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## Au<sub>19</sub>M (M=Cr, Mn, and Fe) as magnetic copies of the golden pyramid

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**An investigation on structure, stability, and magnetic properties of singly doped Au<sub>19</sub>M (M=Cr, Mn, and Fe) clusters is carried out by means of density functional theory calculations. The studied clusters prefer forming magnetic versions of the unique tetrahedral Au<sub>20</sub>. Stable sextet Au<sub>19</sub>Cr is identified as the least reactive species and can be qualified as a magnetic superatom. Analysis on cluster electronic structures shows that the competition between localized and delocalized electronic states governs the stability and magnetic properties of Au<sub>19</sub>M clusters.**

Last decades have witnessed an increasing interest in gold nano-clusters thanks to their precious catalytic, electronic, and optical properties<sup>1–3</sup>. In this respect, geometric and electronic structures of gold clusters with different sizes and charge states have been studied intensively through both theoretical simulations<sup>4–8</sup> and experiments, for instance, infrared vibrational spectroscopy<sup>9–11</sup>, photoelectron spectroscopy<sup>12–14</sup>, photoionization spectroscopy<sup>15,16</sup>, photodissociation<sup>17–19</sup>, and ion mobility measurements<sup>20,21</sup>. The cluster form of gold containing low-coordinated edge atoms<sup>22</sup> can adopt binding geometries and lead to a strong reactivity that differs from the bulk<sup>23</sup>. Enhanced stabilities were observed when the number of gold atoms corresponds to the following “magic” values: 2, 8, 18, 20, 34, 58, and 92, where the electronic supershells of clusters are supposed to be closed<sup>24–29</sup>. A rich structural diversity compared to other coinage metals has been reported for gold clusters due to their strong relativistic effects. It has been revealed that small Au<sub>n</sub> clusters prefer planar structures till the cluster size of 8–13 atoms depending on charge states<sup>20,30–34</sup>. Larger species evolve via hollow cage structures at  $n = 14–18$ <sup>9,35–37</sup>, tube-like structure at  $n = 24–26$ <sup>38,39</sup>, fullerene type at Au<sub>32</sub><sup>40,41</sup>, and a possibly chiral structure at  $n = 34$ <sup>8</sup>. Among the wide range of studied gold nanoclusters, the discovery of the tetrahedral Au<sub>20</sub>, as an outstanding landmark in cluster science, has attracted an exceptional attention than any others<sup>9,12,42,43</sup>. It was reported that Au<sub>20</sub> possesses a perfect pyramidal structure (*T<sub>d</sub>*) with a considerably large highest occupied molecular orbital-lowest unoccupied molecular orbital (HOMO-LUMO) energy gap of 1.77 eV, suggesting its remarkably high stability and offering a potential platform for optical and catalytic nanostructured materials. The underlying physics behind its magic stability has been attributed to the formation of the 20-electron supershell closure in which each Au atom contributes one itinerant 6s electron<sup>42</sup>. Au<sub>20</sub> can also be considered as either a group of ten 2-electron superatoms in superatom-network model or a superatomic molecule Au<sub>16</sub> bonded with four vertex Au atoms<sup>44</sup>.

