# OPEN A modular technique of Booth encoding and Vedic multiplier for low-area and high-speed applications 

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#### Abstract

A technique for efficiently multiplying two signed numbers using limited area and high speed is presented in this paper. This work uses both the Booth and Vedic multiplication sutra methodologies to enhance the speed and reduction in the area by using two VLSI architectures of radix encoding techniques-Radix-4 and Radix-8-with the Vedic multiplier. The functionality of the proposed methods is tested using an Artix-7 Field Programmable Gate Array (FPGA-XC7A100T-CSG324) in Xilinx Vivado 2019.1 and ASIC 45 nm technology. Two methods of Booth encoding using Vedic multiplier (Urdhva-Tiryakbhyam sutra) were used to develop, and examine the benefits of rapid computational multiplier. The results of the proposed multiplier for Booth-Vedic-Radix-4 encoding (BVR-4) decrease area by $89 \%$ and improve Area-Delay Product (ADP) by $72 \%$ for a 16 -bit multiplier when subjected to other existing multipliers. The Booth-Vedic-Radix-8 (BVR-8) method shows that there will be an $89 \%$ reduction in area and an improvement in ADP by $72 \%$ for the 16 -bit multiplier. The performance is evaluated regarding area occupancy (i.e., LUTs number) and propagation delay (output time). In terms of resource utilization, the proposed BVR-4 and BVR-8 multipliers outperform all the current designs with a marginal effect on speed and area for narrower bit-width ranges.


Everyone nowadays wants portable technology that is quick, takes little power, and packs as many components as possible into a small space. To achieve all of these goals, it is critical to develop an algorithm that solves all of these challenges. Although these methods are fast, the actual calculation time is determined by the processor's system clock ${ }^{1}$. In processors, Multiplication is now an essential component of binary computers. Therefore, building multipliers is critical for computer scientists and engineers on both theoretical and practical levels ${ }^{2}$. Multipliers can generally be built in parallel or serial fashion. Serial multipliers are crucial when contemplating low-cost designs. Parallel multipliers are the preferred solution if a high-speed architecture is required. Furthermore, multipliers can be both signed and unsigned ${ }^{3}$.

## Related work

The prevalent multiplication procedure consists of three major phases:

1. Partial product generation (PPG)—Reduction of bitlength.
2. Partial product reduction (PPR)-Vertical processing.
3. Partial product accumulation (PPA)-Addition.

The second phase is critical for power consumption, cost, and overall performance. As a result, the power consumption and performance constraints of the multiplier are essential ${ }^{4}$. The add-and-shift operation of the array multiplier produces more partial products (PP) than the tree multiplier, boosting Power and Delay ${ }^{5}$. Despite having fewer components than an array multiplier, the PPs are organized in rows or columns and have extensive interconnections ${ }^{6}$. Dadda Multiplier has a higher carry propagation adder since it just makes the necessary reduction. Dadda Multiplier outperforms Wallace Multiplier in terms of speed ${ }^{7}$. The Karatsuba algorithm performs quick multiplication. It employs a smaller number of little multipliers than the Wallace tree multiplier ${ }^{8}$. To do the multiplication, a fast Carry-Save Add-shift (CSAs) multiplier is employed, which results in one-third the speed

[^0]of an unsigned multiplier ${ }^{9}$. A fast multiplication in 2's complement format is described to create fewer PP rows from $n / 2+1$ to $n / 2$ before applying the PPR approach to prevent the occurrence of the additional row, which increases multiplication speed for 8 -bit and 16 -bit multipliers ${ }^{10}$.

Using one of the several multiplication algorithms available, the speed of operation can be boosted over the classic shift and add approach. Booth's method, a uniform shift approach, examines two multiplier bits at a time to identify the correct multiplicand multiple to add the $\mathrm{PP}^{11}$. Carry-free addition is accomplished by the use of redundant binary systems. The propagation delay problem is solved by the Redundant Binary adder ${ }^{12}$. For some signed numbers-based applications, it may still be viable to develop the requisite hardware accelerators utilizing unsigned multiplier designs ${ }^{13}$.

The number of PPs is proportional to the Radix-k of Booth encoding by a factor of $\log _{2}(\mathrm{k})$, implying that the number of PPs reduces by half while Radix- k multiplies by four ${ }^{14}$. The Radix-k Booth encoding system is identified by the equation

$$
\begin{equation*}
\text { Radix- } \mathrm{k}=1+\log 2 \mathrm{r}, \tag{1}
\end{equation*}
$$

where $r$ is the number of encoding bits to be considered ${ }^{15}$. For example, Radix-4 Modified Booth Encoding (MBE) requires multiples of the multiplicand (X) of 0,1 , and 2 to generate PPs, lowering the height of the PP matrix from N to $\mathrm{N} / 2$. All of these multiples are easily obtained by using shift and negation operations on X . Similarly, Radix- 8 MBE requires X multiples of $0,1,2,3$, and 4 , while lowering the height of the PP matrix from N to $\mathrm{N} / 3^{16}$. The redundant binary PPG achieves the largest reduction in the number of PPs, around $75 \%$, for a Radix-4 multiplier ${ }^{17}$.

A modified Radix-4 Booth multiplier that only adds non-zero Booth encodings and disregards zero operations ${ }^{18}$. To do the hard multiple 3 X operations, use $3 \mathrm{X}=2 \mathrm{X}+\mathrm{X}^{19}$. Radix-8 Booth multiplier uses the approximation approach by employing an approximate 2 -bit adder ${ }^{20}$. There are two types of modular hybrid adder architectures employed. It is created by combining carry-skip, carry look-ahead, and Ripple Carry Adder (RCA) $)^{21}$. The high-performance Redundant binary multiplier's appeal has been largely attributed to two key features: high modularity and carry-free addition ${ }^{22}$. Table 1 summarizes all of the multipliers and displays their properties in terms of Area, Power, Complexity, Delay, and Implementation.

