SCIENTIFIC REPORTS natureresearch

OPEN

Role of a Concentration Gradient in Malaria Drug Resistance Evolution: A Combined within- and between-Hosts Modelling Approach

Suwat Romphosri¹, Suttikiat Changruenngam¹, Thanat Chookajorn² & Charin Modchang^{1,3,4*}

Resistance to antimalarial drugs is currently a growing public health problem, resulting in more cases with treatment failure. Although previous studies suggested that a concentration gradient facilitates the antibiotic resistance evolution in bacteria, no attempt has been made to investigate the roles of a concentration gradient in malaria drug resistance. Unlike the person-to-person mode of transmission of bacteria, the malaria parasites need to switch back and forth between the human and mosquito hosts to complete the life cycle and to spread the resistant alleles. Here we developed a stochastic combined within- and between-hosts evolutionary dynamics model specific to malaria parasites in order to investigate the influence of an antimalarial concentration gradient on the evolutionary dynamics of malaria drug resistance. Every stage of malaria development in both human and mosquito hosts are individually modelled using the tau-leaping algorithm. We found that the concentration gradient can accelerate antimalarial resistance evolution. The gain in resistance evolution was improved by the increase in the parasite mutation rate and the mosquito biting rate. In addition, even though the rate of resistance evolution is not sensitive to the changes in parasite reduction ratios (PRRs) of antimalarial drugs, the probability of finding the antimalarial drug resistant parasites decreases when the PRR increases.

Malaria is a vector-borne disease caused by the parasitic protozoa in the *Plasmodium* species. There are five species of the *Plasmodium* protozoa, namely, *P. falciparum*, *P. vivax*, *P. ovale*, *P. malariae*, and *P. knowlesi* that can infect humans via the bite of infected *Anopheles* mosquitoes¹. In 2017, the World Health Organisation (WHO) reported 219 million cases with 435,000 deaths worldwide^{2,3}. Malaria is found in many tropical regions, and malaria was considered to be endemic in 91 countries in 2016⁴. Malaria treatment relies only on the administration of antimalarial drug regimens, and the first-line treatment for *P. falciparum* as recommended by WHO is artemisinin combination therapies (ACT), which are to date the most effective antimalarial drugs for uncomplicated *P. falciparum* malaria⁵. ACTs are the combination of artemisinin derivatives and partner drugs. Artemisinin affects the asexual blood stage and the early sexual stage of the parasite⁶, whereas a partner drug clears residual parasites from an artemisinin pulse. ACTs have been used to treat malaria since 1994 and are currently the most widely used malaria treatment regimen.

Nevertheless, resistance to antimalarial drugs is posing a growing public health threat^{7,8}. Antimalarial drug resistance gives the parasite an opportunity to survive under antimalarial pressure. When resistance emerges, it prolongs the illness and delays the clearance time, resulting in treatment failure. This can also increase the mortality, morbidity, and transmissivity rates of the disease. Among the five species of *Plasmodium*, *Plasmodium*, *falciparum* poses the most burden, especially in African countries, and is responsible for most malaria deaths². Resistance to chloroquine, sulfadoxine and pyrimethamine are widespread, while delayed clearance following artemisinin treatment was reported in five countries in the Great Mekong subregion (Cambodia, Laos, Myanmar,

¹Biophysics Group, Department of Physics, Faculty of Science, Mahidol University, Bangkok, 10400, Thailand. ²Genomics and Evolutionary Medicine Unit (GEM), Center of Excellence in Malaria Research, Faculty of Tropical Medicine, Mahidol University, Bangkok, Thailand. ³Centre of Excellence in Mathematics, CHE, Bangkok, 10400, Thailand. ⁴Thailand Center of Excellence in Physics, CHE, 328 Si Ayutthaya Road, Bangkok, 10400, Thailand. *email: charin.mod@mahidol.edu Thailand, and Viet Nam). Moreover, the cases with reduced artemisinin effectiveness were first reported in 2004 near the border between Thailand and Cambodia⁹.

Many factors are likely to accelerate drug resistance evolution in general. One key factor is a drug concentration gradient which is known to promote the evolution of drug resistance in bacteria¹⁰⁻¹³. It has also been shown that antibiotic concentration gradients can arise in both a single-host level (e.g., different organs can absorb different amounts of antibiotics resulting in a concentration gradient between organs within a patient), as well as in a population level (e.g., bacteria can migrate between treated and untreated patients and, therefore, experience different drug concentrations)^{14–16}. Antibiotic resistance, therefore, naturally evolves in environments with antibiotic concentration gradients.

Many experimental studies have investigated the effects of the concentration gradient in the drug resistance evolution of bacteria^{10,11}. For instance, in 2011, the first experimental study of antibiotic resistance evolution in the heterogeneous environment was conducted using a microfluidic device¹⁰. The experiment revealed an important role of a concentration gradient in the resistance evolution of bacteria. Under the drug concentration gradient, the resistance to ciprofloxacin was found within 10 hours, as opposed to 25 hours with no emergence of drug resistance in the homogeneous environment¹⁰. This demonstrated that spatial heterogeneity can accelerate the drug resistance evolution in bacteria. In addition to experimental studies, there are also theoretical works investigating the roles of spatial heterogeneity in antibiotic resistance evolution^{12,13}. For example, in 2012, a group of researchers introduced a staircase model for investigating the role of spatial heterogeneity in the evolution of antibiotic resistance¹³. In this model, a one-dimensional environment was divided into many small isolated compartments in which bacterial migration occurred between these compartments. The drug concentration in each compartment increased from left to right. Bacteria inhabiting each compartment proliferated (grew), migrated, mutated, and died. The results of the study showed that concentration gradients provide a mode of adaptation that is impossible to observe in uniform environments. The analytical and numerical results of this study showed that drug concentration gradients can promote antibiotic resistance.

