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# Magneto-optical fingerprints of distinct graphene multilayers using the giant infrared Kerr effect

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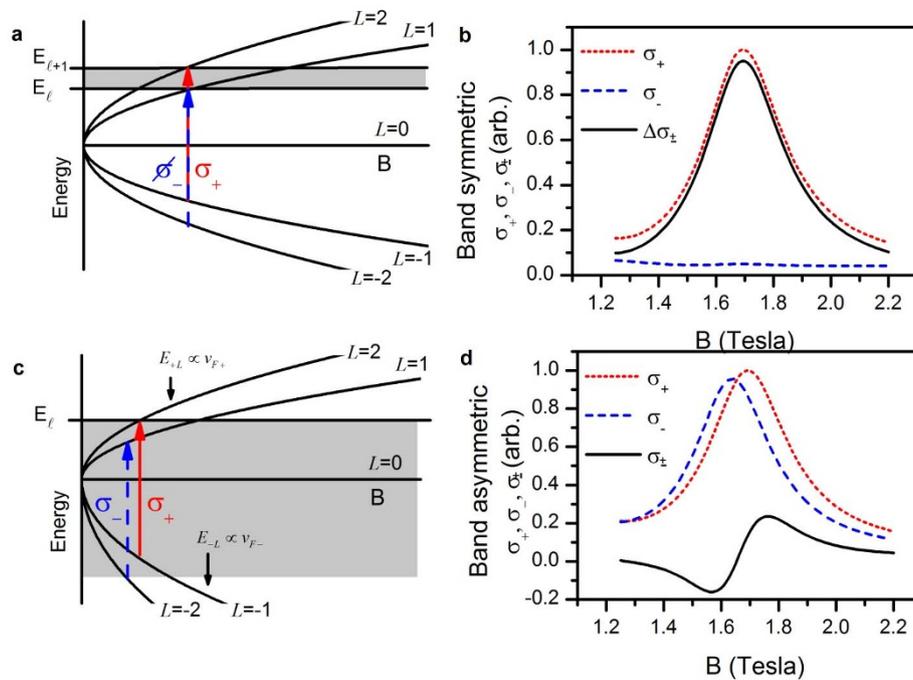
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The remarkable electronic properties of graphene strongly depend on the thickness and geometry of graphene stacks. This wide range of electronic tunability is of fundamental interest and has many applications in newly proposed devices. Using the mid-infrared, magneto-optical Kerr effect, we detect and identify over 18 interband cyclotron resonances (CR) that are associated with ABA and ABC stacked multilayers as well as monolayers that coexist in graphene that is epitaxially grown on 4H-SiC. Moreover, the magnetic field and photon energy dependence of these features enable us to explore the band structure, electron-hole band asymmetries, and mechanisms that activate a CR response in the Kerr effect for various multilayers that coexist in a single sample. Surprisingly, we find that the magnitude of monolayer Kerr effect CRs is not temperature dependent. This unexpected result reveals new questions about the underlying physics that makes such an effect possible.

The discovery of a stable monolayer flake of graphene by Novoselov et al.<sup>1</sup> set off a massive investigation of the remarkable properties of mono- and multilayer graphene. The simple hexagonal carbon lattice of monolayer graphene results in a unique linear dispersion with low energy excitations that are massless and relativistic. From these characteristics arise fascinating properties such as square root magnetic field ( $B$ ) dependence of the cyclotron resonance (CR) frequency, a lowest Landau level (LL) independent of  $B$ , anomalous chiral quantum Hall effects<sup>2</sup>, unusual magnetic field and Fermi energy dependence of the AC Hall conductivity<sup>3</sup>, and the presence of a finite longitudinal conductivity  $\sigma_{xx}$  without charge carriers<sup>4</sup>. Studies of multilayer graphene have proven equally interesting due to the existence of massive Dirac fermions, unique broken symmetry states<sup>5</sup>, and the existence of a readily tunable bandgap<sup>6–8</sup>. In addition, the electronic structure of multilayer graphene is highly dependent upon the stacking geometry and thickness of layers, yielding a wide range of electronic tunability for graphene systems<sup>17,18,24</sup>. To that end, both scientists and engineers alike have been fascinated by graphene and all of its possible applications, such as high frequency analog ballistic transistors<sup>8–10</sup>, surface enhanced spectroscopy<sup>2–4</sup>, photo-detectors<sup>11</sup>, transparent conductors<sup>13</sup>, and as proposed in this Report, ultra-fast optical modulators and tunable polarizers.

When placed in an out-of-plane magnetic field, multilayer graphene's electronic bands condense into discrete energy states (LLs) that are especially sensitive to the coupling strength between layers. This coupling strength is dependent upon the relative orientation of layers and the total number of layers in a graphene stack. Graphene's strong dependence on interlayer coupling has been demonstrated many times for monolayer<sup>5–7</sup> (uncoupled) and bilayer<sup>7–9</sup> (coupled) graphene, which yield LL energies proportional to  $\sqrt{B}$  and  $B$ , respectively. In this study we systematically investigate the effect of more complicated coupling schemes that are obtained from thicker graphene multilayers with various stacking geometries. This is especially of interest since studies suggest that interlayer coupling may play a role in producing asymmetries between the conduction and valence band energies, where band asymmetry has been attributed to the twisting of adjacent layers<sup>10</sup> and next nearest neighbor interactions<sup>11</sup> (trigonal warping effects). However, experiments have also shown that metal electrical contacts on graphene<sup>12,13</sup> may be responsible for band asymmetry, which is consistent with the absence of an observable band asymmetry in unprocessed graphene samples<sup>11,14,15</sup>.



**Figure 1 | Illustration of chiral symmetry breaking mechanisms caused by: (a,b) Pauli blocking of LLs and (c,d) electron hole band asymmetry.** (a) LL energies vs  $B$  for monolayer graphene with symmetric electron-hole bands. For this mechanism, optical chiral symmetry is broken when  $E_\ell < E_F < E_{\ell+1}$  (grey shaded region), which results in the Pauli blocking of  $-\ell-1 \rightarrow \ell$  LL transitions at CR. (b) Calculation of optical conductivities ( $\tilde{\sigma}_+ \neq 0$  and  $\tilde{\sigma}_- \simeq 0$ , red-dotted and blue-dashed curve, respectively) and broken chiral symmetry ( $\Delta\tilde{\sigma}_\pm = \tilde{\sigma}_+ - \tilde{\sigma}_- \neq 0$ , black curve) for Pauli-blocked, band-symmetric graphene. (c) LL energies vs  $B$  for monolayer graphene with an electron-hole band asymmetry ( $|E_L| \neq |E_{-L}|$ ). For this mechanism, optical chiral symmetry is broken by lifting the degeneracy between  $-\ell-1 \rightarrow \ell$  and  $-\ell \rightarrow \ell+1$  transitions, which occurs for a broad range of Fermi energies ( $-E_\ell < E_F < E_{\ell+1}$ , grey shaded region). (d) Calculation of the optical conductivities ( $\tilde{\sigma}_+ \neq 0$  and  $\tilde{\sigma}_- \neq 0$ , red-dotted and blue-dashed curve, respectively) and broken chiral symmetry ( $\Delta\tilde{\sigma}_\pm = \tilde{\sigma}_+ - \tilde{\sigma}_- \neq 0$ , black curve) for graphene with an electron-hole band asymmetry.