A multi-precision binary multiplier architecture was created to reduce hardware and space consumption as well as latency and delay ${ }^{23}$. The beginning of the twentieth century saw the deciphering of the incredible Vedic calculation method. The functionality of Vedic mathematics is its most astounding feature ${ }^{24}$. Table 2 illustrates the strategies and procedures that Tirthaji created to reinforce the rules found in 16 sutras and 13 up-sutras, which were called Vedic Mathematics. The Nikhilam and Urdhva sutras were the focus of most investigations for the development of multipliers ${ }^{25}$. Researchers have also employed Nikhilam and UT multiplication methods. Due to the simultaneous creation and addition of the PPs, the former approach is quick ${ }^{5}$. Beneficial takeaways from both sutras have been made, and a novel architecture for quick and effective multiplication has been constructed ${ }^{26}$.

A multiplier architecture is designed for low-cost power and high-performance applications based on ancient Vedic Mathematics ${ }^{27}$. Vedic methods were used to square, and the results were evaluated using Virtex-4vlx15sf363-12 ${ }^{28}$. The $8 \times 8$ Nikhilam sutra is actualized for three different sets of bases using the idea of UT ${ }^{29}$. For a 16-bit multiplier, a novel Vedic Mathematics architecture built on UT was introduced. To lower the vertical critical route delay, compressors are utilized with full and half adders ${ }^{30}$. The Vedic multiplier is a combination of two compressor types: 4:2 and 7:2. After calculating the area and latency, it was shown to be 1.12 times faster than the other multiplier ${ }^{31}$.

The redundant binary representation of the Signed Vedic multiplier (SVM) architecture was used in the UT sutra. It is possible to achieve carry-free addition in redundant binary representation ${ }^{33}$. The proposed method performs multiplication using a combination of the UT algorithm and Booth encoding. The multiplier is small and requires less space based on Booth encoding, but the UT sutra increases speed ${ }^{34}$. Based on the anurupyena sutra of Vedic arithmetic, it uses a high-performance and area-efficient square architecture for variable bit operands ${ }^{35}$. The Spartan 6 FPGA implementation models the hybrid parallel adder-based multiplier, which is utilized to improve multiplier performance ${ }^{36}$.

One drawback of the current technique is that it takes up more space and has a bigger delay in the PPR (second stage of the multiplication phase) ${ }^{25,33,34}$. All previously substantiated Vedic systems can handle only unsigned integers, which summarises the complexity of the proposed technique. By using the Booth encoding process and the UT technique of the Vedic multiplier in the second step, we have expanded the applicability of Vedic Mathematics to signed integers in this work. The signed Vedic multiplier and Booth encoding both resolve

| S. no. | Parameters | Shift and add | Array multiplier | Modified booth multiplier | Modified booth wallace <br> multiplier | Vedic multiplier |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1. | Serial/parallel | Serial | Parallel | Parallel | Parallel |  |
| 2. | Area | Small | Large | Medium | Medium |  |
| 3. | Power consumption | Small | Large | Medium | Medium |  |
| 4. | Delay | Large | Medium | Small | Medium |  |
| 5. | Complexity | Simple | Simple | Complex | Smallest | Cmallest |
| 6. | Implementation | Easy | Mesy | Complex |  |  |

Table 1. Multipliers circuit comparison ${ }^{14}$.

| S. no. | Name | Meaning |
| :--- | :--- | :--- |
| 1. | Anurupyeshunyamanyat | If one is in ratio, the other is zero |
| 2. | ChalanaKalanabyham | Similarities and differences |
| 3. | Ekadikena Purvena | Compared to the previous one, it is one more |
| 4. | Ekayunene Purvena | Compared to the previous one, it is one less |
| 5. | Gunakasamuchyah | The sum of the factors = factor of the sum |
| 6. | Gunitasmuchyah | The sum of the product = product of the sum |
| 7. | Nikhil Navatashcaramam Dashtah | All from 9 and the last from 10 |
| 8. | Paraavartya Yojayet | Adjust and transpose |
| 9. | Puranapuranabhyam | By non-completion or completion |
| 10. | Sankalana Vyavakalanabhyam | By subtraction and addition |
| 11. | Shesanyankena Charamena | The remainder by the last digit |
| 12. | Sopaantyadvayamantyam | The ultimate and twice the penultimate |
| 13. | ShunyamSaamyasamuccaye | If the sum same and that sum is zero |
| 14. | Urdhva Tiryakbhyam | Cross-wise and vertically |
| 15. | Vyashtisamanstih | Whole and part |
| 16. | Yaavadunam | Whatever the extent of its deficiency |

Table 2. Sixteen Vedic sutras ${ }^{32}$.
the carry-free propagation issue, which is the motivating factor behind the suggested work. The distinctions between the Vedic multiplier and the Booth multiplier have been examined in several survey articles. However, in this paper, a novel efficient architecture for quick multiplication computation is developed by combining the Booth encoding and Vedic multiplier techniques due to the advantages of parallel processing at the PPR stage and by taking into account the key advantages of all the sutras ${ }^{33,37-42}$. Removal of noise in digital images is done through the filter ${ }^{43}$. Less heat dissipation with reversible logic gates was designed ${ }^{44}$.

The contributions of this paper are as follows:

1. This work mainly focuses on the second stage of PPR since it consumes more area with less speed. Recent research focuses on PPR to reduce the area and improve the speed performance. This research focuses on PPR and how Booth encoding methods and Vedic sutras reduce area while improving speed. In the proposed study, both techniques combine the benefits of high speed with the method of Vedic sutras and low area with Booth encoding.
2. The reduction of propagation delay in the PPR using a novel encoder is proposed. The proposed method extends the Vedic architecture to signed integers.
3. Fewer resources were used when the Booth multiplier and Vedic multiplier (UT) sutra were combined.

The section of the paper is structured as follows: The proposed method for the BVR-4 and BVR-8 systems is covered in "Proposed method" section. The findings and a discussion of the suggested BVR-4 and BVR-8 design are given in "Results and discussion" section. In "Conclusion" section, the paper concludes.

## Proposed method

Effective computing units are provided by the Vedic design in the review of existing methods, but only for unsigned values. When thoroughly examined, signed numbers are generally the most appropriate for a variety of purposes. The proposed method expands the applicability of Vedic architecture to signed integers and offers a reduction in area and time-efficient architecture at the PPR level. The recommended method is divided into three stages overall.

