

Received: 18 April 2018 Accepted: 10 July 2018 Published online: 24 July 2018

OPEN Acoustic spin Hall-like effect in hyperbolic metamaterials controlled by the helical wave

Fangfang Ju¹, Ying Cheng^{1,2} & Xiaojun Liu^{1,2}

Because of the spin-less nature of sound, acoustic helical wave with different helical directions can be taken as a "spin-like" degree of freedom. In this Letter, we examine the pseudospin-orbit coupling effect in acoustics when an acoustic helical wave emitter interacts with the acoustic hyperbolic metamaterial (AHMM). The acoustic helical wave emitter is situated at the boundary of the AHMM, which gives rise to the unidirectional excitation with the trajectory controlled by the helical directions, and hence the acoustic spin Hall-like effect (ASHE) is observed. The ASHE is further demonstrated for the string-type and the membrane-type AHMM based on the hyperbolic dispersion. The reported ASHE paves a new way to exploiting signal routing and unidirectional excitation controlled by the helical directions of the acoustic helical wave.

Metamaterials are artificially engineered media made from a periodic spatial modulation of acoustic subwavelength building blocks. Through careful design of the material's composition, size, structure and mutual orientations, many intriguing properties have been realized which cannot be found in nature materials. Over the past decades, there are various structures proposed to realize versatile properties, such as a high-density solid core with soft coating which is the first locally resonant sonic unit to realize the negative dynamic mass density¹, Helmholtz resonators which consist of a short neck and cavity², ultraslow-fluid-like particle which exhibits intense Mie resonances³, coiling up space using curled channels of subwavelength cross section⁴, etc. Such remarkable structures have enabled sound propagation in unprecedented manners, including negative refraction⁵, super-resolution imaging⁶, invisibility cloaking^{7,8}, and zero-index waveguide^{9,10}. However, most applications of metamaterial concentrate on the classical physics in the low frequency range and the wavelength is too large to emerge quantum-like behaviors.

In addition to the quantum-like effects in acoustics studied in the very high frequency range, the close analogies between the classic physical phenomena in acoustic metamaterials and the quantum effects in electronics provide us an ideal platform to study the quantum-like effects in acoustics. Many intriguing properties have been demonstrated which are in close analogy with quantum effects in the electronics, such as Parity-time symmetric acoustics^{11,12}, robust pseudospin-dependent one-way edge sound transport in acoustic topological insulator¹³⁻¹⁸, Dirac-like cone to realize acoustic double zero refractive index metamaterials¹⁹, topological valley transport of sound²⁰, an analogue of Zitterbewegung effects in surface phononic graphene²¹, etc. It is noted that there are also many studies on the optical quantum-like effects as analogies to the quantum effects in the electronics, which give us a more direct route to the realization of the acoustic quantum-like effects since there are many similarities in optical waves and acoustic waves. For example, photonic spin Hall effect in hyperbolic metamaterials is in close analogy to the spin Hall effect for electrons where the different polarizations of photons play the role of "spin"22. With the inspiration of that work, in this letter, we introduce the acoustic spin Hall-like effect (ASHE) in the acoustic hyperbolic metamaterial (AHMM). AHMM is a special class of acoustic metamaterial deriving their name from the unique form of the equifrequency contour (EFC) which is hyperbolic instead of circular as in conventional materials. Thus, AHMMs can transmit sound with very high wavevector components which come to be evanescent in conventional materials. We exemplify the AHMM by multiple arrays of thin string/membrane. The acoustic helical wave with different helical directions is taken as an acoustic "spin-like" degree of freedom, which can be realized by the array of the acoustic point source or the recently proposed acoustic metamaterials giving rise to the orbital angular momentum^{23–25}.

