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Charge-density wave associated with higher-order Fermisurface nesting in monolayer VS_2

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Fermi-surface (FS) nesting originating from Peierls' idea of electronic instabilities in one-dimensional materials is a key concept to stabilize charge-density wave (CDW), whereas its applicability to two-dimensional (2D) materials is under intensive debate. Here we report unusual CDW associated with the higher-order FS nesting in monolayer 2D VS2. Angle-resolved photoemission spectroscopy and scanning tunneling microscopy uncovered stripe CDW with $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ periodicity together with an energy-gap opening on the entire FS. We suggest that this CDW involves the higher-order FS-nesting vector 2**q** twice larger than that of the normal one (**q**), as supported by the anomalies in the calculated phonon dispersion and electronic susceptibility. The present results suggest that the cooperation of **q** and 2**q** nesting leads to the fully gapped CDW state unlike the case of conventional single **q** nesting which produces a partial gap, pointing to an intriguing mechanism of CDW transition.

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INTRODUCTION

The discovery of Dirac fermions in graphene has opened a new avenue to explore emergent quantum phenomena in twodimensional (2D) materials^{1–5}. Atomically thin transition-metal dichalcogenides (TMDs) offer a great opportunity to widen the functionality of 2D materials due to the tunability of band structure associated with the material variety, which has already manifested in the bulk counterparts as the emergence of rich electronic phases such as insulating, metallic, and superconducting phases. Besides the band tunability, two-dimensionalization of bulk TMDs further leads to unique quantum phenomena such as spin-valley Hall effect², Ising superconductivity⁴, and robust Mott-insulator phase⁵, wherein the control of quantum confinement and interlayer interaction plays an essential role.

The most intensively studied quantum phenomenon in bulk and monolayer TMDs is the charge-density wave (CDW). The CDW in TMDs has attracted tremendous attention because it provides an ideal platform to access a long-standing issue on the applicability of the Fermi-surface (FS)-nesting scenario, where the shift of FS with respect to the original one by the CDW wave vector causes the energy gain by the gap opening at the Fermi level (E_F). There is growing evidence that many of the CDWs observed in TMDs cannot be explained in terms of the simple FS nesting, and more exotic mechanisms (e.g., exciton formation, van-Hove band singularity, and **k**-dependent electron–phonon coupling) may be at work in TMDs^{6–9}.

Among TMDs, vanadium dichalcogenides VXc₂ (Xc = S, Se, and Te) are useful for investigating the interplay between FS nesting and CDW because this family of materials commonly undergoes CDW. Bulk 1T-VSe₂ shows CDW with a $4 \times 4 \times \sim 3$ periodicity triggered by the simple FS nesting^{10–12}, whereas the monolayer counterpart exhibits CDW with various periodicities (e.g., 4×4 , 4×1 , $\sqrt{7} \times \sqrt{3}$, $2 \times \sqrt{3}$, $4 \times \sqrt{3}$)^{12–20}. The situation is similar in 1T-

VTe₂ where the bulk exhibits a $3 \times 1 \times 3$ CDW²¹ while the monolayer shows various CDWs with, e.g., 4×4 , 4×1 , 5×1 , or $2\sqrt{3} \times 2\sqrt{3}$ periodicity²²⁻²⁷. This suggests that the simple FS-nesting scenario may be insufficient to account for a variety of CDW periodicities⁶.

To access this guestion, we have deliberately chosen monolayer VS₂ because the comprehensive understanding of CDW of the VXc₂ family may be essential to obtain insights into this problem. However, the nature of CDW in monolayer VS₂ has not been well investigated, partially because of the technical difficulty in employing the sample-fabrication method so far adopted for VSe₂ and $VTe_2^{13-19,22-27}$ due to the high vapor pressure of sulfur atom. In fact, previous works utilized catalytic reaction²⁸ or MBE with FeS source^{29,30} instead of MBE with V and S sources. While the CDW with local $7 \times \sqrt{3}R30^{\circ}$ or $9 \times \sqrt{3}R30^{\circ}$ periodicity³⁰ was observed in such monolayer films, the electronic band structure relevant to the occurrence of CDW and the mechanism of CDW are still unclear. We have overcome the difficulty in obtaining high-quality single-crystalline films by employing a unique sample-fabrication method that combines MBE and topotacticreaction technique, as detailed later. We investigated the electronic structure of grown monolayer film by micro-focused angle-resolved photoemission spectroscopy (µ-ARPES) and scanning tunneling microscopy (STM), together with first-principles band-structure calculations.