First, Booth encoding (multiplier trits are encoded) is performed.
(i) PPG-reduction of Bit length
(ii) PPR-vertical processing
(iii) PPA- addition

## Stage-I: PPG-booth encoding

Radix-4 booth algorithm
The first section discusses how the Radix-4 encoding rule works. A normal multiplication procedure must be used to multiply the multiplicand and multiplier of n bits, which results in n -rows of partial products and an increase in time complexity and area. Comparing the modified Booth multiplier-Radix-4 to other types of serial-parallel multipliers, it is smaller, quicker, and uses less power. An n-bit multiplication operation requires less space when using the Radix-4 Booth encoding approach since only half of the PP rows are required.

As seen in Fig. 1, the contiguous multiplier trits are clustered together with the overlapping of the last bit in the past cluster to generate new encoding groups. For instance, a multiplier bit-width of 4 results in the creation of two new Yn0 and Yn1 encoding groups, which lowers the total PP row to half of its original rows. In the same


Figure 1. Contiguous trits of multiplier-4-bit width. Mlr multiplier bits, Yn0, Yn1 new encoding groups of 1 and 2.
way, Fig. 2 bit-width of 8 results in the formation of four new encoding groups for Yn0, Yn1, Yn2, and Yn3, and Fig. 3 bit-width of 16 results in the formation of eight new encoding groups for Yn0, Yn1, Yn2, Yn3, Yn4, Yn5, Yn6, and Yn7. However, when compared to the conventional multiplication procedure, the number of PP rows will be greater when compared with the Booth encoding procedure. This is the main benefit of the proposed method in the initial PPG step. The PP rows were reduced to half the number of varying operand sizes.

To calculate the PP rows for the operand size of

1. 4 -The number of rows required is 2 .
2. 8 -The number of rows required is 4 .
3. 16 -The number of rows required is 8 .

For the proposed method of BVR-4, the pseudo-code is explained below. The given data is first encoded according to Table 3, and then the multiplication operation is carried out.


Figure 2. Contiguous trits of multiplier-8-bit width. Mlr multiplier bits, Yn0, Yn1, Yn2, Yn3 new encoding groups of 1,2,3 and 4.


Figure 3. Contiguous trits of multiplier-16-bit width. Mlr multiplier bits, Yn0, Yn1, Yn2, Yn3, Yn4, Yn5, Yn6 and $Y n 7$ new encoding groups of $1,2,3,4,5,6,7$ and 8.

| S.no. | Multiplier bits |  |  | Encoding rule | Resultant encoded bits |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{Mrr}_{2}$ | Mlr ${ }_{1}$ | Mlr |  | R2 | R1 | R0 |
| 1. | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2. | 0 | 0 | 1 | +1 | 0 | 0 | 1 |
| 3. | 0 | 1 | 0 | +1 | 0 | 0 | 1 |
| 4. | 0 | 1 | 1 | +2 | 0 | 1 | 0 |
| 5. | 1 | 0 | 0 | -2 | 1 | 1 | 0 |
| 6. | 1 | 0 | 1 | -1 | 1 | 1 | 1 |
| 7. | 1 | 1 | 0 | -1 | 1 | 1 | 1 |
| 8. | 1 | 1 | 1 | 0 | 0 | 0 | 0 |

Table 3. Radix-4 encoding rule.

Rule for combining adjacent trits.
Pseudo code of BVR-4 method:
BEGIN
GET Mld,Mlr BITS $\quad$ *Input-Data given-Mld-Multiplicand, Mlr-Multiplier
INSERT " 0 " at LSB of Mlr
FOR $\mathrm{i}=1$ to N
Mlr-GROUP 3 BITS
END

| MULTIPLY Yn0,Yn1,Mld |
| :--- | :--- |
| FOR $\mathrm{i}=1$ to N |
| PP[i]<<2 |
| END |
| FOR $\mathrm{i}=1$ to N |
| ADD PP[i] |
| END |

1. To check whether the given bit-width is odd or even if it is odd perform a sign extension of 1 bit and if it is even no need to perform a sign extension.
2. The foremost step is to add " 0 " at the LSB of the multiplier bits.
3. Further, the successive clustering of trits is carried out.
4. New encoding groups are created to perform the multiplication operation.

In Table 3, the multiplier trits are encoded using the Radix-4 encoding rule to build a new encoding group in the form of a two's complement representation of the multiplier trits spanning from $0,+1,+2,-2,-1$. The multiplier bits are multiplied with the multiplicand to accomplish the PPG operation, which results in the PP rows, according to the new encoded rule. The following stage of the operation was carried out after the production of incomplete product rows. Following the encoding procedure, the encoded bits create new groups of trits, each of which is represented in non-redundant radix-4 format.

## Radix-8 Booth algorithm

A higher representation radix results in fewer digits when representing a given range of integers. As a result, as we advance to higher radices, a digit-at-a-time multiplication method uses fewer cycles. The Radix-8 Booth method decreases the PP rows even more to $[(N / 3)+1]$, resulting in a substantially smaller area utilized when compared to the Radix-4 approach. The multiple hard problems are solved in this approach by expressing the 2 's complement of multiplier bits and multiplying it with the multiplicand bits.

In Fig. 4, multiplier bits are grouped in terms of the quad to form a new encoding group, for example, a multiplier bit-width of 4 creates 2 new encoding groups with the sign extension of multiplier bits for lack of contiguous quads, thereby reducing the overall PP row into half of their original rows. Similarly, in Fig. 5, for a bit-width of 8, it forms a 3 new encoding group, and similarly, in Fig. 6, for a bit width of 16, it forms a six new encoding group. So, when compared with the Radix-4 encoding rule it produces fewer PP rows. To calculate the PP rows for the operand size of


Figure 4. Contiguous quads of multiplier-4 bit-width. Mlr multiplier bits, Yn0, Yn1 new encoding groups of 1 and 2.


Figure 5. Contiguous quads of multiplier-8 bit-width. Mlr multiplier bits, Yn0, Yn1, Yn2 new encoding groups of 1,2 and 3 .