Interests in synthesizing novel elementary units for advanced nano-structured materials led to extensive search for stable cluster species with desired properties. A presence of impurity (i.e. alkali, coinage, and transition metal) atoms can provide a key to tune the properties of Au<sub>20</sub> clusters with minor effects on its magic stability. In this regard, the structures, binding energies, ionization potentials, electron affinities, and energy gaps of Au<sub>19</sub>X (X = Li, Na, K, Rb, Cs, Cu, and Ag) were systematically examined<sup>45</sup>. Au<sub>19</sub>Li, Au<sub>19</sub>Cu, Au<sub>19</sub>Ag, and Au<sub>19</sub>Pt are found to retain the pyramidal geometry of Au<sub>20</sub><sup>46–51</sup>. Increasing the Ag concentration induces the energy gap and optical transition of Au<sub>19–n</sub>Ag<sub>n</sub><sup>48,49</sup>. Au<sub>19</sub>Cu and Au<sub>19</sub>Pd clusters are potential for adsorption of trivalent arsenic<sup>50</sup>. Substitutional doping of Pt in Au<sub>20</sub> leads to significant enhancement of the cluster binding energy and reactivity while the geometry remains the same as that of Au<sub>20</sub><sup>51</sup>. The 20-electron supershell closure in Au<sub>20</sub> can be reproduced in a stable icosahedral *E*@Au<sub>12</sub><sup>q</sup> system, where *E* is a *p*-block element, through bonding-antibonding interactions between structural shells<sup>52</sup>. The adsorption energies of CO and O<sub>2</sub> on Au<sub>19</sub>H are similar to those on the

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System	Property	This work	Other calculations <sup>a</sup>	Experiments <sup>b</sup>
Au <sub>2</sub>	$R_e$	2.52	2.56	2.47
	$D_e$	2.27	2.14	2.29 ± 0.30
	$IE$	9.53	—	9.20 ± 0.21
	$AE$	2.08	1.82	1.92
AuCr	$D_e$	2.27	—	2.28 ± 0.30
	$M$	6		
AuMn	$D_e$	2.47	2.58	2.01 ± 0.22
	$M$	7	7	
AuFe	$D_e$	2.20	—	2.29 ± 0.30
Au <sub>2</sub> Cr <sup>+</sup>	$M$	6	—	6
Au <sub>2</sub> Mn	$M$	6	6	—

**Table 1.** Theoretical and experimental results of bond length  $R_e$  (Å), dissociation energy  $D_e$  (eV), ionization energy  $IE$  (eV), electron affinity  $EA$  (eV), and spin state  $M$  for Au<sub>2</sub>, AuCr, AuMn, AuFe, Au<sub>2</sub>Cr<sup>+</sup>, and Au<sub>2</sub>Mn. <sup>a</sup>Refs<sup>57–59</sup>. <sup>b</sup>Refs<sup>60–62</sup>.

Au<sub>20</sub> cluster<sup>53</sup>. More recently, selective doping with Hf and Ge atoms has been applied to modify the catalytic activity of Au<sub>20</sub> through transforming the cluster structure<sup>54</sup>.

Although there have been some progress on the structural features and catalytic behavior of doped 20-atom gold clusters, the role of impurities in tailoring the magnetic properties of Au<sub>20</sub> has been far less understood. Considering the fact that Cr, Mn, and Fe are interesting magnetic elements due to their unpaired  $4s^13d^5$ ,  $4s^23d^5$ , and  $4s^23d^6$  valence electrons, respectively, the interaction between these impurities and host electrons is expected to trigger essential changes in the magnetism of 20-atom gold clusters. In this study, we report results on searching for lowest-lying structures of gold clusters doped with a transition metal impurity Au<sub>19</sub>M (M=Cr, Mn, and Fe) and discussing the origin of their magnetic and stability properties. The finding results unravel the possibility of producing new magnetic superatoms in the golden pyramid's family.

