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# Atomic-scale mapping of dipole frustration at 90° charged domain walls in ferroelectric PbTiO<sub>3</sub> films

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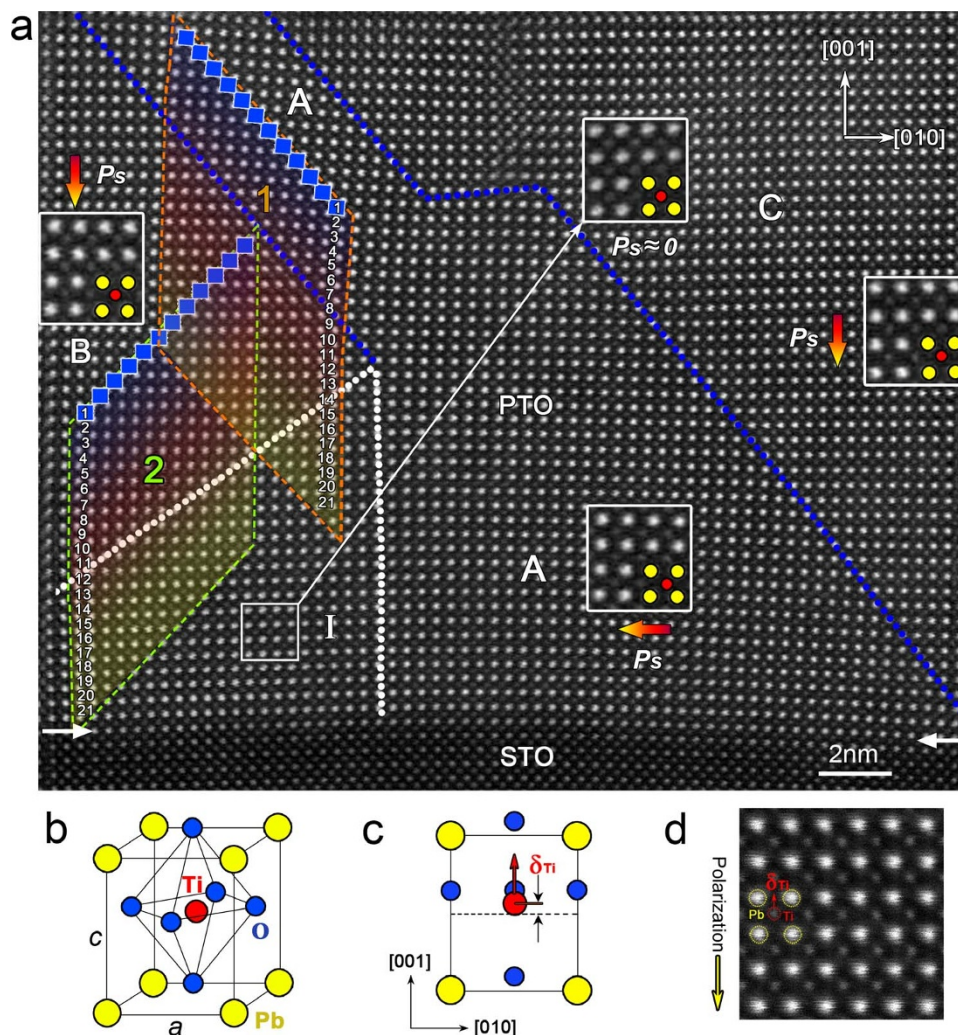
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The atomic-scale structural and electric parameters of the 90° domain-walls in tetragonal ferroelectrics are of technological importance for exploring the ferroelectric switching behaviors and various domain-wall-related novel functions. We have grown epitaxial PbTiO<sub>3</sub>/SrTiO<sub>3</sub> multilayer films in which the electric dipoles at 90° domain-walls of ferroelectric PbTiO<sub>3</sub> are characterized by means of aberration-corrected scanning transmission electron microscopy. Besides the well-accepted head-to-tail 90° uncharged domain-walls, we have identified not only head-to-head positively charged but also tail-to-tail negatively charged domain-walls. The widths, polarization distributions, and strains across these charged domain-walls are mapped quantitatively at atomic scale, where remarkable difference between these domain-walls is presented. This study is expected to provide fundamental information for understanding numerous novel domain-wall phenomena in ferroelectrics.

Ferroelectrics possess controllable polar states and electromechanical couplings, they were found extensive applications as high-density memories, thin-film capacitors and actuators as well as sensors<sup>1–3</sup>. In addition, they are showing multifunctional capabilities, as seen the finding of domain-wall conductivity<sup>3–6</sup> in ferroelectrics. Domain-walls in ferroelectrics are topological interfaces that separate domains with different orientations of polarizations. Historically, the domain-walls in ferroelectrics were thought to be simple, but their physical nature is found to be quite complicated in the past decade<sup>3</sup>. The local structural, chemical, and electric features as well as the dipole-defect interactions of domain-walls are of great importance and the macroscopic physical properties of ferroelectrics are strongly associated with these microstructural characteristics<sup>7–12</sup>.

Tetragonal ferroelectrics generally exhibit two types of domain-walls: 90° and 180° domain-walls, which have dipoles across the domain-walls arranged as 90° (nearly) and 180° configurations, respectively<sup>7–14</sup>. The 180° domains have the same strain, and hence are easy to switch<sup>8,10–12</sup>. However, the strong coupling of the polarization to the elastic strain of 90° domains limits the poling and piezoelectric ability of tetragonal ferroelectrics, which is a large obstacle for their potentials<sup>7–12</sup>. To understand the atomistic mechanisms involved during 90° domains switching, it is highly essential to figure out the structural and electric behaviors of 90° domain-walls on the atomic-scale which is known little up to date. Previously, the width of 90° domain-walls was studied by conventional transmission electron microscopy (TEM), and was 20 nm for BaTiO<sub>3</sub> (ref. 15), then 4–15 nm for BaTiO<sub>3</sub>, (Ba, Pb)TiO<sub>3</sub> and Pb(Zr<sub>0.52</sub>Ti<sub>0.48</sub>)O<sub>3</sub> (refs. 16–18). These measurements might be overestimated due to the limitation of instrument resolution, since the width of 90° domain-walls in PbTiO<sub>3</sub> were later found to be atomically sharp as 1.0–2.8 nm, determined by high resolution transmission electron microscopy (HRTEM) and weak beam transmission electron microscopy<sup>19–22</sup>. In the meanwhile, more and more theoretical works have proposed the presence of atomically sharp 90° domain-walls in tetragonal ferroelectrics<sup>22–24</sup>. Nevertheless, the dipoles across the 90° domain-walls were almost ignored in previous experiments, although the appearance of ‘head-to-head’ domain-walls was inferred in some modified rhombohedral PZT ceramics by the diffraction contrast analysis in a TEM<sup>25</sup>. Generally, the dipole configurations across the 90° domain-walls were arbitrarily treated as ‘head-to-tail’ arrangement in theoretical simulations based on the consideration of the electrostatic energy<sup>15–24</sup>. The newly developed scanning probe microscopy (SPM) based instruments show great potential to map the polarization distribution at ferroelectric surfaces, but its lateral resolution is about 5–30 nm, which is far from atomic-scale<sup>3,26,27</sup>.

