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Phase separation in mullite-composition glass

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Aluminosilicates (AS) are ubiquitous in ceramics, geology, and planetary science, and their glassy forms underpin vital technologies used in displays, waveguides, and lasers. In spite of this, the nonequilibrium behavior of the prototypical AS compound, mullite (40SiO₂-60Al₂O₃, or AS60), is not well understood. By deeply supercooling mullite-composition liquid via aerodynamic levitation, we observe metastable liquid-liquid unmixing that yields a transparent two-phase glass, comprising a nanoscale mixture of AS7 and AS62. Extrapolations from X-ray scattering measurements show the AS7 phase is similar to vitreous SiO₂ with a few Al species substituted for Si. The AS62 phase is built from a highly polymerized network of 4-, 5-, and 6-coordinated AlO_x polyhedra. Polymerization of the AS62 network and the composite morphology provide essential mechanisms for toughening the glass.

Mullite is an eminent material throughout the field of ceramics, from pottery and porcelains to refractories and thermal barrier coatings¹. As a phase in the CaO-MgO-Al₂O₃-SiO₂ (CMAS) system, which is present throughout the Universe, it also represents an important geological material, formed at the Earth's surface when basaltic magmas contact clay minerals². In the aluminosilicate (AS) binary, the mullite composition (40SiO₂-60Al₂O₃, or AS60) is effectively an endmember of AS-based glasses. These constitute a large fraction of functional glasses due to their hardness and toughness³. A key to obtaining these glasses' desirable properties is navigating around the system's metastable liquid-liquid immiscibility during processing, which can lead to phase-separated glasses in the SiO₂-rich region of the phase diagram upon melt quenching⁴. Avoiding or manipulating this immiscibility provides the means to control properties of the resulting glasses.

The known AS miscibility gap ranges qualitatively from near SiO₂ and ends prior to the mullite composition, approximately AS7-AS56. Yet, substantial disagreement persists regarding the compositional and temperature limits of immiscibility (Fig. 1). Many experimental studies have located the mullite composition outside the miscibility gap⁴⁻⁶, while different thermodynamic models have predicted it within^{7,8} or outside⁹⁻¹¹ the gap (see Fig. 1). In this regard, though mullite is ubiquitous in ceramics, its structural role in AS phase separation remains an unsolved mystery. This mainly arises because of the high temperatures involved and the metastable nature of the liquid-liquid phase separation dome, which exists hundreds of degrees below the equilibrium melting point ($T_m \sim 1890$ °C for mullite¹¹). Rosales-Sosa et al.¹² recently reported a mullite-composition glass with exceptional hardness (8.07 GPa) and crack resistance (55.4 N), which sparks renewed curiosity about the structure of mullite-composition glass and an explanation for these desirable properties. (Hereafter, mullite-composition glass is referred to as "mullite glass," defined as the glassy form obtained by melt quenching of the AS60 liquid.) Here, we find that mullite glass is in fact two-phase, with nanometer domains of SiO₂-rich glass embedded in a glassy, polymerized Al₂O₃-rich network. Glass structure and electron microscopy measurements provide unambiguous evidence of liquid-liquid phase separation in mullite and provide an experimentally-based estimate for the high-Al₂O₃ limit of AS immiscibility. Atomic structure modeling of this Al-rich endmember illuminates the structural underpinnings of mullite glass's excellent crack resistance.

Results and discussion

Because of its reticence to vitrify, mullite-composition glasses are often partially crystalline^{13,14}, and fully glassy materials are typically limited to particle sizes of 10s or 100s of microns, prepared via roller quenching or other techniques that achieve extremely fast cooling ($\sim 10^6$ °C s⁻¹)¹. Here, fully glassy beads, approximately 2 mm in diameter, were prepared using aerodynamic levitation and laser beam heating¹⁵, which avoids heterogeneous nucleation while maintaining moderate cooling rates ($\leq 10^3$ °C s⁻¹). This is crucial because the fast rates associated with roller quenching have previously obfuscated the full extent of AS phase separation^{16,17}. Phase separation in the glass is evident from ultra-small and small-angle X-ray scattering (Fig. 2A), which exhibits a peak near Q