In this Report, we use graphene multilayers that vary in thickness and stacking geometry to experimentally investigate how *interlayer coupling* affects graphene's magneto-electronic structure. We achieve this by using magneto-optical, polarization-sensitive, mid-infrared (MIR, 110–224 meV) spectroscopy to study how CRs in multilayer graphene evolve with magnetic field strength ( $B$ ), photon energy ( $E_{ph}$ ), and temperature ( $T$ ). From these measurements we: 1) experimentally demonstrate the validity of theoretical work outlining the LL structure of monolayer<sup>16</sup>, ABA Bernal bilayer and trilayer<sup>17</sup>, and ABC rhombohedral trilayer graphene<sup>18</sup>; 2) reveal an anomalous temperature dependence of monolayer CRs with implications for broadband, room-temperature optoelectronic devices; and 3) find no detectable band asymmetry in our samples. The last point is of particular interest since our samples are epitaxially grown and require no post-processing for our measurements; thus, the absence of asymmetry strongly suggests that band asymmetry is not intrinsic to graphene. Rather, processing techniques may play a role in enhancing band asymmetry. Furthermore, our measurements indicate that the large polarization response that we observe is activated by Pauli blocking certain LL transitions. This effect opens the door to new high-speed devices that can control the polarization of infrared light through electrostatic gating, even at elevated temperatures.

The polar magneto-optical Kerr effect (MOKE) is the change in light polarization upon reflection from a sample placed in an out-of-plane magnetic field (see Methods section for experimental setup). Changes in the polarization are characterized by the complex Kerr angle  $\tilde{\theta}_K$ , where the real and imaginary components are proportional to changes in orientation and ellipticity of the reflected polarization, respectively. In contrast to conventional infrared transmission/reflection measurements that probe the average response of the sample to left and right circularly polarized light, the MOKE signal is proportional to the difference in response for opposite handedness of

circularly polarized light (i.e.,  $\tilde{\theta}_K \propto \Delta\tilde{\sigma}_\pm = \tilde{\sigma}_+ - \tilde{\sigma}_-$ , where  $\tilde{\sigma}_+$  and  $\tilde{\sigma}_-$  are the complex optical conductivities for left and right circularly polarized light, respectively), making it especially sensitive to optical chiral asymmetry ( $\tilde{\sigma}_+ \neq \tilde{\sigma}_-$  or  $\Delta\tilde{\sigma}_\pm \neq 0$ ).

To discuss the expected Kerr effect for graphene, we first consider the simple case of a single monolayer with symmetric electron-hole bands. When applying an out-of-sample-plane magnetic field to graphene, the electronic states condense into discrete energy LLs. For monolayer graphene the LL energies are defined as

$$E_L = \text{sign}(L) \cdot v_F \sqrt{2e\hbar|BL|}, \quad (1)$$

where  $v_F$  is the Fermi velocity,  $L$  is an integer that enumerates the LLs,  $L \geq 0$  and  $L \leq 0$  define the conduction (electron-like) and valence (hole-like) band LL energies, respectively, and  $B$  is the magnetic field strength. As shown in Figure 1a, when the photon energy ( $E_{ph}$ ) satisfies the CR condition ( $E_{ph} = E_L - E_{-L}$ ), graphene's two equal-energy interband LL transitions  $-\ell \rightarrow \ell+1$  and  $-\ell-1 \rightarrow \ell$  are excited, where  $\ell$  is a positive integer that enumerates all possible LL transitions (not to be confused with  $L$ , which is used to enumerate individual LLs). The two allowed transitions absorb the opposite handedness of circularly polarized light (see Figure 1a). Thus, through MOKE measurements we probe asymmetries that exist between the allowed interband transitions in graphene. Such an asymmetry can be caused by two mechanisms: 1) Pauli blocking the  $-\ell-1 \rightarrow \ell$  LL transitions, as illustrated in Figure 1a, b, which yields  $\tilde{\sigma}_- = 0$ ,  $\tilde{\sigma}_+ \neq 0$ , and  $\tilde{\theta}_K \propto \Delta\tilde{\sigma}_\pm \neq 0$  and 2) an electron-hole band asymmetry ( $E_L \neq E_{-L}$ ), which breaks the LL transition energy degeneracy and shifts the left- and right-handed CRs to different  $B$ -values, for equal photon energies (Figure 1c, d). As discussed later, graphene multilayers yield a more complicated LL energy spectrum than monolayers; however, the LL optical selection rules ( $\Delta L = \pm 1$ )



and mechanisms that cause CR features to appear in the Kerr angle data are the same.

Our samples consist of graphene that is epitaxially grown on the carbon terminated face of silicon carbide (C-SiC)<sup>19,20</sup> (see Methods Section for sample details). These samples are ideally suited for our study since C-SiC graphene films are typically comprised of small domains that widely vary in layer thickness and stacking order. Thus, we can study many forms of graphene that coexist in a single sample. Furthermore, these graphene films are known to have high optical mobilities<sup>19,21</sup> ( $200000 \text{ cm}^2\text{V}^{-1}\text{s}^{-1}$ ) that are required in order to observe CR at modest magnetic fields<sup>51</sup>.