¹Key Laboratory of Modern Acoustics, Department of Physics and Collaborative Innovation Center of Advanced Microstructures, Nanjing University, Nanjing, 210093, China. 2State Key Laboratory of Acoustics, Institute of Acoustics, Chinese Academy of Sciences, Beijing, 100190, China. Correspondence and requests for materials should be addressed to Y.C. (email: chengying@nju.edu.cn) or X.L. (email: liuxiaojun@nju.edu.cn)

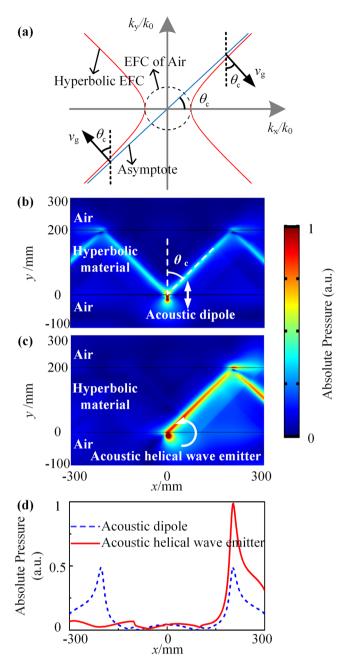


Figure 1. (a) Equifrequency contour of $k_x - k_y$ plot in the AHMM with hyperbolic dispersion ($\rho_x = 1.39 \, \text{kg/m}^3$, $\rho_y = -1.39 \, \text{kg/m}^3$, $K = 152 \, \text{KPa}$). Absolute pressure distribution of (b) acoustic dipole and (c) acoustic helical wave emitter radiating in the vicinity (at $10 \, \text{mm}$ distance from the interface) of an AHMM slab sandwiched by air (See Supplementary Movie 1 for dynamic view). (d) Absolute pressure along the cutline $y = 200 \, \text{mm}$ of (b) and (c).

Results

First, we demonstrate the unidirectional excitation in the AHMM. Figure 1(a) illustrates the EFC of $k_x - k_y$ plot in the AHMM. In two-dimensional (2D) scenarios, the acoustic waves in the anisotropic medium are governed by the density ρ_a , which depends on the propagation direction²²:

$$\frac{k_{\theta}^2}{\rho_{\theta}} = \frac{k_{\mathbf{x}}^2}{\rho_{\mathbf{x}}} + \frac{k_{\mathbf{y}}^2}{\rho_{\mathbf{y}}} \tag{1}$$

where θ is the angle between the wave vector and the x axis. $\rho_{\mathbf{x}}(k_{\mathbf{x}}), \rho_{\mathbf{y}}(k_{\mathbf{y}})$ and $\rho_{\theta}(k_{\theta})$ are the effective mass density (wave vector) in the x direction, y direction, and θ direction, respectively. For the AHMM ($\rho_{\mathbf{x}} > 0, \rho_{\mathbf{y}} < 0$), ρ_{θ} diverges at the angle $\tan^2\theta_{\mathbf{c}} = \left|\frac{\rho_{\mathbf{y}}}{\rho_{\mathbf{x}}}\right|$ which is the direction of the asymptote of the hyperbolic EFC. Thus, the density

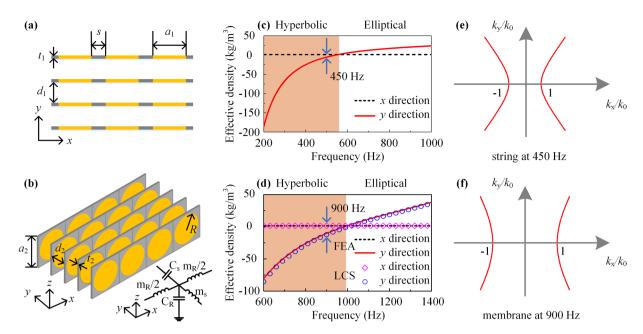


Figure 2. Designs of **(a)** the string-type and **(b)** the membrane-type AHMM. Retrieved effective mass density along the *x* and *y* directions of the **(c)** string-type and **(d)** membrane-type AHMM. The orange region corresponds to the frequency range of the hyperbolic dispersion $(\rho_x \cdot \rho_y < 0)$. The EFC of **(e)** the string-type AHMM at 450 Hz and **(f)** membrane-type AHMM at 900 Hz.

of acoustic states (DOS) at this angle is infinite. As the group velocity must lie normal to the EFC, all acoustic waves will propagate forming a cone with an opening angle of θ_c [see Fig. 1(a)]. i.e., the propagation channel in the AHMM is automatically selected.

