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Anatomical regulation of ice nucleation and cavitation helps trees to survive freezing and drought stress

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Water in the xylem, the water transport system of plants, is vulnerable to freezing and cavitation, i.e. to phase change from liquid to ice or gaseous phase. The former is a threat in cold and the latter in dry environmental conditions. Here we show that a small xylem conduit diameter, which has previously been shown to be associated with lower cavitation pressure thus making a plant more drought resistant, is also associated with a decrease in the temperature required for ice nucleation in the xylem. Thus the susceptibility of freezing and cavitation are linked together in the xylem of plants. We explain this linkage by the regulation of the sizes of the nuclei catalysing freezing and drought cavitation. Our results offer better understanding of the similarities of adaption of plants to cold and drought stress, and offer new insights into the ability of plants to adapt to the changing environment.

In a changing climate, plants will meet new environmental conditions such as different regional temperature and precipitation patterns. These changes will affect the probability of freezing and cavitation¹, i.e. phase change of liquid water to ice or gas, respectively, in the xylem of plants. Freezing and cavitation form a risk for tree function and survival because water conductance inside trees scales with photosynthesis and growth², but water conductance is only possible in liquid form. Cavitation has been recognized as one of the key factors leading to reduced plant productivity and mortality during drought³, and factors influencing the vulnerability of the xylem to cavitation have been studied extensively⁴. It is known that there is a relation between the critical pressure causing cavitation during drought and anatomical plant characteristics^{5–7}, although the causality has not been satisfactory shown. However, the critical temperature causing ice nucleation in the water transport system^{8–10} has not been given much consideration.

Liquid water is vulnerable to phase change into ice at sub-zero temperatures, similarly as it is into vapour at liquid pressures below its saturation vapour pressure¹¹. The ecological significance of the freezing temperature of the xylem to plant productivity and survival worldwide is likely less important in comparison to that of cavitation. However, the factors influencing freezing could be important for plant function and survival in colder environments^{12,13}. Ice nucleation temperature in xylem conduits, the dead cells responsible for transporting water from the roots to the foliage, determines the frozen time period and the number of freeze-thaw cycles a tree experience during winter. Short frozen period and low number of freeze-thaw cycles have a positive effect on tree function and survival because as long as water in the xylem is not frozen, there is no risk for typical freezing damages that are especially enhanced by continuous freeze-thaw cycles. Typical freezing damages in trees adapted to colder environments include bubble formation during freezing and thawing causing winter cavitation and further blockages in water transport¹⁴, and dehydration of unfrozen living cells due to low water potential of extracellular ice as water potential over ice decreases approximately 1.2 MPa per 1 °C decrease in ice temperature^{15,16}. Low ice nucleation temperature also makes it possible for an evergreen tree to photosynthesize on sunny days even when the ambient temperature is below zero¹⁷ which will make them effective carbon sinks¹⁸ and aerosol sources¹⁹. In milder regions, high freezing temperature of xylem water can be beneficial for trees as it protects the living cells by providing temporary cold protection with released heat of fusion²⁰. Also in colder regions, too low ice nucleation temperature could be harmful for trees. Lower freezing temperature increases the risk of intracellular freezing of the living cells as dehydration of the living cells due to the extracellular ice increases their osmotic concentration²¹ and may allow them to tolerate very low freezing temperatures²².

Liquid water is transported in xylem conduits (Fig. 1) under negative pressures according to the cohesion-tension mechanism^{23,24} allowed by strong inter-molecular attraction. Negative pressure, i.e. large water tension

Figure 1 | Schematic presentation of conduits of a deciduous tree species and inter-conduit pits (a) between two water-filled conduits and (b) between a gas-filled and a water-filled conduit. In (a), impurities and other solid particles can enter a conduit through a pit membrane in the case of large enough pores, and become potential ice nuclei. In (b), gas penetrates from a gas-filled conduit to adjacent water-filled conduit through a pit membrane in the case of large enough pores, and induces cavitation.