Figure 6. Contiguous quads of multiplier-16 bit-width. Mlr multiplier bits, Yn0, Yn1, Yn2, Yn3, Yn4 and Yn5 new encoding groups of $1,2,3,4,5$ and 6.

1. 4 -The number of rows required is 2 .
2. 8 -The number of rows required is 3 .
3. 16 -The number of rows required is 6 .

Rule for combining adjacent quads.

Pseudo code of BVR-8 method:
BEGIN
GET Mld,Mlr BITS
INSERT " 0 " at LSB of Mlr
FOR $\mathrm{i}=1$ to N
GROUP 4-BITS-Mlr
END
MULTIPLY Yn0,Yn1,Mld
FOR $\mathrm{i}=1$ to N
PP[i]<<3
END
FOR $\mathrm{i}=1$ to N
ADD PP[i]
END
*Input-Data given-Mld-Multiplicand, Mlr-Multiplier

* Intermediate product-Partial Product
* Arithmetic left shift thrice
*Result-Final Product

1. To check whether the given bit-width is odd or even if it is odd perform a sign extension of a sufficient bit and if it is even no need to perform a sign extension.
2. The foremost step is to add " 0 " at the LSB of the multiplier bits.
3. After adding, the successive grouping of the quad is carried out.
4. New encoding groups are created to perform the multiplication operation.

For the proposed method of BVR-8, the pseudo-code is explained below. The given data is first encoded according to Table 4, and then the multiplication operation is carried out.

In Table 4, the multiplier quads are encoded using the Radix-8 encoding rule to build a new encoding group in the form of a two's complement representation of the multiplier. The multiplier bits are multiplied with the multiplicand to accomplish the PPG operation, which results in the PP rows, according to the new encoded rule. The following stage of the operation was carried out after the production of incomplete product rows. Following the encoding procedure, the encoded bits create new groups of quads, each of which is represented in non-redundant Radix- 8 format.

| S.no. | Multiplier bits |  |  |  | Encoding rule | Resultant encoded bits |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{Mlr}_{3}$ | Mlr ${ }_{2}$ | M1r ${ }_{1}$ | Mlr ${ }_{0}$ |  | R3 | R2 | R1 | R0 |
| 1. | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 2. | 0 | 0 | 0 | 1 | +1 | 0 | 0 | 0 | 1 |
| 3. | 0 | 0 | 1 | 0 | +1 | 0 | 0 | 0 | 1 |
| 4. | 0 | 0 | 1 | 1 | +2 | 0 | 0 | 1 | 0 |
| 5. | 0 | 1 | 0 | 0 | +2 | 0 | 0 | 1 | 0 |
| 6. | 0 | 1 | 0 | 1 | +3 | 0 | 0 | 1 | 1 |
| 7. | 0 | 1 | 1 | 0 | +3 | 0 | 0 | 1 | 1 |
| 8. | 0 | 1 | 1 | 1 | +4 | 0 | 1 | 0 | 0 |
| 9. | 1 | 0 | 0 | 0 | -4 | 1 | 1 | 0 | 0 |
| 10. | 1 | 0 | 0 | 1 | -3 | 1 | 1 | 0 | 1 |
| 11. | 1 | 0 | 1 | 0 | -3 | 1 | 1 | 0 | 1 |
| 12. | 1 | 0 | 1 | 1 | -2 | 1 | 1 | 1 | 0 |
| 13. | 1 | 1 | 0 | 0 | -2 | 1 | 1 | 1 | 0 |
| 14. | 1 | 1 | 0 | 1 | -1 | 1 | 1 | 1 | 1 |
| 15. | 1 | 1 | 1 | 0 | -1 | 1 | 1 | 1 | 1 |
| 16. | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |

Table 4. Radix-8 encoding rule.

## Stage-II: PPR (Vedic multiplication)

Because PPG and PPR occur serially in a typical Booth multiplier, the vertical critical path latency increases. As a result, as a unique feature introduced in this research, the produced PPs are achieved by parallel processing in the second stage of PPR. This is one of the benefits of the unique work that was carried out. Because the second stage consumes the majority of the space, power, and delay in all assessed papers, an innovation was added in the second stage to carry out the PPR approach by employing the notion of Vedic Mathematics. Among the sixteen sutras in Vedic Mathematics, the UT and Nikhilam sutras are ideally suited for multiplication. The former sutra is usable for both binary and decimal multiplication and is best suited for lesser bit widths, whereas the latter sutra is best suited for greater bit widths multiplication. The PPR stage in the proposed work was carried out utilizing the Vedic multiplier idea employing the UT sutra (criss-cross multiplication), which involves its operation by simply conducting the AND gate operation in all bit multiplication procedures.

The newly encoded groups conduct vertical and cross-wise multiplication using the UT sutra. The resulting PPs are formed after conducting the criss-cross procedure. Similarly, the same method is used for operand sizes with varying bit widths.

Furthermore, by employing the UT sutra, there is no need to wait for all PP generations to mature before obtaining the final output. Among the 16 sutras, the UT sutra was chosen specifically because it is suitable for both decimal and binary multiplication. It has a basic construction since it just uses AND gates, half adders, and full adders. Following the multiplication through the AND gate, each PP element is received in parallel, and the final result is achieved.

Figure 7 deliberates about the bit-width of $4 \times 4$ UT sutra, the multiplication operation is accomplished as follows: calculation of the operand was done using a vertical and cross-wise manner with the completion of 6 steps. Similarly, for a bit-width of $8 \times 8$, the same method is followed by conducting 14 steps, and is shown in Fig. 8. Due to the larger size, of the $16 \times 16$ multiplier, the criss-cross method was not specified in the paper, but the procedure is the same as the previous method.

After performing the multiplication using UT sutra, the PP rows are generated according to the bit-width of varying operand sizes. By completing the final addition result, it is eventually sent on to the encoder, where the final addition is performed to achieve the 2 N -bit product result.

Table 5 shows the encoding rule to be followed after the first and second stages of PPG and PPR are over. These values are to be referred to with the above encoding table after the application of both the algorithms of the Booth and Vedic sutras, and these values are finally fed to the adder to perform the final PPA result.

