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# Magnetic fluid film enables almost complete drag reduction across laminar and turbulent flow regimes

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In the race to curb energy and oil consumption, zeroing of wall frictional forces is highly desirable. The turbulent skin friction drag at the solid/liquid interface is responsible for substantial energy losses when conveying liquids through hydraulic networks, contributing approximately 10% to the global electric energy consumption. Despite extensive research, efficient drag reduction strategies effectively applicable in different flow regimes are still unavailable. Here, we use a wall-attached magnetic fluid film to achieve a wall drag reduction of up to 90% in channel flow. Using optical measurements supported by modelling, we find that the strong damping of wall friction emerges from the co-existence of slip and waviness at the coating interface, and the latter is a key factor to obtain almost complete wall drag reduction across laminar and turbulent flow regimes. Our magnetic fluid film is promising and ready to be applied in energy-saving and antifouling strategies in fluid transport and medical devices.

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rag reduction is an intensively researched phenomenon associated with decreased frictional forces and the consequent increase of fluid flow velocity. In wall-bounded flow through boundary layer control strategy, significant drag reduction has been achieved by modifying the wall structure using a thin chemical coating (hydrophilic or hydrophobic), or by generating micro- and nano-textures that trap microscopic gas pockets to form the Cassie-Baxter state (a superhydrophobic surfaces, riblets)<sup>1-3</sup>. The recent lubricant-impregnated surface approach combines and enhances the two approaches, namely coating and texture<sup>4,5</sup>. Alternatively, when the flow is turbulent, a widely adopted eddy transmission control strategy consists in manipulating the carrier fluid rheology, for example, by adding long-chained polymers<sup>6-8</sup>. Other solutions for decreasing drag include active control strategies, such as gas release at the wall or an oscillating wall $^{9-13}$ .

Current strategies have drawbacks that limit their range of applications. *Boundary layer control*<sup>1–5</sup> strategies generally suffer from limitations due to the small slip length, coating detachment, and air layer failure, because their range of validity is mainly confined to the laminar regime. Strategies based on *eddy transmission control*<sup>6–8</sup> require a continuous release of additives near the wall or into the bulk fluid. For *active control*<sup>9–13</sup> solutions, the energy consumption of motors to generate oscillation or pumps for gas release limits the net energy gain due to drag reduction. Furthermore, although active control strategies are effective in both laminar and turbulent regimes, they nonetheless have significant constraints in the maximum achievable drag reduction and range of applicability<sup>14</sup>, for example, due to limited accessibility for the installation of an active device.

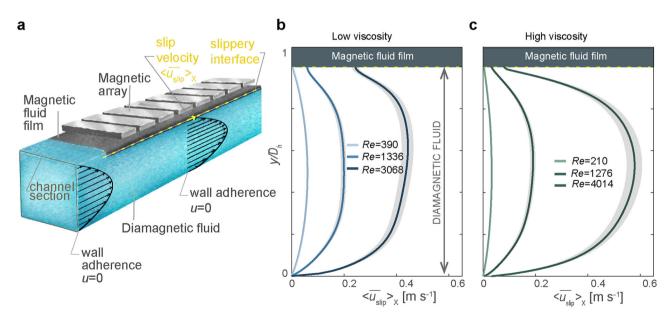
Here we present a drag-reduction technology that overcomes these limitations, offering a new opportunity for highly effective drag reduction in both laminar and turbulent regimes. Our approach relies on covering the channel wall with a magnetic fluid film (Fig. 1a), held in place by the attractive body force on the magnetite nanoparticles in the magnetic fluid colloidal structure<sup>15</sup>. The magnetic fluid coating acts as a slippery surface:

indeed, slip velocities are observed at the coating interface (Fig. 1b, c), with performance that depends on the viscosity ratio between the diamagnetic fluid and the magnetic fluid. In addition to slip, the waviness of the magnetic fluid interface, a local periodic perturbation induced by the magnetic field, further reduces drag. Both slip and waviness are co-current factors that lower the velocity gradient at the coated wall, resulting in drag reduction, up to 80% in the laminar and up to 90% in the turbulent regime.