(see Fig. 2), is created as evaporation at the leaf surfaces pulls water columns, held together by cohesive forces, upwards from the soil through the xylem. Water tension inside the xylem increases with decreasing soil water availability and increasing transpiration rate. At sub-zero temperatures, liquid water is also prone to freezing as the vapour pressure over ice is lower than that over liquid water (see Fig. 2). In these conditions, water inside the xylem is in a unique thermodynamic state in the sense that it is metastable to two directions: it is simultaneously supercooled, i.e. temperature of liquid water is below the equilibrium ice nucleation temperature and under tension, i.e. pressure of liquid water is below the saturation vapour pressure¹¹.

Water can remain in its metastable liquid state as long as there are no solid impurities or gas phases (bubbles or menisci) of large enough size present to act as nuclei and catalyse the formation of a

new phase, i.e. ice or gas. Homogeneous ice nucleation of water takes place at approximately -40°C ¹¹ and homogeneous cavitation of water at approximately -100 MPa ¹¹, which is far below the pressures found in any plants. Heterogeneous ice nucleation at warmer temperatures or cavitation at higher pressures requires the presence of nuclei of sufficient surface properties, geometry and size²⁵. Here we investigate how an important characteristic of xylem anatomy, its conduit diameter, regulates the sizes of nuclei catalysing freezing inside trees, and how this regulation determines the environmental conditions critical for the phase transition into ice. We then compare the sensitivity of ice nucleation temperature on xylem conduit diameter to the previously well-known relationship of cavitation pressure sensitivity on xylem conduit diameter.

Results

We found that the ice nucleation temperature of water in the xylem increased with increasing conduit size regardless of the species or tree part (Fig. 3A). There is no known direct causality that would explain the found relationship. We thus hypothesize that the relationship between ice nucleation temperature and conduit radius can be explained from the basis of the classical nucleation theory and the scaling relations between conduit, pore and nucleus radius. Our theoretical calculation using the classical nucleation theory demonstrated that the maximum supercooling temperature, i.e. the reciprocal of ice nucleation temperature, is inversely proportional to the size of a nucleus at the temperature range in which ice nucleation occurs in trees²⁵ (Fig. 3B). The size of the nuclei present in the xylem sap is determined by the inter conduit pit pores that act as filters allowing water and dissolved nutrients to enter the conduits, but constrict the spreading of gas bubbles and solid impurities in excess of few nanometres (see Fig. 1). It has been empirically confirmed that pore sizes in the pit restrict the size of particles which can enter the conduits^{26,27}, so we further obtain an inverse relation between maximum supercooling temperature and pit pore size. Finally, there are two prevailing hypothesis on the linkage between the pit pore size and conduit size: the pit-resistance hypothesis²⁸ of nearly linear scaling between average pore size and conduit size, and the rear pit hypothesis⁵ of nearly linear scaling between the maximum pore size

Figure 2 | Schematic presentation of the used terminology related to temperature (T) and pressure (P). Freezing temperature and cavitation pressure refer to heterogeneous nucleation; homogeneous freezing takes place at approximately -40°C and homogeneous cavitation at approximately -140 MPa .

Figure 3 | (a) Measurements ($N = 70$) of ice nucleation temperature of water in trees and maximum conduit radius. The narrowest conduits were found in conifers and the widest in deciduous species. Curve for the theoretical relationship is drawn. (b) Theoretical relationship between ice nucleation temperature and ice nucleus radius with varying particle surface properties denoted with θ (equation 5) in the insert. The ice nucleation temperature is calculated to be reached when the nucleation probability exceeds 0.5 in one minute for a sample of 3 cm^3 in volume (a cylinder of 1 cm in radius and 1 cm in height).

and conduit size. Thus we concluded that the maximum supercooling temperature is approximately inversely proportional to conduit size, because the size of the largest particles that are able to penetrate through the pit pores determines the ice nucleation temperature in the xylem.

Figure 4 demonstrates a striking similarity of the relation of ice nucleation temperature to conduit size to the previously known relation of cavitation pressure to conduit size. Both relations are strongly supported by empirical evidence; for ice nucleation from our own results as shown above, and for cavitation from earlier studies^{5–7}. In our theoretical analysis (see Methods section), we linked the susceptibility to freezing and cavitation with plant anatomical characteristics based on the relation between nucleus size (impurity or gas phase) and the ability to penetrate into the metastable region of temperature or pressure, which are both proportional to the inverse of pit pore size.