## Stage-III-PPA-addition

## BVR-4-PPA

As the multiplier bits are sent to the Booth encoding, which executes the Radix-4 encoding procedure in Fig. 9, the PP rows are cut in half when compared to the usual technique. Following the Radix-4 Booth encoding process, the multiplicand bits conduct Vedic multiplication of UT (criss-cross multiplication) with the new encoded groups and then passed onto the encoder to obtain the final 2 N -bit-width result which is achieved by the parallel adder.

One of the examples of the BVR-4 algorithm is mentioned below. The example shown in Fig. 10 is for operand size $4 \times 4$. The multiplicand values are assigned as $\mathrm{X} 0, \mathrm{X} 1, \mathrm{X} 2, \mathrm{X} 3$, and the multiplier values are assigned as $\mathrm{Y}-1$, Y0, Y1, Y2, Y3. After assigning the values for both the multiplicand and the multiplier, a " 0 " is added at the LSB of the multiplier bits, then the multiplier bits are grouped into trits and the process is followed for contiguous trits of successive bits. The newly encoded groups are formed as Yn0, and Yn1, and then, by following the values in Table 3, the multiplication operation is carried out to form the PP rows of 1 and 2. After the generation of the first PP row, the successive row is shifted by 2 -bit values. Those rows are added and form an intermediate result as P0, P1, P2, P3, P4, P5. The relevant encoded values for the obtained partial values in Fig. 10 are to be referred to in Table 5. The final product is obtained using a sign-magnitude representation of encoded values. The following procedure is carried out for varying operand sizes of 8, 16, etc., and shown in Fig. 11.

By the completion of both the stages of PPG and PPR, the encoded bits obtained in the PPR stage are fed to the encoder and each intermediate resultant is sign extended up to 8 bits and added to acquire the final product shown in Table 6.


Figure 7. Vedic multiplication of 4-bit-width using criss-cross sutra.


Figure 8. Vedic multiplication of 8-bit-width using criss-cross sutra.

By the completion of both the stages of PPG and PPR, the encoded bits obtained in the PPR stage are fed to the encoder and each intermediate resultant is sign extended up to 16 bits and added to acquire the final product shown in Table 7.

BVR-8-PPA
When the multiplier bits are assigned to the booth encoding, which conducts the Radix-8 encoding process, the PP rows are reduced from $N$ to ( $\mathrm{N} / 3$ ) +1 when compared to the usual technique. When compared to the Radix- 4

| S.no. | PPs | Encoded values |
| :--- | :---: | :--- |
| 1. | 0 | 0000 |
| 2. | 1 | 0001 |
| 3. | 2 | 0010 |
| 4. | 3 | 0011 |
| 5. | 4 | 0100 |
| 6. | -4 | 1100 |
| 7. | -3 | 1101 |
| 8. | -2 | 1110 |
| 9. | -1 | 1111 |

Table 5. Encoded values.


Figure 9. Proposed architecture for BVR-4.

Booth approach, the PP rows are reduced even further in this encoding process. After completing the Radix-8 Booth encoding procedure, the multiplicand bits conduct Vedic multiplication of UT (criss-cross multiplication) with the newly encoded groups and then passed onto the encoder to obtain the final 2 N -bit-width result, which is achieved by the parallel adder and it is shown in Fig. 12.

One of the examples of the BVR-8 algorithm is mentioned below. The example shown in Fig. 13 is for operand size $4 \times 4$. The multiplicand values are assigned as $\mathrm{X} 0, \mathrm{X} 1, \mathrm{X} 2, \mathrm{X} 3$, and the multiplier values are assigned as Y-1, Y0, Y1, Y2, Y3, Y4 and Y5. After assigning the values for both the multiplicand and the multiplier, a " 0 " is added at the LSB of the multiplier bits, then the multiplier bits are grouped into quads and the process is followed for contiguous quads of successive bits. The newly encoded groups are formed as Yn0, and Yn1, and then, by following the values in Table 4, the multiplication operation is carried out to form the PP rows of 1 and 2. After the generation of the first PP row, the successive row is shifted by 3-bit values. Those rows are added and form an intermediate result as P0, P1, P2, P3, P4, P5 and P6. The relevant encoded values for the obtained partial values in Fig. 13 are to be referred to in Table 5. The final product is obtained employing a sign-magnitude representation of encoded values. The following procedure is carried out for varying operand sizes of 8,16 , etc., and shown in Fig. 14.

By the completion of both the stages of PPG and PPR, the encoded bits obtained in the PPR stage are fed to the encoder and each intermediate resultant is sign extended up to 8 bits and added to acquire the final product shown in Table 8.

By the completion of both the stages of PPG and PPR, the encoded bits obtained in the PPR stage are fed to the encoder and each intermediate resultant is sign extended up to 16 bits and added to acquire the final product shown in Table 9.


Figure 10. Worked out an example for $\mathrm{BVR}-4$ of bit-width $4 . \mathrm{P} 0=\mathrm{X} 0 \mathrm{Yn} 0, \mathrm{P} 1=\mathrm{X} 1 \mathrm{Yn} 0, \mathrm{P} 2=\mathrm{X} 2 \mathrm{Yn} 0+\mathrm{X} 0 \mathrm{Yn} 1$, $\mathrm{P} 3=\mathrm{X} 3 \mathrm{Yn} 0+\mathrm{X} 1 \mathrm{Yn} 1, \mathrm{P} 4=\mathrm{X} 2 \mathrm{Yn} 1, \mathrm{P} 5=\mathrm{X} 3 \mathrm{Yn} 1$, Final Product $=\mathrm{P} 0+\mathrm{P} 1+\mathrm{P} 2+\mathrm{P} 3+\mathrm{P} 4+\mathrm{P} 5$.

## Results and discussion

The design of the proposed BVR-4 and BVR-8 methods consists of design entry, synthesis, simulation, and implementation in various FPGA devices and ASIC tools. The proposed architecture has been coded in Verilog language. When there is no error, then the code is synthesized using the Xilinx tool. The suggested methods mathematical model and algorithm are run and verified using the Xilinx Vivado tool. The simulation results demonstrate that the mathematical model can multiply two signed integers. The suggested architectures of Proposed BVR-4 and BVR-8 functional verification are carried out by creating the architecture in Verilog HDL and simulating it in ISIM RTL Simulator. The HDL code is generated in two platforms, Vivado 2019.1 Xilinx Synthesis Technology of FPGA platform and ASIC TSMC 45 nm standard cell typical libraries.