RESULTS

Fabrication and characterization of monolayer VS₂

First, we explain the fabrication and characterization of monolayer VS_2 . We epitaxially grew monolayer VTe_2 film on bilayer graphene/ SiC(0001) by the MBE method (Fig. 1a) and then replaced Te atoms with S atoms by topotactic-reaction technique in which

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Fig. 1 Fabrication of monolayer VS₂ film by combining MBE and topotactic reaction. a Schematics of topotactic growth procedure for monolayer 1T-VS₂ film. **b**, **c** RHEED patterns of VTe₂ and VS₂ films on bilayer (BL) graphene, respectively. **d** Direct comparison of RHEED intensity profiles between VTe₂ and VS₂. **e** Photoemission spectrum in wide E_B range of monolayer VS₂ measured with hv = 250 eV. Inset shows the comparison around the Te-4*d* core levels between VTe₂ and VS₂. **f** Constant current STM image of monolayer VS₂ in the surface area of 25 × 50 nm² measured at sample bias voltage $V_S = -2$ V and set-point tunneling current $I_t = 50$ pA. **g** Height profile along a red dashed line of (**f**).

sulfurization was carried out by exposing the VTe_2 film to a S atmosphere (for details, see "Methods")³¹. The reflection highenergy electron diffraction (RHEED) pattern for VTe₂ film (Fig. 1b) shows a sharp 1×1 streak pattern to confirm the monolayer nature of grown VTe₂ film²² since it is known that multilayer films have a 2×1 periodicity³². After sulfurization, the RHEED image still maintains a sharp 1×1 feature (Fig. 1c). The intensity profile of the RHEED pattern in Fig. 1d reveals a slight outward shift of peak position relative to the central peak after sulfurization, corresponding to the shrinkage of lattice constant. The photoemission spectrum of the sulfurized film (Fig. 1e) signifies sharp peaks originating from the S $2p_{1/2}$ and $2p_{3/2}$ spin-orbit satellites at binding energy ($E_{\rm B}$) of 162–163 eV. Prominent Te $4d_{3/2}$ and $4d_{5/2}$ spin-orbit satellites at E_B of 40-42 eV observed in monolayer VTe₂ completely vanish after sulfurization (inset to Fig. 1e), indicative of the complete replacement of Te with S. STM measurements for this sulfurized film (Fig. 1f) signify monolayer islands on bilayer graphene with a step height of 0.9 nm (Fig. 1g), supporting its monolayer nature^{33,34} (note that the STM image shows a doublelayer-like island in some areas due to the artifact associated with the shape of the tip, as reported in other monolayer TMDs^{35,36}). These results indicate that a monolayer VS₂ film with a negligible mixture of VTe2 was successfully grown on bilayer graphene/ SiC(0001).

Electronic states of monolayer VS₂

Figure 2a shows the valence-band ARPES intensity of monolayer VTe₂ measured at T = 40 K along the KFM cut of the hexagonal Brillouin zone (BZ). The band structure of monolayer VTe₂ is

characterized by highly dispersive holelike Te 5*p* bands and a weakly dispersive V 3*d* band near E_F^{22} . The topmost Te 5*p* band touches the V 3*d* band at the Γ point near E_F . After sulfurization (Fig. 2b), the holelike bands shift downward, and a relatively flat feature appears at $E_B = 2.5-3.0$ eV. This downward shift, which is attributed to the lower atomic energy level of the S 3*p* orbital relative to that of the Te 5*p* orbital, is better visualized in the ARPES-intensity plot near E_F in Fig. 2c, d. The width of the V 3*d* band along the Γ M cut is enhanced after sulfurization, suggesting the increase in the transfer integral between V 3*d* orbitals due to the shrinkage of the lattice constant.