Similar to bacteria, it has also been suggested that malaria parasites may often experience heterogeneous distribution of antimalarial drugs. This heterogeneity arises due to differences in health infrastructure and drug accessibility among human populations¹⁷. In addition, the circulation of fake and low-quality drugs in some groups of patients may also produce antimalarial concentration gradients among populations^{18,19}. However, although the experimental and the theoretical works suggested that drug concentration gradients facilitate the antibiotic resistance evolution of bacteria^{10–13}, to the best of our knowledge, no attempt has been made to investigate the roles of an antimalarial drug concentration gradient on the resistance evolution of malaria parasites. Unlike the spreading of antibiotic resistance in which the resistant bacteria can transmit directly from one person to another, the transmission of antimalarial drug resistance is much more complicated; the resistant parasites need to migrate back and forth between the human and mosquito hosts. The life cycle of malaria parasites is more complicated, as it requires both human and mosquito hosts to be completed.

In general, mathematical modelling and computer simulation can be used either as predictive tools or as a means of understanding fundamental physical and biological processes. They enable the prediction of outcomes that would not be possible to investigate in the laboratory and in the real world²⁰. Evolutionary dynamics of antimalarial drug resistance also falls into this category. Unlike bacteria, to complete the whole life cycle, malaria parasites need to live in both mosquito and human hosts. This prohibits researchers from conducting experiments on the evolutionary transmission of malaria parasites in the laboratory setting.

In this work, we developed a combined within- and between-host evolutionary dynamics model of malaria parasites to investigate the roles of an antimalarial drug concentration gradient on the evolutionary dynamics of malaria parasites. In our model, all stages of malaria parasites in both human and mosquito hosts are explicitly modelled using a stochastic approach²¹. Parameter values in this model are based on available experimental and clinical data. A sensitivity analysis of certain model parameters that could affect the evolutionary dynamics of antimalarial drug resistance was also conducted.

Methods

The within-host parasite dynamics model. This section describes the proposed computational population dynamics model of malaria parasites in human and mosquito hosts. The complete parasite life cycle in human and mosquito hosts is separately simulated using the τ -leaping algorithm²¹. The model simulation begins with 10 inoculated sporozoites in a human body. Each sporozoite infects the human liver and produces merozoites (the blood stage parasites) at the rate of 30,000 merozoites per 10 days^{22,23}. The merozoites are then released to the blood stream and invade the red blood cells at an invasion rate

$$r = \begin{cases} 1 - N/K, & N < K \\ 0, & N \ge K' \end{cases}$$
(1)

where *N* is the number of infected red blood cells (IRBCs) in the human body and *K* is the parasite carrying capacity of the human host²². 1 - N/K is a logistic growth term representing the limitation of the growth rate caused by, for example, food and space limitations. The merozoites are produced from an IRBC at the rate of 10 merozoites per 2 days^{24,25}. Occasionally, some sexual gametocytes are produced instead of asexual merozoites. The ratio of the number of gametocytes to the number of merozoites produced from an IRBC ranges from 0.001 to 0.40²⁶. In our simulations, unless stated otherwise, this ratio is fixed at 0.1. The gametocytes are produced with the sex ratio of male to female gametocytes of 1:3.6²⁷. The gametocytes can circulate in the human body for an average of 6.4 days²⁶ and may be carried by a mosquito via biting at a rate of 0.344 per day²⁸. The within-host model of malaria parasite dynamics in a human body is summarised in Fig. 1A.



Figure 1. The parasite dynamics model. (**A**) A schematic of the malaria parasite dynamics in the human host. After 10 sporozoites are injected into the host body, they travel to the host liver and produce new offspring (merozoites). Each sporozoite produces merozoites at rate of 30,000 merozoites per 10 days. Each released merozoite invades a red blood cell at the rate of 1 - N/K and then begins the 48-hour reproduction cycle. In addition to merozoites, gametocytes may be produced from IRBCs at the ratio of 0.1. (**B**) A schematic of the malaria parasite dynamics in the mosquito host. A male and a female gamete combine together to form a zygote. This zygote develops into an oocyst that can then produce sporozoites at rate of 10,000 sporozoites per 10 days. (**C**) A schematic of the between-host transmission dynamics of malaria parasites.

.....

In the mosquito host (Fig. 1B), male and female gametocytes both develop into mature gametes²⁴. A male and a female gamete mates to form a zygote. This mobile zygote or ookinete then develops at the midgut in the form of oocyst for 7 days²⁹. When an oocyst reaches the mature stage, it produces approximately 10,000 sporozoites³⁰. The sporozoites within the mosquito saliva can be transferred to a human host via a mosquito bite. The parameters and their values used in this model are summarised in Table 1.

The between-host transmission dynamics model. The within-host parasite dynamics model proposed in the previous section can only separately describe the proliferation of the malaria parasites in an infected human and an infected mosquito host. However, to simulate the whole life cycle of malaria parasites within both human and mosquito hosts, the between-host transmission dynamics of the parasites are needed. The between-host transmission dynamics of gametocytes from an infectious human to a susceptible mosquito, and the transmission of sporozoites from an infectious mosquito to a susceptible human (Fig. 1C). These two events can separately occur through a mosquito bite and are governed by two parameters, namely, a biting rate, defined as the number of mosquito bites that each human individual receives in a day, and an infection probability describing a chance for a mosquito or a human to obtain an infection through a bite.

When a susceptible mosquito bites an infectious human, the mosquito can obtain an infection with an infection probability that is proportional to the density of the gametocytes within the infectious human at the time of biting³¹ (see Fig. S1 and the Supplementary Methods). If the bite leads to infection, gametocytes will be transferred to the mosquito. The number of gametocytes that will be transferred to the mosquito is proportional to the gametocyte density in the human body at the time of the biting. We assume that a mosquito takes 1 μ L of blood during a blood meal. Based on a previous study²⁹, the number of oocysts in a mosquito after blood feeding ranges from 1 to 200 (median 7.28) and the number of gametocytes per bite can range from 2 to 300; however, to reduce the simulation time, the maximum number of gametocytes per bite is limited to 20 gametocytes per bite. Limiting the maximum number of gametocytes per blood meal to 20 does not significantly affect the evolutionary dynamics of parasites because only one pair of male and female gametocytes is enough to infect a mosquito (see the analysis in the Sensitivity analysis section). While the probability of transmission of gametocytes from an infectious human to a susceptible mosquito depends on the density of the gametocytes within a target host³¹, the transmission of the sporozoites from an infectious mosquito to a susceptible human is assumed to definitely occur. When an infectious mosquito bites a human, 10 sporozoites are transferred into the human body²². In our model, the biting rate is fixed at 0.34 per human per day²⁸.