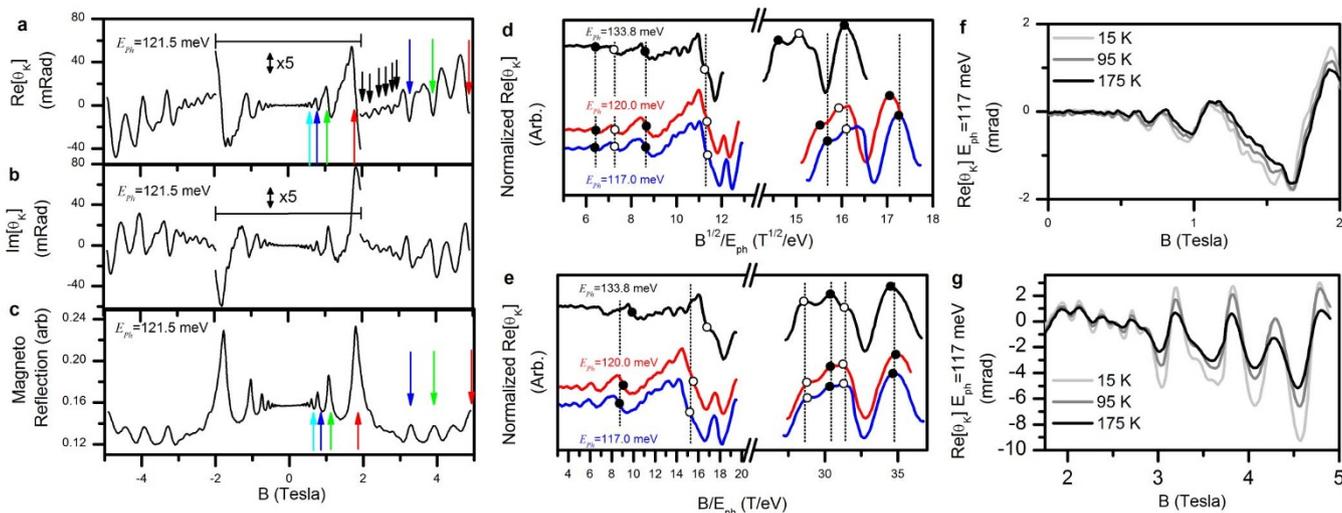
## Results

**Monolayer and bilayer contributions to the Kerr angle.** Figure 2a–c shows typical results of Kerr angle measurements performed on multilayer C-SiC graphene. We measure  $\tilde{\theta}_K$  as a function of  $B$ , with a fixed photon energy ( $E_{ph} = 114.5\text{--}133.8 \text{ meV}$ ,  $230\text{--}250 \text{ meV}$ ) and temperature ( $T = 15\text{--}175 \text{ K}$ ). The data display two distinct sets of CR transition features. The first set, lying in the region  $|B| < 2 \text{ T}$  is caused by interband LL transitions in monolayer graphene, as indicated by the square-root  $B$  scaling ( $\sqrt{B}$ ) of the CR energies versus  $E_{ph}$ , shown in Figure 2d. This monolayer response results from rotational stacking faults that frequently occur in C-SiC graphene<sup>22,23</sup>, which effectively decouple adjacent layers<sup>5,24–26</sup>. The second set of CRs is found throughout the entire magnetic field range; however, the strongest features occur for  $|B| > 2 \text{ T}$ . These CRs are characteristic of LL transitions with energies that vary linearly with  $B$  (linear- $B$ ), shown in Figure 2e. This behavior is consistent with expectations for ABA<sup>17</sup> and ABC<sup>18</sup> multilayers, where significant interlayer coupling results in LL energies that evolve linearly with  $B$ . The most prominent CR Kerr features yield changes in the polarization up to 60 mrad at  $B = 5 \text{ T}$ . The large magnitude of these polarization changes is comparable to those observed in transmitted far-infrared (FIR,  $10\text{--}80 \text{ meV}$ ) radiation<sup>27</sup>. However, the highly doped graphene layers measured in the FIR work<sup>27</sup> resulted in a large, classical CR polarization response with

$E_L \propto B$ . For our work the  $\sqrt{B}$  nature of MIR CRs indicates that our multilayers are not in the classical CR regime. We also measured  $\tilde{\theta}_K$  at elevated temperatures as high as 175 K. Interestingly, the magnitude of the CR Kerr features for mono- and multilayer graphene show strikingly different temperature dependences. As depicted in Figure 2f, g, changes in the magnitude of monolayer Kerr effect CRs with increasing temperature are negligible, while linear- $B$  features undergo a 34% reduction in their magnitude over the range of  $15\text{--}175 \text{ K}$ . As discussed later in this Report, the nearly constant behavior of monolayer features at high temperatures is not expected.

The long downward arrows in Figure 2a, c mark the three most distinct linear- $B$  features that are associated with LL transitions between the upper valence and lower conduction bands in AB bilayer graphene<sup>17,28</sup>. It is surprising that AB bilayers produce such large CR Kerr features since both theory and experiments show that stability is reduced for AB multilayers in C-SiC<sup>8,29</sup>. Previous magneto-optical transmission measurements reveal that AB bilayers are 10 times more scarce than monolayers in C-SiC graphene samples, as indicated by the relative strengths of strong and weak CR absorption features observed for monolayer and AB bilayers<sup>8</sup>, respectively. Our magneto-optical reflectivity measurements agree with the previous transmission results, where we see a significantly stronger signal associated with the compositionally dominant graphene monolayer response (see  $|B| < 2 \text{ T}$  features in Figure 2c). However, our Kerr angle data show the opposite effect, where AB bilayer CR features have a much larger magnitude than features associated with monolayer graphene. This indicates that the magnitude of  $\tilde{\theta}_K$  does not reflect the relative proportion of the various forms of graphene that coexist in a single sample. Additionally, many of the linear- $B$  CRs that appear in the MOKE measurements do not appear in the magneto-reflectivity, indicating that  $\tilde{\theta}_K$  is significantly more sensitive to small traces of multilayer graphene.

**Multilayer contributions to Kerr angle data.** While determining the spectral contributions to  $\tilde{\theta}_K$  from monolayer and AB stacked bilayer graphene is straightforward, understanding the cause of the



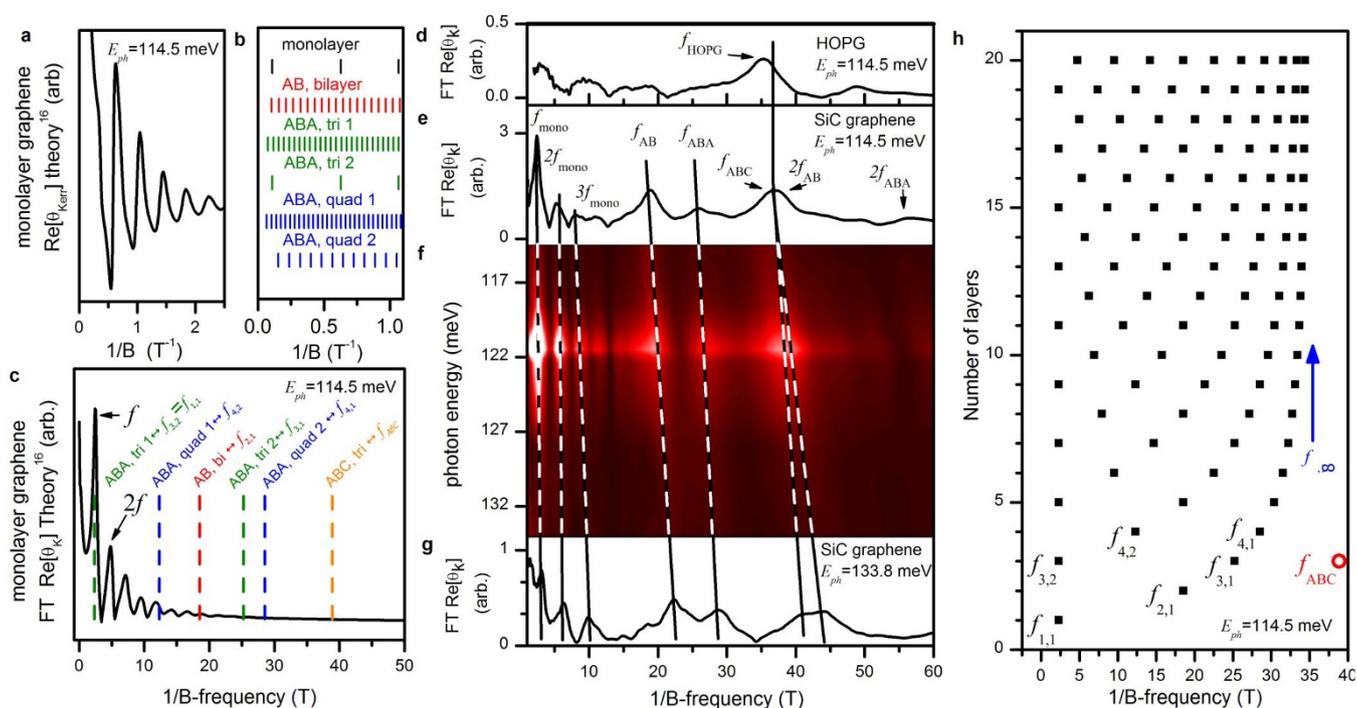
**Figure 2 | General structure of (a) Kerr rotation  $\text{Re}[\theta_K]$ , (b) Kerr ellipticity  $\text{Im}[\theta_K]$ , and (c) magneto-reflection for  $E_{ph} = 121.5 \text{ meV}$ . The Kerr angles are magnified by a factor of 5 for  $|B| < 2 \text{ T}$  showing monolayer LL transition features with  $E_L \propto \sqrt{B}$  behavior (up arrows). Structure in the range  $|B| > 2 \text{ T}$  corresponds to LL transition features with  $E_L \propto B$ . Long and short down arrows correspond to features associated with AB bilayer and thicker ABA/ABC stacked multilayer graphene, respectively. (d) Kerr data at three photon energies with the horizontal axis rescaled to  $\sqrt{B}/E_{ph}$ . A vertical alignment of the CRs indicates  $\sqrt{B}$  scaling of LL energies. Features at low  $B$  clearly show this behavior, suggesting that they correspond to CR in monolayer graphene. (e) Kerr data at three photon energies with horizontal axis rescaled to  $B/E_{ph}$ . A vertical alignment of the CRs indicates linear- $B$  scaling of LL energies. Features at high  $B$  clearly show this behavior suggesting that they correspond to interband LL transitions in ABA and ABC multilayer graphene. (f) Temperature dependence of  $\sqrt{B}$  features. Negligible changes occur for temperature ranging from  $15\text{--}175 \text{ K}$ . (g) However, linear- $B$  features decrease by 34% at 175 K.**