As the helical wave can be expressed in the form of a dipolar moment $\mathbf{p} = [1, \pm i]$, we consider a 2D acoustic emitter with a dipolar moment $\mathbf{p} = [p_x, p_y]$, and then the pressure field can be written as $P(x, y) = ik_0\rho_0c_0\mathbf{p} \cdot \nabla g(|\overrightarrow{r}-\overrightarrow{r_0}|)$, where k_0 is the wave vector; ρ_0 is the density; c_0 is the sound speed of the medium; r_0 is the position of the acoustic emitter²⁶. $g(|\overrightarrow{r}-\overrightarrow{r_0}|) = \frac{e^{ik|\overrightarrow{r}-\overrightarrow{r_0}|}}{4\pi|\overrightarrow{r}-\overrightarrow{r_0}|}$, and $r = \sqrt{(x-x_0)^2+(y-y_0)^2}$. Since the angular spectrum representation of the function g(r) is derived that $\frac{e^{ikr}}{4\pi r} = \frac{i}{2\pi} \int_{-\infty}^{\infty} \frac{e^{ik_xx+ik_y|y|}}{4\pi r} dk_x$ and the angular spectrum representation of the pressure field P(x,y) can be written as $P(x,y) = \int_{-\infty}^{\infty} P(k_x,y) e^{ik_xx} dk_x$, it can be derived as

$$P(k_{x}, y) = -\frac{ik_{0}\rho_{0}c_{0}}{2\pi} \left(\frac{k_{x}}{k_{y}}p_{x} \pm p_{y}\right) e^{ik_{y}|y-y_{0}|}$$
(2)

where $k_y = \sqrt{k_0^2 - k_x^2}$, the angular frequency $\omega = k_0 c_0$, and the phasor notation $P(\overrightarrow{r},t) = \text{Re}[P(\overrightarrow{r}) \mathrm{e}^{-i\omega t}]^{7,28}$. The upper (lower) sign in Eq. (2) applies to $y > y_0 (y < y_0)$. Here three remarks should be noted: (1) An arbitrarily acoustic wave emitter situated in the near-field of the AHMM can be coupled to the high DOS modes of the AHMM efficiently. The high DOS modes in the AHMM are mainly made up of the superposition of different evanescent components with $k_x \gg k_0$ or $k_x \ll -k_0$ depending on the interface relation between the air and the AHMM $k_y = i\sqrt{k_x^2 - k_0^2} \approx \pm ik_x$, where the upper (lower) sign corresponds to $k_x \gg k_0$ ($k_x \ll -k_0$). (2) An acoustic dipole situated in the near-field of the AHMM excites the high DOS modes to the right and left equally. For example, for acoustic vertical dipole with the dipolar moment of $\mathbf{p} = [0, 1]$, $P(k_x, y)$ corresponding to $k_x \gg k_0$ and $k_x \ll -k_0$ are equal to each other [see Fig. 1(b)]. (3) The destructive interference condition applied to $y > y_0$ can be fulfilled if

$$p_{\mathbf{x}}k_{\mathbf{x}} + p_{\mathbf{y}}k_{\mathbf{y}} = 0 ag{3}$$

Thus, an acoustic helical wave emitter situated in the near-field of the AHMM results in the unidirectional excitation since it has the form $\frac{p_y}{p_x} = \pm i$. For example, for the acoustic counterclockwise helical wave emitter p = [1, -i], Eq. (3) can be only fulfilled when $k_x \ll -k_0$, and thus unidirectional excitation is observed [see Fig. 1(c)]. The absolute pressure along the cutline y = 200 mm in the Fig. 1(b and c) verify the analysis demonstrated above [see Fig. 1(d)].