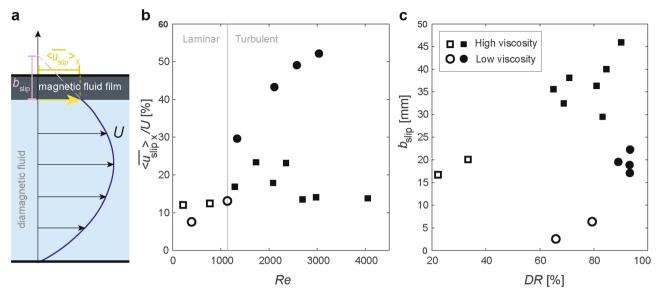
### **Results**

**Performance: slip velocity, slip length, and drag reduction.** Applying the magnetic fluid film to a channel surface results in slip velocities  $\langle \bar{u}_{\text{slip}} \rangle_x$  at the interface between the coating layer and the diamagnetic fluid (Fig. 2a). Measurements using particle tracking velocimetry record the flow field inside a square channel with section  $10 \text{ mm} \times 10 \text{ mm}$ , where a 1 mm-thick film of magnetic fluid is held at the upper wall by a permanent magnetic field [see Methods and Supplementary Figure S1].

Overall, we observe slip velocities in the range of 8-50% of the mean channel flow velocities, while varying the Reynolds number in the range of 400-4000 by changing the flow rate of the diamagnetic fluid (Fig. 2b). In addition to the slip velocity, drag reduction performance also depends on the slip length (Fig. 2a,c). Here, we achieve slip lengths,  $b_{\rm slip}^{1}$ , up to values of 45 mm. For comparison, most other boundary layer control techniques, such as the superhydrophobic surfaces and lubricant-infused surfaces<sup>17</sup>, achieve slip lengths of the order of 30-40 µm. A performance of the same order of magnitude as that reported here is reached, for instance, by heated superhydrophobic surfaces, with a slip length of about 15 mm<sup>18</sup>. The main bottlenecks for preventing higher slip lengths in previous techniques have mainly been the micrometric thickness of the fluid layer and the detachment of the coating from the surface. Here we overcome these limitations by adopting a coating firmly attached to the wall by the attractive body force exerted by the magnetic field.



**Fig. 1 Drag-reduction strategy: Wall-attached magnetic fluid film trapped by an array of magnets. a** Sketch of the working principle, where in absence of magnetic fluid film (MFF) we observe wall adherence and in the presence of MFF we observe the formation of a slippery interface with a slip velocity; (**b**, **c**) Time (denoted by the overbar) and horizontally (denoted by angular brackets) averaged velocity profiles in the diamagnetic fluid section with a magnetic fluid film at the top wall characterized by (**b**) low viscosity and (**c**) high viscosity. Experimental profiles at different Reynolds numbers,  $Re = U D_h / \nu$ , where U is the mean velocity,  $D_h$  is the equivalent diameter equal to the characteristic length of the channel, and  $\nu$  is the kinematic viscosity of the fluid. The shaded grey area indicates a 5% confidence interval, in accordance with the analysis presented in the Supplementary Material (Supporting Note 6).



**Fig. 2 Performance of the magnetic fluid coating technique. a** Sketch of the experimental setup, where slip length  $b_{\text{slip}}$  and slip velocity  $\langle \bar{u}_{\text{slip}} \rangle_x$  are depicted; (**b**) Ratio between the slip velocity to the cross-sectional mean fluid velocity in the channel  $\langle \bar{u}_{\text{slip}} \rangle_x / U$ , plotted as a function of Reynolds number Re. **c** Slip length,  $b_{\text{slip}} \rangle_x \mu_f / \tau_c^{-1}$  plotted as a function of the drag reduction,  $DR = (\tau_w - \tau_c) / \tau_w$ .100 [%]. Here,  $\mu_f$  is the magnetic fluid viscosity,  $\tau_c$  is the average shear stress at the coating interface and  $\tau_w$  is the average shear stress at the uncoated wall. The shear stress is here estimated as the product of the diamagnetic fluid viscosity  $\mu_r$ , and the velocity gradient at the interface,  $d < \bar{u} > / dy$ . Circles indicate experiments carried out for a viscosity ratio  $\eta_r = 6$ , while squares indicate experiments with  $\eta_r = 60$ . Unfilled symbols represent the laminar regime and filled symbols the turbulent regime.