The atomic and electronic behaviors of ferroelectrics have become readily accessible through aberration-corrected scanning transmission electron microscopy (STEM)<sup>28,29</sup> and accurate mapping of order-parameter



**Figure 1 |** Aberration-corrected HAADF images showing the  $90^\circ$  domain-walls in  $\text{PbTiO}_3$  film and electric dipoles formed by the relative displacements of the  $\text{Ti}^{4+}$  and  $\text{Pb}^{2+}$  cation columns. (a) HAADF images where the horizontal arrows denote the interface between the  $\text{PbTiO}_3$  and  $\text{SrTiO}_3$  layers. The blue dotted line traces the ‘head-to-tail’  $90^\circ$  domain-walls, while the white dotted line denotes the area with ‘head-to-head’  $90^\circ$  domain-wall (area I). The colored arrows denoted by ‘ $P_s$ ’ show the directions of the polarization of  $\text{PbTiO}_3$  beside the  $90^\circ$  charged-domain-wall. The insets show magnifications of the dipoles formed by the displacements of ions in corresponding domains (yellow:  $\text{Pb}^{2+}$ , red:  $\text{Ti}^{4+}$ ). Note that, in some PTO units within the area I, no obvious displacement of the  $\text{Ti}^{4+}$  and  $\text{Pb}^{2+}$  columns are observed, indicating that the polarizations in these unit-cells are restrained. (b) Schematic perspective view of the unit-cell of ferroelectric  $\text{PbTiO}_3$ . (c) Projection of the unit-cell along the  $[100]$  direction showing the  $\delta_{Ti}$ . (d) A representative HAADF image of the dipoles in  $\text{PbTiO}_3$  crystal. The positions of  $\text{Pb}^{2+}$  columns are brighter than those of the  $\text{Ti}^{4+}$  columns.  $\delta_{Ti}$  is also marked, which is opposite to the spontaneous polarization direction of the  $\text{PbTiO}_3$ , denoted by the yellow arrow.

fields such as lattice<sup>30,31</sup>, polarization<sup>14,32–34</sup> and octahedral tilts<sup>35–37</sup> has recently become feasible. In this study, we have grown  $\text{PbTiO}_3/\text{SrTiO}_3$  multilayer films and mapped atomic details and polarization distributions across the  $90^\circ$  domain-walls in an aberration-corrected STEM at high angle annular dark field (HAADF) mode. We have directly observed not only positively charged but also negatively charged  $90^\circ$  domain-walls at atomic scale.

## Results

$\text{PbTiO}_3/\text{SrTiO}_3$  multilayer films were prepared by pulsed laser deposition (PLD). The films were deposited on  $\text{GdScO}_3$  (GSO) substrate, which exert tensile strain on the epitaxial  $\text{PbTiO}_3/\text{SrTiO}_3$  superlattices<sup>38</sup>. Such ferroelectric/paraelectric heterostructures have attracted lots of interests because they offer a huge space for exploring the subtle interplay between their multiple order parameters<sup>39–41</sup>.

**Identification of  $90^\circ$  positively-charged-domain-wall.** Figure 1a shows an atomic resolution HAADF image of a  $\text{PbTiO}_3$  (PTO) layer near the  $\text{PbTiO}_3/\text{SrTiO}_3$  (PTO/STO) interface. The four

insets are magnification of images overlying the respective areas. Yellow cycles denote  $\text{Pb}^{2+}$  columns and red cycles denote  $\text{Ti}^{4+}$  columns.  $\text{O}^{2-}$  columns are invisible due to its weak scattering effects of electrons. As illustrated by the schematic diagrams in figure 1b and c, the atom arrangement of ferroelectric PTO exhibits shifts of the atoms with respect to the cubic perovskite structure. Both the  $\text{Ti}^{4+}$  and  $\text{O}^{2-}$  columns are shifted upward (along the  $[001]$  direction) towards the upper  $\text{Pb}^{2+}$  positions and away from the respective lower ones, but the  $\text{O}^{2-}$  columns are shifted more strongly. As a consequence, a charge dipole forms in the PTO unit-cell because of the separation of negative ( $\text{O}^{2-}$ ) and positive ( $\text{Ti}^{4+}$  and  $\text{Pb}^{2+}$ ) charges, as seen by means of coherent high-resolution imaging with negative  $C_s$  technique<sup>14</sup>. This dipole defines the direction of the vector of spontaneous polarization  $P_s$  (pointing from net negative to net positive charge and thus is opposite with the displacement of  $\text{Ti}^{4+}$ , Fig. 1d) parallel to  $[00\bar{1}]$ . Thus the atomic resolution HAADF imaging technique could be employed to record the electric dipoles unit-cell by unit-cell (Fig. 1d). The  $P_s$  direction (yellow arrow in Fig. 1d, colored arrows in Fig. 1a) of

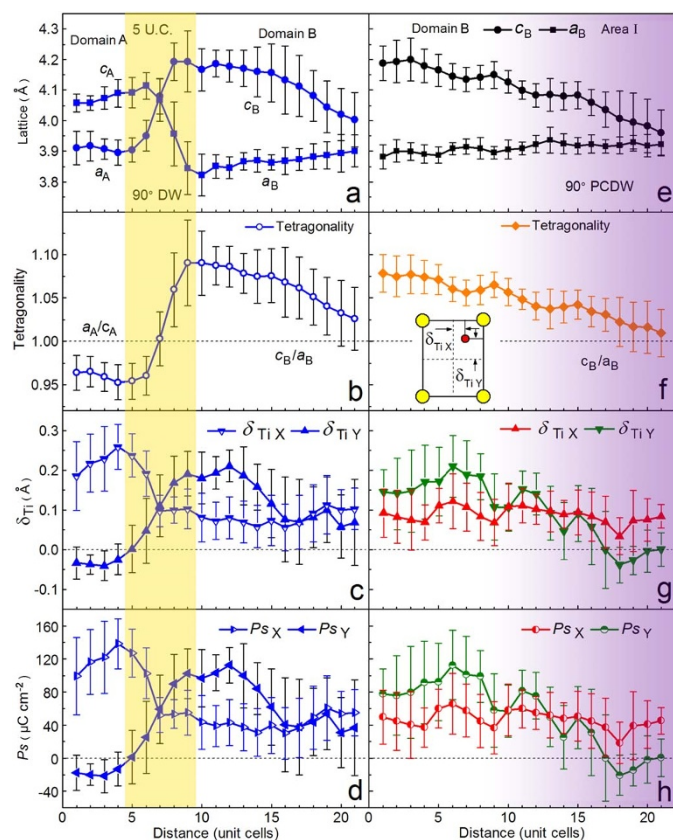


PTO unit-cells can be determined from the displacement of  $\text{Ti}^{4+}$  ( $\delta_{\text{Ti}}$ ) measured in the atomic resolution HAADF image. A careful inspection reveals that in figure 1a there are three polarization domains: lower right, domain A; middle left, domain B; upper right, domain C. The strong tetragonal nature of PTO ( $a = 0.389$  nm,  $c = 0.414$  nm, ref. 38) makes remarkable difference between scalings of  $a$  and  $c$  domains (In Fig. 1a, domain A is an  $a$  domain, domain B and C are  $c$  domains), thus domain A is shorter than domain B and C on both sides. This results in a complex strain state near the coherent PTO/STO interface which makes a bending of the STO lattice. The changing of one domain to another gives rise to the switching of polarization vector by  $90^\circ$ . Domain C has the same  $P_s$  direction as domain B. The position of these  $90^\circ$  domain-walls (DWs), indicated by the blue dotted lines, can be determined directly by mapping the  $\delta_{\text{Ti}}$  vectors of each PTO unit-cells. It is of interest to notice that the left  $90^\circ$  domain-wall terminates within the PTO matrix, this scenario is suggestive of some unusual dipole behaviors at the bottom left corner of figure 1a, because the  $P_s$  directions in domain A and B have to encounter each other. Thus, a  $90^\circ$  charged-DW (CDW) is identified, with a 'head-to-head' arrangement of  $P_s$  vectors. Such a  $90^\circ$  CDW is actually a broad area (labeled *area I*, as will be specified in the following) and thus is marked by two white dotted lines (Fig. 1a). Nominally, the 'head-to-head' arrangement of  $P_s$  produces positive bound charges near the

