(III) Complexes. *J. Brazil Chem. Soc.* **20**, 1638–1645 (2009).
- Freire, R. O. & Simas, A. M. Sparkle/PM6 Parameters for all Lanthanide Trications from $\text{La}(\text{III})$ to $\text{Lu}(\text{III})$. *J. Chem. Theory Comput.* **6**, 2019–2023 (2010).
- Dutra, J. D. L. *et al.* Sparkle/PM7 Lanthanide Parameters for the Modeling of Complexes and Materials. *J. Chem. Theory Comput.* **9**, 3333–3341 (2013).
- Filho, M. A. M., Dutra, J. D. L., Rocha, G. B., Freire, R. O. & Simas, A. M. Sparkle/RM1 parameters for the semiempirical quantum chemical calculation of lanthanide complexes. *RSC Adv.* **3**, 16747–16755 (2013).
- Filho, M. A. *et al.* RM1 Model for the Prediction of Geometries of Complexes of the Trications of Eu, Gd, and Tb. *J. Chem. Theory Comput.* **10**, 3031–3037 (2014).
- Filho, M. A. M., Dutra, J. D. L., Rocha, G. B., Simas, A. M. & Freire, R. O. Semiempirical Quantum Chemistry Model for the Lanthanides: RM1 (Recife Model 1) Parameters for Dysprosium, Holmium and Erbium. *Plos One* **9**(1), e86376 (2014).
- Filho, M. A. M., Dutra, J. D. L., Rocha, G. B., Simas, A. M. & Freire, R. O. RM1 modeling of neodymium, promethium, and samarium coordination compounds. *RSC Adv.* **5**, 12403–12408 (2015).

25. Dutra, J. D. L., Filho, M. A. M., Rocha, G. B., Simas, A. M. & Freire, R. O. RM1 Semiempirical Quantum Chemistry: Parameters for Trivalent Lanthanum, Cerium and Praseodymium. *PLoS One* **10**, e0124372 (2015).
26. MOPAC2012, Stewart, J.J.P., Stewart Computational Chemistry, Colorado Springs, CO, USA, 2012 (<http://OpenMOPAC.net>).
27. Dutra, J. D. L., Lima, N. B. D., Freire, R. O. & Simas, A. M. Europium Luminescence: Electronic Densities and Superdelocalizabilities for a Unique Adjustment of Theoretical Intensity Parameters. *Sci. Rep.* **5**, 13695 (2015).
28. de Sa, G. F. *et al.* Spectroscopic properties and design of highly luminescent lanthanide coordination complexes. *Coord. Chem. Rev.* **196**, 165–195 (2000).
29. Carnall, W. T., Crosswhite, H. & Crosswhite, H. M. Energy level structure and transition probabilities of the trivalent lanthanides in LaF₃, in Argonne National Laboratory Report (1978). Available at: <http://www.osti.gov/scitech/biblio/6417825>. (Accessed: 29th October 2015).
30. Binnemans, K., De Leebeeck, H., Görrler-Walrand, C. & Adam, J. L. Visualisation of the reliability of Judd–Ofelt intensity parameters by graphical simulation of the absorption spectrum. *Chem. Phys. Lett.* **303**, 76–80 (1999).
31. Weber, M. J., Varitimo, T. E. & Matsinge, B. H. Optical Intensities of Rare-Earth Ions in Yttrium Orthoaluminate. *Phys. Rev. B* **8**, 47–53 (1973).
32. Judd, B. R. Optical Absorption Intensities of Rare-Earth Ions. *Phys. Rev.* **127**, 750–761 (1962).
33. Ofelt, G. S. Intensities of Crystal Spectra of Rare-Earth Ions. *J. Chem. Phys.* **37**, 511–520 (1962).
34. Freeman, A. J. & Desclaux, J. P. Dirac-Fock Studies of Some Electronic Properties of Rare-Earth Ions. *J. Magn. Magn. Mater.* **12**, 11–21 (1979).
35. Malta, O. L., Ribeiro, S. J. L., Faucher, M. & Porcher, P. Theoretical Intensities of 4f–4f Transitions between Stark Levels of the Eu³⁺ Ion in Crystals. *J. Phys. Chem. Solids* **52**, 587–593 (1991).
36. Malta, O. L. & Silva, F. R. G. E. A theoretical approach to intramolecular energy transfer and emission quantum yields in coordination compounds of rare earth ions. *Spectrochim Acta A* **54**, 1593–1599 (1998).
37. Malta, O. L. A Simple Overlap Model in Lanthanide Crystal-Field Theory. *Chem. Phys. Lett.* **87**, 27–29 (1982).
38. Malta, O. L. Theoretical Crystal-Field Parameters for the YOCl:Eu³⁺ System. A Simple Overlap Model. *Chem. Phys. Lett.* **88**, 353–356 (1982).
39. Bethe, H. Term aufspaltung in Kristallen. *Ann. Physik* **395**, 133–208 (1929).
40. Lima, N. B. D., Silva, A. I. S., Gonçalves, S. M. C. & Simas, A. M. Synthesis of mixed ligand europium complexes: Verification of predicted luminescence intensification. *J. Lumin.* in press (2015).
41. Allen, F. H. The Cambridge Structural Database: a quarter of a million crystal structures and rising. *Acta Crystallogr. B* **58**, 380–388 (2002).
42. Allen, F. H. & Motherwell, W. D. S. Applications of the Cambridge Structural Database in organic chemistry and crystal chemistry. *Acta Crystallogr. B* **58**, 407–422 (2002).
43. Bruno, I. J. *et al.* New software for searching the Cambridge Structural Database and visualizing crystal structures. *Acta Crystallogr. B* **58**, 389–397 (2002).

Acknowledgements

The authors appreciate the financial support of the following Brazilian Agencies and Institutes: FACEPE (Pronex), CNPq, FAPITEC/SE, and INCT/INAMI.

Author Contributions

A.M.S. and N.B.D.L. identified the need for a chemical partition of the radiative decay rate of luminescence. A.M.S. derived the theory formalism. J.D.L.D. and R.O.F. coded the necessary modifications in LUMPAC to implement the chemical partition. N.B.D.L., A.M.S. and S.M.C.G. arrived at the application of the chemical partition to guide the choice of ligands for the design of mixed-ligand complexes displaying boosted luminescence. R.O.F. wrote the introductions of the article and of the Supplementary Information. All authors wrote and reviewed the manuscript.

Additional Information

Supplementary information accompanies this paper at <http://www.nature.com/srep>

Competing financial interests: The authors declare no competing financial interests.

How to cite this article: Lima, N. B. D. *et al.* Chemical Partition of the Radiative Decay Rate of Luminescence of Europium Complexes. *Sci. Rep.* **6**, 21204; doi: 10.1038/srep21204 (2016).

This work is licensed under a Creative Commons Attribution 4.0 International License. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in the credit line; if the material is not included under the Creative Commons license, users will need to obtain permission from the license holder to reproduce the material. To view a copy of this license, visit <http://creativecommons.org/licenses/by/4.0/>