Definitions	Values	Refs.
Number of inoculated sporozoites via a mosquito bite	10 sporozoites	22
Production rate of merozoites from a sporozoite	30,000 merozoites per 10 days	22,23,34
Production rate of merozoites from an IRBC	10 merozoites per 2 days	24,25
Production rate of gametocytes from an IRBC	10 gametocytes per 10 days	46
Gametocyte to merozoite ratio	0.1	26
Average gametocyte circulation time	6.4 days	26
Parasite carrying capacity	10 ¹² per host	22
Gametocyte sex ratio (male:female)	1:3.6	27
Parasite reduction ratio of artemisinin monotherapy	10 ³	47
Number of male gametes produced from a male gametocyte	8 gametes	24
Number of female gametes produced from a female gametocyte	1 gamete	24
Time from zygote to oocyst	7 days	29
Number of sporozoites produced from a mature oocyst	10,000 sporozoites per 10 days	30

Table 1. A summary of the parameters and their values used in the within-host population dynamics model.

The spatial heterogeneity and evolutionary dynamics. To investigate the roles of the spatial heterogeneity in the antimalarial drug resistance dynamics, following the method presented in¹³, we consider a spatial environment that is divided into several relatively isolated compartments. Both the human and mosquito populations are also divided into subpopulations living in different compartments; hence, each compartment represents a co-living area of human and mosquito hosts (Fig. S2 in the Supplementary Material). All of the compartments are aligned in one-dimensional space.

The encounter rate between a human host living in compartment *i* and a mosquito inhabiting compartment *j* depends on the distance between compartments *i* and *j*. We assume that mosquitoes only stay in their home compartments while individual humans can travel to the other compartments. The encounter rate between a human individual and a mosquito can therefore be computed using a human mobility model. Following the human mobility model presented in ref. ³², the probability density that an individual living in compartment *i* will travel to compartment *j* (P_m) is given by

$$P_m(\Delta r_{ij}) = (\Delta r_{ij} + \Delta r_0)^{-\omega} exp(-\Delta r_{ij}/\kappa),$$
(2)

where $\Delta r_{ij} = |j - i|d$ is the distance between compartment *i* and *j*, $\omega = 1.75$, $\kappa = 80$, $\Delta r_0 = 1.5$ km, and d = 1 km is the width of each compartment. Therefore, in our model, each human individual living in compartment *i* can be bitten by a mosquito inhabiting in any compartment *j* with a probability that is proportional to $P_m(\Delta r_{ij})$. It is worth noting that in this study, we did not explicitly simulate human movement between compartments, but instead, we used the travel probability density (Eq. 2) to estimate how likely a human individual will be bitten by a mosquito living in each compartment. By combining the travel probability density $P_m(\Delta r_{ij})$, the biting rate, and the mosquito infection probability $P_{Inf}(n)$, the parasites can migrate throughout the entire environment.

Figure 2 illustrates the evolutionary model of antimalarial drug resistance in a heterogeneous environment. Following the method presented in¹³, we consider an environment that is divided into a series of relatively isolated compartments (Fig. 2A). Each compartment is associated with a fixed antimalarial drug concentration that linearly increases from left to right. The genotype of each parasite is characterised by a positive integer *g* plotted vertically. This integer *g* indicates a drug concentration level that can kill the parasites. For example, the parasites with g = 2 can be killed by a drug if they live in a compartment that is associated with the drug concentration level ≥ 2 , that is, they can be killed if they live in a compartment *i* ≥ 2 . Importantly, parasites with a larger *g* are more resistant and cannot be killed at a lower drug concentration level.

Each parasite is capable of proliferating, migrating via human travel and mosquito bites, getting killed by an antimalarial drug, and accumulating mutations in a human host. Although a mutation of the parasites may occur at any stage of their life cycle, in our model we assumed that the mutations occur mainly during the reproduction cycle of merozoites. This is reasonable because the number of parasites in the blood stage is highest; hence, it is more likely that the mutations will occur during this reproduction cycle. A forward mutation occurring at a rate of μ_f increases g by one, whereas a backward mutation does the opposite by decreasing g by one at a rate of μ_b . Gametocytes with a genotype g can be produced from a merozoite with the same genotype g. On the other hand, in an infected mosquito, when a male gamete with a genotype g_m mates with a female gamete with a genotype g_{f_p} we assume that a zygote with either genotype g_m or g_f will be produced with equal chance. We have also checked that in all of our model realisations there is no gamete recombination in which g_m and g_f differ more than one. Parasite proliferation is simulated using the within-host parasite dynamics model (Fig. 1).

In addition, the population dynamics of parasites does not only vary from one compartment to another, but also depends on the disease states of each individual. We classify the human hosts into four categories, namely, susceptible, exposed, infectious, and recovered, based on the number of parasites within their bodies. When an infectious mosquito bites a susceptible human, parasites are transmitted into the human. After being infected, the susceptible human progresses to the exposed class. Humans in this class have already acquired the infection, but the numbers of parasites within their bodies are not high enough to be noticed. Therefore, the parasites within these exposed people will not encounter any antimalarial drug. In contrast, the number of parasites within



Figure 2. The evolutionary model of antimalarial drug resistance. (**A**) We consider an environment divided into several compartments (plotted horizontally) in which malaria parasites can (**B**) migrate through human travel and a mosquito bite, (**C**) proliferate (grow), (**D**) mutate, and (**E**) die due to drug treatments. The malarial genotypes are characterised by an integer *g*, plotted vertically in (**A**), representing antimalarial drug resistance levels. A mutation increases or decreases g by one. The concentration of an antimalarial drug, represented by the green shaded areas, increases from left to right. The parasites living in compartment i will be killed by a drug if they have $g \leq i$.

infectious individuals is high enough to be noticed. Based on the study in³³, approximately 82.9% of 76 febrile patients had a number of parasites greater than 10⁹. We therefore assume that the infected individuals with a number of parasites more than 10⁹ will receive an antimalarial drug treatment, and their state will change to the infectious state. After infectious individuals receive the drug treatment and all of the parasites in their bodies are cleared out, they progress to the recovered state. We assume that the recovered individuals gain the ability to suppress parasites. The recovered individuals may be re-infected through a bite from an infectious mosquito, but they will not develop any symptoms and will not seek treatment. The number of parasites within the re-infected recovered individuals will be suppressed below the detection limit of 10⁸²². The default values of the model parameters are summarised in Table 2. The combined within- and between-hosts evolutionary dynamics model was simulated using the τ -leaping algorithm²¹ with a time step (τ) of 0.1 days. All of the information related to each malaria parasite, human individual, and mosquito (e.g., parasite stage, human and mosquito infection stage, compartmental location *i*, genotypic index *g*) was recorded and updated at each time step τ .