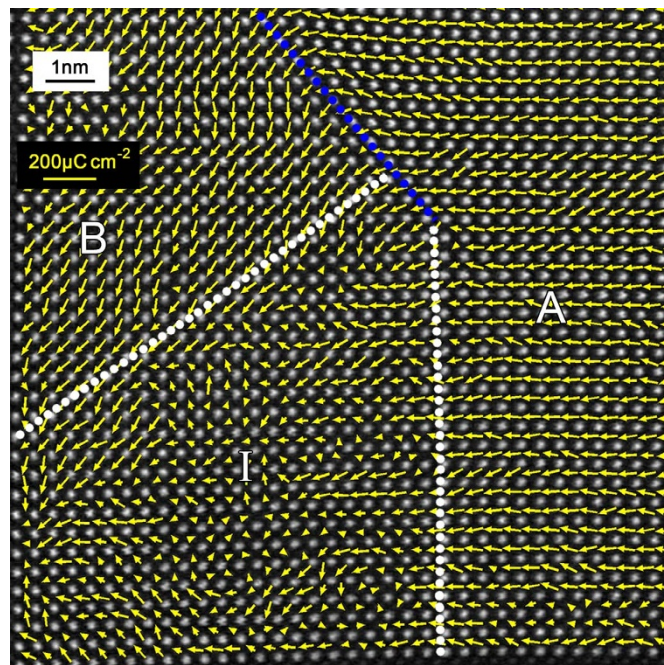
CDW<sup>42</sup>, so here we name it in terms of  $90^\circ$  positively-charged-domain-wall (PCDW). Similarly, the  $90^\circ$  uncharged-domain-wall is short-written as  $90^\circ$  UCDW.

A careful observation indicates that, on both structural and electric level, the  $90^\circ$  PCDW is rather wider than the  $90^\circ$  UCDW. According the famous Kittel's law, the DW width is a crucial factor for determining the DW patterns and thus the properties such as nonlinear electro-optics<sup>3</sup>. The local behaviors of the present  $90^\circ$  PCDW (rhombus-highlighted area labeled '2' in the lower left of figure 1a) are comparatively studied with the  $90^\circ$  UCDW (rhombus-highlighted area labeled '1' in the upper left of figure 1a), and the average data are obtained along PTO $\{110\}_p$  (subscript  $p$  denotes pseudo-cubic), which is generally thought to be the location of  $90^\circ$  DWs in tetragonal ferroelectrics<sup>22–24</sup>. The magnitudes of  $P_s$  vectors are determined by corresponding  $\delta_{\text{Ti}}$  because the relationship between the  $\delta_{\text{Ti}}$  and the  $P_s$  is well-known<sup>33</sup>. The image drifting are calibrated with reference to the lattice parameter ( $a = 0.5488$  nm, ref. 43) of the orthorhombic GSO substrate (not shown here). The structural and polar characters of the  $90^\circ$  UCDW at the upper left of figure 1a (The wall that separates domain A and domain B) are shown in figure 2a–d.

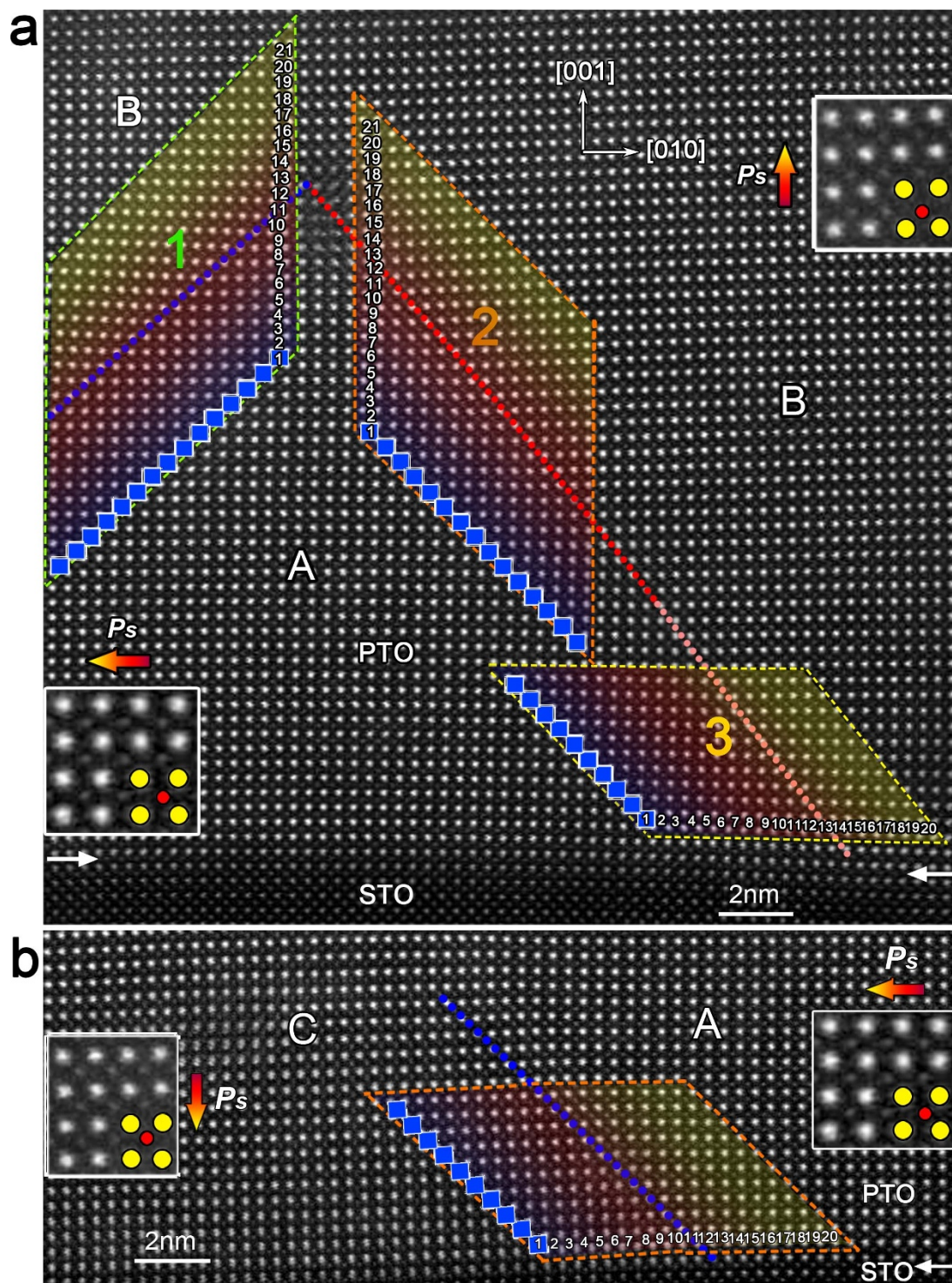
It is seen that the changing of lattice and polarization happens rapidly across the  $90^\circ$  UCDW (Fig. 2a–d), which exhibits the twin-walls character in tetragonal ferroelectrics<sup>9</sup>. The DW thickness is about 5 unit-cells (yellow shadowed in Fig. 2a–d) derived from the measurements of the local structural (lattice and tetragonality in Fig. 2a,b) and electric ( $\delta_{\text{Ti}}$  and  $P_s$  in Fig. 2c,d) changes. In comparison, the structural and polar characters across the  $90^\circ$  PCDW are measured, shown in figure 2e–h, which correspond to the lower left area in figure 1a (The wall that separates domain B and *area I*, across the left white dotted line). Amazingly, the changing of both lattice and polarization is much slowly across the  $90^\circ$  PCDW. From domain