### Computational setup

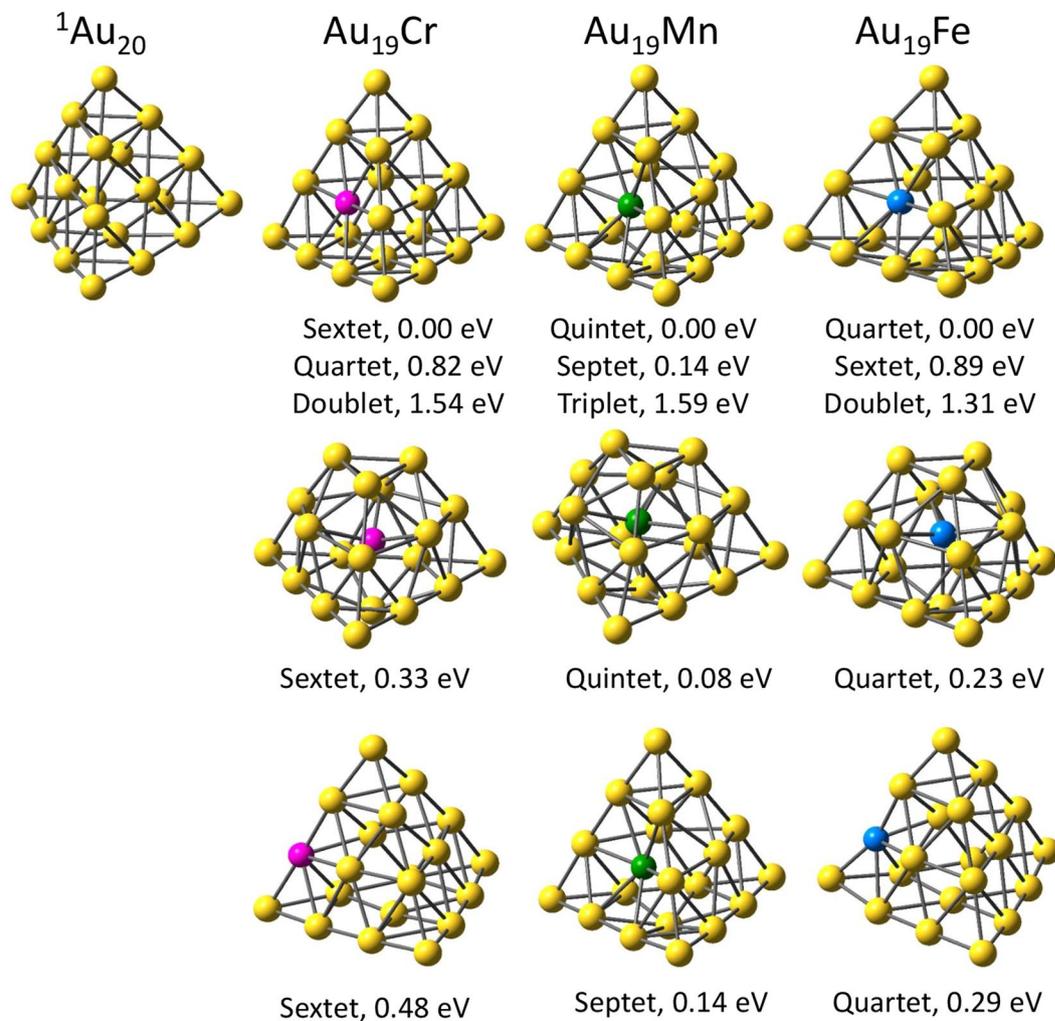
The structural optimization of Au<sub>19</sub>M clusters have been carried out by density functional theory (DFT) calculations implemented in the Gaussian 09 software<sup>55,56</sup>. We used the BP86 functional in conjunction with basis sets cc-pvDZ-pp for Au and cc-pvDZ for Cr, Mn, and Fe. Possible structures of Au<sub>19</sub>M clusters were generated using a stochastic algorithm<sup>57</sup>. In addition, the local minima of previously-reported doped Au<sub>n</sub> clusters also served as reference input. All guessing structures were initially optimized using the BP86 functional in jointing with cc-pvDZ-pp for Au atoms and cc-pvDZ for Cr, Mn and Fe dopants. Isomers having relative energies within 2.0 eV were selected for recalculating single point energies at the same functional but combining with larger basis set, cc-pvTZ-pp for Au and cc-pvTZ for Cr, Mn, and Fe. In the following, we discuss the structural, stability, and magnetic aspects of the doped Au<sub>19</sub>M clusters.