Results

Parasite dynamics within the human and mosquito hosts. Figure 3 shows the separated dynamics of parasites within an infected human host and a mosquito. In a human host, after being infected by a bite from an infectious mosquito, 10 sporozoites were initially transferred into the host body. Without any interference, the number of parasites increases rapidly and reaches the detection limit (10⁸ parasites) in 2 weeks, which approximately equals the time required for the liver schizont to release the first wave of merozoites^{22,34}. After this point, the number of parasites continues to increase and approaches maximum of 10¹² parasites within 3 weeks (Fig. 3A). In a mosquito vector, after being infected by biting an infectious human individual, gametocytes were transferred into the mosquito body. The number of sporozoites in the infected mosquito subsequently increases rapidly after the infection (Fig. 3B).

We then incorporated the effects of an antimalarial drug into our within-host parasite dynamics model and compared our simulation results with the available experimental data reported in³⁵. Usually, malaria symptoms can be observed in 2 weeks after an infective mosquito bite³⁶. Based on the study in³³, 17.1% of 76 febrile patients had a number of parasites less than 10⁹. Therefore, in our model, if the number of parasites reaches 10⁹, the drug treatment will be administered. As shown in Fig. 3C, our simulation results agreed with the observational data. The parasite reduction ratios (PRRs), defined as the ratio of parasitaemia numbers at the initial treatment time to the number at 48 hours, of artesunate monotherapy and artesunate-mefloquine combination therapy were approximately 10³ and 10⁴, respectively. In addition, as resistance to antimalarial drugs results in delayed parasite clearance time and the reduction in PRRs, our simulation results indicate that both PRRs of artesunate monotherapy and artesunate-mefloquine combination therapy and artesunate-mefloquine combination therapy and artesunate the both PRRs of artesunate monotherapy and artesunate the both PRRs of artesunate monotherapy and artesunate the both PRRs of artesunate monotherapy and artesunate-mefloquine combination therapy and artesunate both PRRs of artesunate monotherapy and artesunate both PRRs of artesunate monotherapy and artesunate-mefloquine combination therapy and artesunate both PRRs of artesunate monotherapy and artesunate-mefloquine combination therapy of resistant parasites drop below 10².

Definitions	Values	Refs.
Number of human population in each compartment	100	[Assumed]
Number of mosquito population in each compartment	300	[Assumed]
Total number of compartments	10	[Assumed]
Total number of <i>g</i>	10	[Assumed]
Forward mutation rate	10^{-7} per generation	[Assumed]
Backward mutation rate	10^{-4} per generation	[Assumed]
Parasite reduction ratio	10 ³	47
Number of parasites that leads patients to receive treatments	10 ⁹	33
Maximum number of parasites within recovered individuals (below the detection limit)	108	22
Biting rate	0.344 per person per day	28

Table 2. A summary of the default values of the model parameters.



Figure 3. Population dynamics of parasites within an infected human and an infected mosquito. (**A**) The number of parasites in an infected human host as a function of time after the infection of the human host (the time since the susceptible human got the infection from the infectious mosquito). The blue and red curves show the number of infected red blood cells and gametocytes with their standard deviations, respectively. (**B**) The number of sporozoites in an infected mosquito as a function of time since the infection of the mosquito (the time since the susceptible mosquito got the infection from the infectious human) with the standard deviation. (**C**) Simulation results showing the parasite dynamics in the human host under antimalarial drug treatment. The parasite density represents the percentage of the number of parasites compared to that at the treatment starting time. The open circle lines show the experimental data (adapted from³⁵), and the dashed lines show the simulation results.

Roles of a concentration gradient on the evolutionary dynamics. In this section, we investigate the evolutionary dynamics of antimalarial drug resistance in both heterogeneous and homogeneous environments. Figure 4 shows snapshots of the parasite population evolving antimalarial drug resistance (see also Supplementary Movie S1). The simulation started with 10 infected human hosts in compartment 1; each is infected with 10 non-resistant sporozoites (g = 1). These parasites reproduce in the infected hosts according to the proposed within-host parasite dynamics (Fig. 1A). The first resistant strain (g = 2) rises and dominates in compartment 1 at approximately day 39. At day 138, the parasites with g = 3 dominate in compartment 2 while the parasites with



Figure 4. Snapshots showing the parasite population evolving antimalarial drug resistance. The colour maps indicate the number of infected red blood cells (IRBCs) of human individuals. Initially, 100 non-resistant parasites (g = 1) infect susceptible human individuals in compartment 1. The parasite population adapts and expands simultaneously to invade the other compartments. While most of the parasite population climbs the staircase to obtain the higher level of drug resistance, some of the low resistant population spreads horizontally to the areas with higher drug concentrations. Parameters: $\mu_f = 10^{-7} day^{-1}$, $\mu_b = 10^{-4} day^{-1}$, PRR = 10³, and $\tau = 0.1 day$; all of the others are listed in Tables 1 and 2.

g=1 can be found at some distant compartments (for example, compartments 5 and 7). At day 348, the parasites with g=4 can be found. The parasites with g=1 and 2 now spread to all of the compartments. As shown in Fig. 4, the parasite population grows and then spreads upward and rightward. Antimalarial drug resistance develops at the edges of the staircase and then spreads horizontally to the right compartments. At the end of the simulation, the coexistence of several parasite strains can be found in all of the compartments.