**Figure 2** | Quantitative analysis of the structural and electric parameters of the  $90^\circ$  PCDW and  $90^\circ$  UCDW. The structural and electric parameters were averaged along  $\{110\}$  (pseudo-cubic) to insure the statistical analysis is parallel to the DWs. (a)–(d) Lattice parameters, tetragonality,  $\delta_{\text{Ti}}$  and  $P_s$  extracted from the rhombus-highlighted area marked with '1' in Fig. 1a. (e)–(h) Lattice parameters, tetragonality,  $\delta_{\text{Ti}}$  and  $P_s$  extracted from the rhombus-highlighted area marked with '2' in Fig. 1a. The error bars show the standard deviation with respect to averaging along  $\{110\}$  PTO for each  $\{110\}$  atomic row. The inset in (f) shows the schematic definition of out-of-plane ( $\delta_{\text{TiY}}$ ) and in-plane ( $\delta_{\text{TiX}}$ ) components of the  $\delta_{\text{Ti}}$  respectively.



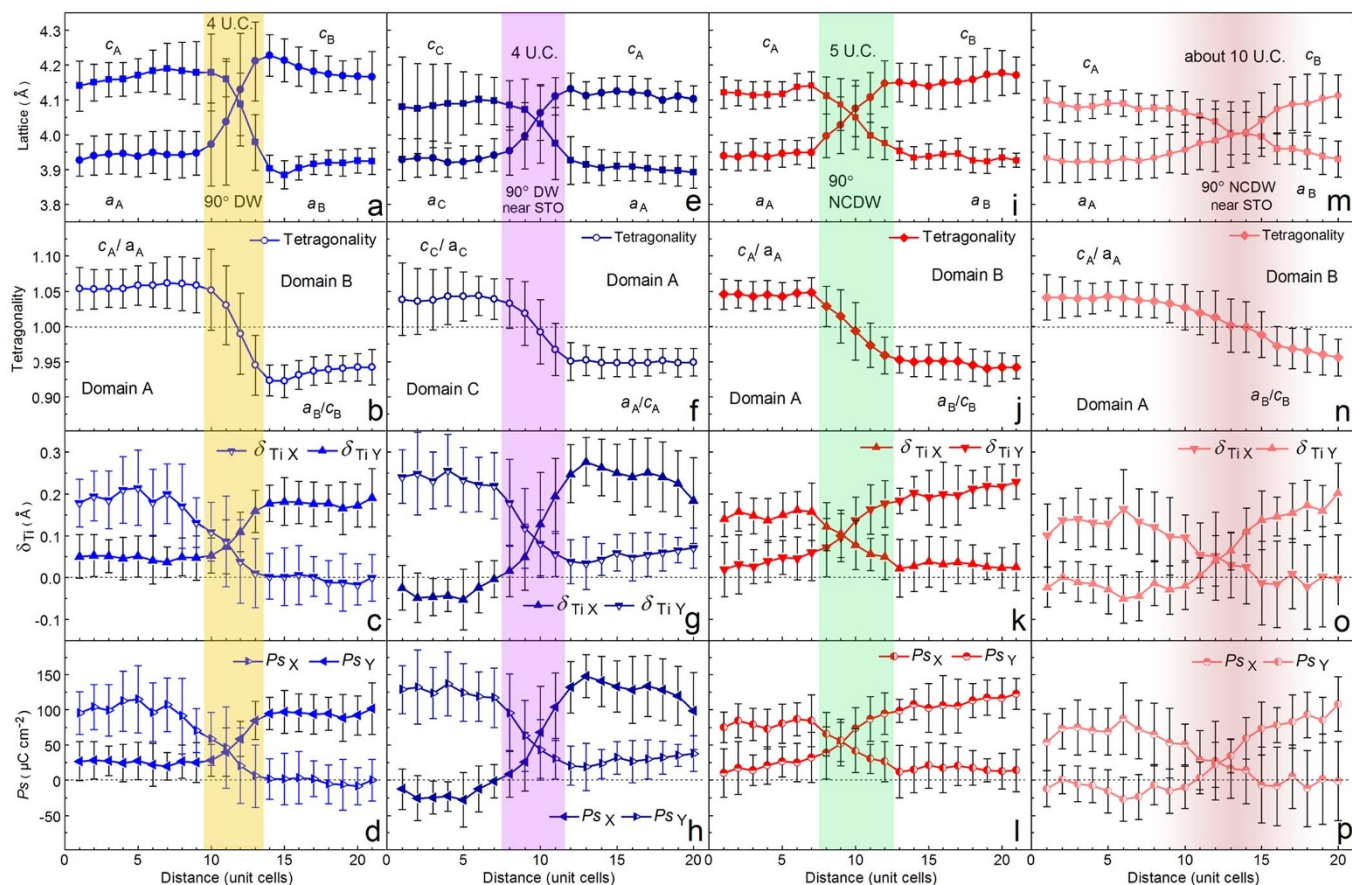
**Figure 3** |  $P_s$  vector mapping across the  $90^\circ$  PCDW and  $90^\circ$  UCDW in Fig. 1a.  $P_s$  vectors calculated through the  $\delta_{\text{Ti}}$  of both the  $90^\circ$  PCDW and  $90^\circ$  UCDW away from PTO/STO interface was shown. The blue dotted line denotes the  $90^\circ$  UCDW, the white dotted lines embrace the  $90^\circ$  PCDW area (*area I* in Fig. 1a). Note the restriction and disorder of the  $P_s$  vectors at the  $90^\circ$  PCDW, signifying that there is no obvious 'domain-wall' at the encounter of the  $P_s$  vectors. The length of the yellow arrows represents the modulus of the  $P_s$  with respect to the yellow scale bar in the upper left corner.