Across flow regimes spanning from laminar (390 <  $Re \le 1200$ ) to turbulent (1200  $\lesssim Re < 4010$ ) <sup>19,20</sup>, differences in the slip velocities are mainly related to the mean velocity of the diamagnetic fluid and the viscosity ratio. An increase in the mean flow velocity causes an increase in the slip velocity (Fig. 2b), namely the velocity at the coating interface (Fig. 2a, yellow arrow). This finding is expected since a faster mean flow leads to an increase in the shear at the interface. We also observe that the viscosity ratio consistently influences the slip velocity in the turbulent regime ( $Re \gtrsim 1200$ ). Specifically, for a similar Reynolds number but higher magnetic fluid viscosity, we obtain a lower slip velocity (filled symbols in Fig. 2b). A magnetic fluid characterized by higher magnetite concentration (higher magnetic fluid density) exhibits a higher degree of magnetization when exposed to an external magnetic field, due to the formation of stronger magnetite chains<sup>15</sup>. Consequently, it displays a higher viscosity for a given shear and magnetic field strength [see rheology curves in Supplementary Note 1, Fig. S2], which implies stronger wall attachment and resistance to motion as expressed by the wall adherence condition (see Materials and Methods section).

The magnetic fluid coating technique yields a drastic reduction in drag: up to 80% for the laminar regime and up to 90% for the turbulent regime (Fig. 2c). Magnetic fluid films characterized by high viscosity show low values of slip velocity and high values of slip length compared to the low viscosity case (Fig. 2b,c).

The underlying mechanisms for drag reduction: slip and waviness. Two concurrent factors at the fluid interface contribute to the observed drag reduction by lowering the velocity gradient at the coated wall, namely, (i) the slip caused by the shearing force and (ii) the waviness owing to the magnetic field perturbation.

The interface waviness is characterized by long waves (wavelength  $\sim\!200$  mm, amplitude  $\sim\!0.1$  mm), as shown qualitatively in the long-exposure images of the flow streamlines recorded at 500 Hz (Fig. 3a, b). The wave amplitude increases with increasing the Reynolds number, whereas the wavelength is almost constant and is controlled by the distance between

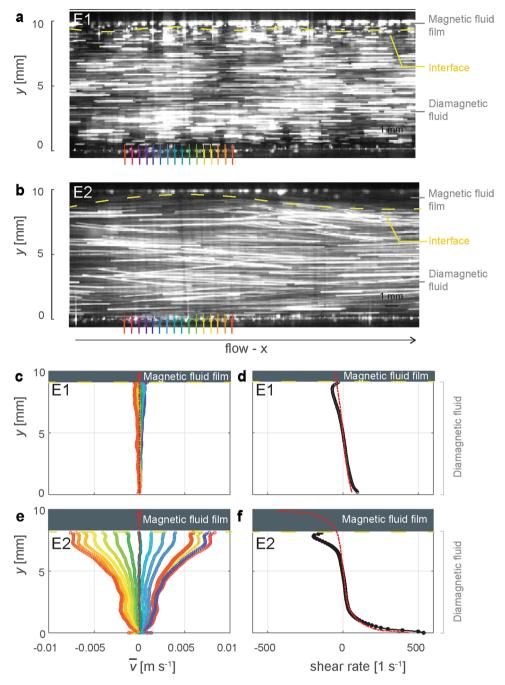
individual magnets in the array. This is expected since the discrete sum of each magnetic field acts as a triggering condition for interface perturbations<sup>21</sup>. The presence of waves at the interface is associated with upwelling/downwelling regions at the coated wall, as shown by the profiles of the vertical component of the velocity: its change of sign is consistent with a transition from upwelling to downwelling behaviour of the flow associated with the undulations at the interface (Fig. 3c, e). The presence of waviness at the interface is responsible for the depletion of shear at the interface, while shear is enhanced below the interface, reaching a local maximum near the edge of the maximum wave height before decaying towards the centre of the channel (Fig. 3d, f).