## FPGA implementation

In FPGAs, a look-up-table (LUT) is a small asynchronous SRAMs that is used to implement combinational logic circuits, while flip-flops are single-bit memory cells that are used to hold state. Table 10 shows the comparison of Floating Point, Booth, and Vedic multiplier with the proposed methods, and it is implemented with the Xilinx Vivado Artix-7 XC7A100T-CSG324 device specification. The proposed architecture of BVR-4 is compared with the various multiplier techniques and shows a LUT (Look-up-table) and ADP improvement of $42 \%, 20 \%$ for a bit-width of 4 , for a bit-width of 8 it is $94 \%$ and $84 \%$, and for 16 -bit width range it is $96 \%$ and $90 \%$. The proposed architecture of BVR-8 is compared with the various multiplier techniques and shows a LUT (Look-up-table) and ADP improvement of $89 \%, 83 \%$ for a bit-width of 4 , for a bit-width of 8 it is $94 \%$ and $90 \%$, and for 16 -bit width range it is $89 \%$ and $72 \%$ respectively. The area is calculated in terms of LUTs, Flip-flops, and configurable logic blocks. This table shows a clear view that the proposed method of BVR-4 and BVR-8 is very efficient when we combine the techniques of both Booth and Vedic multiplier concepts.

Figure 15 shows the graphical representation of the performance ratings of the LUTs with the existing multiplier. However, when all the parameters are considered together, it is evident from the graph that proposed BVR-4 improves for higher bit-widths and BVR-8 shows a better improvement for smaller bit-widths. It has a significant reduction in LUTs compared to existing multiplier architecture.

Figure 16 shows that the delay was decreased when compared with the prior state-of-the-art multipliers. It shows the comparison of the delay for the proposed BVR-4 and BVR-8 with the existing multipliers.

All the architectures, exploiting the different number of bits for the operands and three different architectures, are compared with the proposed method of BVR-4 and BVR-8 described for the techniques used and analyzed the Area-Delay product it is shown in Fig. 17.
$127 \mathrm{X}-1=127$


Figure 11. Worked out an example for BVR-4 of bit-width $8 . \mathrm{P} 0=\mathrm{x} 0 \mathrm{yn} 0, \mathrm{P} 1=\mathrm{xlyn} 0$,
$\mathrm{P} 2=\mathrm{x} 2 \mathrm{yn} 0+\mathrm{x} 0 \mathrm{yn} 1, \mathrm{P} 3=\mathrm{x} 3 \mathrm{yn} 0+\mathrm{x} 1 \mathrm{yn} 1, \mathrm{P} 4=\mathrm{x} 4 \mathrm{yn} 0+\mathrm{x} 2 \mathrm{yn} 1+\mathrm{x} 0 \mathrm{yn} 2, \mathrm{P} 5=\mathrm{x} 5 \mathrm{yn} 0+\mathrm{x} 3 \mathrm{yn} 1+\mathrm{x} 1 \mathrm{yn} 2$, $\mathrm{P} 6=\mathrm{x} 6 \mathrm{yn} 0+\mathrm{x} 4 \mathrm{yn} 1+\mathrm{x} 2 \mathrm{yn} 2+\mathrm{x} 0 \mathrm{yn} 3, \mathrm{P} 7=\mathrm{x} 7 \mathrm{yn} 0+\mathrm{x} 5 \mathrm{yn} 1+\mathrm{x} 3 \mathrm{yn} 2+\mathrm{x} 1 \mathrm{yn} 3, \mathrm{P} 8=\mathrm{x} 6 \mathrm{yn} 1+\mathrm{x} 4 \mathrm{yn} 2+\mathrm{x} 2 \mathrm{yn} 3$, $P 9=x 7 y n 1+x 5 y n 2+x 3 y n 3, P 10=x 6 y n 2+x 4 y n 3, P 11=x 7 y n 2+x 5 y n 3, P 12=x 6 y n 3, P 13=x 7 y n 3$.

| $\mathbf{8}$ | $\mathbf{7}$ | $\mathbf{6}$ | $\mathbf{5}$ | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{P P}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | P0 |
| 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | P1 |
| 0 | 0 | 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | - | - | P2 |
| 0 | 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | - | - | - | P3 |
| 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | - | - | - | - | P4 |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | - | - | - | - | - | P5 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | Final product |

Table 6. Sign extension of 8-bits of Radix-4. Significant values are in bold.

| $\mathbf{1 5}$ | $\mathbf{1 4}$ | $\mathbf{1 3}$ | $\mathbf{1 2}$ | $\mathbf{1 1}$ | $\mathbf{1 0}$ | $\mathbf{9}$ | $\mathbf{8}$ | $\mathbf{7}$ | $\mathbf{6}$ | $\mathbf{5}$ | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{P P}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{P 0}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{-}$ | $\mathbf{P} 1$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | $\mathbf{P 2}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | - | $\mathbf{P 3}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | - | - | $\mathbf{P 4}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | - | - | - | $\mathbf{P 5}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | - | - | - | - | - | - | $\mathbf{P 6}$ |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | - | - | - | - | - | - | - | $\mathbf{P} 7$ |
| 0 | 0 | 0 | 0 | 0 | $\mathbf{0}$ | 0 | $\mathbf{0}$ | - | - | - | - | - | - | - | - | $\mathbf{P 8}$ |
| 0 | 0 | 0 | 0 | $\mathbf{0}$ | 0 | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | $\mathbf{P 9}$ |
| 0 | 0 | 0 | $\mathbf{0}$ | 0 | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | $\mathbf{P 1 0}$ |
| 0 | 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | - | $\mathbf{P} 11$ |
| 0 | $\mathbf{0}$ | 0 | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | - | - | $\mathbf{P 1 2}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | - | - | - | $\mathbf{P 1 3}$ |
| $\mathbf{1}$ | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | 1 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{F i n a l}$ product |

Table 7. Sign extension of 16 -bits of Radix-4. Significant values are in bold. The colored (highlighted) digits represent the encoded value according to the Radix- 4 and Radix- 8 rules.