**Figure 4** | Aberration-corrected HAADF imaging of the electric dipoles formed near the  $90^\circ$  NCDW in  $\text{PbTiO}_3$ . (a) A  $\text{PbTiO}_3$  film near a  $\text{SrTiO}_3$  layer shows both charged and uncharged  $90^\circ$  domain-walls. The blue dotted line traces the  $90^\circ$  UCDW, the red dotted line traces the upper  $90^\circ$  NCDW, while the light red dotted line traces the lower  $90^\circ$  NCDW near the STO/PTO interface. The insets are magnifications of the dipoles formed by the displacements of ions in corresponding domains. (b) A  $\text{PbTiO}_3$  film near a  $\text{SrTiO}_3$  layer shows  $90^\circ$  UCDW (blue dotted line) near the PTO/STO interface. The insets are magnifications of the dipoles formed by the displacements of ions in corresponding domains. This  $90^\circ$  UCDW is the connection between domain A (in fig. 4a) and a  $c$  domain (named as 'domain C', as illustrated). Domain C was located at the left side of domain A (fig. 4a). The atomic images in rhombus-highlighted area is used to extract lattice parameters, tetragonality,  $\delta_{Ti}$  and  $P_s$ .

B to area I, the out-of-plane lattice ( $c_B$ ) continuously changes from 0.42 nm to 0.395 nm without a sharp jump, while the in-plane lattice ( $a_B$ ) almost kept constant of about 0.39 nm (black solid circles and squares denoted in Fig. 2e). The ratio of  $c_B/a_B$  indicates a slow changing of tetragonality, from 1.075 to 1.01 (Fig. 2f). There is no inter-

section of  $c_B$  and  $a_B$  lattice, and thus no sudden jump of tetragonality, which displays some unusual features of the  $90^\circ$  PCDW compared with the uncharged domain-walls. Generally, the  $P_s$  and strain in ferroelectric materials are coupled<sup>8,33</sup>, as a result, the  $P_{sY}$  also changes slowly from domain B (about  $80\text{--}100 \mu\text{Ccm}^{-2}$ ) to area I (0)



**Figure 5 | Quantitative analysis of the structural and electric parameters of the  $90^\circ$  NCDW and  $90^\circ$  UCDWs.** (a)–(d) Lattice parameters, tetragonality,  $\delta_{Ti}$  and  $P_s$  extracted from the rhombus-highlighted area marked with ‘1’ in Fig. 4a. (e)–(h) Lattice parameters, tetragonality,  $\delta_{Ti}$  and  $P_s$  extracted from a  $90^\circ$  UCDW near the PTO/STO interface (the rhombus-highlighted area in Fig. 4b). (i)–(l) Lattice parameters, tetragonality,  $\delta_{Ti}$  and  $P_s$  extracted from the rhombus-highlighted area marked with ‘2’ in Fig. 4a. (m)–(p) Lattice parameters, tetragonality,  $\delta_{Ti}$  and  $P_s$  extracted from the rhombus-highlighted area marked with ‘3’ in Fig. 4a. The error bars show the standard deviation with respect to averaging along  $\{110\}$  atomic row. Note that the  $90^\circ$  UCDWs near the PTO/STO interface and away from the interface share the same characteristics of a sharp jump of structural and electric behaviors. In contrast, the structural and electric parameters of the lower  $90^\circ$  NCDW near the interface are remarkably different from those away from the interface.

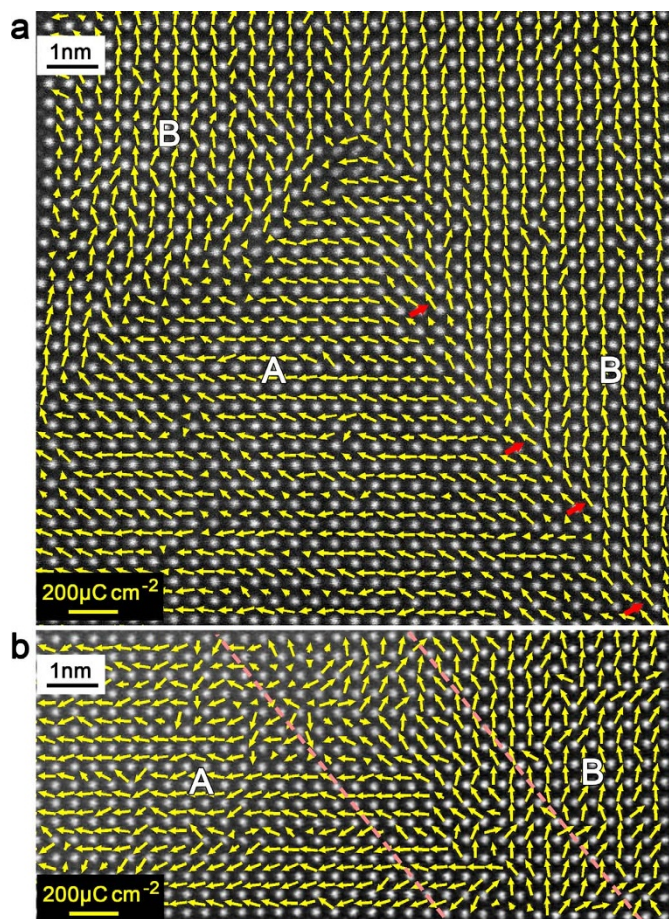
(olive-circle curve in Fig. 2h). However,  $P_{sX}$  almost keeps almost a constant value of about  $40 \mu\text{Ccm}^{-2}$  (red-circle curve in Fig. 2h). It is proposed that the accumulated bound charges induced by the  $90^\circ$  PCDW might be responsible for the invariable  $P_{sX}$ . The continuous and slow changing of lattice and  $P_s$  indicate that there is no obvious DW across the domain B and area I (violet gradual shadows in Fig. 2e–h). In other words, here the  $90^\circ$  PCDW is a broad area where the  $P_s$  vectors are disordered.

To directly gain insight into the polarization distributions, the  $P_s$  vectors of each unit-cell near the  $90^\circ$  PCDW were mapped and superimposed on the HAADF image (Fig. 3). The arrows located at the  $\text{Ti}^{4+}$  column positions indicate the directions and modulus of the  $P_s$  vectors. For most PTO cells, the  $P_s$  values are in the range of  $70$ – $100 \mu\text{Ccm}^{-2}$ . Unlike the  $90^\circ$  UCDW, where the directions of the  $P_s$  vectors changed rapidly, the  $P_s$  is strongly restricted and disordered at the  $90^\circ$  PCDW. According to the disorder of the  $P_s$  vectors, no obvious ‘domain-wall’ could be identified, which is consistent with its lattice behavior (Fig. 2e, f). Bound charges produced by the ‘head-to-head’ dipole arrangement may be responsible for the restriction and disorder of the  $90^\circ$  PCDW.

**Identification of  $90^\circ$  negatively-charged-domain-wall.** In addition to the  $90^\circ$  PCDW,  $90^\circ$   $P_s$  vectors configured as ‘tail-to-tail’ CDW is also identified in the present films. Since the ‘tail-to-tail’  $P_s$  arrangement may nominally induce negative bound charges near

the CDW<sup>42</sup>, here we name it as  $90^\circ$  negatively-charged-domain-walls ( $90^\circ$  NCDW). We will see that the structural and electric parameters of  $90^\circ$  NCDW are remarkably different from those of  $90^\circ$  PCDW.