We continue to demonstrate the physical prototypes of the AHMM. The string-type AHMM is illustrated in Fig. 2(a). Each of the two frames has a separation distance of $d_1 = 9.875$ mm, and the thickness of the frame is $t_1 = 0.125$ mm, and thus the frame in the y direction has a periodicity of $D_1 = d_1 + t_1 = 10$ mm. The widths of

the frame and the string are s=2 mm and $a_1=18$ mm, respectively. The design of the membrane-type AHMM is illustrated in Fig. 2(b). Each of the two frames has a separation distance of $d_2=9.875$ mm, and the thickness of the frame is $t_2=0.125$ mm, and thus the frame in the y direction has a periodicity of $D_2=d_2+t_2=10$ mm. The radius of the membrane is R=9 mm, and the width of the square frame is $a_2=20$ mm. The string/membrane has a thickness of 0.125 mm. The string/membrane-type AHMM consists of 21×80 string/membranes unit cells, but there are only 4×3 string unit cells shown in Fig. 2(a) and 5×4 membrane unit cells in Fig. 2(b) for clarity. The frames are acoustically rigid. The strings/membranes are fixed securely on the rigid frames to achieve the clamped boundary condition. No tension is applied on the strings/membranes. Two rigid panels cover the top and bottom of the membrane-type AHMM to ensure 2D wave propagation.

We use the transmission line model to understand the proposed membrane-type AHMM, which can be represented by the 2D array of the unit structure [see the inset in Fig. 2(b)]. The voltage U at one node in the grid is related to its neighbors via the Kirchhoff current law²⁹:

$$Y_{x}(U_{x-1,y} + U_{x+1,y}) + Y_{y}(U_{x,y-1} + U_{x,y+1}) - 2U_{x,y}(Y_{x} + Y_{y}) = U_{x,y}Y_{z}$$
(4)

where x and y denote the node position, and Y_x are the respective admittances. Y_z corresponds to the admittance of the shunt element. Equation (4) can be recast in a continuous form:

$$Y_{x}\partial_{xx}\widetilde{U} + Y_{y}\partial_{yy}\widetilde{U} = \frac{1}{S}Y_{z}\widetilde{U}, \tag{5}$$

where S is the area of the unit cell, and \widetilde{U} is the continuous counterpart of U. Considering $Y_x = \frac{1}{i\omega L_x} Y_y = \frac{1}{i\omega L_y + 1/(i\omega C_y)}, Y_z = i\omega C_z$, Eq. (5) can be recast as:

$$\frac{k_{\rm x}^2}{L_{\rm x}} + \frac{k_{\rm y}^2}{L_{\rm y} \left(1 - \frac{1}{\omega^2 L_{\rm y} C_{\rm y}}\right)} = \frac{\omega^2}{S/C_{\rm z}}$$
(6)

It can be shown that ${L'}_{\rm x}=L_{\rm x}, {L'}_{\rm y}=L_{\rm y}\Big[1-\frac{\omega_c^2}{\omega^2}\Big]$ and $C'=C_{\rm z}/S$, where $\omega_c=\sqrt{1/(L_{\rm y}C_{\rm y})}$.