A numerical simulation reproducing the wavy geometry and the slip condition at the coating interface corroborates our experimental results in terms of velocity profile and shear profile in the case of laminar flow [see Supplementary Note 2]. The results at the wavy interface show that: (i) the mean velocity profile has a lower gradient than in the case of a straight interface (Figure S2a in the Supplementary Note 2); (ii) and the mean shear profile has a maximum below the wavy surface (Figure S2b in the Supplementary Note 2).

It is worth noting that with the interface waviness, we observed the formation of a shear layer away from the interface and a velocity profile that features an inflection point near the edge of the maximum wave height. This is qualitatively similar to the observations made in flow with submerged flexible vegetation, indicating a possible analogy to canopy flow<sup>22</sup>.

The relative contributions of slip and waviness to drag reduction in laminar and turbulent regimes. In the laminar regime, the waviness of the coating interface provides the dominant contribution to drag reduction. In the turbulent regime, both slip and waviness play an important role. In this case, the dominance of one factor over the other depends mainly on the viscosity ratio.

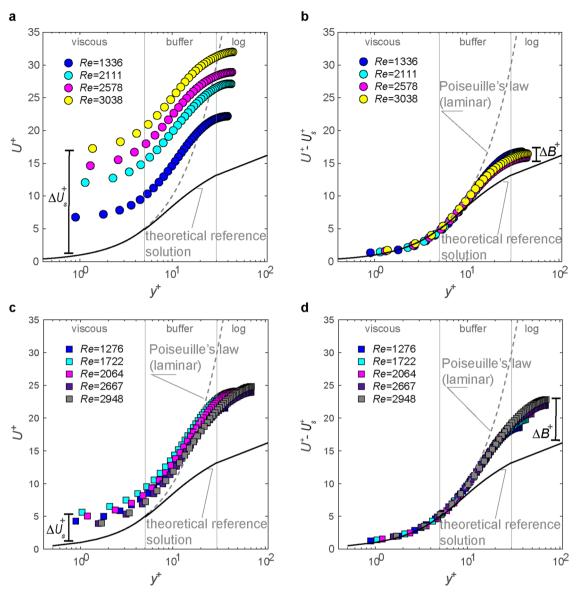
In the laminar case, we derived the theoretical flow velocity field solution by solving the magnetohydrodynamics equations [Supplementary Note 3] assuming a flat coating interface. The



**Fig. 3 Waviness at the coated wall. a, b** Long-exposure images of fluid streamlines acquired at 500 Hz. Data from experiments with coating and viscosity ratio  $\eta_r = 6$ : upper row (**c**, **d**) with Re = 1335 (E1), lower row (**e**, **f**) with Re = 3038 (E2). **c**, **e** Profiles of the time-averaged vertical velocity (acquisition at 3000 Hz) for 16 locations, depicted with symbols of different colours at the bottom of (**a**, **b-d-f**) Spatial average of the mean shear rate profile. The grey rectangle depicts the area of the magnetic fluid layer. The red dashed lines in (**c-d-f**) show the experimental time-averaged vertical component of the velocity and the experimental shear rate profile for the case of rigid wall without coating, respectively Re = 450 in the upper row and Re = 2495 in the lower row. The velocity data presented, acquired through particle image velocimetry, is subject to a 5% confidence interval, aligning with the analysis provided in the Supplementary Material (Supporting Note 6).

velocity profile of the magnetic fluid film is characterized by a counter flow, given by the sum of a parabolic term and a linear term, as in the case of a combined Couette–Poiseuille flow. The parabolic profile is induced by the magnetic body force, while the linear term is due to the shear at the interface between the two fluids [Supplementary Note 3]. The mean velocity of the magnetic fluid film is zero. The theoretical velocity profile of the attached magnetic fluid film was validated through optical microfluidic observations [Supplementary Note 4]. In the microfluidic

channel, we experimentally observed that the velocity field of the trapped volume of magnetic fluid is governed by an internal recirculation zone [Supplementary Movie 1], confirming an assumption made while performing numerical simulations in  $^{23}$ . The theoretical solution derived in Supplementary Note 3 provides reliable estimates of the slip velocity at the interface between the diamagnetic fluid and the magnetic fluid coating, but it fails to estimate the corresponding shear rate, i.e., the velocity gradient du/dy (Fig. 4a, b).