Figure 4a shows an atomic resolution HAADF image of a PTO layer containing twin structures. Using the same methodology as that in figure 1, the position of  $90^\circ$  UCDWs is outlined, as marked by the blue dotted lines in the upper left part of figure 4a. By mapping the  $\delta_{Ti}$  vectors of each PTO unit-cell,  $90^\circ$  DW with ‘tail-to-tail’ arrangement of  $P_s$  vectors is identified, as traced by the red (upper segment) and light red (lower segment near the PTO/STO interface) dotted lines. The  $90^\circ$  NCDW separates domain A and B in figure 4a, with  $P_s$  directions pointing to left and top, respectively (magnified insets in Fig. 4a). Different from the  $90^\circ$  PCDW, the upper segment of the  $90^\circ$  NCDW is much narrower like that of the uncharged ones, while the lower segment is broadened similar to that of the  $90^\circ$  PCDW. The local behaviors of the two segments of the  $90^\circ$  NCDW are comparatively analyzed with the  $90^\circ$  UCDWs. In figure 5, the upper  $90^\circ$  NCDW (rhombus-highlighted area labeled ‘2’ in Fig. 4a) is compared with the left  $90^\circ$  UCDW (rhombus-highlighted area labeled ‘1’ in Fig. 4a), while the lower  $90^\circ$  NCDW (rhombus-highlighted area labeled ‘3’ in Fig. 4a) is compared with a  $90^\circ$  UCDW which is also near the PTO/STO interface neighboring with the  $90^\circ$  NCDW, seen in figure 4b. Here this  $90^\circ$  UCDW is the connection between domain A and a c domain, which was located at the left side of domain A. The



**Figure 6** | Mappings of the  $P_s$  vectors across the  $90^\circ$  NCDW and  $90^\circ$  UCDW. (a)  $P_s$  vectors of  $90^\circ$  UCDW and  $90^\circ$  NCDW away from PTO/STO interface. Note the bifurcation of the  $P_s$  and the trend of diagonal  $P_s$  directions (marked with red arrows) across the  $90^\circ$  NCDW. (b)  $P_s$  vectors across the  $90^\circ$  NCDW near the PTO/STO interface. It is seen that the scattering of the  $P_s$  vectors at this  $90^\circ$  NCDW makes the “wall” into a “band”. In (a) and (b), the length of the yellow arrows represents the modulus of the  $P_s$  with respect to the yellow scale bar in the lower left corner.

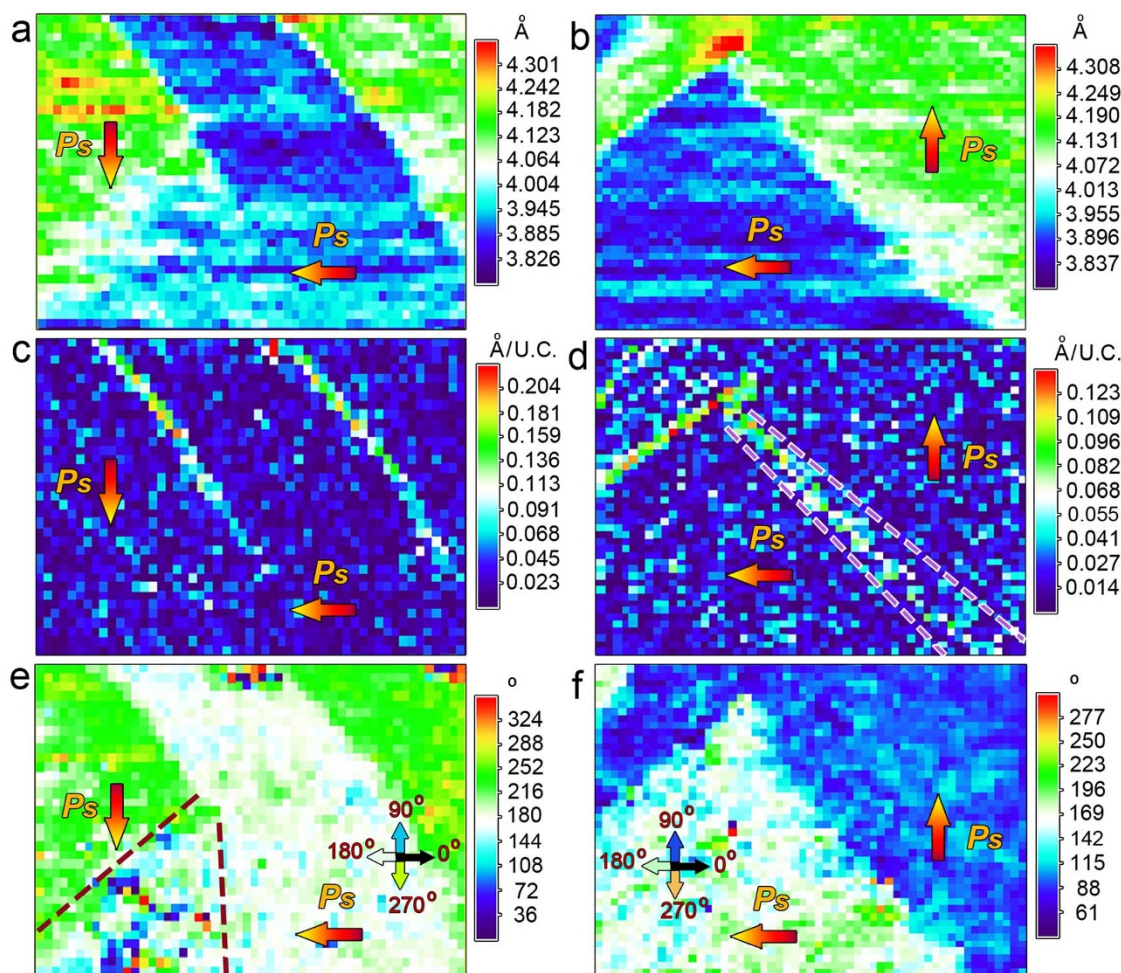
lattice and  $P_s$  characters of the left  $90^\circ$  UCDW (Fig. 4a) as well as the  $90^\circ$  UCDW near the PTO/STO interface (Fig. 4b) are shown in figure 5a–d and figure 5e–h. We can see that the width of  $90^\circ$  UCDW was not disturbed by the PTO/STO interface (Fig. 5e–h), since both the structural and electric parameters changed rapidly across these  $90^\circ$  UCDWs. However, the lattice parameters of these two  $90^\circ$  UCDW are different: the  $c$ -axis in domain A and B in figure 5a (0.415–0.42 nm) are bigger than those in domain C and A in figure 5e (about 0.41 nm). These differences were probably induced by the complex strains near the PTO/STO interface<sup>33</sup>. According to the sharp change of lattice and  $P_s$  vectors, both the  $90^\circ$  UCDWs possess the same width about 4 unit-cells, which is qualitatively the same as the  $90^\circ$  UCDW in figure 2a.

The structural and electric parameters of the upper and lower segments of the  $90^\circ$  NCDW were analyzed (Fig. 5i–l and Fig. 5m–p). The lattice and polarization also change rapidly across the upper  $90^\circ$  NCDW. This DW width is about 5 unit-cells, almost the same as the  $90^\circ$  UCDW, shadowed in light blue in figure 5i–l. However, for the lower segment of the  $90^\circ$  NCDW, the corresponding parameter slopes are obviously abated. The width of this DW is about 10 unit-cells (gradually shadowed in red in Fig. 5m–p), which is much bigger than that of the  $90^\circ$  UCDW. Nevertheless, like the  $90^\circ$  UCDW, the location of the  $90^\circ$  NCDW is still along  $\{110\}$  PTO.