To get a better understanding of the potential significance of ice nucleation temperature in xylem for tree functioning, we made some calculations from weather data measured in Southern Finland (SMEAR II station²⁹ $61^\circ 51' \text{ N}$, $24^\circ 17' \text{ E}$). Within a 15-years follow-up period, the time that the xylem was frozen was half shorter and the number of freeze-thaw cycles was only 15% for a tree with ice nucleation temperature of -10°C compared to a tree with ice nucleation temperature of -1°C .

To confirm that the found relationship between conduit radius and ice nucleation temperature was not an artefact caused by the

Figure 4 | Empirical results concerning the relationship between drought cavitation pressure and conduit radius are compared with the theoretical relationship between ice nucleation temperature and conduit radius that is also supported by the empirical data ($R^2 = 0.35$, $P < 0.0001$). Drought cavitation is described with the pressure reducing 50% of the hydraulic conductivity (P_{50}). The linear regression line of Wilson and Jackson⁶ was drawn visually from the original figure. The definition of conduit radius was different in different studies: mean conduit radius⁵, hydraulically weighted mean radius ($\Sigma r^5 / \Sigma r^4$)⁶ and mean radius of conduits responsible for 95% of water flow⁷ were used. In this study we used maximum conduit radius.

varying sample size and cooling rate^{30–32}, we tested the effect of these variables together with conduit radius. Conduit radius increased the freezing temperature highly significantly ($p < 0.0001$, Fig. 5C), sample volume barely significantly ($p = 0.036$, Fig. 5A), but there was no effect of cooling rate ($p = 0.269$, Fig. 5B) on ice nucleation temperature. There was some dependency between conduit radius and sample volume ($R = 0.29$). This dependency results from the general trend between conduit size and branch/stem diameter³³. However, the multicollinearity was not severe and allowed separation of the studied effects in the statistical analysis.

We further modified the surface energy of the water-ice nuclei by adding a surfactant to the xylem sap. The addition of the surfactant to water decreased the surface energy of the nuclei and increased the average ice nucleation temperature from the average of -4.3°C ($N = 3$, s.d. = 0.9) and -4.2°C ($N = 3$, s.d. = 0.5) to -2.1°C ($N = 3$, s.d. = 0.5) and -2.5°C ($N = 3$, s.d. = 0.1) in *Pinus sylvestris* and *Betula pendula*, respectively. This result, along with the sharp exotherms associated with the freezing events (Supplementary Fig. S1) and thawing occurring always at the equilibrium ice nucleation temperature around 0°C , demonstrate that the freezing of the xylem sap was not an equilibrium freezing but the xylem sap was supercooled (Fig. 1).

Discussion

We showed that the temperature at which the xylem of a plant freezes is dependent on its anatomical characteristics as conduit size determines the size of the largest particles that are able to penetrate through the pit pores and catalyse ice nucleation. The theoretical size range of solid particles catalysing ice nucleation in the empirically measured temperature range coincides with empirical findings of particle sizes being able to penetrate through pits into conduits in trees^{26,27}. Different sized organic and inorganic nuclei, of either external origin or synthesized by the plant itself, are commonly found in plants and their presence has been shown to affect ice nucleation³⁴; the ice-like structures of nuclei catalyse the organization of water molecules into an ice crystal lattice²⁰. It has also been suggested that conduit walls would act as ice nuclei^{35,36}, and that the

Figure 5 | Relationship of ice nucleation temperature with (a) sample volume, (b) cooling rate and (c) maximum conduit radius. The lines represent statistical prediction between ice nucleation temperature and sample volume (a) and ice nucleation temperature and maximum conduit radius (c) when the effect of other variables in the multivariate model were fixed to data averages. There was no significant dependency between ice nucleation temperature and cooling ratio (b).

properties of conduit walls would correlate with conduit size³⁶. It seems that in the absence of impurities in xylem water, conduit walls can act as ice nuclei but only at considerably lower temperature compared to the ice nucleation temperatures typically found from plants in nature^{36,37}. The surfaces of the conduit walls do not have the sufficient surface properties to induce ice nucleation at such high temperatures as found in the experiments^{36,37}. It is thus much more probable that nuclei catalysing ice nucleation in conduits have similar nature as aerosols in atmospheric ice nucleation in clouds³⁸. Also gas bubbles created by cavitation have been found to be potential ice nucleation sites³⁹.