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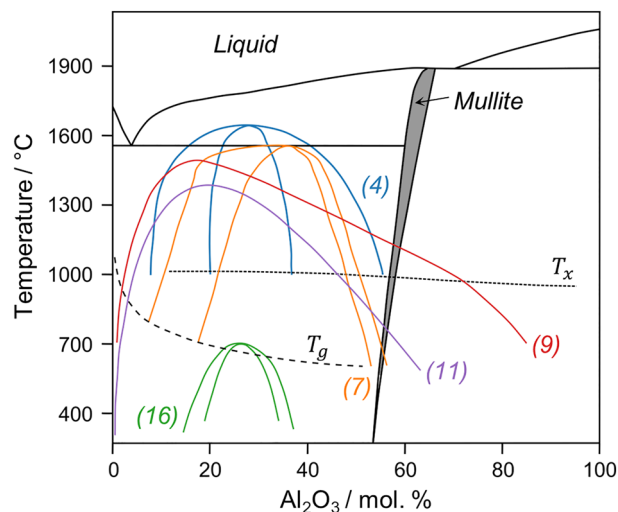


Figure 1. Metastable liquid–liquid immiscibility in $\text{SiO}_2\text{-Al}_2\text{O}_3$. Numerous locations for the miscibility gap have been proposed based on experimental observations of quenched glasses and thermodynamic calculations (colored curves with Ref. numbers given in figure). The compositional and temperature limits of immiscibility vary substantially between studies, with the Al_2O_3 -rich endmember intersecting T_g anywhere from 56 to >85 mol. %. Equilibrium phase diagram adapted from Mao et al.¹¹. Glass transition is T_g ⁷, and crystallization of glasses upon heating is T_x ⁴¹.

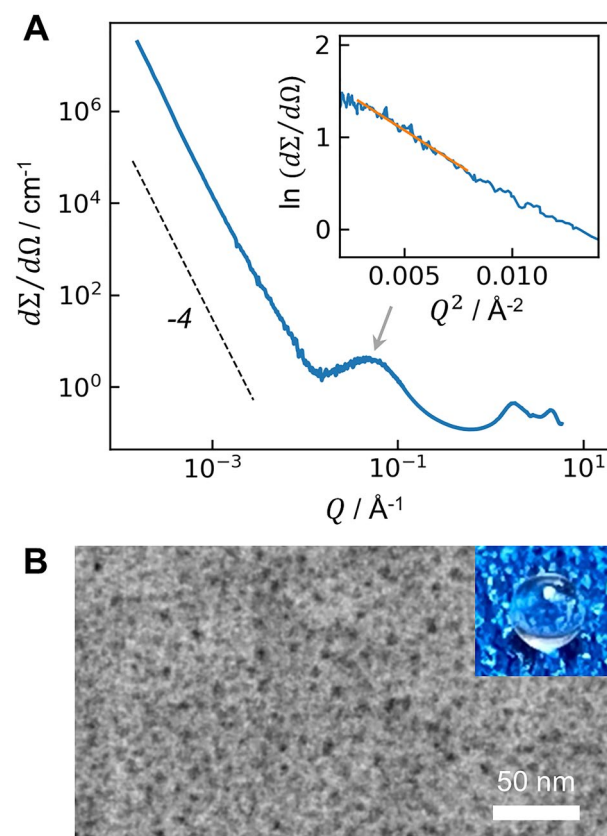


Figure 2. Phase separation in mullite-composition glass. **(A)** X-ray scattering differential cross section exhibits a Porod slope to the right of a small-angle peak near 0.05 \AA^{-1} (gray arrow), indicative of phase-separated domains. Inset: Guinier analysis predicts an average domain size of 5.5 nm. **(B)** High-angle annular dark field STEM image of a 40–100 nm thick mullite-composition glass specimen, revealing contrast between the 4–6 nm Si-rich domains (black) and surrounding Al-rich matrix. Inset: transparent glass bead, 1.3 mm in diameter.