other smaller linear- $B$  features, depicted by the small down arrows in Figure 2a, is not easily accomplished. The increased complexity of these data arises from the large variety of multilayers known to exist in C-face samples<sup>29,30</sup>, each having a unique LL spectrum<sup>17,18</sup>. In particular, ABA stacked graphene with  $N$  layers complicates the magneto-optical response, since each multilayer contributes at least  $N/2$  distinct sets of CRs. To simplify and better understand the many contributions to our Kerr angle measurements, we exploit the periodic occurrence of graphene's LL transitions versus inverse magnetic field strength ( $1/B$ ). This enables the use of Fourier analysis to reveal CR  $1/B$ -frequency components that correspond to each form of multilayer graphene (hereafter, we refer to this technique as Fourier transform Kerr spectroscopy or FTKS). For example, Figure 3a shows the periodic behavior of  $\text{Re}[\theta_K]$  for monolayer graphene versus  $1/B$ , which is calculated from the complex optical response functions determined by Gusynin et al.<sup>16</sup>. As indicated in Figure 3b, ABA multilayers also produce periodic CR Kerr features versus  $1/B$ . These  $1/B$ -periods can be detected as  $1/B$ -frequencies ( $f$ ) when applying Fourier analysis to the MOKE signal versus  $1/B$ . Figure 3c shows the results of applying this technique to the theoretical Kerr angle response of monolayer graphene, calculated in Figure 3a. Clear peaks are seen at  $f$  and higher harmonics ( $2f, 3f, \dots$ ), where the latter results from the non-sinusoidal-behavior the Kerr/CR response versus  $1/B$ . The frequencies detected by FTKS act as a fingerprint for different types of graphene since  $f$  is strongly dependent upon the number

of layers  $N$  and stacking geometry that make up a multilayer (See Supporting Note 1). Thus, FTKS is capable of separating and identifying many different multilayer contributions that coexist in the large probe area of our measurements ( $9 \text{ mm}^2$ ). Applying the FTKS technique to the measured data dramatically simplifies the signal, as displayed in Figure 3e–g. In total, seven large  $1/B$ -frequency peaks are seen in the FTKS spectrum. These observed  $1/B$ -frequencies are consistent with the theoretical expectations for monolayers as well as AB and ABC stacked graphene multilayers.

For  $E_{ph} = 114.5 \text{ meV}$  (Figure 3e) we find multiple peaks corresponding to fundamental and higher harmonic  $1/B$ -frequencies that are characteristic of monolayer graphene ( $f_{mono} = 2.6 \text{ T}$ ,  $2f_{mono} = 5.3 \text{ T}$ ,  $3f_{mono} = 8.0 \text{ T}$ ). These peaks indicate the presence of rotationally-faulted layers and/or AB multilayers with odd  $N$ , where the latter contribution will be discussed later in this Report. At higher  $f$ , several peaks occur that are consistent with the theoretical expectations for ABA multilayers<sup>17</sup>. The peaks observed at  $f_{AB} = 18.4 \text{ T}$  and  $f_{ABA} = 25.8 \text{ T}$  correspond to stacked AB bilayer and ABA trilayer graphene, respectively. These  $1/B$ -frequencies are in good agreement with theory<sup>17</sup>, where the magneto-optical response of ABA multilayers ( $N \geq 2$ ) is determined by dividing the system up into sublayers and summing over their individual spectral contributions. For ABA graphene multilayers with an even (odd) number of layers there are  $M = N/2$  ( $M = (N + 1)/2$ ) sublayers. Thus, a single AB multilayer with  $N \geq 2$  is broken down into  $M$  sublayers. Each sublayer contributes a full set of LL



**Figure 3** | (a) Theoretical prediction<sup>16</sup> of  $\text{Re}[\theta_K]$  for monolayer graphene versus  $1/B$ , revealing periodic behavior ( $E_{ph} = 114.5 \text{ meV}$ ). (b) Positions of periodic transition features versus  $1/B$  for monolayer and ABA multilayer graphene, as predicted by Koshino and Ando<sup>17</sup> ( $E_{ph} = 114.5 \text{ meV}$ ,  $\gamma_{bi} = 0.4 \text{ eV}$ ). Note, as predicted by Ref. 17, two sets of periodic transitions for tri- and quadlayer graphene. (c) Fourier transformed Kerr spectrum (FTKS) for monolayer graphene calculated from the curve in Figure 2a, showing a clear fundamental  $1/B$ -frequency ( $f_{mono}$ ) and higher harmonics ( $2f_{mono}, 3f_{mono}, \dots$ ). In addition, the predicted  $1/B$ -frequency positions of thicker ABA multilayers are indicated by vertical dashed lines. (d) Measured FTKS spectrum of HOPG for  $E_{ph} = 114.5 \text{ meV}$ . (e) SiC graphene FTKS data for  $E_{ph} = 114.5 \text{ meV}$  marking frequency positions of monolayer ( $f_{mono}$ ), AB bilayer ( $f_{AB}$ ), ABA trilayer ( $f_{ABA}$ ), ABC trilayer ( $f_{ABC}$ ), and their higher harmonics. (f) Photon energy dependence of FTKS. Dark and light areas indicate low and high FTKS magnitudes, respectively. The weakening of the Kerr response away from  $E_{ph} = 121 \text{ meV}$  is associated with the Reststrahlen band of SiC. (g) SiC graphene FTKS data for  $E_{ph} = 133.8 \text{ meV}$  showing multilayer peaks. Note that the  $f_{ABC}$  and  $2f_{AB}$  peaks are separated at this photon energy, as expected (see Supporting Note 2 for details). (h)  $1/B$ -frequencies  $f_{N-m}$  predicted<sup>17</sup> for the  $m^{\text{th}}$  sublayer of ABA multilayers with  $N$  layers (black, square symbols). Frequencies are calculated for  $E_{ph} = 114.5 \text{ meV}$  and  $\gamma_{bi} = 0.4 \text{ eV}$ . We also show the predicted  $1/B$ -frequencies for ABC trilayer<sup>7</sup> ( $f_{ABC}$ , red, empty circle) and bulk ABA stacked graphite<sup>50</sup> ( $f_{\infty-1}$ , blue arrow).



transitions. Thus, for every multilayer there are  $M$  unique sets of CRs and  $M$  distinct  $1/B$ -frequency components. The LL energies for each sublayer are given by<sup>17</sup>