We further suggest that conduit size links together ice nucleation and drought cavitation via pit pore size. Drought cavitation most commonly develops in trees by spreading of the gas phase from one conduit to another through heterogeneous nucleation⁴⁰. It has been suggested that the rare largest pit pore in a conduit determines the water tension in which the gas phase enters the conduit from adjacent conduit through inter-conduit pits^{5,26}. This indicates that similar xylem anatomy secures safety in plants growing in either cold or dry environments. There is one difference in the spreading of the gaseous or ice phase following nucleation: inter conduit pit pore size determines spreading of the gaseous phase separately for each conduit, whereas freezing propagates from one conduit to another within a plant organ rather freely following a single ice nucleation event⁸. However, it has been shown that the extent of supercooling varies between organs within a tree as there can be ice barriers between tree organs⁹.

Running a surfactant through samples of *Pinus sylvestris* and *Betula pendula* branches before freezing decreased the degree of supercooling by approximately 40–50% in both species. Similarly to our results, lowering the surface tension has been found to increase the pressure required for cavitation in both conifers and angiosperms^{40–42}.

As ice nucleation is a stochastic phenomenon, both sample volume and exposure time to a given temperature affect ice nucleation probability^{30–32}. In our experiments, we settled for varying sample volume and exposure time as the probability for nucleation will in practice increase from values very close to zero to values approaching one in a narrow temperature range (Supplementary Figs. S2, S3). This was also shown empirically as sample volume had a barely significant effect and exposure time had no effect on the ice nucleation temperature (Fig. 5). We also used single measurements instead of averages of several measurements despite of the stochastic nature of nucleation, because theoretical calculations showed that the nucleation probability increases from zero to one in a very narrow range of the nucleus particle diameter (Supplementary Fig. S4), meaning that the largest impurity is practically always expected to act as nucleus for phase transition.

Figure 6 | Schematic presentation of the relationship between conduit anatomy and the trade-off between water transport safety and efficiency at whole tree level. Conduit size scales with the degree of metastability the tree can experience before spreading of cavitation or freezing. Different sized conduits are favoured in different environmental conditions.

Table 1 | List of the sampled species and tree organs. The range of maximum conduit radii is in parenthesis. Samples marked with (T) were used in the Tween 80 surfactant experiment; these samples were not included in Fig. 3A

Species	Branch	Stem	Root
<i>Acer platanoides</i> (26 μm)	1		
<i>Alnus glutinosa</i> (30–41 μm)		1	2
<i>Alnus incana</i> (18–42 μm)	1	1	
<i>Betula pendula</i> (16–27 μm)	5 + 3(T)	1	
<i>Cupressus</i> sp. (7 μm)	1		
<i>Juniperus communis</i> (7 μm)	2		
<i>Malus domestica</i> (20 μm)	1		
<i>Picea abies</i> (6–31 μm)	5	6	2
<i>Picea pungens</i> (8 μm)	1		
<i>Pinus sylvestris</i> (8–33 μm)	13 + 3(T)	6	4
<i>Populus</i> sp. (25–30 μm)	1		2
<i>Salix caprea</i> (24–31 μm)	2		1
<i>Sorbus aucuparia</i> (13–18 μm)	10		
<i>Vaccinium vitis-idaea</i> (9 μm)	1		

Our results offer better understanding of the anatomical similarities of adaption of plants to cold and drought stress as in global climatic distribution of species, mean conduit diameter has been found to decrease with the probability of both sub-zero temperatures¹³ and drought⁴³. In cold climates, trees with small conduits have been shown to suffer less from low temperatures and to have superior productivity compared to trees with larger conduits¹². Large conduits enable efficient water transport, whereas small conduits are reliable in water transport, i.e. safe from phase transition from liquid to gas or liquid to solid ice. Efficient and safe water transport is essential for plants because the exchange of water and carbon needed for photosynthesis takes place through the same stomata openings on leaf surface; the rate of water transport scales with metabolism rate on whole plant level².