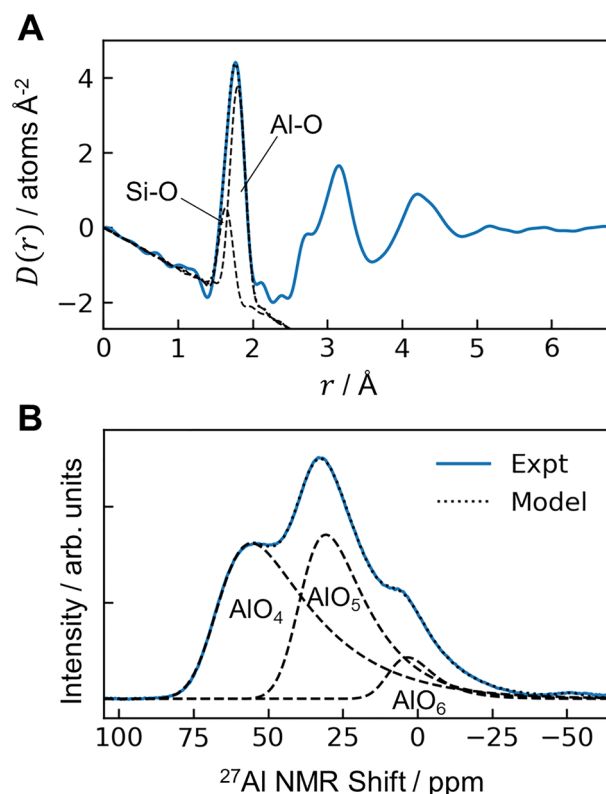


Figure 3. Average local atomic structure in mullite-composition glass. **(A)** Differential PDF from high-energy X-ray diffraction. The slope for $r < 1 \text{ \AA}$ is $-4\pi\rho$, with $\rho = 2.912 \text{ g cm}^{-3}$, or $0.08640 \text{ atoms \AA}^{-3}$. Gaussian functions were fit for the weighted Si-O and Al-O partial pair correlations. **(B)** The ^{27}Al MAS NMR spectrum exhibits three peaks corresponding to different Al speciation.

$= 0.05 \text{ \AA}^{-1}$, where Q is the momentum transfer given by $Q = 4\pi \sin(\theta)/\lambda$ and 2θ is the scattering angle. Using Guinier analysis (Fig. 2A inset) and assuming a spherical scatterer, this peak corresponds to domains with a diameter of 5.5 nm. High-angle annular dark field scanning transmission electron microscopy (STEM, Fig. 2B) reveals separated Si-rich domains within an Al-rich matrix, with a domain size of 4–6 nm consistent with the Guinier analysis. From the apparent areal fractions in the STEM image and assuming a Si-rich endmember composition of AS7, based on previous studies^{7,18,19}, the Al-rich endmember phase has a composition of 61.9(7) mol% Al_2O_3 (~AS62). This AS62 estimate significantly extends the experimentally-observed immiscibility range beyond the AS56 limit suggested by previous direct observations^{4,5}, and it coincides with the intersection of T_g with the miscibility gap proposed by Mao et al.¹¹ in their thermodynamic reassessment of the SiO_2 - Al_2O_3 system (Fig. 1, purple curve). Despite the phase separation, the mullite glass is optically transparent (Fig. 2B, inset).

According to an exhaustive review of phase separation behavior in binary silicate systems by Hudon and Baker²⁰, liquid-liquid separation in aluminosilicates is driven by coulombic repulsions between poorly screened Al^{3+} cations. In these glasses, Al^{3+} is an amphoteric cation, referring to its ability to adopt different coordination numbers with oxygen: 4, 5, and 6. The partial covalent character of tetrahedral AlO_4 species reduces their electrostatic repulsions with other cations, but the Al^{3+} in octahedral AlO_6 species are poorly screened. To achieve stoichiometric charge balance in the AS binary system, both AlO_4 and AlO_6 coexist, thus leading to phase separation.