Our first-principles band-structure calculations for free-standing monolayer 1T-VS₂ capture the overall characteristics observed in the experiment. As seen from a comparison of Fig. 2b, e, the relatively flat feature at $E_{\rm B} = 2.5 - 3.0$ eV and the highly dispersive topmost S 3p band observed in the experiment are well reproduced in the calculation. This suggests that our monolayer VS₂ film has the 1T structure. Also, the quantitative matching in the energy position of S 3p bands at the Γ point between experiments and calculations suggests a negligible charge transfer from the graphene substrate due to a weak van der Waals coupling at the interface. We also found small quantitative mismatches in the energy position and bandwidth between experiments and calculations. For example, the width of the V 3d band near $E_{\rm F}$ is 0.5 eV in the experiment, whereas it is 0.75 eV in the calculation. This is likely due to the mass-renormalization effect associated with the correlation of V 3d electrons. We found no evidence for the energy splitting of V 3d bands at T = 40 K within our experimental uncertainty, consistent with the DFT



Fig. 2 Band structure of monolayer VTe₂ and VS₂. a, **b** ARPES-intensity plots of monolayer VTe₂ and VS₂ films, respectively, measured along the K Γ M cut at T = 40 K. **c**, **d** Same as (**a**) and (**b**), but expanded around $E_{\rm F}$. Dashed curves in (**a**–**d**) are a guide for the eyes to trace the band dispersion. **e** Calculated band structure of monolayer 1T-VS₂ obtained with first-principles band calculations. Note that the overall intensity profile of VS₂ seems more diffuse than that of VTe₂, likely due to the increase in chalcogen defects and disorders in the crystal after sulfurization and the resultant enhancement in the electron scattering.

calculation for the non-magnetic phase (Fig. 2e), suggesting the absence of ferromagnetism.

To clarify the electronic states near $E_{\rm F}$, we have performed ARPES measurements in 2D k-space for monolayer VS₂. Figure 3a shows the contour plots at representative $E_{\rm B}$ slices at T = 40 K, together with the calculated equi-energy plots (red curves) for monolayer 1T-VS₂. At $E_B = E_F$, one can recognize a single bright intensity spot concentrated at the Γ point. This is in sharp contrast to the calculation that predicts a large ellipsoidal electron pocket centered at the M point. While such disagreement is seen up to $E_{\rm B} \sim 0.2 \, {\rm eV}$, the ARPES intensity appears to follow the calculated contours at $E_{\rm B} \ge 0.3$ eV. This can be recognized from the gradual movement of the intensity maxima from the Γ point toward the M point with increasing $E_{\rm B}$, which roughly follows the **k** location of the corner of ellipsoids. These results suggest that the spectralweight suppression on the ellipsoidal pocket is associated with the energy-gap opening. To see more clearly the gap opening, we show in Fig. 3b the ARPES intensity at T = 40 K measured along representative k cuts (cuts 1-5 in Fig. 3a), which cross the ellipsoidal pocket. Along cut 5 (Fig. 3b5), which nearly passes the M points, one can see two U-shaped features corresponding to the electron bands bottomed at $E_{\rm B} \sim 0.4$ eV at each M point. These features are qualitatively reproduced by the calculation along the same **k** cut in Fig. 3c, although the bandwidth is narrower in the experiment due to the mass-renormalization effect. Intriguingly, although the calculation shows a clear $E_{\rm F}$ -crossing of bands, the experimental dispersive feature loses its intensity around $E_{\rm F}$ due to the gap opening. This suppression is also observed along the **k** cuts around Γ (e.g., cut 1), while the energy scale of the suppression is systematically reduced on approaching the Γ point (cut 5 to 1).

Characteristic **k** dependence of the gap is better visualized by the energy distribution curves (EDCs) at the Fermi wave vectors (k_F 's) in Fig. 3d. At point 5 (which is almost on the MK line), one can find a broad hump at $E_B \sim 0.35$ eV, reflecting a large energy gap. This hump gradually moves toward E_F on approaching the Γ point and reaches $E_B \sim 0.1$ eV at the corner of the ellipsoidal pocket (point 1), accompanied by a positive leading-edge shift as seen in the inset to Fig. 3d. This suggests that the energy gap opens on the entire pocket at T = 40 K and is strongly