We conclude that the linkage between ice nucleation temperature and drought cavitation is significant from an evolutionary point of view. Besides the already widely accepted trade-off at the whole tree level⁴⁴ between efficient water transport and safety from cavitation through conduit size, there also seems to be a trade-off between efficient water transport and low ice nucleation temperature (Fig. 6). The role of conduit anatomy in determining the length of the frozen period and the number of freeze-thaw cycles a tree encounters each winter, offers new insights into the ability of trees to adapt to the changing climate. Boreal trees with low ice nucleation temperature are effective also in climate change point of view decreasing the global warming by being carbon sinks¹⁸ and aerosol sources¹⁹ also during winter.

Methods

Experimental work. We collected 70 samples during March and April from winter acclimated woody species in Southern Finland near Helsinki. The samples represented 9 deciduous species and 5 conifer species (Table 1). Different tree parts including roots, stems and branches were covered among the sample set and sample size thus varied from 0.03 to 1 178 cm^3 .

The freezing experiments were conducted in a climate chamber (Weiss Umwelttechnik WK11 – 340/40) directly after cutting the samples using cooling rates between 0.06 and 2.9°C Min^{-1} . Temperature of the samples was detected at a measuring interval of 10 seconds with thermocouples inserted a few mm inside the sapwood. Ice nucleation releases heat seen as a freezing exotherm (Supplementary Fig. S1).

After the freezing experiment, 100- μm -thick cross-cuts were cut from the samples with a sliding microtome, stained with safranin, rinsed with water and dehydrated in alcohol. In the case of stem samples, a random cut was taken from the two outermost growth rings that typically have the largest cells⁴⁵. The maximum conduit lumen area of each sample cross-cut was measured with imaging software, and the conduit radius calculated assuming the conduits to be circular.

Because of the stochastic nature of ice nucleation, large sample size and long exposure time can be expected to increase the probability of a nucleation event and thus increase the ice nucleation temperature^{30–32}. Increasing sample size may increase

the ice nucleation temperature also because the likelihood of having an efficient ice nucleator present increases with sample size. To confirm that the found relationship between conduit radius and ice nucleation temperature was not an artefact, we tested the effect of conduit radius on ice nucleation temperature in a multivariate analysis together with the effects of cooling rate and sample volume (measured over bark). The used method was generalized linear modelling (PROC GENMOD, SAS 9.2, SAS Institute Inc.), so the explanatory variables conduit radius and sample volume were transformed with natural logarithm to obtain a linear relationship with ice nucleation temperature.

We made few additional freezing experiments, where we artificially lowered the surface tensions in the xylem sap using a surfactant (Tween 80) and compared the results with control samples in order to see the effect of nuclei surface energy to the ice nucleation temperature. We ran the surfactant solution (0.5 % v/v), which decreases the surface tension of water to 36 Nm^{-146} , through three *Pinus sylvestris* branch samples and three *Betula pendula* branch samples for an hour. The sample was connected to a plastic tube and soap solution was poured into the tube from 1.5 meters height in order to create pressure difference large enough to ensure fluent water conduction.

Theoretical analyses. Part I. Effect of particle size on ice nucleation according to classical nucleation theory. The equilibrium ice nucleation temperature is 0°C at atmospheric pressure for pure bulk water, and slightly (typically only a few tenths of a degree) lower for the water in the conduits of trees due to dissolved solutes. Below the equilibrium ice nucleation temperature, phase change to ice would allow the water in conduits to fall to a lower, more favourable energy state. However, before the phase change can occur, new surfaces between the new ice phase and liquid phase need to be constructed which requires energy. Change in the free energy (ΔG) of a spherical ice crystal in a phase change from liquid to ice is^{11,47}

$$G = -\frac{4}{3}\pi r_{ice}^3 \frac{L\Delta T}{T_E} + 4\pi r_{ice}^2 \sigma_{LI} \quad (1)$$