**Fig. 4 Relative contribution to drag reduction at the coating interface of slip and waviness in the turbulent regime.** The mean velocity profiles for experiments with magnetic fluid films of low viscosity ( $\mathbf{a}$ ,  $\mathbf{b}$ ) and high viscosity ( $\mathbf{c}$ ,  $\mathbf{d}$ ) at different Re numbers. Drag reduction due to slip through the shift upward from the reference case  $\Delta U_s^+$  ( $\mathbf{a}$ - $\mathbf{c}$ ) and due to wall shape represented by the upward shift  $\Delta B^+$  in the region  $y^+ > 30$  ( $\mathbf{b}$ - $\mathbf{d}$ ). The mean profiles are represented in terms of  $y^+$  and  $U^+$ , according to the generalized mean velocity distribution in drag-reduced flow<sup>33</sup>. The colours used in the legend correspond to experiments conducted at different Reynolds numbers. The same colour is selected for a set of experiments with different viscosities when the Reynolds number falls within a proximal range.

Indeed, the theoretical solution predicts the maximum shear at the interface (Fig. 4c), whereas the experimental data show the maximum shear rate shifted below the interface, where we observe the inflection point of the shear rate profile. The shift of the location of the maximum shear rate is responsible for the large drag reduction observed in the experiments, resulting in DR one order of magnitude higher than that predicted by the theoretical solution (Fig. 4c). The shallower velocity gradients established at the wall lead to a considerable drag reduction of 79% in the laminar regime with the low viscosity magnetic fluid. In the same regime, the theoretical solution for high-viscosity magnetic fluid still underestimated the drag reduction, although the performance is lower than that with the low-viscosity magnetic fluid (22% vs 79%, see Fig. 4c, d). It is thus the waviness of the coating interface that causes a decrease in the velocity gradient, providing the dominant contribution to drag

reduction in the laminar case, regardless of the viscosity of the magnetic fluid (Fig. 4c, d).

In the turbulent regime, it is not possible to compare the wavy regime with an exact theoretical solution as in the laminar case because of the complexity of the problem. However, following<sup>24,25</sup>, we use of the fact that drag reduction leads to a shift of the velocity profile in the logarithmic layer.

That is, to evaluate the relative contribution to drag reduction at the coating interface of slip and waviness, we compare the temporally and horizontally averaged velocity profiles of our experiments with the logarithmic law of the wall. Qualitatively similar to the laminar case, the presence of waviness at the interface is responsible for a shallow velocity gradient at the wall and for a shift of the maximum value of the shear rate away from the interface (Fig. 3f, g). The shift of the maximum shear value away from the wall can be interpreted as the formation of a

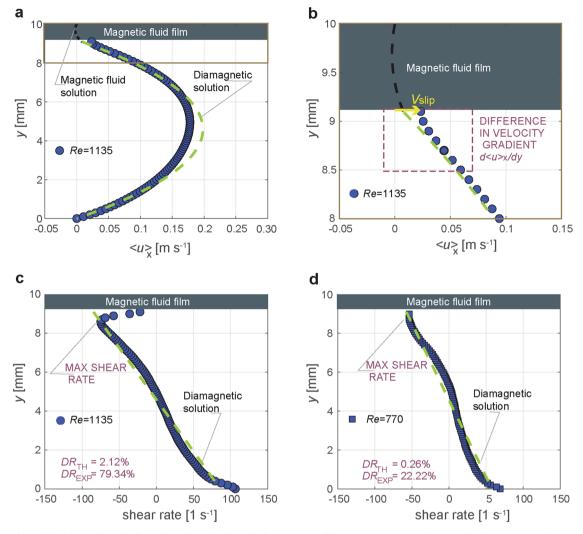


Fig. 5 Estimation of the drag reduction based on the velocity and shear rate profiles. a-c Comparison between the theoretical profiles (dashed lines) within the magnetic fluid FF (black) and the diamagnetic layer (green) and the experimental data (blue filled points) measured in the diamagnetic layer for laminar flow (Re = 1135) and a low viscosity magnetic fluid. a Velocity profile within the entire channel and (b) magnified view of the interface region. c Corresponding shear rate profiles. d Theoretical shear rate profile within the diamagnetic layer (green dotted line) and experimental data measured in the diamagnetic layer for laminar flow (Re = 770) and a high viscosity magnetic fluid (blue circles). The brown box in panel (a) indicates the boundaries of the magnified view of the interface region presented in panel b. The grey rectangle in panels (a-d) represents the magnetic fluid layer.