Fig. 3 CDW-gap opening on the entire Fermi surface. a Plots of ARPES intensity as a function of 2D wave vector at representative E_B 's for monolayer VS₂. Red solid curves indicate the calculated FS for monolayer 1T-VS₂. k_x and k_y are defined according to the BZ of BL graphene. Black solid lines represent the BZ of monolayer VS₂. **b1–b5** ARPES-intensity plots as a function of the wave vector and E_B , measured at T = 40 K along representative \mathbf{k} cuts shown by red dashed lines in (a) (cuts 1–5). **c** Calculated band dispersions in the normal state corresponding to cut 5. **d** EDCs at T = 40 K at representative \mathbf{k}_F points on the elongated pocket (points 1–5 of inset). The \mathbf{k}_F points were determined by tracing the minimum gap locus of the EDCs. The peak position is indicated by dots. Inset shows a comparison of EDC around E_F between gold (black curve) and monolayer VS₂ (red curve) obtained at point 1. **e** Magnitude of CDW gap at different \mathbf{k}_F points (points 1–5) estimated from the peak position and leading-edge midpoint of the EDCs.

anisotropic, as also highlighted by the plot of gap size Δ and leading-edge midpoint against k (Fig. 3e), which always takes a positive value irrespective of k (note that the leading-edge shift serves as an effective energy gap under a strong spectral broadening; for details, see Supplementary Note 1). We have confirmed that the gap is robust against temperature variation, as seen from the fact that it survives even at room temperature at point 1 (see Supplementary Fig. 1). It is noted that the EDCs in Fig. 3d always show a residual spectral weight around $E_{\rm F}$, reminiscent of the pseudogap in underdoped high- T_c cuprate superconductors³⁷. Such a pseudogap was also recognized in the CDW phase of other monolayer TMDs such as VSe_2 and $VTe_2^{10,14-17,22,23}$. While the exact mechanism to produce the pseudogap is unclear at the moment, we speculate that the strong damping of quasiparticle lifetime due to many-body interactions, such as coupling of electrons to CDW fluctuations and electron-electron scattering associated with electron correlation may play a role.

Stripe charge-density wave of monolayer VS₂

To clarify the origin of the energy gap, we have performed STM measurements. One can recognize a stripe feature associated with the CDW formation in the STM image at T = 4.8 K (Fig. 4a). The Fast Fourier transformation (FFT) image in Fig. 4b signifies the superstructure spots with a $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ periodicity. Intriguingly, this periodicity is apparently different from that of

bulk crystal $(3\sqrt{3} \times 3\sqrt{3}R30^{\circ})^{38}$. Further, it is also different from those of VSe₂ and VTe₂ monolayers in the CDW phase $(4 \times 4, 4 \times 1, \sqrt{7} \times \sqrt{3}, 2 \times \sqrt{3}, and 4 \times \sqrt{3}$ for VSe₂^{17,18}; $4 \times 4, 4 \times 1, 5 \times 1$, and $2\sqrt{3} \times 2\sqrt{3}$ for VTe₂^{23–27}). It is noted here that a recent STM study on monolayer VS₂³⁰ has reported the CDW composed of $7 \times \sqrt{3}R30^{\circ}$ and $9 \times \sqrt{3}R30^{\circ}$ superstructures and its gapless behavior at $E_{\rm F}$. This is in contrast to the present study showing a full gap at $E_{\rm F}$ associated with $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ CDW, which cannot be reproduced by the combination of $7 \times \sqrt{3}R30^{\circ}$ and $9 \times \sqrt{3}R30^{\circ}$ CDW (see Supplementary Fig. 2). Note that there exist intrinsic differences between our work and the work of ref.³⁰ regarding the experimental observation and interpretation of the CDW mechanism (for details, see Supplementary Note 3).

Reciprocal lattice vectors of the observed superlattice, \mathbf{g}_1 and \mathbf{g}_2 (white arrows in Fig. 4b), are written as $\mathbf{g}_1 = (2/9)\mathbf{b}_1 - (1/9)\mathbf{b}_2$ and $\mathbf{g}_2 = -(1/9)\mathbf{b}_1 + (5/9)\mathbf{b}_2$ with the original 1×1 reciprocal lattice vectors, \mathbf{b}_1 and \mathbf{b}_2 . The corresponding crystal structure drawn after the structural optimization in our first-principles band-structure calculations is shown in Fig. 4d, in which both V and S atoms are slightly displaced to form a superlattice with a large parallelogram unit cell. To clarify the influence of CDW on the band structure, we have performed band calculations for this superstructure, and the obtained band structure projected onto the original 1×1 BZ is shown in Fig. 4e (note that we assumed the existence of three domains rotated by 120° from each other, by taking into account the crystal symmetry). One can recognize that although the overall



spectral weight in the CDW phase traces the band structure of the original 1×1 lattice (dashed red curves), there exist characteristic deviations. For example, while the original V 3*d* band crosses E_F midway between the M and K points, the spectral weight in the CDW phase is suppressed around the crossing point, accompanied by a marked deviation of the band position from the original one. Such a CDW signature in the calculation is better visualized in an expanded view near E_F of the calculated spectral weight along the