The selection of the BP86/cc-pvDZ-pp and cc-pvDZ functional resulted from test calculations for Au<sub>2</sub>, AuCr, AuMn, AuFe, Au<sub>2</sub>Cr<sup>+</sup>, and Au<sub>2</sub>Mn. The calculated results are presented in Table 1, along with available computational and experimental data for comparison. It can be seen that the used level provide reliable results for all of the examined properties. For example, the calculated spin states of all dimers and molecules are in excellent agreement with the other theoretical and experimental values<sup>58–63</sup>. The computed  $D_e$  of Au<sub>2</sub>, AuCr, and AuFe are 2.27, 2.27, and 2.20 eV, which are well consistent with the experimental ones,  $2.29 \pm 0.30$ ,  $2.28 \pm 0.30$ , and  $2.29 \pm 0.30$  eV, respectively. Although the predicted  $D_e$  of AuMn obtained in this work likely overestimates the experimental one, it is apparently in closer agreement with experiment than that of other calculations. It is worth to mention that the BP86 functional has been proved to yield the most reliable results for yttrium and vanadium doped gold species<sup>64–66</sup>. Therefore we are confident that the used computational approach is suitable to describe the structures and properties of Au<sub>19</sub>M clusters.

### Results and Discussions

The geometries of low-lying Au<sub>19</sub>M isomers with M=Au, Cr, Mn, and Fe are shown in Fig. 1. Although a large number of different structures and spin configurations are considered for each cluster, only the lowest-energy isomers are discussed. As expected, singlet Au<sub>20</sub> is found to be very stable in form of a tetrahedral with a calculated HOMO-LUMO energy gap of 1.80 eV, in an excellent agreement with the measured value (1.77 eV)<sup>12</sup>. It is noteworthy that the ground-state geometry of all investigated clusters favor a slightly distorted tetrahedral form caused by the displacement of the impurity, where the dopant substitutes for a gold atom on the surface center. The second lower-lying isomers of Au<sub>19</sub>Cr, Au<sub>19</sub>Mn, and Au<sub>19</sub>Fe have the same motif of an endohedrally-doped truncated pyramid, lying at 0.33, 0.08, and 0.23 eV above their corresponding ground states, respectively. A tetrahedron with a substituted dopant atom on the edge serves as the next isomers of Au<sub>19</sub>Cr and Au<sub>19</sub>Fe with relative energies of 0.48 and 0.29 eV, respectively. On the other side, that of Au<sub>19</sub>Mn is a spin isomer (septet) of the corresponding ground state, locating at 0.14 eV higher in energy.