Importantly, the evolutionary dynamics exhibited in the heterogenous environment (Fig. 4) differ from those in the homogeneous environment. In the homogeneous environment (see Figs. S3–S6 in the supplementary results), resistance to antimalarial drugs occurs by chance. Although the resistance to low drug concentrations is easy to find, the resistance to higher drug concentrations is rare. By assuming that the parasites evolve drug resistance via a forward mutation that occurs only once in a generation, wild-type parasites cannot immediately resist high drug concentrations in only one mutation. In a homogeneous environment with a level-2 drug concentration (Fig. S5), the parasites require two forward mutations to survive. The time to find the parasite with g= 3 is approximately 765 days, while it takes only 140 days to find the parasite with g = 3 in the heterogeneous environment. In the homogeneous environment, two consecutive forward mutations are required to increase gto g = 3 before the parasite is cleared out by the drug. In contrast, in the heterogeneous environment, two forward mutations are not required to occur consecutively. Since the antimalarial drug concentration is increased stepwise, the parasites can rest and accumulate mutations before they go to the other compartments with higher drug concentrations.

Based on the proposed evolutionary model, under antimalarial treatment, only the parasites with g > i can survive in compartment *i*. To quantify the speed of the parasite adaptation, we therefore measured a fixation time of parasites with genotype g, which is defined as the earliest time that the parasites with g = i + 1 dominate in compartment *i*. Nevertheless, the fixation time will indicate only how fast the evolution of resistance is, but not how likely it will occur. Therefore, we also measured a fixation probability of the parasites with g = i + 1 in compartment *i* calculated from the number of simulation runs that the fixation of the parasite with g = i + 1 was found within 1,000 days since the treatment began divided by the total number of simulation runs. Figure 5 shows the measured fixation times and the corresponding fixation probabilities. Obviously, parasites with a lower resistant level can be found more easily than the higher resistant parasites.

Figure 5. The fixation times and fixation probabilities of parasites. The left vertical axis shows the fixation times. Each cyan dashed line indicates the fixation time measured from the individual simulation. The blue solid line shows the mean fixation time averaged from 50 simulation runs. The right vertical axis shows the fixation probability. The red line shows the fixation probability calculated from 50 simulation runs.

Sensitivity analysis. In this section, a sensitivity analysis of certain model parameters on antimalarial drug resistance evolution is performed. We first investigated the effects of the parasite mutation rates on the parasite evolutionary dynamics. Obviously, the resistant parasites usually emerge faster and more frequently when the forward mutation rate increases (Fig. 6). Next, a sensitivity analysis of the biting rate was performed. This parameter can affect the speed of parasite migration. If humans are bitten more frequently, the parasites are more likely to be transmitted between human individuals. As shown in Fig. 7, the relationship between the fixation time, the fixation probability, and the biting rate may be classified into two scenarios. In the low biting rate scenario (less than 0.3 per human per day), the fixation times of drug resistant parasites decrease rapidly as the biting rates increase. After the biting rate exceeds 0.3 per human per day (the high transmission scenario), the fixation times continue to decrease but at slower rates. More interestingly, in the low transmission scenario, the fixation probabilities of resistant parasites generally increase as the biting rates increase. In contrast, in the high transmission scenario, the fixation probabilities of higher resistant parasites, for example, g = 5 and 6, decrease as the biting rates increase. This may be because, in the high transmission scenario, the parasites spread rapidly, and therefore the strains with lower resistant level can occupy most compartments before the parasites with higher resistant level arrive. Next, we investigated the effects of the parasite reduction ratios (PRRs) on the parasite evolutionary dynamics. As shown in Fig. S7A in the supplementary information section, the fixation times of the resistant parasites do not depend on the PRRs. This is similar to the result found in the study of antibiotic resistance evolution in bacteria, in which the bacterial adaptation rate does not depend on the drug killing rate¹³. In addition, we found that the fixation probabilities of higher resistant parasites (g = 5 and 6) slightly decreased with the increasing PRRs (Fig. S7B). This indicates that higher resistant parasites might be less likely to be found if they are under antimalarial treatment with a higher PRR. Finally, we investigated whether limiting the maximum number of gametocytes that a mosquito can take during a blood meal to 20 will affect the evolutionary dynamics of parasites or not. As shown in Fig. S8, we found that the fixation times and the fixation probabilities of the resistant parasites do not significantly depend on the maximum number of gametocytes that a mosquito can take during a blood meal.

Similar to the antibiotic resistance evolution in bacteria, the adaptation of antimalarial resistant parasites usually carries a fitness cost of mutation³⁷⁻³⁹. To investigate the effect of the fitness cost of mutation on the fixation time and the fixation probability, we slightly modified the within-host model of malaria parasites. Following the methodology presented in¹³, we assumed that all parasites in mosquitoes and humans, except only the blood-stage merozoites, grow a factor 1 - s more slowly than the drug-sensitive parasites, where *s* is a normalised fitness cost of mutation. In our model, only the blood-stage merozoites are under the drug pressure; they, therefore, gain an advantage from being resistant. The fitness gain was assumed to be equal to the fitness cost of mutation so that there is no fitness cost for the blood-stage merozoites. However, if the blood-stage merozoites are more resistant than necessary (g > i), their fitness cost will be dominated; they, therefore, will grow a factor 1 - s more slowly than the drug-sensitive merozoites. As shown in Fig. S9, we found that the fitness cost of mutation can prolong the fixation time of the resistant parasites excepts the resistant parasites with g = 2 where only one step of mutation is required. In addition, the fixation probability of high resistant parasites (g = 3 - 6) also decreases when the fitness cost of mutation increases.

Discussion

The staircase model proposed in⁴⁰ provides a basic framework for studying the roles of a concentration gradient in drug resistance evolution. The original staircase model was used to assess the evolutionary dynamics of antibiotic resistance in bacteria. In the present report, we adapted the original framework to investigate the roles of a concentration gradient in malaria drug resistance evolution in malaria parasites. Since the life cycle of malaria

Figure 6. The fixation times and fixation probabilities as a function of the forward mutation rates. (**A**) The fixation times generally decrease when the forward mutation rates increase. The error bars show the standard error of the mean. (**B**) The fixation probabilities generally increase with the increasing forward mutation rates. The drug resistant parasites can be found more frequently when the forward mutation rate increases. The results were averaged from 50 simulations.