MK cut in Fig. 4f. Corresponding ARPES intensity shown in Fig. 4g also signifies the spectral-weight suppression near E_F . To clarify the influence of CDW on the ARPES intensity in more detail, we compare in Fig. 4h, i the calculated spectral weight in the CDW phase with the ARPES intensity at T = 40 K along the KГM cut. Although the bandwidth of the topmost V 3*d* band is smaller in the experiment due to the mass-renormalization effect associated with the electron correlation, the overall ARPES intensity shows a

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Fig. 4 STM and band calculation of monolayer VS₂. a High-resolution STM image in surface area of $8 \times 8 \text{ nm}^2$ for monolayer VS₂ at T = 4.8 K. White broken rhombus indicates the unit cell of $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ superstructure, whereas the red solid rhombus corresponds to the original 1×1 unit cell. **b** FFT image of (**a**). White arrows indicate primitive reciprocal lattice vectors **g**₁ and **g**₂ for the $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ superstructure. **c** Calculated FS of monolayer 1T-VS₂ obtained by the first-principles band calculation. White arrows indicate **g**₁ and **g**₂. The absolute value of Fermi velocity $v_{\rm F}$ is depicted by gradual coloring. **d** The $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ superstructure obtained by the structural optimization. **a**₁ and **a**₂ indicated by black arrows are primitive lattice vectors of the original 1×1 1T structure. The black dashed rhombus corresponds to the unit of the cell of the $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ superstructure effect band structure for the 1×1 phase. **f**, **g** Comparison between the calculated band structure for the $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ superstructure and the ARPES intensity at T = 40 K along the KMK cut. The white dashed curve in (**f**) corresponds to the calculated band dispersion for the 1×1 phase. **h** Calculated spectral weight for the $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ superstructure and the ARPES intensity at T = 40 K. White dashed curves in (**h**) correspond to calculated band dispersion for the 1×1 phase.

better agreement with the calculated spectral weight for the CDW phase in comparison to the calculated band structure for the undistorted 1T phase (white dashed curves). Specifically, the V 3d band located slightly below $E_{\rm F}$ at the Γ point is well reproduced by the calculation for the CDW phase, whereas the calculated band for the undistorted phase is located above $E_{\rm F}$. Such a critical difference can also be confirmed by the band dispersion along the FK cut (left half of Fig. 4i), which signifies the existence of a dispersive V 3d band below $E_{\rm F}$ associated with the band folding due to the superstructure-induced periodic potential, consistent with the calculation for the CDW phase, but inconsistent with that for the 1×1 phase showing fully unoccupied bands along the FK cut (Fig. 4h). These results suggest that the anisotropic gap observed by ARPES originates from CDW, and some other mechanisms such as electron correlation are unlikely responsible for the gap opening (see Supplementary note 4). We also found from the quantitative analysis that the calculated energy gap along cut 1 (the FM cut) in Fig. 3a is 110 meV, whereas that along cut 5 (the MM cut) is 260 meV, qualitatively consistent with the anisotropic gap observed by ARPES (Fig. 3d). The CDW origin of the energy gap is also supported by the STM image which exhibits clear charge reversal between positive and negative bias voltages, which is a typical characteristic of the CDW (see Supplementary Fig. 5).