The local atomic structure in mullite glass was probed with high-energy X-ray diffraction and ^{27}Al magic angle spinning nuclear magnetic resonance (MAS NMR) spectroscopy. For X-ray diffraction, the total structure factor, $S(Q)$, is Fourier transformed to obtain the real-space differential pair distribution function (PDF), $D(r)$, shown in Fig. 3A (see Supplementary Information S1 (SI) for PDF definitions). The first PDF peak near 1.77 Å comprises overlapping contributions from the Si-O and Al-O atomic partial pair correlations. Fitting Gaussian functions to these peaks and integrating the Al-O peak yields the mean atomic coordination, $n_{\text{AlO}} = 4.38(7)$. The glass lacks significant local order beyond the second (Si/Al)-O coordination shell, i.e., above 5 Å. The ^{27}Al MAS NMR spectrum (Fig. 3B) contains three overlapping peaks at 67.9, 40.4, and 9.9 ppm, corresponding to AlO_4 , AlO_5 , and AlO_6 species, respectively¹⁴. Using peak shapes guided by separate ^{27}Al triple-quantum MAS (3QMAS) NMR measurements on the same glass (SI, Fig. S1), integration of these peaks yields relative population fractions of 0.498(42), 0.430(41), and 0.072(10), respectively, and a mean coordination of $n_{\text{AlO}} = 4.57(27)$ consistent with the X-ray analysis. The presence of AlO_5 and AlO_6 species is also consistent with reports of Raman spectroscopy for Al_2O_3 -rich silicate glasses^{13,21}. The substantial AlO_5 fraction, absent in crystalline mullite²², is a structural motif shared in common with the liquid²³ that is quenched into the glass structure⁶.

To gain further structural insights, experimentally-constrained models for the phase-separated endmembers are sought. X-ray diffraction interference functions, $Q(S(Q) - 1)$, were measured for compositions AS12-AS61 (Fig. 4A), spanning the immiscibility range. These glasses are each phase-separated into the same endmembers, whose relative fractions vary linearly with glass composition. The interference functions were therefore extrapolated²⁴ to predict the interference functions for the AS7 and AS62 endmembers (Fig. 4B), for which atomistic models were obtained by Empirical Potential Structure Refinement (EPSR)²⁵.

The structure of AS7 (Fig. 4C) is similar to that of SiO₂ glass: O atoms are 93% bridging (i.e., connecting two (Si/Al)O_x polyhedra), 5% form triclusters²⁶ (Fig. 4D), and the network comprises 99% corner-sharing between polyhedra that form rings with a distribution modal size of 7 cations (Fig. 4E). In contrast, the AS62 structure contains 60% O as triclusters, making it much more topologically rigid²⁷. Oxygen triclusters are a charge balancing mechanism²⁰ and here are associated with Al-rich environments such as O-Al₃ and O-SiAl₂. While substantial, this large tricluster fraction is consistent with molecular dynamics (MD) simulations for mullite glass²⁸ and is reasonable in comparison to MD predictions of 82% triclusters in melt quenched Al₂O₃²⁹. The AS62 network contains a mixture of AlO_x species: 57% 4-, 37% 5-, and 6% 6-coordinate. These polyhedra and the SiO₄ are connected via 86% corner- and 13% edge-sharing, forming more than 3 × the number of rings as compared to AS7. This large number of rings makes AS62 highly polymerized.

Nanoscale phase separation and atomic structure are the keys to understanding AS glasses' trend of increasing hardness—and, anomalously, crack resistance—with Al₂O₃ content¹². For a single phase, hardness is proportional to density¹², so the higher density of AS62 leads to higher hardness compared to AS7. For any glass composition within the miscibility gap, the glass comprises domains of the two endmember phases, AS7 and AS62, with relative volume fractions that are linearly dependent on composition. This linear dependence of the volume fractions explains the linear relationship of hardness with increasing Al₂O₃ content. This trend also matches the linear increase of O triclusters (SI, Fig. S2A), which topologically harden the atomic network. Cracking resistance (CR) in glass is often attributed to the availability of free volume to accommodate plastic deformation, so CR typically decreases with density, yet the opposite is observed for the AS compositional series. Rosales-Sosa et al. hypothesized this is due to rearrangement of the multiple AlO_x environments, enabling shear deformation¹², which is supported by the low energy barrier predicted by MD for AlO₅ configurational transitions in AS glasses³⁰.