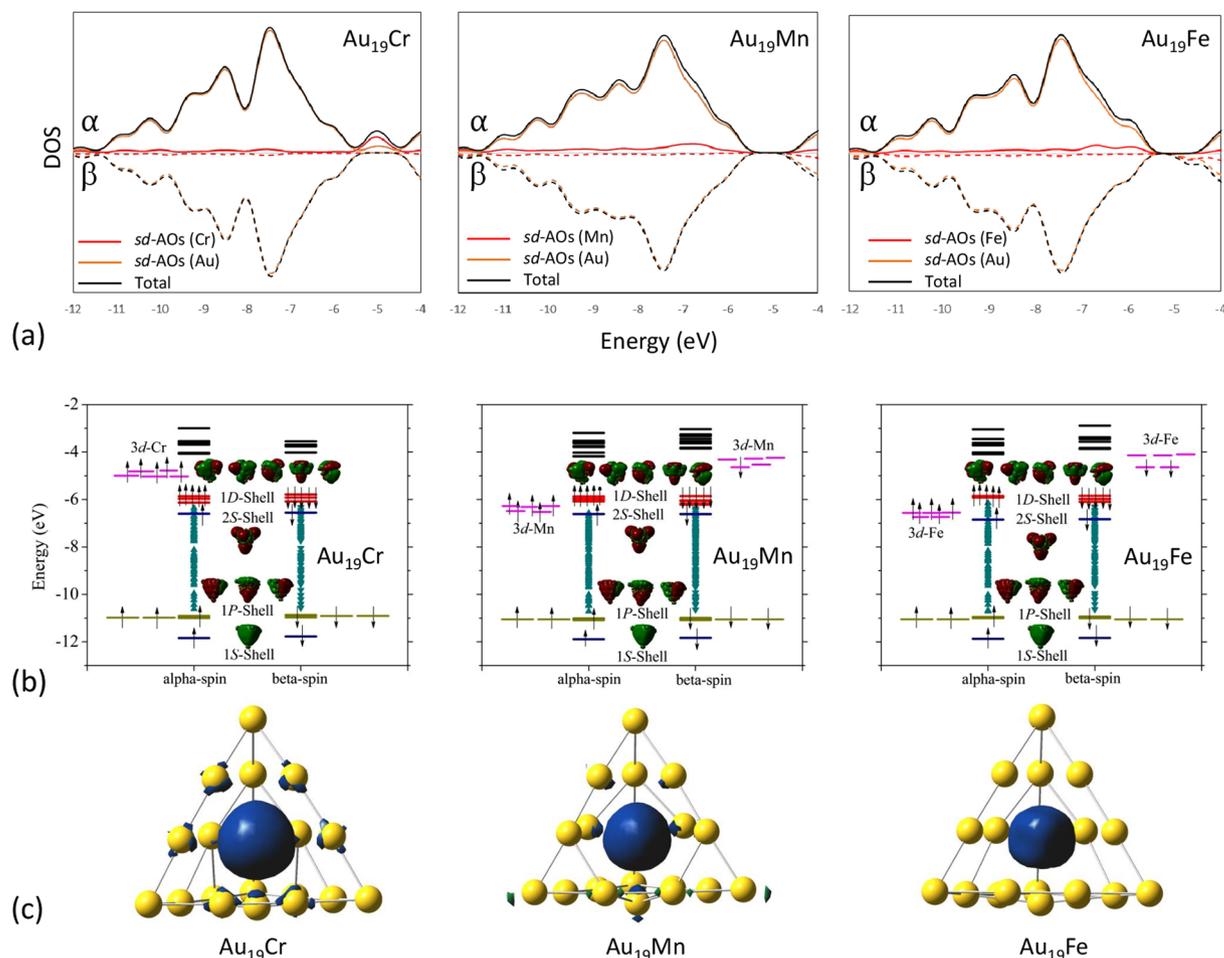
The most interesting feature of Au<sub>19</sub>M clusters is their magnetic behavior. Unlike the non-magnetic Au<sub>20</sub>, the ground state spin multiplicities of Au<sub>19</sub>Cr, Au<sub>19</sub>Mn, and Au<sub>19</sub>Fe clusters are sextet, quintet, and quartet, corresponding to total magnetic moments of 5, 4, and  $3 \mu_B$ , respectively. The decreasing trend of the total magnetic



**Figure 1.** Optimized shapes and lowest-lying spin multiplicities of  $\text{Au}_{19}\text{M}$  ( $M=\text{Cr}$ ,  $\text{Mn}$ , and  $\text{Fe}$ ) clusters with relative energies. The yellow, purple, green, and blue spheres represent Au, Cr, Mn, and Fe atoms, respectively.

moments with the increasing number of dopant's valence electrons is noticeable. Other low-lying spin isomers are examined and listed in Fig. 1. It is found that the ground states of Cr and Fe doped  $\text{Au}_{19}$  clusters have relatively robust spin configurations. In particular, the next spin excitations of  $\text{Au}_{19}\text{Cr}$  are quartet and doublet at 0.82 and 1.54 eV, respectively. For  $\text{Au}_{19}\text{Fe}$ , at least 0.89 eV is needed to excite it from quartet to sextet states and 1.31 eV is required for the quartet-to-doublet transition. The spin stability of  $\text{Au}_{19}\text{Cr}$  and  $\text{Au}_{19}\text{Fe}$  is again reflected by the fact that their second and third lowest-energy isomers also favor the same spin states as the ground state ones. Whereas, the spin ground state of  $\text{Au}_{19}\text{Mn}$  is less stable since an energy amount of 0.14 eV is sufficient to trigger a spin excitation.