While we cannot completely rule out the possibility of a nonnesting-originated CDW mechanism at the moment, a natural starting point to understand the CDW mechanism may be the FS nesting which connects parallel segments of the elongated pocket. The regular nesting vector is $\mathbf{q} = \mathbf{g}_1$ or $\mathbf{q} = \mathbf{g}_2$, as widely discussed in many 2D and quasi-2D materials. In both cases, the k space spanned by \mathbf{g}_1 or \mathbf{g}_2 reproduces the superlattice spots in the FFT image of STM data. We shifted the calculated FS of monolayer VS₂ with respect to the original one by $\mathbf{q} = \mathbf{g}_2$ (Fig. 5a) and found that the parallel segments of FSs are not well connected; it only produces several crossings of original and shifted FSs at discrete k points as shown by orange circles. This would be natural because the \mathbf{g}_2 vector is not parallel to the 1D array of superspots in the FFT image and, thereby, unsuited to represent the observed CDW periodicity. On the other hand, the parallel segments of the vertically elongated pockets centered at M₁ appear to show a rather good nesting condition with $\mathbf{q} = \mathbf{g}_1$, whereas a large area of side pockets at M₂ and M₃, as well as the curved region of pockets around the Γ point remains un-nested. Obviously, the normal FS nesting with $\mathbf{q} = \mathbf{g}_1$ (as well as $\mathbf{q} = \mathbf{g}_2$) is insufficient to explain the gap opening on the entire FS, unlike the case of some other TMDs where the simple FS nesting plays a dominant role^{10,11} (note that the consideration of 3q nature of CDW is still insufficient to explain the gap opening at the curved region of the pockets; for details, see Supplementary Fig. 6).

DISCUSSION

Higher-order Fermi-surface nesting

We propose that a key to pinning down the mechanism of CDW in VS₂ lies in consideration of a longer **q** vector, $\mathbf{q'} = 2\mathbf{g}_1$, termed here higher-order FS nesting vector, which also reproduces the superlattice points in the FFT image. The nesting vector twice (integer times in the more general form) larger than that of the original nesting vector $\mathbf{q} (= \mathbf{g}_1)$ is not usually taken into account as a CDW nesting vector. As shown in Fig. 5c, the original and shifted FSs show an overlap in a larger **k** area, not only in the straight segment part of the pockets at M₂ and M₃ but also in the curved region around the corner of these pockets. Although the nesting vector $\mathbf{q}' (= 2\mathbf{g}_1)$ does not cover the whole pocket by the nesting with leaving the poorly nested region, e.g., along the pocket at M₁, the cooperation of two nesting vectors $\mathbf{q} = \mathbf{g}_1$ and $\mathbf{q}' = 2\mathbf{g}_1$ enables the full-gap opening as observed by ARPES, since the nested area almost fully covers the pocket as shown in Fig. 5d. Such a visual argument on the FS nesting is more quantitatively supported by our calculations. Calculated electronic susceptibility $\chi(\mathbf{q})$ shows a local enhancement (see Supplementary Fig. 7), and the calculated acoustic phonon dispersion shows a negative frequency (see Supplementary Figs. 8–10) at $\mathbf{q'} = 2\mathbf{g}_1$, supporting the CDW instability at this wave vector. These results suggest that the cooperation of **q** and 2**q** nesting is likely responsible for the occurrence of CDW in monolayer VS₂. It is noted that the CDW gap monotonically increases on moving away from the BZ center, as shown in Fig. 3d, e. Since this seems to be not fully consistent with the fine structure of the FS-overlap condition discussed in Fig. 5d, one may need to take into account the influence of strong spectral broadening associated with the many-body interactions that smears out fine structures in the FS-overlap condition. Also, one may need to consider that the nesting vector of \mathbf{g}_1 and $2\mathbf{g}_1$ plays primary and secondary roles, respectively, to the total magnitude of the CDW gap, while consideration of **q**-dependent electron-phonon coupling may be necessary to fully account for the observed k-dependence of the CDW gap. We will come back to this point later.

Difference between VS₂ and VTe₂

The 2**q** nesting proposed in this study captures the difference in the CDW behavior between monolayer VS₂ and monolayer VTe₂. The calculated χ (**q**) and phonon dispersion for monolayer VS₂ show a local enhancement also at the commensurate wave vector of **q** ~ 1/2ΓM, which corresponds to the 4 × 4 periodicity. However, the 4 × 4 CDW is not realized in monolayer VS₂. The calculated free energy for the $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ superstructure per VS₂ primitive unit cell is 18 meV lower than that of the original 1T structure. On the other hand, the free energy for the 4 × 4 superstructure is 4 meV lower than that of the original 1T structure³⁰. This suggests the more stable nature of $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ CDW. As opposed to the case of monolayer



Fig. 5 Schematics of FS-nesting condition. a-c Calculated FS (red solid curves) and its shifted replicas (blue broken lines) that take into account the nesting vector $\mathbf{q} = \mathbf{g}_2$, \mathbf{g}_1 , and $2\mathbf{g}_1$, respectively. \mathbf{g}_1 and \mathbf{g}_2 vectors are indicated by black solid arrows. Nesting vectors with positive and negative signs are indicated by blue solid and blue dashed arrows, respectively. FS segments where the original and shifted FSs overlap are indicated by orange circles and orange shades. \mathbf{d} Schematics of nested FS region, which simultaneously takes into account $\mathbf{q} = \mathbf{g}_1$ (same as (b)) and $\mathbf{q} = \mathbf{g}_2$ (same as (c)) nesting vectors.