The similarity between the Eq. (6) and the dispersion relation implies the one-to-one correspondences for all quantities. The constitutive parameters L'_x and L'_y for the circuit corresponds to the effective mass density of the system and the C' corresponds to the bulk modulus. The effective density along the x direction remains the same as air, $\rho'_x = \rho_{\rm air}$, because there are no membrane arranged in the x direction. The effective bulk modulus $B' = B_{\rm air}$, because the thin membrane has a negligible effect on the effective bulk modulus. From Eq. (6), it is noted that the effective density along the y direction $\rho'_y = \rho' \left(1 - \frac{\omega_c^2}{\omega^2}\right)$. Clearly, at a frequency below the first resonance frequency, the effective density along the y direction is negative, resulting in a broadband negative density. The membranes have a very good accuracy with a series resonant circuit with acoustic mass $m_{\rm am}$ and compliance $C_{\rm am}$ expressed by 30 :

$$m_{\rm am} = 1.8830 \frac{\rho_{\rm m}h}{\pi R^2}, C_{\rm am} = \frac{\pi R^6}{196.51D}$$
 (7)

here, h is the thickness of the membrane, and $D=Eh^3/12(1-\nu^2)$ represents its flexural rigidity. The parameters of the lumped element model in the y direction in the inset of Fig. 2(b) can be given by $m_{\rm s}=m_{\rm a}+m_{\rm am}$ and $C_{\rm s}=C_{\rm am}$, where $m_{\rm a}=\rho_{\rm air}(d-h)/S$ is the acoustic mass of the air section and S is the cross section area of the unit. The compliance of the air section is negligible since the size of the unit of the membrane-type AHMM is far less than the wavelength. The acoustic mass and the acoustic compliance of the lumped element model of air can be calculated according to the density ($\rho_{\rm air}$) and the bulk modulus ($K_{\rm air}$) of air such as $m_{\rm R}=\rho_{\rm air}d/\Delta S$ and $C_{\rm R}=\Delta S\times d/K_{\rm air}$, where ΔS is the area of the cross section. It follows that, the sound transmission in both the membrane network and the air can be simulated with the parameters demonstrated above. The parameters of the membrane network can be derived that $Y_{\rm x}=\frac{1}{i\omega I_{\rm x}}=\frac{1}{i\omega m_{\rm x}}, Y_{\rm y}=\frac{1}{i\omega m_{\rm x}+1/(i\omega C_{\rm s})}, Y_{\rm z}=i\omega C_{\rm R}$. In order to verify the broadband negative density of the AHMMs, a rigorous retrieving method is used to obtain its effective parameters S^{3} . The effective density of a unit cell in the string/membrane-type AHMM is negative over the hyperbolic frequency band [see Fig. 2(c,d)]. The dispersion is clearly hyperbolic below the first resonance frequency [see Fig. 2(e,f)].

In order to present the ASHE in the prototypes of proposed AHMMs, the full-wave numerical simulations are performed. Figure 3 shows the pressure field when the acoustic dipole or the helical wave emitter is in near-field of the string-type AHMM. The numerical simulation is realized at 450 Hz where the dispersion of the string-type AHMM is hyperbolic according to Fig. 2(e). The boundary of the domain is set to be radiative and the acoustic wave emitter in air is situated 20 mm away from the string array. Both the acoustic horizontal and vertical dipoles excite the high DOS modes equally to the right and left from its position [see Fig. 3(a,b)]. The acoustic helical wave emitter is shown to support the unidirectional excitation [see Fig. 3(c,d)], which is in good agreement with the destructive interference condition (Eq. (3)). Changing the helical direction of the helical wave switches the direction of the emission. The phenomenon in Fig. 3 has proved the ASHE in the string-type AHMM. A 16 dB power ratio radiated in different directions is found for acoustic clockwise and counterclockwise helical wave emitters and the string-type AHMM is shown to support the strongly confined subwavelength modes with about

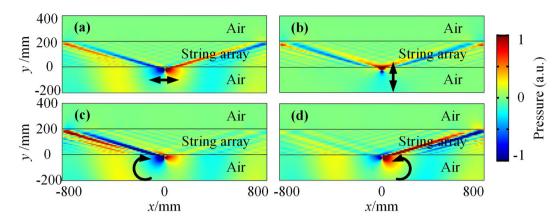


Figure 3. ASHE in the string-type AHMM. The pressure field excited by (a) the acoustic horizontal dipole p = [1, 0], (b) the acoustic vertical dipole p = [0, 1], (c) the acoustic clockwise helical wave emitter p = [1, i] and (d) the acoustic counterclockwise helical wave emitter p = [1, -i] situated in the near-field of the string-type AHMM (See Supplementary Movie 2).