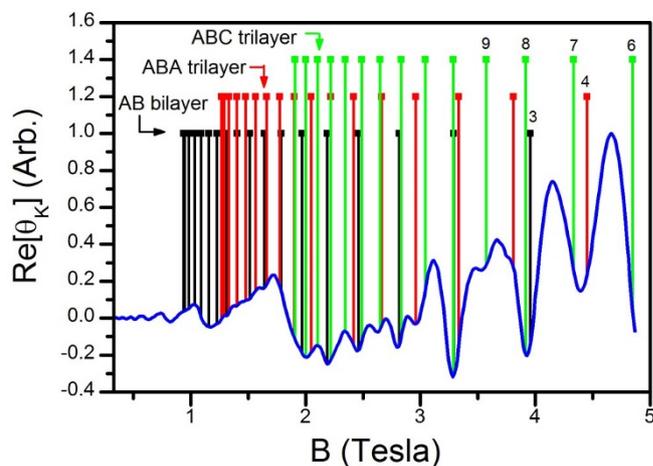
$$E_{N,m,L} = \frac{\text{sign}(L)}{\sqrt{2}} \left[ (\lambda_{N,m}\gamma_{bi})^2 + (2L+1)\Delta_B^2 - \sqrt{(\lambda_{N,m}\gamma_{bi})^4 + 2(2L+1)(\lambda_{N,m}\gamma_{bi})^2\Delta_B^2 + \Delta_B^4} \right]^{1/2}, \quad (2)$$

$$\lambda_{N,m} = 2 \cos\left(\frac{m\pi}{N+1}\right),$$

where  $m$  is an integer enumerating each sublayer,  $L$  is the usual LL index,  $\lambda_{N,m}$  is a scaling factor,  $\gamma_{bi}$  is the interlayer coupling for isolated AB bilayer graphene, and  $\Delta_B = v_F\sqrt{2\hbar e|B|}$  is the magnetic energy. In this formulation each sublayer yields LLs that are reminiscent of those expected for an AB bilayer with a scaled interlayer coupling ( $\lambda_{N,m}\gamma_{bi}$ ). Using equation (2), we numerically determine the unique  $1/B$ -frequencies  $f_{N,m}$  for each sublayer, as shown in Figure 3h. In the special case of multilayers with an odd number of AB stacked graphene layers ( $N_o$ ), the sublayer index  $m_o = (N_o + 1)/2$  produces  $\lambda_{N_o,m_o} = 0$ , yielding an effective interlayer coupling of zero and sublayer LLs that are equivalent to monolayer graphene [i.e., equation (2) reduces to equation (1)]. Thus, ABA trilayer graphene will yield both monolayer  $f_{mono} = f_{3,1}$  and bilayer  $f_{ABA} = f_{3,2}$  FTKS peaks, as shown in Figure 3b, c. The observed  $f_{ABA} = f_{3,1}$ ,  $f_{AB} = f_{2,1}$  and  $f_{mono} = f_{1,1}$  peaks agree with the theoretical  $1/B$ -frequencies that are shown in Figure 3h. We also observe a peak in the FTKS data near 36.3 T (labeled as  $2f_{AB}$  and  $f_{ABC}$  in Figure 3e), which is consistent with predictions for both the second harmonic AB bilayer and fundamental ABC trilayer components<sup>18</sup> (see Supporting Note 2 for more details). At higher  $E_{ph}$  these peaks separate, as predicted by theory, allowing them to be clearly distinguished (see Figure 3g). To the best of our knowledge, CRs associated with both ABA and ABC trilayer graphene have not been observed in previous studies, making this data set the first to validate the theories presented by References 17 and 18 for thin graphene multilayers. Note that frequencies characterizing thinner multilayers start re-occurring for thicker multilayers (e.g., see Figure 3h, where  $f_{2,1} = f_{5,2} = f_{8,3}$ ). The fact that only a few frequencies are found in our FTKS results suggests that our C-SiC samples are mostly composed of few-layer graphene. For example, an ABA multilayer with  $N = 11$  is expected to have six peaks; however, such features are not observed in the FTKS spectrum.

Considering the thick nature of our C-SiC graphene films, one may also expect to find graphitic inclusions in our sample. Theory<sup>17</sup> predicts a fundamental ABA graphite FTKS peak near  $f_{\infty,1} = 35$  T for  $E_{ph} = 114.5$  meV (blue arrow in Figure 3h); however, no such features are observed for our samples. The absence of bulk graphite inclusions is also confirmed by performing FTKS measurements on bulk highly ordered pyrolytic graphite (HOPG). Figure 3d shows the results of these measurements, which confirms the existence of a bulk graphite FTKS peak at  $f_{HOPG} = 35.3$  T. This peak is absent in our measurements on C-SiC, as seen by comparing Figures 3d and 3e, indicating that no graphitic inclusions are present in our multilayer graphene sample.

**Band parameter determination.** By exploiting the energy dependence of the FTKS features, shown in Figure 3e–g, we are able to determine the fundamental band parameters for the multilayers present in the sample (see Supporting Note 1 for fitting details), and further confirm the correct associations of each FTKS component. Fits to  $f_{mono}$  and  $f_{AB,bi}$  yield  $v_F = (1.033 \pm .002) \cdot 10^6$  m/s and  $\gamma_{bi} = 399 \pm 4$  meV, respectively. Both parameters are consistent with previous work<sup>10,21,31</sup>. Additionally,  $f_{ABA}$  and  $f_{ABC}$  allow the experimental determination of band parameters for both types of

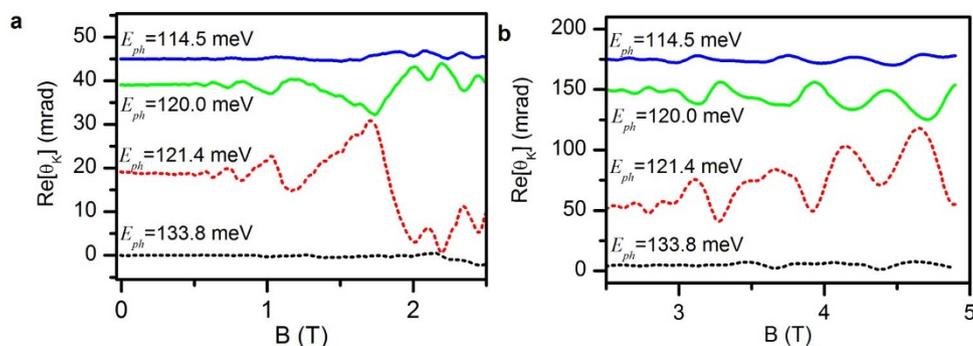


**Figure 4 | Identification of CR features in Kerr angle data vs B.** Predicted CR  $B$ -values for AB bilayers (black droplines), ABA trilayers (red droplines), and ABC trilayers (green droplines). The CR  $B$ -values are calculated using the band parameters determined by the  $E_{ph}$  dependence of the FTKS data (Fig. 3). The calculation explains the appearance of CR features in the Kerr angle data (blue solid curve). Numeric labels denote the starting LL transition index ( $\ell$ ) for each type of multilayer graphene. Larger  $\ell$  occur at lower magnetic fields.

graphene trilayers. The energy dependence of  $f_{ABA}$  yields an effective bilayer interlayer coupling of  $\lambda_{3,1}\gamma_{bi} = 562 \pm 12$  meV, which is in excellent agreement with the expected value that is given by equation 2 ( $\sqrt{2}\gamma_{bi} = 566$  meV), further validating the theory of Koshino and Ando<sup>17</sup>. For ABC trilayer graphene we find  $\gamma_{ABC} = 384 \pm 8$  meV, which is consistent with previous infrared spectroscopy measurements<sup>32</sup>. As shown in Figure 4, by using these experimentally determined band parameters and LL theory for monolayer, ABA multilayer, and ABC multilayer graphene, all major linear- $B$  CR features are accounted for in our  $\theta_K$  data. The energy-dependent FTKS data also show a dramatic increase in the magnitude of  $\tilde{\theta}_K$  (Figures 3e–g and 5a, b) at  $E_{ph} = 121$  meV. The sharp enhancement and sign change of the Kerr features is not due to graphene itself; rather, this effect results from the Reststrahlen band of the SiC substrate, where the Kerr angle is maximized as the substrate index of refraction approaches unity near  $E_{ph} \approx 121$  meV<sup>33</sup>.