Figure 12. Proposed architecture for BVR-8.

## ASIC implementation

The proposed architectures are realized in the ASIC environment to evaluate the efficiency of the design in terms of the VLSI parameters like area, power, delay, Area Delay Product (ADP), and power delay-product (PDP). A tool Command Language (TCL) script is written to automate the synthesis process of the Verilog HDL code in Mentor Graphics. The design is synthesized for different operand sizes 4,8 , and 16 with TSMC 45 nm standard cell typical libraries. The same process is repeated for the state-of-the-art multipliers considered for the comparison, and the results are given in Table 11.

Table 11 shows that the Proposed BVR-4 and BVR- 8 multiplier architecture outperforms in all three aspects followed by traditionally signed CSA and parallel prefix architecture because of less area, increased speed with reduced power. If the number of transistors is optimized, it offers a better output of the proposed methods of BVR-4 and BVR-8. So, 45 nm technology is significantly preferable to reduce area, power, and delay. In 45 nm BVR-4 architecture contains area improvement of $22 \%$, power improvement of $7 \%$, and speed improvement of $50 \%$ for the bit-width of 4 . While for the bit-width of 8 , it shows an area improvement of $28 \%$, power


Figure 13. Worked out an example for BVR-8 of bit-width 4. $\mathrm{P} 0=\mathrm{X} 0 \mathrm{Yn} 0, \mathrm{P} 1=\mathrm{X} 1 \mathrm{Yn} 0, \mathrm{P} 2=\mathrm{X} 2 \mathrm{Yn} 0$, $\mathrm{P} 3=\mathrm{X} 3 \mathrm{Yn} 0+\mathrm{X} 0 \mathrm{Yn} 1, \mathrm{P} 4=\mathrm{X} 1 \mathrm{Yn} 1, \mathrm{P} 5=\mathrm{X} 2 \mathrm{Yn} 1, \mathrm{P} 6=\mathrm{X} 3 \mathrm{Yn} 1$, Final Product $=\mathrm{P} 0+\mathrm{P} 1+\mathrm{P} 2+\mathrm{P} 3+\mathrm{P} 4+\mathrm{P} 5+\mathrm{P} 6$.
improvement of $8 \%$, and speed improvement of $61 \%$ and for the operand size of 16 it shows an area improvement of $42 \%$, power improvement of $1 \%$ and speed improvement of $84 \%$ when compared with the CSA architecture. The proposed BVR-8 architecture contains an area improvement of $49 \%$, power improvement of $13 \%$, and speed improvement of $62 \%$ for the bit-width of 4 , while for the bit-width of 8 , it shows an area improvement of $35 \%$, power improvement of $13 \%$ and speed improvement of $64 \%$, for the operand size of 16 it shows an area improvement of $44 \%$, power improvement of $3 \%$ and speed improvement of $85 \%$.

Figure 18 shows the BVR-4 architecture contains $0.035,0.25$ and 1.76 of Area-Delay Product for the Bit-width range of 4,8 and 16 when compared with the previous CSA and parallel prefix architecture in 45 nm ASIC standard cell libraries. For BVR-8 architecture it contains $0.001,0.21$, and 1.577 for the operand size of 4,8 and 16 .

Figure 19 shows the power-delay product comparison of BVR- 4 and BVR- 8 with the existing CSA and parallel prefix architecture. It shows a PDP of $0.04,0.02$, and 0.03 for the BVR- 4 method, and for BVR-8 it shows 0.002 , 0.026 , and 0.02 respectively.

## Conclusion

In this paper, a new method of signed digit multiplication is presented. The proposed design is based on both the techniques of Booth and the Vedic multiplier concept using the sutra of Urdhva-tiryakbhyam (criss-cross) multiplication technique. First, the scope of the booth multiplier is extended to the Vedic multiplication to perform parallel processing at the stage of partial product reduction stage, which leads to a decreased propagation delay. The propagation delay issue is resolved using an adder and in sign-magnitude representation. The proposed design is found to have a high speed with minimal area consumption with various state-of-the-art architectures. For Booth-Vedic-Radix-4 encoding (BVR-4) decreases area by $89 \%$ and improves area-delay product (ADP) by $72 \%$ for a 16 -bit multiplier when subjected to the Conventional Radix-4 booth multiplier of different operand sizes. The Booth-Vedic-Radix-8 (BVR-8) method shows that there will be an $89 \%$ reduction in area and improves
 Figure 14. Worked out an example for BVR-8 of bit-width $8 . P 0=x 0 y n 0, P 1=x 1 y n 0, P 2=x 2 y n 0, P 3=x 3 y n 0+x 0 y n 1, P 4=x 4 y n 0+x 1 y n 1, P 5=x 5 y n 0+x 2 y n 1, P 6=x 6 y n 0+x 3 y n 1+x 0 y n 2$, $\mathrm{P} 7=\mathrm{x} 7 \mathrm{yn} 0+\mathrm{x} 4 \mathrm{yn} 1+\mathrm{x} 1 \mathrm{yn} 2, \mathrm{P} 8=\mathrm{x} 5 \mathrm{yn} 1+\mathrm{x} 2 \mathrm{yn} 2, \mathrm{P} 9=\mathrm{x} 6 \mathrm{yn} 1+\mathrm{x} 3 \mathrm{yn} 2, \mathrm{P} 10=\mathrm{x} 7 \mathrm{yn} 1+\mathrm{x} 4 \mathrm{yn} 2, \mathrm{P} 11=\mathrm{x} 5 \mathrm{yn} 2, \mathrm{P} 12=\mathrm{x} 6 \mathrm{yn} 2, \mathrm{P} 13=\mathrm{x} 7 \mathrm{yn} 2$.