VS₂, the 4×4 CDW emerges in monolayer VTe₂²³⁻²⁷. A key to understanding this difference may lie in the difference in the FS topology. VS₂ hosts an elongated electron pocket at the M point (Fig. 3a), whereas VTe₂ hosts a triangular hole pocket at the K point, giving rise to a marked difference in the FS shape around the Γ point (see Supplementary Fig. 12). This causes the poorer nesting condition with the higher-order nesting vector so that $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ CDW is not stable in VTe₂. In other words, the curved segments of the elongated pocket in VS_2 around the Γ point are effectively nested by the 2q vector and contribute to the energy gain to stabilize CDW. As a consequence, a CDW gap opens on the entire FS in VS_2 (Fig. 3d) by the cooperation of primary **q** and secondary 2**q** nesting vectors, in contrast to VTe₂ where the corner of the triangular pocket remains gapless due to the insufficient nesting (see Supplementary Fig. 12). It is emphasized again that to account for the gap anisotropy of VS_{2} , one may need to consider the primary and secondary roles of the q and 2q nesting vectors, respectively. In other words, the probability of electron scattering via 2q phonon is much lower than that via ${\boldsymbol{\mathsf{q}}}$ phonon, so the latter plays a primary role in stabilizing CDW. The primary **q** vector, which connects parallel segments of the elongated pocket around the M₁ point, effectively reduces the total energy to stabilize CDW, leading to the larger CDW gap along the MK cut. On the other hand, the 2**q** vector, which essentially connects curved segments of FS around the F point, plays a secondary role in stabilizing CDW so that the CDWgap size around the Γ point is relatively small, leading to the anisotropic gap nature in monolayer VS₂. It is noted, though, that this argument is based on our speculation and needs to be further

corroborated by experiments that modulate the FS-nesting condition (by carrier doping, electrical gating, or epitaxial strain) to see the disappearance/weakening of CDW and also by the sophisticated theoretical modeling.

Historically, the importance of higher-order nesting in CDW formation was theoretically proposed in the 1970s for a purely 1D system with a half-filled condition as the $4k_{\rm F}$ CDW^{39,40}, which involves Umklapp scattering. In quasi-2D TMDs and quasi-1D conductors, the CDW, which involves a longer **q** vector extending the first BZ, was proposed to account for the lock-in transition between incommensurate and commensurate CDW⁴¹⁻⁴⁴ and the unidirectional incommensurate CDW^{45,46}. On the other hand, the cooperation of ordinary nesting and higher-order nesting has not been spectroscopically clarified, presumably because of the lack of a suitable material platform. In this regard, monolayer VS₂, which shows a peculiar CDW with the incommensurate $\sqrt{21}R10.9^{\circ} \times \sqrt{3}R30^{\circ}$ periodicity, is a suitable platform to demonstrate such nesting because the FS curvature is welloptimized to promote the 2q nesting. The concept of higherorder-nesting-driven CDW proposed in this study may be applied to some other low-dimensional materials where a simple nesting scenario is hard to account for the peculiar CDW behaviors.

METHODS

Sample preparation

Monolayer VS₂ film was fabricated by two steps; MBE of VTe₂ film and topotactic reaction to replace Te with S atoms. First, monolayer VTe₂ film was prepared on bilayer graphene by