.....

parasites is much more complicated than that of bacteria, studying the roles of a concentration gradient in the malaria drug resistance evolution process in parasites is challenging.

We proposed a novel stochastic model to investigate the roles of a concentration gradient on malaria drug resistance evolution. The aims of the model were to investigate the evolutionary dynamics of malaria drug resistance within the human hosts and the spread of resistant parasites in heterogeneous environments. Our model consists of many sub-compartments representing individual hosts and mosquitoes. Parasites can cross to the other compartments only via human travel and mosquito bites. Since a malaria parasite develops through several life stages and lives within both the human host and mosquito hosts, malaria treatment will not affect all parasite stages. Parasites in certain stages will never encounter the antimalarial drugs, for example, all stages in the mosquito. Environments in which the parasites can live without being killed by an antimalarial drug act as sanctuaries for the parasites to avoid the antimalarial drug. This is different from the original staircase model in which all of the bacteria in the same compartment encounter the same drug concentration⁴⁰.

Our work focuses on the evolutionary dynamics of malaria drug resistance within a human body and the transmission of the resistant parasites among human and mosquito populations. To investigate the evolutionary dynamics of malaria drug resistance on the scale of the parasite's population in a human body, the within-host population dynamics model was constructed to simulate the whole life cycle of *P. falciparum*^{22,24–30,33,36}. All of the model parameters were based on experimental and clinical reports (see Table 1). Although parasites can independently live within a single human host, they can be transmitted to other human individuals via mosquito bites. In addition, as the parasites live within individual hosts, they can travel to different geographical locations with their hosts. To take into account the effect of human mobility in carrying the parasites to different geographical locations, the between-host transmission dynamics are also integrated into the model. Moreover, the notable roles of spatial heterogeneity were investigated by comparing the fixation times of parasites in homogeneous environments with those in heterogeneous environments. To the best of our knowledge, this study presents the first computational analysis of the roles of a concentration gradient on the evolutionary dynamics of malaria drug resistance.

The within-host population dynamics model was used to simulate the parasite population dynamics within both individual humans and mosquitos (Fig. 1A,B). The model was constructed based on the experimental and

Figure 7. The fixation times and fixation probabilities as a function of the biting rates. (**A**) The fixation times decrease when the biting rates increase. If humans are bitten more frequently, drug resistant parasites will emerge earlier. The error bars show the standard error of the mean. (**B**) In the regime of a high biting rate, the fixation probabilities of parasites with higher *g* decrease with the increasing biting rates. The results were averaged from 50 simulations.

reported clinical data^{22,24-30}. The simulation results were also validated with the clinical data^{33,36}. The artemisinin treatment was employed in our model. Artemisinin exerts its malaria treatment effect by targeting the blood stage parasites⁶. Artemisinin is one of the most effective drugs and can be combined with other compounds for combination therapy. We found that the simulation results are in good agreement with the experimental data (Fig. 3)³⁵.

The within-host population dynamics model was then extended to include the between-host transmission dynamics (Fig. 1C). The mosquito infection probability, which is the probability that a mosquito will carry the parasites with a blood meal from a target human, is determined by the gametocyte density within the target host (Fig. S1)³¹. Furthermore, to integrate the effects of spatial heterogeneity, both human and mosquito populations were divided into subpopulations living in different spatial compartments. Each compartment represents a co-living area of human and mosquito hosts (Fig. S2). By assuming that humans can travel to the other compartments, the parasites can migrate to the other compartments along with the human hosts. To describe the movement of human individuals, the human mobility model was also integrated into the transmission dynamics³².

In heterogeneous environments, a concentration gradient exists across the environment. Similar to the result found in the study of antibiotic resistance evolution, the antimalarial drug gradient can lead to a mode of adaptation that is different from those occurring in homogeneous environments. Our results show that the time to find high-resistant strains in heterogeneous environments is shorter than that in homogeneous environments (Figs. 4 and S3–S6). In heterogeneous environments, the sources and sinks of parasites are provided by the concentration gradient. We found that in heterogeneous environments, the first drug resistant parasite appears at approximately day 36, which is close to the time to find the first resistant parasite in the homogeneous environment with the level-1 drug concentration (Fig. S4). In this case, the parasites need only one forward mutation to increase g from g=1 to g=2 to resist the antimalarial drug. However, in the homogeneous environment with a higher level of drug concentration, the evolution of the antimalarial drug resistance is significantly slower than that in the heterogeneous environment (Figs. S5 and S6). In this case, two or more consecutive steps of the forward mutation are required for the parasites to survive in the environment.

We found that the rate of resistance evolution in the high transmission setting (high mosquito biting rate) is slower than in the low transmission setting. This is because in the high transmission setting, the lower resistance strains have a higher chance to migrate to and fully occupy the distant compartments before the strains with higher resistance level emerge. As parasites can linger within recovered individuals who show no signs of

symptoms and will not seek medical treatment, the parasites can survive and spread to the distant compartments without being killed by antimalarial drugs.

Similar to the antibiotic resistance evolution in bacteria¹³, we found that the killing rates of antimalarial drugs are not likely to affect the evolutionary rate of antimalarial drug resistance (Fig. S7). This is probably because, under the concentration gradient, the resistance evolution can most likely occur through two "evolutionary paths"¹³. Each path involves only one mutation and one migration event. In the first path, the parasite first mutates in a compartment with a lower drug concentration and then migrates to another compartment with a higher drug concentration occurs first and then is followed by a mutation. Increasing the PRR decreases the time that the parasites with lower resistant level can live under the staircase and therefore only affects the second path¹³. When the drug killing rate is lower than the parasite reproduction rate, the resistance evolution through the two paths is likely to occur at the same rate. However, when the antimalarial drug killing rate is higher than the parasite reproduction rate, the rate of the resistance evolution through the first path is dominant and is not affected by the increase in the PRR.