'virtual wall,' representing a hypothetical wall located in the plane where the maximum shear stress is observed. The presence of a virtual wall implies that we set the origin of the vertical axis in that location and determine  $u^*$  using the shear stress there. This provides a reasonable correspondence of the experimental data  $(y^+ \text{ vs } U^+)$  with the theoretical reference solution (black line) (Fig. 5a, c), and a collapse of the curves for different Re when the slip velocity is subtracted (Fig. 5b, c). The mean velocity profiles show a higher velocity at any point  $y^+$  compared to the reference case (Fig. 5a, c). This evidences that drag is reduced, firstly, due to the slip through a shift of the profile upwards from the reference case  $\Delta U_s^+$  (Fig. 5a, c) and, secondly, due to the wall shape represented by the upward shift of the profile  $\Delta B^+$  in the region  $y^+ > 30$  (Fig. 5b, d). In line with our observations, the upward shift  $\Delta B^+$  was also observed in other studies, considering different wall geometries<sup>24</sup>. Similarly, an important contribution in terms of  $\Delta B^+$  for the turbulent regime was also documented by<sup>25</sup> when investigating the performance of drag reduction for streamwise travelling waves. Finally, in the turbulent regime, the low viscosity magnetic fluid shows a dominant contribution of  $\Delta U_s^+$  to drag reduction acting in the region close to the interface (the boundary

layer), while the high viscosity magnetic fluid shows a greater contribution of  $\Delta B^+$  acting in the flow region further from the interface (outside the boundary layer) (Fig. 5a-d).

The contribution to drag reduction hence manifests in an upward shift of the velocity profile. The upward shift in the region next to the interface (boundary layer) is due to the slip condition<sup>26</sup>, while in the region further from the interface (outer layer), it is due to the waviness. In the turbulent regime, both slip and waviness play an important role. The dominance of one factor over the other depends mainly on the viscosity ratio. That is, the slip factor is dominant in a low-viscosity magnetic fluid, while the waviness factor is dominant in high-viscosity magnetic fluids (Fig. 5).

Range of applicability. The drag-reducing strategy based on a magnetic fluid-coated wall is capable of drag reduction, with better performance in the laminar regime with a low viscosity magnetic fluid (drag reduction up to 80%) and in the turbulent regime with a high viscosity magnetic fluid (drag reduction up to 90%) (Fig. 2c and Fig. 6).

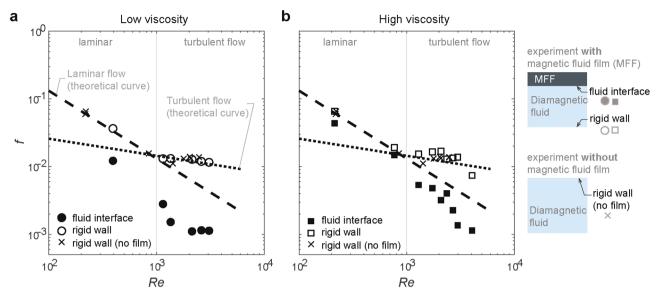


Fig. 6 Resistance to the motion evaluated in terms of friction factor, f, for rigid and magnetic fluid-coated walls. a Experiments with viscosity ratio  $\eta_r = 6$ ; (**b**) experiments with viscosity ratio  $\eta_r = 60$ . The dotted line is the theoretical solution for laminar flow f = c/Re with c = 14.22 for a square channel  $^{34,35}$ , and the dashed line for turbulent flow f = 0.079 ( $c_d *Re$ )- $^{0.25}$  with  $c_d = 1.125$  for a square channel  $^{36,37}$ . In the infographic on the right, we explain the symbols used in graphs (**a**, **b**). Data from experiments with magnetic fluid films are represented with filled symbols for the fluid interface (circles for low viscosity and squares for high viscosity experiments), and empty symbols for the bottom rigid wall. Data from experiments conducted without a magnetic fluid coating are denoted as references (indicated by the 'x' symbol).