MBE^{22,32}. Bilayer graphene was fabricated by resistive heating of an *n*-type SiC(0001) single-crystal wafer at 1100 °C for 30 min. Subsequently, monolayer VTe₂ film was grown by evaporating V atoms on the bilayer graphene substrate in a Te-rich atmosphere. The substrate was kept at 250 °C during epitaxy, and then the asgrown monolayer VTe₂ film was annealed for 30 min. Second, we fabricated monolayer VS_2 film by replacing Te with S atoms by using the topotactic reaction^{31,47}. The monolayer VTe_2 film was annealed in a S atmosphere under high vacuum ($\sim 1 \times 10^{-7}$ Torr); the substrate was heated up to 300 °C during the sulfurization, and then the as-grown film was annealed for 30 min at 300 °C. In the sulfurization process, the sulfur source (99.999%) in a glasstube cell equipped with a homemade evaporator was melted by heating by a ribbon heater. The sulfur flux was precisely controlled by tuning the leak rate of the variable leak valve. Although we were unable to estimate the exact sulfur flux, we monitored the relative flux by reading the vacuum inside the growth chamber during evaporation. To effectively proceed with the sulfurization, we tried several experimental conditions with different (1) sulfur flux, (2) annealing temperature, and (3) annealing time of the sample during and after the evaporation. As a result, we found that the optimized conditions are (1) 1×10^{-7} Torr in the growth chamber during the evaporation for the sulfur flux (note that the base pressure of the growth chamber is 1×10^{-10} Torr), (2) 300 °C for the annealing temperature during/after evaporation, and (3) at least 30 min for the annealing time. The growth process was monitored by RHEED and low-energy electron diffraction (LEED). After the growth, the film was transferred to the ARPES measurement chamber without exposing it to air.

ARPES and STM measurements

ARPES measurements were performed by using a DA-30 electron energy analyzer with a micro-focused synchrotron-radiation at the beamline BL-28A of Photon Factory (KEK). The beam spot was $10 \times 12 \,\mu m^{248}$. Circularly polarized light of $hv = 100 \, eV$ was used to excite photoelectrons. The energy and angular resolutions were set to be 25–50 meV and 0.2–0.3°, respectively. STM measurements were performed using a custom-made ultrahigh vacuum (UHV) STM system⁴⁹ at $T = 4.8 \, \text{K}$ under UHV below $2.0 \times 10^{-10} \, \text{Torr}$. Te capping with ~20 nm thickness was deposited on VS₂ film to protect the surface. This capping was removed in the STM chamber by Ar-ion sputtering for 30 min and subsequent annealing at 250 °C for 120 min. We used PtIr tips. All STM images were obtained in constant current mode.

First-principles calculations

First-principles band-structure calculations were carried out by using Quantum ESPRESSO code^{50,51} with generalized gradient approximation⁵² with the Perdew–Burke–Ernzerhof (PBE) realization using PSLibrary⁵³. A pseudopotential of the Augmented-Plane-Wave (APW) type was used. The plane-wave cutoff energy and uniform k-point mesh were set to be 60 Ry and $24 \times 24 \times 1$, respectively. Also, the charge cutoff energy was set to be 700 Ry. The k grid in the DFT calculation for the supercell was set to be $6 \times 3 \times 1$. All structures were fully relaxed for monolayer VS₂ with lattice constant a = 3.18 Å. The thickness of inserted vacuum layer was set to be more than 15 Å to prevent interlayer interaction. We have carried out the unfolding of bands for the $\sqrt{21R10.9^\circ} \times \sqrt{3R30^\circ}$ superstructure by using a method proposed in the previous literature⁵⁴. All the atoms are fully relaxed until the Hellmann–Feynman force becomes lower than 1×10^{-4} eV/Å. Phonon calculations were carried out using the density functional perturbation theory (DFPT) implemented in Quantum ESPRESSO. The phonon dispersions were obtained by setting at $24 \times 24 \times 1$ k-mesh and $12 \times 12 \times 1$ q-grid. The electronic temperature (Fermi-Dirac smearing) was set at 0.01 Ry for entire calculations. The DFT calculation based on the CDW-induced superstructure

unit cell was carried out by using ISODISTORT tools⁵⁵. Specifically, we have taken into account 12 types of phonon modes from the consideration of crystal symmetry. By changing the initial atomic position of V sites, we have structurally optimized the atomic coordinates of all the S atoms in the unit cell.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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AUTHOR CONTRIBUTIONS

The work was planned and proceeded by discussion among T.K., K.S., K.N., and T.S. T.K. and K.S. fabricated ultrathin films. T.K. carried out the band-structure calculations. T.K., K.S., K.Y., S.S., and K.N. performed the ARPES measurements. H.O. and T.F. performed the STM measurements. T.K., K.S., T.T., and T.S. finalized the manuscript with inputs from all the authors.

COMPETING INTERESTS

The authors declare no competing interests.

ADDITIONAL INFORMATION

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