**Band asymmetry.** In addition to the band parameters, the symmetry of the conduction and valence bands in graphene is of fundamental interest, since it plays a critical role in shaping the electronic structure. Band asymmetries are widely observed in graphene; however, the mechanism responsible for the band asymmetry depends on the graphene growth technique and the type of sample processing techniques used. In particular, band asymmetries have been attributed to: the twisting of adjacent layers<sup>10</sup>, with asymmetries reaching 14% for smaller rotations ( $\theta \sim 3.5^\circ$ ); electrostatic gating of graphene<sup>12,13</sup>; and next nearest neighbor interactions (trigonal warping effects)<sup>11</sup>. Band asymmetry may play a key role in producing the optical chiral symmetry breaking (i.e.,  $\Delta\tilde{\sigma}_\pm \neq 0$ , Figure 1c, d) necessary to activate the Kerr angle response. Additionally, changes in the Kerr angle may also be caused by the occupation of  $E_\ell$  LL states, which Pauli blocks  $-\ell - 1 \rightarrow \ell$  transitions, as shown in Figure 1a, b. By investigating the  $E_{ph}$  dependence of the Kerr angle we are able to put an upper limit on the magnitude of the band asymmetry for the probed layers and determine that the Kerr angle features are primarily caused by the Pauli blocking mechanism.

The band asymmetry for graphene monolayers can be measured quantitatively by comparing FIR intraband CR measurements,

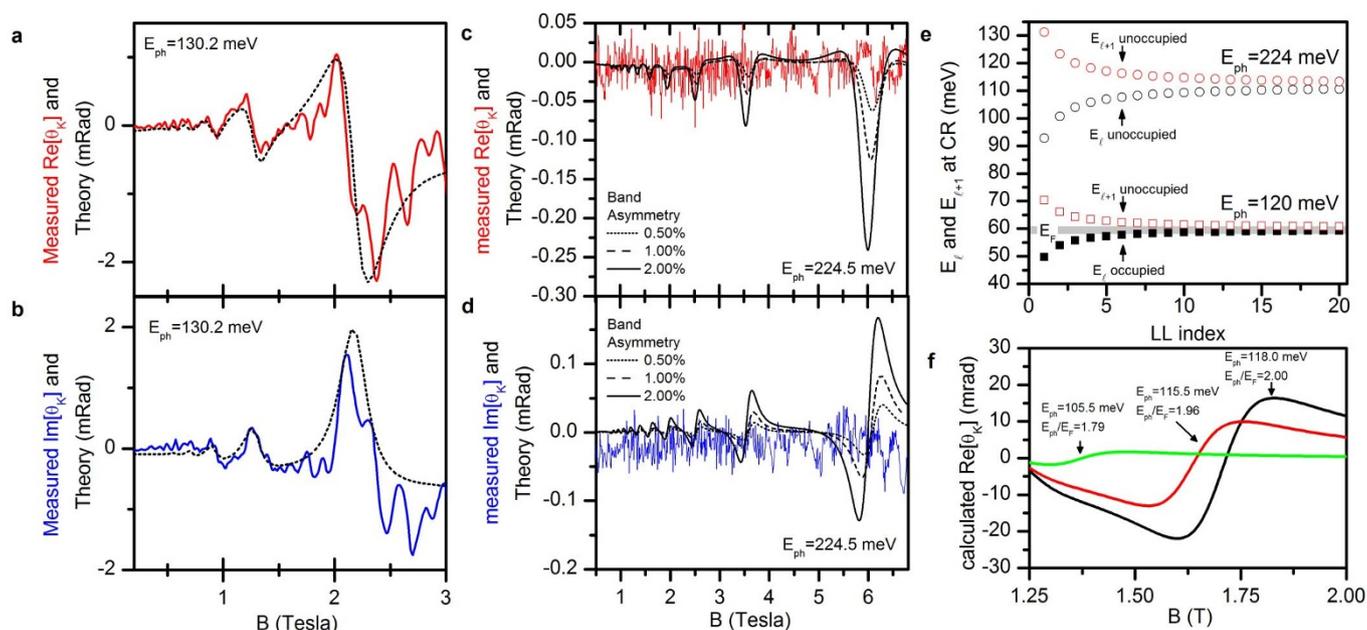


**Figure 5** | (a)  $\sqrt{B}$  CR Kerr features for  $114.5 \text{ meV} < E_{ph} < 133.8 \text{ meV}$ . (b) Linear- $B$  CR Kerr features for  $114.5 \text{ meV} < E_{ph} < 133.8 \text{ meV}$ . The Reststrahlen band of SiC is responsible for the sign change of features in solid and dotted curves.

which probe the conduction band shape only, with MIR interband CR measurements that probe the shapes of both conduction and valence bands. Far-infrared measurements of the  $0 \rightarrow 1$  intraband CR transition in the same sample enables us to obtain the Fermi velocity  $v_{F+} = (1.024 \pm .002) \cdot 10^6 \text{ m/s}$  for the conduction band alone<sup>34</sup>. Comparing this to the MIR interband CR transitions, which are related to both the conduction ( $v_{F+}$ ) and valence ( $v_{F-}$ ) band Fermi velocities, enables us to determine an upper limit of 2% for the band asymmetry ( $A = v_{F+}/v_{F-} - 1$ ) of monolayers in our sample. The small band asymmetry is in agreement with previous work<sup>34</sup> and our fits to the lineshapes of monolayer CR features. For the fitting, we calculate the Kerr angle<sup>35</sup> from the analytical expressions for the complex optical conductivities of graphene ( $\tilde{\sigma}_+$  and  $\tilde{\sigma}_-$ ) developed by Gusynin et al.<sup>16</sup>. In general, the CR lineshape is most affected by the choice of Fermi energy and band asymmetry. We find that the best agreement between the MIR Kerr angle data and theory occurs when  $E_F \simeq 60 \text{ meV}$  and  $A \simeq 0 - 2\%$ , as shown in Figure 6a, b for  $E_{ph} = 130.4 \text{ meV}$ . In order to match the magnitude of CR features

in the data and theory, we must employ an overall scaling parameter, which reflects the fact that samples are not uniformly covered by graphene layers that contribute to the measured Kerr response (see Supporting Note 3). The excellent agreement between the modeled and measured CR lineshapes indicates that band asymmetry does not significantly contribute to the CR Kerr features observed.