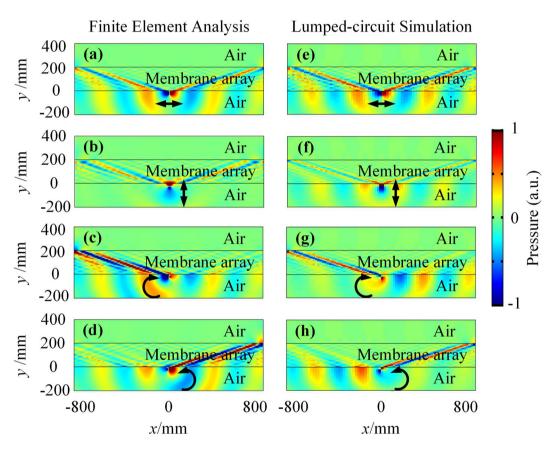


Figure 4. ASHE in the membrane-type AHMM. The pressure field excited by (a) the acoustic horizontal dipole p = [1, 0], (b) the acoustic vertical dipole p = [0, 1], (c) the acoustic clockwise helical wave emitter p = [1, i] and (d) the acoustic counterclockwise helical wave emitter p = [1, -i] situated in the near-field of the membrane-type AHMM. (e-h) Corresponding lumped-circuit simulation results (See Supplementary Movie 3).

 λ /8 full width at half maximum (FWHM). Since the only requirement on the helical-wave-induced routing by the metamaterial is its hyperbolic dispersion, the reported unidirectional excitation is inherently broadband for the string-type AHMM.

Furthermore, in terms of the similar properties of the membrane and the string, the membrane-type AHMM is also demonstrated to enable the ASHE, which can be realized more straightforward. Figure 4 shows the pressure field when the acoustic dipole or the helical wave emitter is in near-field of the membrane-type AHMM through

three-dimensional (3D) full-wave acoustic simulations as well as Lumped-circuit (LC) simulations. Similar to the ASHE in the string-type AHMM, while an acoustic horizontal or vertical dipole excites equally the high DOS modes to the right and left from its position [see Fig. 4(a,b)], the acoustic helical wave emitter destructively interferes in one direction [see Fig. 4(c,d)] depending on the helical directions. In the LC simulations, the metamaterial slab is represented by periodically repeating the unit cell in the inset of Fig. 2(b). The LC simulation results [see Fig. 4(e-h)] show good agreement with the corresponding acoustic simulation results [see Fig. 4(a-d)]. The phenomenon in Fig. 4 has proved the ASHE in the membrane-type AHMM. A 14 dB power ratio radiated in different directions is found for acoustic clockwise and counterclockwise helical wave emitters and the membrane-type AHMM is shown to support the strongly confined subwavelength modes with about $\lambda/6$ FWHM. The reported unidirectional excitation is inherently broadband for the membrane-type AHMM too.

Discussion

The ASHE in the string-type AHMM and the membrane-type AHMM has been observed. The ASHE has a remarkably close analogy to the SHE for electrons and the photonic spin Hall effect. In our realization, the ASHE effect is observed due to the inversion symmetry broken by the acoustic helical wave emitter. The directional broadband excitation of guided modes is achieved with an acoustic helical wave emitter, which is in close analogy to the electron sorting by their spins in a current flow and the unidirectional emitting of photons with different polarizations. The emergence of the phenomenon was numerically demonstrated with the string-type AHMM at 450 Hz and the membrane-type AHMM at 900 Hz. The experiment of the ASHE in the membrane-type AHMM is believed to be implemented where the membrane array is conducted by thick plastic walls with round openings, and polyethylene film attached airtight to the rims³². The other point of the experiment is the acoustic helical emitter, which can be realized with four point sources with phase step of $\pi/2$. The applications of the demonstrated phenomenon are not limited in unidirectional excitation. The proposed ASHE can also be applied to detect the orbital angular momentum of the acoustic waves and provide a possibility to the new quantum-like effect of the acoustic chirality.