The discovery of phase separation in mullite glass and the structure of the Al-rich endmember point to two additional CR mechanisms. First, the highly polymerized network in AS62 makes it more difficult to form cavities that lead to crack formation, according to MD simulations of high- and low-brittleness single-phase AS glasses under mechanical loading³¹. These simulations also showed that cracking is mitigated by the breaking of larger rings (containing ~ 6 cations) into 3- and 4-member rings, so the much larger population of rings in AS62 is supportive of its higher CR compared to AS7. Second, CR has been observed to increase nonlinearly with Al₂O₃ content: from 8 to 20 N for AS30 to AS55, then jumping to 55 N for AS60¹². This jump can be explained by the relative fractions and morphologies of the phase-separated domains. As Al₂O₃ content increases from AS55 to AS60, the more easily-cracked AS7 phase becomes sufficiently disconnected (Fig. 2B) such that cracks can no longer propagate continuously through AS7, so the more crack-resistant AS62 matrix thus suddenly increases CR.

Commercial glasses can be toughened by surface modification (e.g., ion exchange³²) and/or by creating a composite structure that results in crack deflection (e.g., in glass-ceramics³³). This work shows the potential for using phase-separated vitreous materials. The presence of a highly polymerized network and the composite nature of the two-phase glass offer additional design approaches in the toolbox for glass strengthening. Combination of techniques, for example, selective ion exchange of only one phase in a separated glass, may open up new possibilities. Though mullite is a reluctant glass former, its ~ 390 °C difference between T_g and T_x (Fig. 1) suggests it could be formed in thin sheets, where cooling rates are sufficiently high and heterogeneous nucleation can be avoided.

Methods

Full information on the experimental methods is provided in the SI.

Glass beads were prepared from mixtures of SiO₂ and Al₆Si₂O₁₃ powders using aerodynamic levitation and heating with a 10.6 μm CO₂ laser beam¹⁵. Nominal compositions of 10, 20, 30, 35, 40, 50, and 60 mol. % Al₂O₃ (AS10-AS60) were heated to 2000 °C and then cooled at rates < 10³ °C s⁻¹ to obtain colorless, transparent glass beads 1.5–2 mm in diameter. Evaporation of SiO₂ caused 2–10% mass loss during melt processing, resulting in final compositions consistent with energy dispersive spectroscopy on polished cross-sections: AS12, 23, 33, 38, 42, 54, and 61. For the mullite glass (AS61), annular dark field STEM images were collected at 200 keV beam energy. Specimens were prepared by in situ lift-out from a glass cross-section, followed by ion beam thinning at 5 keV. The composition of the Al₂O₃-rich endmember was estimated to be 61.9(7) mol. % Al₂O₃, or ~ AS62, from the areal fractions observed in STEM, assuming a SiO₂-rich endmember composition of AS7^{7,18,19}.

²⁷Al MAS NMR spectroscopy was conducted at an external field strength of 16.4 T, spinning at 22 kHz, and referenced to an external shift standard of aqueous aluminum nitrate at 0.0 ppm. Data were processed with VnmrJ and DMFit softwares, using the Cjzjek function to represent each of the three resonances³⁴. The quadrupolar coupling constant, isotropic chemical shift, and peak areas were extracted from peak fits³⁵. ²⁷Al 3QMAS NMR data were collected using standard two-pulse experiments with a z-filter, and analyses of these data were used to further guide fitting of the ²⁷Al MAS NMR data.

X-ray scattering measurements were collected for the ultra-small and small-angle range with 21 keV X-rays³⁶, as well as the small- and wide-angle range with 60 keV X-rays³⁷. For PDF analysis, dedicated wide-angle scattering (100 keV) data were reduced to obtain the total structure factors and then Fourier transformed to obtain the PDFs³⁸. Mean bond distances and coordinations for Si–O and Al–O were extracted from the PDFs with Gaussian peak fits³⁹. Structure factors for glasses in the AS12-AS42 compositional range were extrapolated to estimate the structure factors for the AS7 and AS62 phase-separated endmembers. Structural models for AS7 and AS62 were