We further investigate the band asymmetry of monolayer graphene by taking advantage of the fact that CR Kerr features caused by band asymmetry are expected to increase in magnitude with increasing  $B$  and  $E_{ph}$ . This effect is attributed to an increase in the  $B$ -field separation of CR features for  $-\ell \rightarrow \ell + 1$  and  $-\ell - 1 \rightarrow \ell$  LL transitions at larger  $E_{ph}$ , which increases the difference between  $\tilde{\sigma}_+$  and  $\tilde{\sigma}_-$ . However, at  $E_{ph} = 224 \text{ meV}$ , where the band asymmetry and CR Kerr features are expected to be larger (if bands are asymmetric), no features are seen (Figure 6c, d). Using the parameters determined from the lineshape fitting of the data in the 114–134 meV range, we compare the measurements at  $E_{ph} = 224 \text{ meV}$  with theoretical expectations for the Kerr angle in the presence of



**Figure 6** | (a,b) Measured (solid, colored curves) complex Kerr angle at  $E_{ph} = 130 \text{ meV}$ , which is consistent with theoretical calculation (black, dotted curves) of the complex Kerr response for monolayer graphene systems without electron-hole band asymmetry. (c,d) Absence of CR features in measured complex Kerr angle at  $E_{ph} = 224 \text{ meV}$ , which is not consistent with expectations for a band asymmetric graphene system. Black curves are calculations of MIR Kerr response for graphene on SiC with different band asymmetries of 2.00% (solid curve), 1.0% (dashed curve), and 0.5% (dotted curve). The noise of the measurement is sufficiently small to detect the presence of a 0.5% asymmetry if it were present. (e) Plot of the Fermi energy limits  $E_{F,\min} = E_l = E_{ph} - \Delta_B \sqrt{l + 1}$  and  $E_{F,\max} = E_{l+1} = E_{ph} - \Delta_B \sqrt{l}$  for activation of CR Kerr features for  $E_{ph} = 120 \text{ meV}$  and  $224 \text{ meV}$ . At  $E_{ph} = 224 \text{ meV}$  the  $E_l$  and  $E_{l+1}$  LLs are well above  $E_F$  and are not occupied, which leads to a null Kerr response since  $\tilde{\sigma}_+ = \tilde{\sigma}_-$ . (f) Calculation of the weakening of the MIR Kerr angle response in a band symmetric monolayer graphene system for  $-1 \rightarrow 2$  CR transition as  $E_{ph}$  deviates from  $E_{ph,\text{optimal}} = 2E_F$ .



band asymmetries ranging from 0.5–2% (taking into account optical effects of the SiC substrate). As shown in Figure 6c, d, no CR features are observed in measurements to within the noise level, and the magnitude of calculated CR features drops below the measurement noise level for asymmetries less than 0.5%, further suggesting that CR Kerr features are primarily caused by Pauli-blocked transitions. Although we do not have theoretical models to quantitatively determine the band asymmetry for ordered graphene multilayers, we find that these layers also have symmetric bands, since the  $\theta_K$  measurements at  $E_{ph} = 224$  meV show no CR features associated with ABA or ABC graphene multilayers.

This result is an interesting contrast to other works where electron-hole band asymmetries are often detected in exfoliated monolayer flakes on Si/SiO<sub>2</sub> substrates (2.5%)<sup>36</sup> and twisted graphene multilayers grown by chemical vapor deposition (14% and 8% for layers with 3.5° and 21.5° twisting angles, respectively)<sup>10</sup>. The latter work is of particular interest since it suggests that a large asymmetry could exist for a large fraction of SiC graphene multilayers with rotational stacking faults, where adjacent graphene layers are typically rotated by approximately 30°<sup>24,37</sup>. However, no such asymmetry is observed in our samples, which is consistent with previous studies of unprocessed samples<sup>11,14,15</sup>, suggesting that band asymmetries are strongly enhanced by the chemical transfer process and/or presence of metal contacts or substrates in the vicinity of the graphene areas probed by the measurements<sup>12,13</sup>. Since our measurements show that the band asymmetry in C-SiC graphene is less than 0.5%, we suggest that commensurate rotations alone do not cause band asymmetry. Additionally, calculations by Plochocka *et al.*<sup>11</sup> predict asymmetries due to next nearest neighbor hopping in multilayer graphene, where the energy difference between  $-\ell-1 \rightarrow \ell$  and  $-\ell \rightarrow \ell+1$  transitions increases with field strength as  $\Delta E_{\ell}^{\pm} \simeq 0.08B[T]$  meV. Thus, for the  $-1 \rightarrow 2$  transition with  $E_{ph} = 224$  meV we expect  $\Delta E_{\ell}^{\pm} \simeq 0.49$  meV, yielding 1.4% asymmetry that should make CR Kerr features observable in our measurements. However, these features are not present in our data.

For the band-symmetric Pauli blocking model, CRs appear in the Kerr angle when  $E_{\ell} < E_F < E_{\ell+1}$  and the CR condition are satisfied simultaneously (illustrated in Figure 1a). As derived in Supporting Note 4, using the monolayer CR condition yields the Pauli blocking condition

$$E_{ph} \sqrt{\ell} / \left( \sqrt{\ell+1} + \sqrt{\ell} \right) < E_F < E_{ph} \sqrt{\ell+1} / \left( \sqrt{\ell+1} + \sqrt{\ell} \right), \quad (3)$$

which indicates that the range of photon energies that yield CR Kerr features is restricted by  $E_F$ . Figure 6e depicts how the limits of equation 3 evolve with the LL transition index  $\ell$ . At large  $\ell$ , the energy separation of  $E_{\ell}$  and  $E_{\ell+1}$  at CR decreases, converging on an optimal photon energy ( $E_{ph,optimal} = 2E_F$ ) that Pauli blocks all  $-\ell-1 \rightarrow \ell$  transitions, but allows all  $-\ell \rightarrow \ell+1$  transitions. Thus, as  $E_{ph}$  deviates from the optimal photon energy, the Pauli blocking condition is not met and CR features in the Kerr angle weaken, as shown by theoretical calculations in Figure 6f (multilayers also exhibit this behavior, see Supporting Note 4).

Typically, C-SiC multilayers possess a wide range of Fermi energies. The layers closest to the SiC-graphene interface have the largest  $E_F$ <sup>27,38</sup>, often exceeding 300 meV, which exponentially decays with increasing distance from the substrate<sup>39–41</sup>. The wide range of  $E_F$  throughout the sample implies that equation 3 will be satisfied for many  $E_{ph}$ , where graphene layers at different depths (with different  $E_F$ ) contribute optimally to the CR Kerr response different values of  $E_{ph}$ . Considering the typical range of  $E_F$  for C-SiC it is surprising that CR features are not observed at  $E_{ph} = 224$  meV, where graphene layers with  $E_F = 112$  meV are expected to contribute to the Kerr response. The absence of features may be explained by the degradation of layer mobility for increasing  $E_F$ <sup>34,41,42</sup>. It is also possible that the SiC-graphene interface layers, in our sample, have a much lower  $E_F$

than expected. This was recently observed by Johansson *et al.*<sup>42</sup>, where  $E_F$  in substrate interface layers was in the 75–85 meV range.