| $\mathbf{8}$ | $\mathbf{7}$ | $\mathbf{6}$ | $\mathbf{5}$ | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{P P}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | P0 |
| 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ |  | P1 |
| 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ |  |  | P2 |
| 0 | 0 | 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |  |  |  | P3 |
| 0 | 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |  |  |  |  | P4 |
| 0 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ |  |  |  |  |  | P5 |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ |  |  |  |  |  |  | P6 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | Final product |

Table 8. Sign extension of 8-bits of Radix-8. Significant values are in bold.

| $\mathbf{1 5}$ | $\mathbf{1 4}$ | $\mathbf{1 3}$ | $\mathbf{1 2}$ | $\mathbf{1 1}$ | $\mathbf{1 0}$ | $\mathbf{9}$ | $\mathbf{8}$ | $\mathbf{7}$ | $\mathbf{6}$ | $\mathbf{5}$ | $\mathbf{4}$ | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{P P}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{P 0}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | $\mathbf{P 1}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | $\mathbf{P 2}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | - | $\mathbf{P 3}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | - | - | $\mathbf{P 4}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | - | - | - | - | - | $\mathbf{P 5}$ |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | - | - | - | - | - | - | $\mathbf{P 6}$ |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | - | - | - | - | - | - | - | $\mathbf{P 7}$ |
| 0 | 0 | 0 | 0 | 0 | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | $\mathbf{P 8}$ |
| 0 | 0 | 0 | 0 | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | $\mathbf{P 9}$ |
| 0 | 0 | 0 | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | $\mathbf{P 1 0}$ |
| 0 | 0 | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | - | $\mathbf{P 1 1}$ |
| 0 | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | - | - | $\mathbf{P 1 2}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | - | - | - | - | - | - | - | - | - | - | - | - | - | $\mathbf{P 1 3}$ |
| $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{1}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{F i n a l}$ product |

Table 9. Sign extension of 16 -bits. Significant values are in bold. The colored (highlighted) digits represent the encoded value according to the Radix-4 and Radix-8 rules.

| Number of bit-width | Multipliers | LUTs | Delay | ADP |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Floating point multiplier ${ }^{45}$ | 19 | 4.1 | 77.9 |
|  | Booth multiplier ${ }^{46}$ | 16 | 4.1 | 65.6 |
|  | Vedic multiplier ${ }^{47}$ | 16 | 4.6 | 73.6 |
|  | Proposed method (Booth Vedic Radix-4) | 11 | 5.363 | 61.996 |
|  | Proposed method (Booth Vedic Radix-8) | 2 | 6.461 | 12.922 |
| 8 | Floating point multiplier ${ }^{45}$ | 118 | 4.7 | 554.6 |
|  | Booth multiplier ${ }^{46}$ | 101 | 4.7 | 474.4 |
|  | Vedic multiplier ${ }^{47}$ | 71 | 4.7 | 333.7 |
|  | Proposed method (Booth Vedic Radix-4) | 7 | 12.59 | 88.172 |
|  | Proposed method (Booth Vedic Radix-8) | 5 | 10.554 | 52.77 |
| 16 | Floating point multiplier ${ }^{45}$ | 548 | 6.3 | 3452.4 |
|  | Booth multiplier ${ }^{46}$ | 455 | 6.3 | 2866.5 |
|  | Vedic multiplier ${ }^{47}$ | 294 | 7.6 | 2234.4 |
|  | Proposed method (Booth Vedic Radix-4) | 18 | 18.57 | 334.314 |
|  | Proposed method (Booth Vedic Radix-8) | 59 | 15.83 | 934.383 |

Table 10. FPGA synthesis results. Significant values are in bold.

ADP by $72 \%$ for the 16 -bit multiplier. This work can be further incorporated into the image compression technique to achieve the rapid result.

## Comparison of LUTs



Figure 15. Performance of LUTs for BVR-4 and BVR-8.


Figure 16. Analysis of delay for BVR-4 and BVR-8.

Comparison of Area-Delay product


Figure 17. Comparison of Area-Delay Product for the proposed method of BVR-4 and BVR-8.

| N | Multipliers | Area ( $\mu \mathrm{m}^{2}$ ) | Power ( $\mu \mathrm{W}$ ) | Delay (ns) | Area-delay product (ADP)- $\mathbf{p m}^{2 *}{ }^{\text {s }}$ | Power-delay product (PDP)-pJ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | CSA architecture ${ }^{48}$ | 114 | 11 | 0.8 | 0.09 | 0.008 |
|  | Parallel-prefix architecture ${ }^{48}$ | 140 | 12 | 0.8 | 0.1 | 0.009 |
|  | Proposed BVR-4 | 88 | 10.2 | 0.4 | 0.035 | 0.004 |
|  | Proposed BVR-8 | 58 | 9.5 | 0.3 | 0.001 | 0.002 |
| 8 | CSA architecture ${ }^{48}$ | 452 | 35 | 2.1 | 0.97 | 0.07 |
|  | Parallel-prefix architecture ${ }^{48}$ | 587 | 40 | 0.8 | 0.46 | 0.03 |
|  | Proposed BVR-4 | 322 | 32 | 0.8 | 0.25 | 0.02 |
|  | Proposed BVR-8 | 291 | 30.23 | 0.75 | 0.21 | 0.026 |
| 16 | CSA architecture ${ }^{48}$ | 2030 | 208 | 9.5 | 19.18 | 1.976 |
|  | Parallel-prefix architecture ${ }^{48}$ | 2679 | 260 | 6.0 | 16.07 | 1.56 |
|  | Proposed BVR-4 | 1176 | 205 | 1.5 | 1.76 | 0.03 |
|  | Proposed BVR-8 | 1123 | 200 | 1.4 | 1.577 | 0.02 |

Table 11. Performance comparison of BVR-4 and BVR-8.

Comparison of Area-Delay product


Figure 18. Comparison of Area-Delay Product with existing multipliers.

Comparison of Power-Delay Product


Figure 19. Comparison of power-delay product of proposed BVR-4 and BVR-8.

## Data availability

The data analyzed during the current study available from the corresponding author on reasonable request.
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## Author contributions

C.M.K.: Data curation, Conceptualization, Methodology, Writing—original draft. R.S.S.: Supervision, Writ-ing-review \& editing.

## Competing interests

The authors declare no competing interests.

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