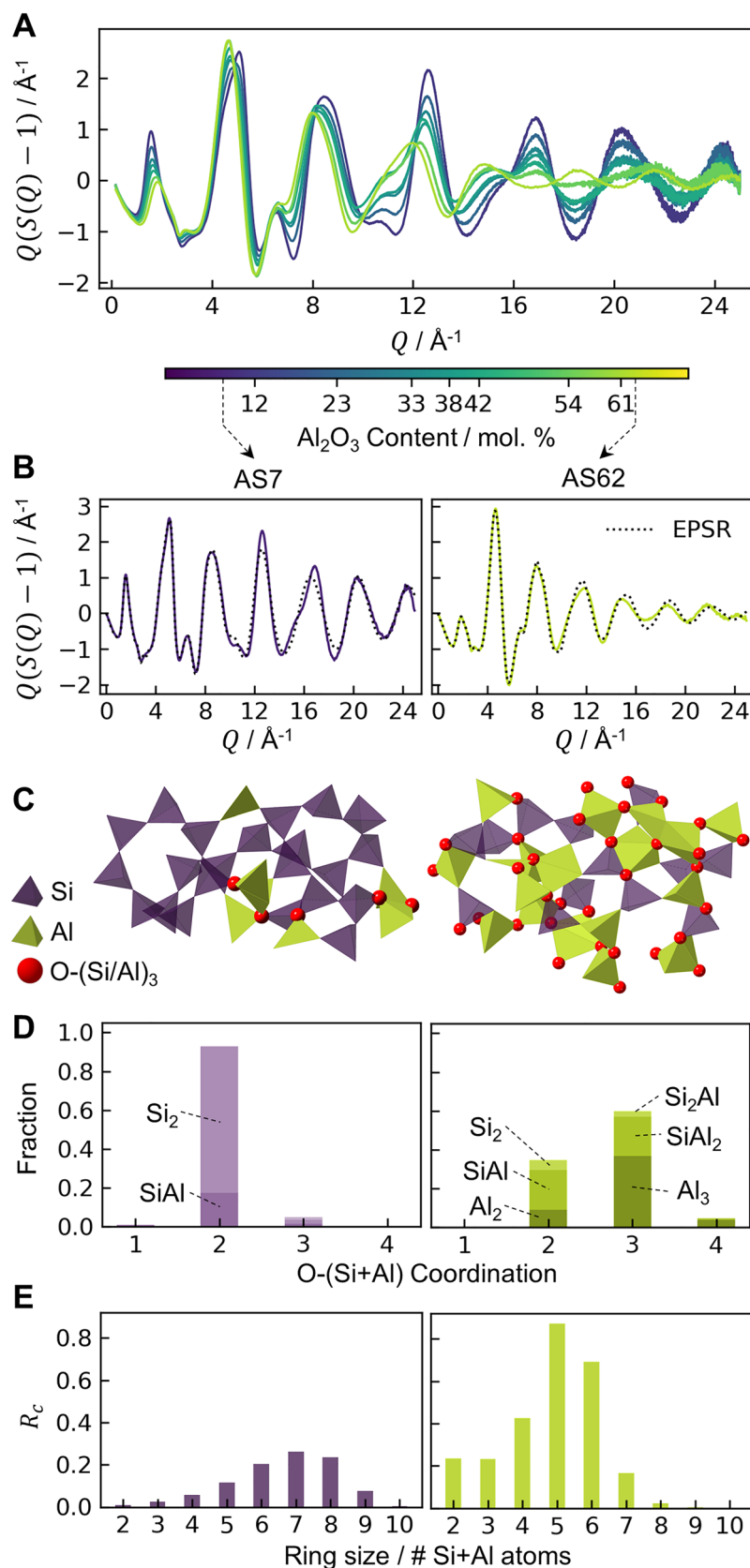


Figure 4. Structure of the endmembers in phase-separated mullite and aluminosilicate glasses. **(A)** X-ray diffraction interference functions of phase-separated glasses, with compositions ranging from AS12–AS61. **(B)** Interference functions for the endmember compositions, AS7 and AS62, linearly extrapolated from the glasses in **(A)**. EPSR provides structural models of the endmembers consistent with the experimental data: **(C)** structure visualizations, **(D)** oxygen coordination environments, and **(E)** ring size distributions of AS7 and AS62 endmembers. R_c is the number of -O-(Si/Al)- rings normalized by the number of atoms in the simulation volume.

created using EPSR²⁵, a Monte Carlo based technique that perturbs a system with known composition, density, and simple interatomic potentials, to optimize agreement between the experimental and simulated scattering. Atomic coordination distributions and ring statistics⁴⁰ were calculated from these models.

Data availability

All data are available upon reasonable request from the corresponding author. Structure factor data are provided in the SI for the X-ray diffraction measurements.

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Competing interests

The authors declare no competing interests.

Additional information

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