To gain insight into the magnetic behavior of  $\text{Au}_{19}\text{M}$  clusters, the total/partial density of states (DOS), the molecular orbitals (MO) diagram, and the spin distribution of  $\text{Au}_{19}\text{M}$  clusters are calculated and plotted in Fig. 2. Typically, when a metallic cluster is doped with a magnetic atom, the outermost orbitals of the magnetic impurity can hybridize with delocalized orbitals of the host to form supershells. Cr, Mn, and Fe atoms have electronic configurations of  $[\text{Ar}]4s^13d^5$ ,  $[\text{Ar}]4s^23d^5$ , and  $[\text{Ar}]4s^23d^6$  corresponding to 6, 7, and 8 valence electrons, respectively. Assuming the each gold atom delocalizes one 6s electron, adding a Cr atom to the cluster of nineteenth gold atoms can create a pool of 25 itinerant electrons. Ordinarily, this forms an open shell of  $2P^5$  and does not lead to the observed spin state. However, there is another possibility in which valence orbitals of the Cr atom and delocalized MOs of the host hybridize and form a localized and a delocalized MO sets<sup>67</sup>. Once the delocalized MO set occupies states of itinerant electrons, the localized MO set has enough exchange splitting to cause a magnetic moment. With this picture in mind, the first 20 delocalized electrons of a  $\text{Au}_{19}\text{Cr}$  cluster might be used to fill the molecular shell of  $1S^21P^62S^21D^{10}$ , which leads to the stable species. Its five remaining localized electrons are taken to partially fill the  $d$ -Cr atomic shell, which results in a total magnetic moment of  $5\mu_B$ . Similar argument can be applied for  $\text{Au}_{19}\text{Mn}$  and  $\text{Au}_{19}\text{Fe}$ , in which their delocalized electrons fulfill a shell configuration of  $1S^21P^62S^21D^{10}$  and magnetic moments oscillates between 4 and  $3\mu_B$ , depending on the number of valence electrons in dopant atoms.



**Figure 2.** (a) Partial and total density of electronic states (DOS) and (b) one-electron-energy-level molecular diagrams (MO) of Au<sub>19</sub>M clusters. The black lines represent energy levels of the lowest unoccupied molecular orbitals (LUMO). The red, blue, dark yellow, and navy lines depict orbitals corresponding to the 1D, 2S, 1P, and 1S supershells, respectively. The magenta lines describe the localized 3d-M orbitals. The light blue triangles correspond to filled *d*-orbitals of Au atoms, which do not contribute to the supershell. Each upward (or downward) arrow represents one alpha-spin (or beta-spin) electron. (c) Total spin distribution of Au<sub>19</sub>M clusters plotted at a density of 0.004. The navy basins are for alpha-spin while the green ones are for beta-spin.