It is worth noting that, to simplify the within-host model, we assume that gametocytes can be produced immediately after the production of merozoites in the liver. This assumption might not be realistic since literature suggests that the liver stage of infection should last around a week before the liver merozoites are released into the host circulation, where they can invade red blood cells and subsequently produce gametocytes^{41,42}. However, we do believe that the conclusion of this work is not affected by this assumption. This is because the number of merozoites produced during the liver stage is tiny as compared to the number of merozoites that can be produced in the blood stage (about 10^5 merozoites can be produced in the liver stage while 10^{12} merozoites can be produced in the blood stage). Therefore, the number of gametocytes that may be produced during the liver stage is very small as compared to the number of gametocytes produced from the blood merozoites. We have confirmed this by running a slightly modified version of our within-host model in which the rate (r) that the liver merozoites are released to the blood stream and invade the red blood cells was changed to:

$$r = \begin{cases} 0, & t \le t_0 \\ 1 & -N/K, & N < K, \text{ and } t > t_0 \\ 0, & N \ge K, \text{ and } t > t_0 \end{cases}$$
(3)

In this modified model, the liver merozoites cannot infect the red blood cells and, therefore, cannot produce gametocytes before a time threshold t_0 . We ran the modified model with different values of t_0 and calculated the mosquito infection probability using the relationship shown in Fig. S1A. As shown in Fig. S1B in the Supplementary Material, we found that restricting the gametocytes to be produced precisely after 1–10 days does not significantly affect the mosquito infection probability. The effect of t_0 on the infection probability is noticeable only when t_0 is extreme such as 12–13 days, which might be rare in reality^{20,43}. Note also that even the case of $t_0 = 1$ day, our calculated mosquito infection probability starts to increase only after approximately 10 days; this agrees well with the fact that malaria has an incubation period of about 6–14 days in human⁴⁴.

We presented a stochastic combined within- and between-hosts evolutionary dynamics model of malaria parasites to investigate the antimalarial resistance evolution in the presence of an antimalarial concentration gradient. Although the proposed evolutionary model was build based mainly on available experimental and clinical data related to antimalarial resistance, the antimalarial concentration gradient employed in this study was highly idealised. The pattern of the concentration gradient was purposefully kept simple so that the roles of the concentration gradient could be quantitatively characterized. In addition, to allow a direct comparison of the roles of a concentration gradient in antimalarial resistance evolution to those in the antibiotic resistance evolution, a linear concentration gradient was employed in this study; as this kind of concentration gradient was used in previous studies of antibiotic resistance evolution^{13,45}. However, we do expect that several basic results found in this study will hold up for a more realistic concentration gradient as long as there exist compartments with a low antimalarial concentration where they can act as sanctuaries (or reservoirs) and allow mutations to be accumulated.

Data availability

The authors declare that the data supporting the findings of this study are available within the paper and its Supplementary Information file. Computer code are available from the authors upon reasonable request.

Received: 7 October 2019; Accepted: 26 March 2020; Published online: 10 April 2020

References

- 1. White, N. J. et al. Malaria. The Lancet 383, 723-735, https://doi.org/10.1016/S0140-6736(13)60024-0 (2014).
- 2. Organization, W. H. World malaria report 2018. (2018).
- 3. Organization, W. H. World malaria report 2017. (2017).
- 4. Organization, W. H. World malaria report 2016. (2016).
- 5. Organization, W. H. Guidelines for the treatment of malaria. Third edition. (2015).
- 6. White, N. J. Qinghaosu (Artemisinin): The Price of Success. Science 320, 330 (2008).
- 7. Tyagi, R. K. *et al.* High-level artemisinin-resistance with quinine co-resistance emerges in P. falciparum malaria under *in vivo* artesunate pressure. *BMC Medicine* **16**, 181, https://doi.org/10.1186/s12916-018-1156-x (2018).
- Menard, D. & Dondorp, A. Antimalarial Drug Resistance: A Threat to Malaria Elimination. Cold Spring Harbor Perspectives in Medicine 7, https://doi.org/10.1101/cshperspect.a025619 (2017).