where r_{ice} is radius of the spherical ice crystal, L is latent heat of fusion ($333.55 \times 10^6 \text{ J m}^{-3}$ for a temperature of 273.15 K), T_E is equilibrium ice nucleation temperature (273.15 K), ΔT is supercooling temperature, i.e. the temperature minus the equilibrium ice nucleation temperature (Fig. 1), and σ_{LI} is surface energy between the two phases (0.030 Nm^{-1})⁴⁷. The first term on the right side is the bulk energy term, and the second is the surface energy term. Phase change to ice will occur only if ΔG is positive. The sign of (ΔG) at a given temperature is dependent on the radius of the ice crystal. Differentiating equation (1) with respect to r_{ice} and solving for $\Delta G = 0$ gives the critical radius of the ice crystal r_{ice}^*

$$r_{ice}^* = \frac{2\sigma_{LI}T_E}{L\Delta T} \quad (2)$$

Ice crystals smaller than this are crushed by surface forces, while ice crystals larger than this are able to grow indefinitely. Ice crystals of radius above the critical size are created by thermodynamic fluctuations which have the energy of the order of kT , where k is the Boltzmann constant ($k = 1.38 \times 10^{-23} \text{ J K}^{-1}$). The rate (homogeneous nucleation rate, J_{hom}) at which these ice crystals are created can be predicted by the classical nucleation theory to be^{11,47}

$$J_{hom} = J_0 \exp\left(\frac{-\Delta G(r_{ice}^*)}{kT}\right) \quad (3)$$

where J_0 is a kinetic pre-factor which has been estimated in the following way⁴⁸

$$J_0 = \frac{NkT}{h} \exp\left(\frac{-Q_D}{kT}\right)$$

where N is the molecular density of water ($3.35 \times 10^{22} \text{ molecules cm}^{-3}$), h is the Planck's constant ($6.626 \times 10^{-34} \text{ Js}$), and Q_D is the activation energy for diffusion in the liquid ($2.8 \times 10^{-23} \text{ J per molecule}^{11}$). In practice, this equation will give a nucleation rate larger than zero only when temperature approaches the homogeneous ice nucleation temperature of water, which is almost -40°C . Ice nucleation in conduits must therefore occur by heterogeneous nucleation

$$J_{het} = J_0 \frac{a}{N^{1/3}} \exp\left(\frac{-\Delta G(r_{ice}^*)(1-f)}{kT}\right) \quad (4)$$

where a is the surface area available for heterogeneous nucleation per unit bulk volume of liquid. For a spherical ice crystal on a convex surface (Supplementary Fig. S5), the geometrical correction factor f to obtained formation energy of critical cluster in the case of heterogeneous nucleation^{47,49}

$$f = \frac{1}{2} \left[1 - \left(\frac{1+Xm}{g} \right)^3 - X^3 \left(2 - 3 \left(\frac{X+m}{g} \right) + \left(\frac{X+m}{g} \right)^3 \right) + 3mX^2 \left(\frac{X+m}{g} - 1 \right) \right] \quad (5)$$

Where X is the ratio of the radius of the ice nucleus ($r_{particle}$) to the critical ice crystal radius (r_{ice}^*).

$$X = \frac{r_{particle}}{r_{ice}^*}$$

$$m \equiv \cos \theta = \frac{(\sigma_{L, \text{particle}} - \sigma_{I, \text{particle}})}{\sigma_{LI}}$$

$$g = \sqrt{1 - X^2 - 2Xm}$$

where $\sigma_{L, \text{particle}}$ is surface energy between liquid and solid particle, and $\sigma_{I, \text{particle}}$ is surface energy between ice and solid particle.

Nucleation is a stochastic process, so that a nucleation will only have a given probability to occur for given conditions. In other words, a nucleation temperature cannot strictly be defined. The probability that heterogeneous nucleation will occur in a wood volume of V within a time of exposure (t) to a certain temperature is³⁰

$$P_{\text{nuc}} = 1 - \exp(-J_{\text{het}} V t) \quad (6)$$

Supplementary Figure S2 shows the nucleation probability as a function of temperature for varying exposure times to a given temperature. As the figure demonstrates, the probability for nucleation will in practice increase from values very close to zero to values approaching one in a narrow temperature range (similarly to the case for cavitation by heterogeneous nucleation³⁰). However, experimental evidence points out to a slightly wider spread in nucleation temperatures³¹.