To evaluate the potential range of applicability, we investigated the difference in friction factor at the coated and uncoated walls (Fig. 6). For our experiments in wall-bounded flow with a coated wall, the coated wall (filled symbols, Fig. 6) is always characterized by a lower Fanning friction factor  $(f = 2\tau/\rho U^2)$  than the uncoated wall (open symbols, Fig. 6). The experimental data acquired in a channel without magnetic fluid (x symbols, Fig. 6) follow either the laminar  $(Re \lesssim 1200)$  or the turbulent  $(Re \gtrsim 1200)$  solution. This holds for the uncoated wall of the magnetic fluid experiments as well. The experimental data show friction factors much lower than the laminar solution for the coated wall and fall along a slope similar to the laminar solution, but shifted substantially below the laminar curve. Although the slope of the trend indicates that the laminar regime in the magnetic fluid case might be sustained for higher *Re* compared to the uncoated one, we find that the flow is not laminar at  $Re \gtrsim 1200$ also in the coated case. However, the magnetic fluid coating dampens turbulence, as manifested by smaller root mean squared velocity fluctuations  $\langle \bar{u}_{rms} \rangle$  and Reynolds shear stresses [Supplementary

For the low viscosity magnetic fluid (Fig. 6a), we obtained effective drag reduction (>60%) in both laminar and turbulent regimes, whereas, for the higher magnetic fluid viscosity (Fig. 6b), we have pronounced drag reduction (>60%) only for the turbulent regime and weaker performance for the laminar regime (20-30%) (Fig. 2c). Therefore, high viscosity magnetic fluids are suitable for application in turbulent regimes due to their higher resistance to the shear force at the interface and their good performance in terms of drag reduction. Low-viscosity magnetic fluids are recommended for applications ranging from laminar to low turbulence regimes, provided that the shear does not exceed the threshold for detachment (see adherence condition in Material and Methods). However, low-viscosity magnetic fluid may also be applicable beyond the maximum Re investigated here, when using a larger length scale (i.e., larger channels) and/or lower velocity so that the shear remains in the range presented in this work.

The magnetic fluid-coating technique is a highly promising approach to achieve considerable drag reduction for applications

in the transport and industrial sectors, such as navigation, pipelines, and bearings. Indeed, the results shown here were obtained with a saline solution, but they also apply to other diamagnetic fluids like freshwater, alcohol, and oil<sup>27,28</sup>. Moreover, due to the high shear resistance, the technique is also indicated for applications where slippery liquid-attached surfaces are required to achieve biofouling resistance, such as avoiding the accumulation of microorganisms, plants, or algae. The accumulation of microorganisms is indeed inhibited by creating an unfavourable hydrodynamic condition at the interface, i.e., a slip condition and a shift of the maximum value of shear rate away from the interface. Indeed, microorganisms will hardly attach and proliferate because of the continuous change/rearrangement of the surface. Leveraging biocompatible magnetic fluids<sup>29</sup>, we also envisage applications in the biomedical devices sector. This technique might represent an innovative solution for preventing thrombus formation and infection because the magnetic fluid film could prevent platelet adhesion and inhibit protein attachment<sup>30</sup>. Moreover, the magnetic fluid coating technique could mitigate the risks of combating infection (deterring attachment of bacteria and biofilm formation) and thrombosis (deterring protein adsorption and platelet adhesion) associated with biomedical devices, thereby reducing the need for pharmacological treatments with anticoagulant or antibiotic drugs, hence decreasing healthcare costs and improving outcomes.

## Methods

Magnetic fluid characteristics. To generate the magnetic fluid film, we adopted two commercial products, EFH1 (dynamic viscosity 0.006 Pa s, density 1210 kg m<sup>-3</sup>) and EMG900 (dynamic viscosity 0.06 Pa s, density 1740 kg m<sup>-3</sup>) (Ferrotec USA corporate; more details about their characteristics can be found on the manufacturer's website). These magnetic fluids are characterized by a shear-thinning rheological behaviour. We determined their rheological characteristic curves by dedicated microfluidic experiments [Supplementary Note 1].