- Dondorp, A. M. et al. Artemisinin resistance: current status and scenarios for containment. Nature Reviews Microbiology 8, 272, https://doi.org/10.1038/nrmicro2331 (2010).
- Zhang, Q. et al. Acceleration of emergence of bacterial antibiotic resistance in connected microenvironments. Science 333, 1764–1767, https://doi.org/10.1126/science.1208747 (2011).
- 11. Baym, M. et al. Spatiotemporal microbial evolution on antibiotic landscapes. Science 353, 1147-1151, https://doi.org/10.1126/science.aag0822 (2016).
- Hermsen, R. & Hwa, T. Sources and sinks: a stochastic model of evolution in heterogeneous environments. *Phys Rev Lett* 105, 248104, https://doi.org/10.1103/PhysRevLett.105.248104 (2010).
- Hermsen, R., Deris, J. B. & Hwa, T. On the rapidity of antibiotic resistance evolution facilitated by a concentration gradient. Proceedings of the National Academy of Sciences of the United States of America 109, 10775–10780, https://doi.org/10.1073/ pnas.1117716109 (2012).
- 14. Andersson, D. I. & Hughes, D. Microbiological effects of sublethal levels of antibiotics. Nature Reviews Microbiology 12, 465 (2014).
- Baquero, F. & Negri, M. C. Challenges: Selective compartments for resistant microorganisms in antibiotic gradients. *Bioessays* 19, 731–736 (1997).
- 16. Moreno-Gamez, S. *et al.* Imperfect drug penetration leads to spatial monotherapy and rapid evolution of multidrug resistance. *Proceedings of the National Academy of Sciences* **112**, E2874–E2883 (2015).
- 17. Cui, L. et al. Malaria in the Greater Mekong Subregion: heterogeneity and complexity. Acta tropica 121, 227–239 (2012).
- Dondorp, A. et al. Fake antimalarials in Southeast Asia are a major impediment to malaria control: Multinational cross-sectional survey on the prevalence of fake antimalarials. Tropical Medicine & International Health 9, 1241–1246 (2004).
- 19. Newton, P. N. *et al.* A collaborative epidemiological investigation into the criminal fake artesunate trade in South East Asia. *Plos medicine* 5, e32 (2008).
- 20. Legros, M. & Bonhoeffer, S. A combined within-host and between-hosts modelling framework for the evolution of resistance to antimalarial drugs. *Journal of the Royal Society Interface* 13, 20160148 (2016).
- Gillespie, D. T. Approximate accelerated stochastic simulation of chemically reacting systems. J. Chem. Phys. 115, 1716–1733, https://doi.org/10.1063/1.1378322 (2001).
- White, N. J. & Pongtavornpinyo, W. The de novo selection of drug-resistant malaria parasites. *Proceedings. Biological sciences/The Royal Society* 270, 545–554, https://doi.org/10.1098/rspb.2002.2241 (2003).
- Rosenberg, R., Wirtz, R. A., Schneider, I. & Burge, R. An estimation of the number of malaria sporozoites ejected by a feeding mosquito. Transactions of the Royal Society of Tropical Medicine and Hygiene 84, 209–212 (1990).
- 24. Sherman, I. W. Molecular approaches to Malaria., (ASM Press, 2005).
- 25. Bannister, L. & Mitchell, G. The ins, outs and roundabouts of malaria. Trends in parasitology 19, 209-213 (2003).
- Eichner, M. et al. Genesis, sequestration and survival of Plasmodium falciparum gametocytes: parameter estimates from fitting a model to malariatherapy data. Transactions of the Royal Society of Tropical Medicine and Hygiene 95, 497–501 (2001).
- Robert, V. et al. Effect of gametocyte sex ratio on infectivity of Plasmodium falciparum to Anopheles gambiae. Transactions of the Royal Society of Tropical Medicine and Hygiene 90, 621–624 (1996).
- Kabbale, F. G., Akol, A. M., Kaddu, J. B. & Onapa, A. W. Biting patterns and seasonality of Anopheles gambiae sensu lato and Anopheles funestus mosquitoes in Kamuli District, Uganda. *Parasites & vectors* 6, 340, https://doi.org/10.1186/1756-3305-6-340 (2013).
- Morlais, I. et al. Plasmodium falciparum mating patterns and mosquito infectivity of natural isolates of gametocytes. Plos One 10, e0123777, https://doi.org/10.1371/journal.pone.0123777 (2015).
- Menard, R. *et al.* Circumsporozoite protein is required for development of malaria sporozoites in mosquitoes. *Nature* 385, 336–340, https://doi.org/10.1038/385336a0 (1997).
- Churcher, T. S. et al. Predicting mosquito infection from Plasmodium falciparum gametocyte density and estimating the reservoir of infection. eLife 2, e00626, https://doi.org/10.7554/eLife.00626 (2013).
- Gonzalez, M. C., Hidalgo, C. A. & Barabasi, A. L. Understanding individual human mobility patterns. Nature 453, 779–782, https:// doi.org/10.1038/nature06958 (2008).
- 33. Ali, H. *et al.* Parasite density and the spectrum of clinical illness in falciparum malaria. *J Coll Physicians Surg Pak* **18**, 362–368, 06.2008/JCPSP.362368 (2008).
- Soulard, V. et al. Plasmodium falciparum full life cycle and Plasmodium ovale liver stages in humanized mice. Nature communications 6, 7690, https://doi.org/10.1038/ncomms8690 (2015).
- Dondorp, A. M. et al. Artemisinin Resistance in Plasmodium falciparum Malaria. New England Journal of Medicine 361, 455–467, https://doi.org/10.1056/NEJMoa0808859 (2009).
- 36. Organization, W. H. Fact sheet about Malaria. (2017).
- Bunditvorapoom, D. et al. Fitness loss under amino acid starvation in artemisinin-resistant Plasmodium falciparum isolates from Cambodia. Scientific reports 8, 1–9 (2018).
- Kümpornsin, K. et al. Origin of robustness in generating drug-resistant malaria parasites. Molecular biology and evolution 31, 1649–1660 (2014).
- Gabryszewski, S. J., Modchang, C., Musset, L., Chookajorn, T. & Fidock, D. A. Combinatorial genetic modeling of pfcrt-mediated drug resistance evolution in Plasmodium falciparum. *Molecular biology and evolution* 33, 1554–1570 (2016).
- 40. Hermsen, R., Deris, J. B. & Hwa, T. On the rapidity of antibiotic resistance evolution facilitated by a concentration gradient. *Proceedings of the National Academy of Sciences* **109**, 10775–10780, https://doi.org/10.1073/pnas.1117716109 (2012).
- 41. Khoury, D. S. et al. Within-host modeling of blood-stage malaria. Immunological reviews 285, 168-193 (2018).
- 42. Malaria liver-stage biology, https://www.mmv.org/newsroom/infographics/malaria-liver-stage-biology (2017).
- Agusto, F. B., Leite, M. & Orive, M. E. The transmission dynamics of a within-and between-hosts malaria model. *Ecological Complexity* 38, 31–55 (2019).
- 44. Orish, V. et al. In Open forum infectious diseases. ofy169 (Oxford University Press US).
- 45. Hermsen, R. The adaptation rate of a quantitative trait in an environmental gradient. Physical biology 13 (2016).
- 46. Adjalley, S. H. et al. Quantitative assessment of Plasmodium falciparum sexual development reveals potent transmission-blocking activity by methylene blue. Proceedings of the National Academy of Sciences of the United States of America 108, E1214–1223, https:// doi.org/10.1073/pnas.1112037108 (2011).
- 47. White, N. J. Assessment of the pharmacodynamic properties of antimalarial drugs *in vivo*. *Antimicrobial agents and chemotherapy* **41**, 1413–1422 (1997).

Acknowledgements

This project was financially supported by the Royal Golden Jubilee PhD Programme (Grant No. PHD/0079/2560), the Thailand Research Fund and Mahidol University (Grant No. TRG5880157), the Thailand Center of Excellence in Physics (ThEP), and the Centre of Excellence in Mathematics, the Commission on Higher Education, Thailand.

Author contributions

C.M., T.C. and S.R. conceived and designed the experiments. S.R. conducted the experiments. S.R., S.C., T.C. and C.M. discussed the results. C.M. and S.R. wrote the first draft of the manuscript. All of the authors edited the manuscript and approved the final version.

Competing interests

The authors declare no competing interests.

Additional information

Supplementary information is available for this paper at https://doi.org/10.1038/s41598-020-63283-2.

Correspondence and requests for materials should be addressed to C.M.

Reprints and permissions information is available at www.nature.com/reprints.

Publisher's note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2020