Methods

Throughout the paper, the numerical simulations of Finite Element Analysis (FEA) are performed by the commercial finite element package COMSOL Multiphysics. The mass density ($\rho_{\rm m}$), Young's modulus (E), and Poisson's ratio (ν) of the string/membrane are 1420 kg/m³, 2.5 GPa, and 0.34, respectively. The mass density and the bulk modulus of air are $\rho_{\rm air}=1.39$ kg/m³ and $K_{\rm air}=152$ KPa, respectively. The parameters are identical with the ref 27³³. The Lumped-circuit simulations (LCS) are performed by the Advanced Design System. The parameters in the LCS can be retrieved by the transmission line model demonstrated above.

Data availability. The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

References

- 1. Liu, Z. et al. Locally resonant sonic materials. Science 289, 1734-1736 (2000).
- Lemoult, F., Fink, M. & Lerosey, G. Acoustic resonators for far-field control of sound on a subwavelength scale. Phys. Rev. Lett. 107, 064301 (2011).
- 3. Cheng, Y. *et al.* Ultra-sparse metasurface for high reflection of low-frequency sound based on artificial Mie resonances. *Nat. Mater.* 14, 1013–1019 (2015).
- 4. Liang, Z. & Li, J. Extreme acoustic metamaterial by coiling up space. Phys. Rev. Lett. 108, 114301 (2012).
- Kaina, N., Lemoult, F., Fink, M. & Lerosey, G. Negative refractive index and acoustic superlens from multiple scattering in single negative metamaterials. *Nature* 525, 77–81 (2015).
- 6. Li, J., Fok, L., Yin, X., Bartal, G. & Zhang, X. Experimental demonstration of an acoustic magnifying hyperlens. *Nat. Mater.* **8**, 931 (2009)
- Cheng, Y., Yang, F., Xu, J. Y. & Liu, X. J. A multilayer structured acoustic cloak with homogeneous isotropic materials. Appl. Phys. Lett. 92, 151913 (2008).
- 8. Xia, B., Dai, H. & Yu, D. Symmetry-broken metamaterial for blocking, cloaking, and supertunneling of sound in a subwavelength scale. *Appl. Phys. Lett.* **108**, 251902 (2016).
- 9. Gu, Y., Cheng, Y., Wang, J. S. & Liu, X. J. Controlling sound transmission with density-near-zero acoustic membrane network. *J. Appl. Phys.* 118, 024505 (2015).
- 10. Li, Y., Liang, B., Gu, Z.-M., Zou, X.-Y. & Cheng, J.-C. Unidirectional acoustic transmission through a prism with near-zero refractive index. Appl. Phys. Lett. 103, 053505 (2013).
- 11. Shi, C. et al. Accessing the exceptional points of parity-time symmetric acoustics. Nat. Commun. 7, 11110 (2016).
- 12. Zhu, X., Ramezani, H., Shi, C., Zhu, J. & Zhang, X. PT-Symmetric Acoustics. *Phys. Rev. X* **4**, 031042 (2014).
- 13. Zhang, Z. et al. Topological creation of acoustic pseudospin multipoles in a flow-free symmetry-broken metamaterial lattice. Phys. Rev. Lett. 118, 084303 (2017).
- 14. Mei, J., Chen, Z. & Wu, Y. Pseudo-time-reversal symmetry and topological edge states in two-dimensional acoustic crystals. *Sci. Rep.* **6**, 32752 (2016).
- 15. He, C. et al. Acoustic topological insulator and robust one-way sound transport. Nat. Phys. 12, 1124 (2016).
- 16. Huang, H., Chen, J. & Huo, S. Simultaneous topological Bragg and locally resonant edge modes of shear horizontal guided wave in one-dimensional structure. *J. Phys. D: Appl. Phys.* **50**, 275102 (2017).
- 17. Wei, Q., Tian, Y., Zuo, S.-Y., Cheng, Y. & Liu, X.-J. Experimental demonstration of topologically protected efficient sound propagation in an acoustic waveguide network. *Phy. Rev. B* **95**, 094305 (2017).
- 18. Peng, Y-G. et al. Experimental demonstration of anomalous Floquet topological insulator for sound. Nat. Commun. 7, 13368 (2016).
- Dubois, M., Shi, C., Zhu, X., Wang, Y. & Zhang, X. Observation of acoustic Dirac-like cone and double zero refractive index. Nat. Commun. 8, 14871 (2017).
- 20. Lu, J. et al. Observation of topological valley transport of sound in sonic crystals. Nat. Phys. 13, 369-374 (2017).
- 21. Yu, S.-Y. et al. Surface phononic graphene. Nat. Mater. 15, 1243-1247 (2016).
- 22. Kapitanova, P. V. et al. Photonic spin Hall effect in hyperbolic metamaterials for polarization-controlled routing of subwavelength modes. Nat. Commun. 5, 3226 (2014).