The magnetic fluid film wall adherence is well defined by a balance equation between body force and momentum,  $\mu_0$   $MH > \rho U^2$ , where

 $\mu_0$  is the vacuum permeability, M is the magnetic fluid magnetization, H is the magnetic field generated by permanent magnets, and  $\rho$  and U are the fluid density and mean flow velocity of the diamagnetic fluid in the channel. This defines the threshold flow condition above which we observe the detachment of the magnetic fluid layer<sup>31</sup>.

The dynamics of the trapped volume of magnetic fluid at the wall is characterized by a flow recirculation zone. This was investigated here by performing microfluidic experiments that allowed observation of the dynamics of magnetite-chain formation within the magnetic fluid flow [Supplementary Note 5].

**Experimental setup**. The experimental conduit consisted of a Plexiglas square channel with a section of 10 mm × 10 mm and a total length of 1.5 m. The flow in the channel was driven by a flow loop system. The flow rate could be adjusted to give a range of Re of 300–4000, for  $Re = U D_h/v$ , where U is the mean velocity,  $D_h$  is the equivalent diameter equal to the characteristic length of the channel and v is the kinematic viscosity of the fluid. The diamagnetic fluid pumped in the loop system was saltwater (density 1010 kg m<sup>-3</sup>). The magnetic fluid film, about 1 mm thick, was attached at the top wall. We use a diamagnetic fluid flowing in the channel, in direct contact with the magnetic fluid film at rest at the wall. We have tested different commercial fluids covering a range of viscosity ratios  $\eta_r$ (dynamic viscosity ratio between the coating fluid and the diamagnetic fluid). The magnetic fluid magnetization and the magnetic field can tune the shear resistance of the magnetic fluid coating, ensuring an attached magnetic fluid film in the flow regimes investigated [details in Methods Magnetic fluid characteristics]. The magnetic field was generated by an array of permanent neodymium magnets (N45, Supermagnete, with unit size  $20 \times 4 \times 6$  mm arranged in series along the channel with a gap of 2 mm between units). Each magnet functioned as a single "unit" capable of attracting a fixed volume of magnetic fluid. The array of magnets that guaranteed the adherence of the magnetic fluid film at the wall was located 8 mm above the flow channel and covered the entire channel length.

We used a high-speed video camera (Photron) to capture up to 16,000 frames per second at full resolution and record the flow field using particle tracking velocimetry (PTV) with acquisition at 3000 Hz. For these measures, the flow was seeded with neutrally buoyant anisotropic particles (average diameter 11  $\mu$ m) illuminated by a vertical laser light sheet crossing the centre of the channel. The velocity field was measured 130 x  $D_h$  downstream of the flow entrance to avoid flow entrance disturbances. The PTV method was preferred over the particle image velocimetry (PIV) method due to its superior accuracy near the wall<sup>32</sup>. The accuracy of the velocity estimates (5%) was assessed by comparing data from a numerical solution in COMSOL with experimental data acquired under identical forcing conditions (Re = 1135) [Supplementary Note 6, Fig. S7].

The magnetic field H at the magnetic fluid layer was determined through a numerical simulation in COMSOL Multiphysics (Burlington, MA). We used the Magnetostatics package, which estimates a time-independent field without electric currents. Starting from the constitutive relation between magnetic flux B, magnetic field H and magnetization field M,  $B \equiv \mu_0 (H + M)$ , considering magnetostatic conditions, we have  $\nabla B = 0$  and  $\nabla \times H = 0$ . It follows that the magnetic field H can be expressed as the gradient of a scalar magnetic potential,  $V_{\rm m}$ ,  $H = -\nabla V_{\rm m}$ . Using this approach, at the coating layer, we estimated a mean magnetic field intensity of 7200 A m<sup>-1</sup>.

# **Data availability**

The experimental dataset generated and analyzed during the current study is available from the authors upon request.

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### **Author contributions**

L.S. and M.H. designed research; L.S. performed research and analyzed data; E.S. and L.S. performed the microfluidics experiments; L.S., and M.H. wrote the paper; and all authors edited the manuscript.

# **Competing interests**

The authors declare no competing interests.

### **Additional information**

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