The  $P_s$  vectors of each unit-cell near the  $90^\circ$  NCDW are also mapped and superimposed on the HAADF image (Fig. 6a, b). The  $90^\circ$  UCDW and the upper segment of the  $90^\circ$  NCDW are shown in figure 6a. Unlike the  $90^\circ$  UCDW, where the  $P_s$  directions rotate sharply with  $90^\circ$  at the DW, the  $P_s$  is almost maintained and rotates inchmeal at the  $90^\circ$  NCDW. The  $P_s$  vectors, in one or two units away from the  $90^\circ$  NCDW, are somewhat inclined to the NCDW both in domain A and B. And this trend is most obvious at the  $90^\circ$  NCDW because the  $P_s$  vectors rotate about  $45^\circ$  respective to horizontal or vertical plane (marked with red arrows in Fig. 6a), which produces diagonal  $P_s$  directions along the  $90^\circ$  NCDW. This inclination of  $P_s$  vectors along the  $90^\circ$  NCDW may help to relieve the bound charges and thus lower the depolarization field<sup>3</sup>, and to stabilize the narrow  $90^\circ$  NCDW. In contrast, the  $P_s$  vectors seem to be strongly disturbed at the lower segment of the  $90^\circ$  NCDW near the PTO/STO interface, as shown in figure 6b. According to the diffusion of the  $P_s$  vectors, no obvious ‘domain-wall’ could be identified. Instead, it is more like a ‘domain-wall-band’ with a thickness about 10 unit-cells, which is consistent with the lattice behaviors (Fig. 5m, n). Except for the bound charges, the PTO/STO interface may also be responsible for the diffusion of the lower segment of the  $90^\circ$  NCDW because of the interface-induced depolarization field which is very common in thin film ferroelectrics<sup>3</sup>.

To directly visualize the 2D structural parameters and  $P_s$  angles, unit-cell-wise structure and  $P_s$  angle mapping are displayed. The lattice parameter, gradient of the lattice parameter and  $P_s$  angles of the PTO unit-cells near the  $90^\circ$  PCDW and NCDW are mapped unit-cell by unit-cell, as shown in Figure 7. The out-of-plane lattice spacing mapping results clearly exhibit the  $90^\circ$  UCDWs, since there is sudden jump of the lattice spacing (blue to green, presumably corresponds to 0.39–0.42 nm, Fig. 7a, b). Although the  $90^\circ$  PCDW is diffused since the lattice spacing slowly changes from 0.395 to 0.42 nm (light blue to white then to green) with a width about several tens unit-cells (Fig. 7a, which is consistent with Fig. 2e), we note that the  $90^\circ$  NCDW is much sharper (Fig. 7b). To visually show the differences among the uncharged, positively and negatively-charged  $90^\circ$  DWs, in-plane lattice gradient of the out-of-plane lattice spacing are mapped. The lattice gradient is defined as  $|c_{x+1} - c_x|/1\text{U.C.}$ , where  $c_x$  denotes an out-of-plane lattice spacing and  $c_{x+1}$  denotes the out-of-plane lattice spacing of the right neighbor unit-cell of  $c_x$ , and ‘unit-cell’ is abbreviated as ‘U.C.’, (Fig. 7c, d). The uniform dark blue means there is no in-plane lattice gradient since there is no lattice change in a single domain. The sudden change of lattice  $c$  to  $a$  (or  $a$  to  $c$ ) across the  $90^\circ$  UCDWs makes obvious contrast in figure 7c, d. The maximum of the lattice gradient is about 0.01 to 0.015 nm/U.C. across the  $90^\circ$  UCDWs. It is clear that the left  $90^\circ$  UCDW in figure 7c terminates in the matrix, which results in the formation of the  $90^\circ$  PCDW. Compared with the uncharged DWs, the lattice gradient of the  $90^\circ$  PCDW is invisible (Fig. 7c), this means the lattice change across the  $90^\circ$  PCDW is much slower. Such a status is also seen in figure 2e. However, the  $90^\circ$  NCDW possesses visible lattice gradient (Fig. 7d). Moreover, the lattice gradient of the upper segment is comparable to the  $90^\circ$  UCDW (note that their color-scales are almost the same). Nevertheless, as seen in figure 7d, the color-scale of the  $90^\circ$  NCDW changes gradually from green to light blue as the DW tracing from top to bottom. This indicates that when the  $90^\circ$  NCDW reaches the PTO/STO interface, the lattice gradient is continuously relieved. In addition, the DW is broadened simultaneously with relief of the lattice gradient, as marked with the violet dotted lines (Fig. 7d). Such a status is also seen in figure 5m.

The  $P_s$  angles of each unit-cell near the  $90^\circ$  PCDW and  $90^\circ$  NCDW are also mapped (Fig. 7e, f). It is seen that the  $P_s$  directions change rapidly across the  $90^\circ$  UCDWs, behaving like their lattice gradient. However, the  $P_s$  directions at the  $90^\circ$  PCDW are strongly disordered (see the color fluctuation in Fig. 7e). Moreover, this wedgy disordered area is much broader than the uncharged ones with tens



**Figure 7** | 2-D mappings of structural and electric behaviors showing the differences between  $90^\circ$  CDWs and  $90^\circ$  UCDWs. (a, b) Out-of-plane lattice spacing mapping for the  $90^\circ$  PCDW and NCDW. (c, d) Lattice gradient mappings (lattice gradient of the out-of-plane lattice mappings along in-plane direction, mapped unit-cell by unit-cell) for the two types of domains. Note the alleviated lattice gradient across the  $90^\circ$  CDWs, especially of the  $90^\circ$  PCDW, compared with sharp lattice gradient across the  $90^\circ$  UCDWs. (e, f)  $P_s$  angle mappings for the two types of domains. The definition of  $0^\circ$ ,  $90^\circ$ ,  $180^\circ$ , and  $270^\circ$  are marked with colored arrows with corresponding color-scale. In case of the  $90^\circ$  PCDW, the  $P_s$  angles are markedly disordered.

of unit-cells at the bottom. For the  $90^\circ$  NCDW, the change of  $P_s$  angles are much sharper than those of the  $90^\circ$  PCDW. This is almost comparable to the  $90^\circ$  UCDWs for the upper segment and just somewhat relieved for the lower segment (Fig. 7f).

## Discussion

Although the  $180^\circ$  CDWs are common in uniaxial<sup>42,44</sup> and possible in multiaxial ferroelectrics<sup>14,45</sup>, the  $90^\circ$  CDW in tetragonal ferroelectrics in our experiments is the first direct atomic-scale observation. Generally, it is proposed that internal charge carriers, for example, oxygen vacancies or electron holes, can screen the bound charges accompanying with the CDW<sup>3,42,45,46</sup>, thus the CDW could be stabilized. In the case of present PTO/STO films, it is proposed that the charge carriers are probably oxygen vacancies ( $\text{Vo}^{2+}$ ), which possess positive charges screening the negative bound charges induced by the  $90^\circ$  NCDW. This inference is constant with our observation because the  $90^\circ$  NCDW is less disturbed compared with the  $90^\circ$  PCDW, and the later probably deserved a depletion layer of  $\text{Vo}^{2+}$ , which was repulsed by the positive bound charges<sup>44</sup>. In addition, for ferroelectrics with a specific charge carriers (positive, such as  $\text{Vo}^{2+}$  and electron holes, or negative, such as electrons), only one kind of CDW can be effectively screened<sup>42,44</sup>. On this condition, if a ferroelectric possesses both PCDW and NCDW simultaneously, only one kind of CDW could be neutralized, that is probably the situations of our

present observation, which was proposed in theoretical work<sup>42</sup>. Our results suggest the lattice and polarization are coupled ideally for all kinds of  $90^\circ$  DWs in PTO. This is remarkably different from the decoupling observed by AFM and PFM in  $\text{BaTiO}_3$  (Refs. 47) which showed the polarization distribution is much wider than that of lattice.