- 23. Naify, C. J. et al. Generation of topologically diverse acoustic vortex beams using a compact metamaterial aperture. Appl. Phys. Lett. 108, 223503 (2016).
- 24. Ye, L. et al. Making sound vortices by metasurfaces. AIP Adv. 6, 085007 (2016).
- 25. Jiang, X., Li, Y., Liang, B., Cheng, J.-C. & Zhang, L. Convert acoustic resonances to orbital angular momentum. *Phys. Rev. Lett.* 117, 034301 (2016).
- 26. Morse, P. M. & Ingard, K. U. Theoretical acoustics. (Princeton university press, 1968).
- 27. Novotny, L. & Hecht, B. Principles of nano-optics. (Cambridge university press, 2012).
- Rodríguez-Fortuño, F. J. et al. Near-field interference for the unidirectional excitation of electromagnetic guided modes. Science 340, 328–330 (2013).
- 29. Chshelokova, A. V. et al. Hyperbolic transmission-line metamaterials. J. Appl. Phys. 112, 073116 (2012).
- 30. Bongard, F., Lissek, H. & Mosig, J. R. Acoustic transmission line metamaterial with negative/zero/positive refractive index. *Phy. Rev. B* **82**, 094306 (2010).
- 31. Fokin, V., Ambati, M., Sun, C. & Zhang, X. Method for retrieving effective properties of locally resonant acoustic metamaterials. *Phy. Rev. B* 76, 144302 (2007).
- 32. Park, C. M. et al. Amplification of acoustic evanescent waves using metamaterial slabs. Phys. Rev. Lett. 107, 194301 (2011).
- 33. Shen, C. et al. Broadband acoustic hyperbolic metamaterial. Phys. Rev. Lett. 115, 254301 (2015).

Acknowledgements

This work was supported by the National Basic Research Program of China (2017YFA0303702), NSFC (Grant Nos 11674172, 11574148, 11474162), Jiangsu Provincial NSF (BK20160018), and the Fundamental Research Funds for the Central Universities (020414380001 and 020414380053).

Author Contributions

F.J. and Y.C. performed the theoretical analysis and numerical simulations. F.J. and Y.C. conceived the idea and wrote the manuscript. All authors reviewed the manuscript.

Additional Information

Supplementary information accompanies this paper at https://doi.org/10.1038/s41598-018-29359-w.

Competing Interests: The authors declare no competing interests.

Publisher's note: Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit https://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2018