The observed temperature dependence of monolayer CR Kerr features is especially interesting when considering the band symmetric model. At elevated temperatures near 175 K, the Fermi occupation function broadens and  $k_B T \approx 15$  meV becomes comparable to the LL spacing ( $E_{\ell+1} - E_{\ell} = 5 - 20$  meV for 1–5 T). This reduces the Pauli blocking of  $-\ell-1 \rightarrow \ell$  transitions. Thus, it is expected that the magnitude of CR Kerr features will decrease with increasing temperature. As seen in Figure 2g, the magnitude of ABA and ABC stacked multilayer features behaves as expected. However, monolayer features exhibit a nearly constant magnitude over the range of measured temperatures 15–175 K.

## Discussion

The dominant role of Pauli blocking in producing CR Kerr features in graphene is exciting and holds much promise in the development of future optoelectronic devices. In particular, this work opens the door to devices that can control the polarization of light by tuning: 1)  $E_F$  away from the ideal value  $E_{ph}/2$  with an electrostatic gate, 2)  $E_{ph}$  away from  $2E_F$ , and 3)  $B$  or  $E_{ph}$  away from CR. The first point is of particular interest, since an electrostatic gate can modulate  $E_F$ , and, therefore, the polarization of infrared light, very quickly. Such a device is especially important for infrared applications, since current technologies are limited to fixed-frequency, sinusoidal modulation of infrared polarization<sup>43</sup>. In contrast, a graphene-based device is capable of modulating the polarization with arbitrary wave forms at arbitrary frequencies that are an order of magnitude larger than current technologies. Furthermore, comparing the magnitude of measured and theoretical Kerr angles suggests that the maximum changes in polarization, caused by CRs in homogeneous graphene monolayers, may be ten times larger than the angles observed in this work. It may also be possible to further enhance the polarization effects of graphene by exploiting the amplification effect of the Reststrahlen band in SiC substrates. The realization of a tunable graphene polarizer has the potential to greatly enhance current infrared polarization modulation devices, which are crucial to molecular sensing/identification and also play a role in infrared free space communications.

As demonstrated in this Report, graphene multilayers are capable of producing a large, reflected polarization response (up to 60 mrad) that is mediated through a combination of CR and optical chiral symmetry breaking. Such behavior is especially evident in highly-heterogeneous, high-quality, large-area graphene that is grown on C-SiC, where we observe over 18 CRs that are attributed to the coexistence of ABA, ABC, and rotationally faulted graphene multilayers with nearly symmetric electron-hole bands. The excellent agreement between theory and experiment for these multilayers indicates that CR Kerr features are not only predictable, but also highly tunable through the control of layer thickness, stacking order, and the Fermi energy. This understanding of how the magneto-optical properties of graphene evolve from 2D to 3D is of fundamental interest to the nanoscience community, where many of the proposed graphene applications aim to exploit a specific trait of a particular type of graphene. Furthermore, the measurement and analysis techniques employed in this Report are able to probe the electronic structure of many types of graphene that may coexist in heterogeneous graphene systems, even if they are stacked on top of each other. Such information can aid in the characterization and optimization of newly proposed devices that are based on graphene heterostructures, such as supercapacitors<sup>44</sup> and vertical transistors<sup>45</sup>.

## Methods

**Sample preparation.** In all, four samples are studied. Each sample consists of epitaxial graphene synthesized on nominally on-axis, C-face terminated, semi-insulating 4H-SiC by etching the samples in hydrogen and then annealing the



resulting surface at about 1600°C in vacuum ( $\sim 10^{-4}$  mbar) using a commercial chemical vapor deposition system<sup>19</sup>. The samples consist of a patchwork of multilayer graphene dominated by regions containing up to 50 layers; a small fraction consists of fewer layers, as is confirmed by optical microscopy, micro-Raman spectroscopy, and atomic force microscopy. The C-Face SiC samples are highly heterogeneous and consist of multilayers with a variety of stacking orders, each having unique electronic properties. The simplest case, AA stacking, consists of neighboring hexagonal layers that have not been shifted in the 2D plane. AB multilayers are defined by repeated stacking of A and B layers where B layers are translated along one of the nearest neighbor vectors by exactly one bond length. Similarly, ABC multilayers, consists of repeated stacking of A, B, and C layers, where the C layer is shifted two bond lengths along the nearest neighbor vector with respect to layer A. In addition, a significant portion of C-face SiC graphene is known to be commensurate with the C-face SiC lattice, which leads to rotational stacking faults every 1.6–2.5 layers<sup>23</sup>. While the majority of graphene multilayers on C-face SiC exhibits stacking faults with adjacent layers rotated by 30°, other rotations have also been observed in smaller quantities<sup>22</sup>. Commensurate stacking arrangements result in an effective decoupling of adjacent layers, which gives rise to their monolayer-like graphene behavior<sup>24,26</sup>.

**Measurement system.** Measurements are performed on graphene in a magneto-optical cryostat with sample temperatures ranging from 15–200 K and an applied out-of-sample-plane magnetic field up to 7 T. We employ discrete spectral lines from tunable, linearly polarized, mid-infrared (MIR) CO<sub>2</sub> (112–138 meV energy, 11–9 μm wavelength) and CO (206–248 meV energy, 5–6 μm wavelength) lasers to probe the Kerr effect. This MIR light is directed onto the sample at near normal incidence, and the reflected beam polarization is analyzed using a combination of photoelastic modulation and lock-in techniques that allow for the simultaneous determination of the complex Kerr angle ( $\text{Re}[\theta_K] \sim$  rotation,  $\text{Im}[\theta_K] \sim$  ellipticity) and the magneto-reflectivity<sup>35,46–48</sup>. The probing beam at the sample is on the order of hundreds of microns in diameter and therefore our measurements probe a mixture of response from all forms of graphene present in the laser spot. All measurements consist of positive and negative magnetic field sweeps performed with fixed temperature and probing photon energy.

**Inverse magnetic field periodicity.** Here we show that monolayer graphene's interband CRs are periodic versus inverse magnetic field. This optical effect is analogous to Shubnikov-de Haas oscillations, which are used in DC magneto-transport measurements to characterize the quantum mechanical nature of 2D electron systems<sup>49</sup>. The LL energies of monolayer graphene are given by equation (1), where  $L < 0$  ( $L > 0$ ) defines the valence (conduction) band. Considering an interband transition in graphene, the CR condition yields

$$E_{ph} = \Delta E_{-\ell, \ell+1} = E_{\ell+1} - E_{-\ell} = v_F \sqrt{2e\hbar B_T} \left( \sqrt{\ell+1} + \sqrt{\ell} \right), \quad (4)$$

Where  $B_T$  is the magnetic field strength at CR. Rearranging equation (4) we find  $1/B_T$  is approximately proportional to  $\ell/E_{ph}^2$  for  $\ell > 1$ . For fixed  $E_{ph}$ , the nearly linear dependence of  $1/B_T$  on  $\ell$  implies that CRs are periodic with inverse magnetic field. Similarly, this can also be shown for AB multilayer graphene and ABC multilayer graphene by using the LL energies defined by Koshino and Ando<sup>17</sup> and Yuan et al.<sup>18</sup> (see Supporting Note 1 for further details).

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## Author contributions

C.T.E. and J.C. devised the experiment. C.T.E., J.C., and J.G.T. wrote the manuscript. C.T.E., M.H.K., and A.V.S. carried out MIR Kerr measurements. C.T.E. performed analysis and theoretical modeling. J.G.T. and E.R.G. performed preliminary magneto-optical characterization of samples. R.L.M., J.L.T., C.R.E., D.K.G. carried out the growth of multilayer graphene samples.

## Additional information

**Supplementary information** accompanies this paper at <http://www.nature.com/scientificreports>

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