The charge carrier accumulation was hypothesized to be a cause for the increased conductivity at the CDWs in ferroelectrics<sup>3,44</sup>. In hexagonal ferroelectric  $\text{HoMnO}_3$ , the widths of  $180^\circ$  PCDW and NCDW were also found to be different, based on the conductive atomic force microscopy (cAFM) observation where the DW width was absent from atomic-scale information limited by the AFM tip radius. In tetragonal  $\text{PbTiO}_3$  films of the present study, the difference between the  $90^\circ$  PCDW (carrier depletion) and NCDW (carrier accumulation) at atomic scale may qualitatively explain the different conduction behaviors between ‘head-to-head’ and ‘tail-to-tail’  $180^\circ$  DWs in  $\text{HoMnO}_3$  (ref. 44). In addition, the coupling of  $P_s$  and elastic strain for the  $90^\circ$  DWs is much stronger than the  $180^\circ$  DWs<sup>8,10–12</sup>. This implies that, during the  $180^\circ$  switching the  $90^\circ$  CDWs may generally exist, at least in a dynamical style. Earlier PFM studies showed that this kind of  $90^\circ$  CDWs may play an important role for the retention failure of the PZT memories because the switched  $180^\circ$  domains could be reversed by the  $90^\circ$  CDW as time elapses<sup>48,49</sup>.

In summary, by using aberration-corrected STEM, the unusual frustration of dipole arrangements and strain behaviors of  $90^\circ$



CDWs in PTO/STO multilayer films are identified on the atomic-scale, where the widths, polarization distributions, and strains across these charged domain walls are mapped quantitatively. “Glass-like” dipole behaviors are observed at the  $90^\circ$  CDWs. We anticipate the present atomic-scale investigations of the uncharged and charged  $90^\circ$  DWs may help to interpret the switching behaviors, the newly realized domain-wall functions, and the retention failure mechanism in ferroelectrics. Moreover, the present study is expected to clarify the long-standing argument about the width of the  $90^\circ$  DWs in tetragonal ferroelectrics. During the review stage of this paper, a research group in Michigan University reported an occurrence of  $90^\circ$  charged domain walls in  $\text{Pb}(\text{Zr}_{0.2}\text{Ti}_{0.8})\text{O}_3$  thin films formed by in-situ electric response<sup>50</sup>.

## Methods

**Thin-film synthesis and STEM sample preparations.** The  $\text{PbTiO}_3/\text{SrTiO}_3$  thin films were deposited on  $\text{GdScO}_3$  substrates by pulsed laser deposition (PLD), using a Lambda Physik LPX 305i KrF ( $\lambda = 248$  nm) excimer laser. The  $\text{PbTiO}_3$  targets were 3 mol% Pb-enriched sintered ceramics. The target-substrate distance was 40 mm. The background pressure was  $10^{-5}$  Pa. During the growth of  $\text{PbTiO}_3$ , the substrate temperature was kept at  $650^\circ\text{C}$ , with a laser energy density of  $2\text{ Jcm}^{-2}$ , a laser repetition rate of 5 Hz and under an oxygen pressure of 20 Pa. For the growth of  $\text{SrTiO}_3$  layers, the substrate temperature was also  $650^\circ\text{C}$ , with a laser energy density of  $1\text{ Jcm}^{-2}$ , a laser repetition rate of 2 Hz and under an oxygen pressure of 8 Pa. Before deposition, the  $\text{GdScO}_3$  substrate was pre-heated at  $750^\circ\text{C}$  for 5 min to clean the substrate surface and then cooled down to the growth temperature ( $10^\circ\text{C}/\text{min}$ ). The laser was focused on the ceramic target for 30 min pre-sputtering to clean the target surface. After deposition, the film was in-situ-annealed at  $650^\circ\text{C}$  in an oxygen pressure of  $5 \times 10^4$  Pa for 10 min, and then cooled down to room temperature at a cooling rate of about  $5^\circ\text{C}/\text{min}$ . The samples for the STEM experiments were prepared by slicing, gluing, grinding, dimpling, and finally ion milling. A Gatan PIPS was used for the final ion milling.

**STEM imaging and analysis.** One of the great advantages of HAADF-HRSTEM imaging mode is that it is not sensitive to the variety of local specimen thickness, and therefore, it is quite suitable for large-scale imaging. The finding of the novel domain configurations in the relatively large scale in this work is believed to benefit from the HAADF imaging mode. In addition, the aberration-corrected TEM used in this study features very little drift; for example, the STEM spot drift and specimen drift are  $0.14\text{ nm}/\text{min}$  and  $0.16\text{ nm}/\text{min}$ , respectively. HAADF images in this study were recorded using aberration-corrected scanning transmission electron microscopes (Titan Cubed 60–300 kV microscope (FEI) fitted with a high-brightness field-emission gun (X-FEG) and double Cs correctors from CEOS, and a monochromator operating at 300 kV). The convergence angle of the electron beam is 25 mrad, yields a probe size of less than 0.10 nm. The determination of the atom coordinates in the HAADF-STEM images were carried out by fast Fourier transform (FFT) filtering the images using only a low-pass annular mask restricted slightly more than the resolution limit of the image, thus the lattice spacing and  $\text{Ti}^{4+}$  shifts ( $\delta_{\text{Ti}}$ ) were deduced. The atom positions were determined accurately by fitting them as 2D Gaussian peaks by using Matlab<sup>14,33,34,51</sup>. The  $\delta_{\text{Ti}}$  were calculated as a vector between each  $\text{Ti}^{4+}$  and the center of mass of its four nearest A-site neighbor  $\text{Pb}^{2+}$ . The  $P_s$  vectors were deduced by the  $\delta_{\text{Ti}}$ . The visualization of the 2D  $P_s$  vectors (Fig. 3 and Fig. 6) was carried out using Matlab. The visualization of the lattice, lattice gradient and  $P_s$  angles (Fig. 7) was carried out using the combination of Matlab and ImageJ software<sup>34</sup>.

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## Author contributions

The project of interfacial STEM characterization in oxides was conceived by Y.L.Z. and X.L.M.; thin film growth, TEM specimen preparation and STEM observations were performed by Y.L.T.; Y.J.W. participated digital analysis of the HAADF-STEM images; W.Y.W., Y.B.X., W.J.R. and Z.D.Z. have contributions in thin film growth; Y.L.T., Y.L.Z. and X.L.M. jointly interpreted the data and wrote the paper.

## Additional information

**Competing financial interests:** The authors declare no competing financial interests.

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