Re-arranging equation (4), the temperature at which the nucleation (freezing) occurs can be written

$$\Delta T = \left(\frac{16\pi(1-f)\sigma_{LI}^3 T_E^2}{3k T L^2 \ln\left(\frac{J a N^{-1/3}}{J_{\text{req}}}\right)} \right)^{1/2} \quad (7)$$

J_{req} is the nucleation rate which is required for nucleation to occur, here $P = 0.5$. J_{req} can be explicitly written by substituting J_{req} for J_{het} in equation (6) and rearranging

$$J_{\text{req}} = \frac{\ln(1-P)}{Vt} \quad (8)$$

In the calculation of the ice nucleation temperature (see Fig. 3B) a value of 0.003 m^3 (corresponding to a cylinder of 1 cm in radius and 1 cm in height) is used for the volume (V), 60 s is used for the time (t), and 0.5 is used for the nucleation probability (i.e. nucleation has a 50% probability of occurring). However, the values chosen for the parameters in calculating J_{req} in equation (7) influenced the predicted ice nucleation temperature only marginally (Supplementary Fig. S3) due to the dominating effect of other terms in equation (6). A value of 10^{-5} m^2 was used for a in equation (4). The value used for a affected the results so marginally that its value could be changed by many orders of magnitude in either direction without a noticeable effect on the result.

Part II. Scaling of conduit size with cavitation pressure and ice nucleation temperature. Gas will penetrate through the pores in the pits when the pressure difference ($\Delta P = P_g - P_L$) between the gas ($P_g \sim 1 \text{ atmosphere}$) and liquid phase (P_L) over the pores in the pit membrane exceeds¹

$$\Delta P \propto r_{\text{pore}}^{-1} \quad (9)$$

where r_{pore} is pore size.

The supercooling temperature at nucleation, i.e. the reciprocal of the nucleation temperature, calculated from equation (9) is essentially inversely related to size of the solid impurities (Fig. 3B), i.e. we can write

$$\Delta T \propto r_{\text{particle}}^{-1} \quad (10)$$

In practice, the result indicates that a particle can act as an ice nucleus only if it is large enough. Given that the maximum size of the particles present inside a conduit is limited by the sizes of pores in the pit membrane, i.e. ($r_{\text{particle}} \propto r_{\text{pore}}$), and that the largest impurity is expected practically always to be the nucleus (nucleation probability increases from zero to one in a very narrow range of the nucleus particle diameter, see Supplementary Fig. S4 for an example), an inverse relation is obtained between the maximum supercooling temperature and pore size in the pit membrane

$$\Delta T \propto r_{\text{pore}}^{-1} \quad (11)$$

In both cases, i.e. in cavitation (equation 9) and ice nucleation (equation 11), the limit of penetration in to the metastable region of pressure/temperature will be approximately proportional to the inverse of pit pore size.

Further, either average^{28,52} or maximum pit pore size^{5,26} or both, scale linearly with conduit size at conduit level. The first proposed relation stems from optimizing the carbon usage so that the proportion of resistance in pit pores vs. conduit lumens remains approximately constant²⁸, whereas the second proposed relation stems from statistical possibilities of having large individual pit pores present when the total pore area per conduit is large⁵. Both of these options could explain the size of the largest particles found inside conduits at tissue level, but we now assume linear scaling between average pit pore size and conduit size following the pit resistance hypothesis²⁸, i.e. we can write

$$r_{\text{pore}} \propto k_{\text{conduit}} \quad (12)$$

Assuming that conduit conductance is $k_{\text{conduit}} \propto r_{\text{conduit}}^4$ and pit pore conductance is $k_{\text{pore}} \propto r_{\text{pore}}^4$ ⁷, we get a relation between pore and conduit diameter

$$r_{\text{pore}} \propto r_{\text{conduit}} \quad (13)$$

Combining equations (7) and (11), we obtain a relation between ice nucleation temperature and conduit size

$$\Delta T \propto r_{\text{conduit}}^{-1} \quad (14)$$

and a relation between cavitation pressure and conduit size

$$\Delta P \propto r_{\text{conduit}}^{-1} \quad (15)$$

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Author contributions

A.L. performed the empirical part of the work and wrote the paper, T.H. and M.K. were responsible for the theoretical analysis and T.H. writing the theoretical analyses. All authors discussed the results and commented on the manuscript.

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