The results presented in Fig. 2 confirm the latter picture. The total/partial DOS [Fig. 2(a)] in combination with the MO diagram [Fig. 2(b)] indicate that the *s* orbitals from Au atoms play an essential role to the cluster shell orbitals while the half-filled *sd* orbitals of transition metal dopants become a key factor for the magnetic moment of studied species. In particular, the hybridized *sd*-M and *s*-Au electrons in Au<sub>19</sub>M clusters form both localized and delocalized electronic states. Similar to Au<sub>20</sub>, the delocalized states can be expressed in the full occupied electron shell sequence of 1S<sup>2</sup>1P<sup>6</sup>2S<sup>2</sup>1D<sup>10</sup>. Two low-energy DOS peaks at −11.9 and −11.0 eV response for the molecular shell orbitals 1S and 1P (navy and dark yellow levels), respectively. The molecular shell orbitals 2S and 1D (blue and red levels) that overlap with atomic orbitals *d* of Au atoms (light blue levels) are observed at −6.5 and 6.0 eV, respectively. Meanwhile, the localized states (magenta levels) are used to fill the atomic five *d* orbitals from the dopant atom with five, six, and seven electrons from Au<sub>19</sub>Cr, Au<sub>19</sub>Mn, and Au<sub>19</sub>Fe clusters, respectively. Since the delocalized states account for the 20-electron supershell closure, the unpaired electrons in the localized *d* orbitals cause the magnetic moments of clusters. It can be approximately considered that the chromium atom provides one electron to the cluster supershells and five others to the majority spin channel of *d* atomic subshell orbitals. Similarly, the manganese (iron) atom donates one electron to the cluster supershell orbitals, five electrons to the majority spin channel, and one (two) other(s) to the minority spin channel, respectively. According to the energy levels in MO diagrams, the electronic configurations of Au<sub>19</sub>Cr, Au<sub>19</sub>Mn, and Au<sub>19</sub>Fe clusters can be written as 1S<sup>2</sup>1P<sup>6</sup>2S<sup>2</sup>3d<sub>↑</sub><sup>5</sup>1D<sup>10</sup>, 1S<sup>2</sup>1P<sup>6</sup>2S<sup>2</sup>3d<sub>↑</sub><sup>5</sup>1D<sup>10</sup>3d<sub>↑</sub><sup>1</sup>, and 1S<sup>2</sup>1P<sup>6</sup>2S<sup>2</sup>3d<sub>↑</sub><sup>5</sup>1D<sup>10</sup>3d<sub>↑</sub><sup>2</sup>, respectively. This picture can be further examined by mapping the spin distribution of studied Au<sub>19</sub>M clusters. As shown in Fig. 2(c), the total spin of the clusters is largely localized at the dopant atom, provided by the 3d state electrons as described in their aforementioned electronic configurations. A small amount of ferrimagnetic spin alignment adding to the total magnetic moments is found in Au atoms. Calculated local magnetic moments of Au<sub>19</sub>M clusters (not shown here)

Clusters	$\epsilon_{\text{HOMO}}^{\text{alpha}}$	$\epsilon_{\text{LUMO}}^{\text{alpha}}$	$\epsilon_{\text{HOMO}}^{\text{beta}}$	$\epsilon_{\text{LUMO}}^{\text{beta}}$	$\delta_1$	$\delta_2$
Au <sub>19</sub> Cr	-4.83	-4.06	-5.79	-4.05	0.78	1.73
Au <sub>19</sub> Mn	-5.86	-4.18	-4.44	-4.31	1.55	0.26
Au <sub>19</sub> Fe	-5.84	-4.08	-4.66	-4.10	1.74	0.58

**Table 2.** Calculated HOMO and LUMO energies (in eV) of the majority and minority spin channels and the values (in eV) of  $\delta_1$  and  $\delta_2$  for Au<sub>19</sub>M (M=Cr, Mn, and Fe).

supports our argument that the total magnetic moments in Au<sub>19</sub>M clusters essentially result from the localized 3d-M orbitals.

Inheriting the major 20-electron supershell closing  $1S^21P^62S^21D^{10}$  and highly symmetric geometry from the tetrahedral Au<sub>20</sub>, Au<sub>19</sub>Cr, Au<sub>19</sub>Mn, and Au<sub>19</sub>Fe are potentially stable species. Their dopant-dependent stability can be reflected through the comparison between corresponding binding energies per atom  $E_b$  with that of Au<sub>20</sub>. The calculated average binding energy of Au<sub>20</sub> is found as 2.25 eV, which is in good agreement with the previously reported values<sup>58</sup>. Whereas,  $E_b$  of alloy species are slightly higher, that are 2.29, 2.30, and 2.31 eV for Au<sub>19</sub>Cr, Au<sub>19</sub>Mn, and Au<sub>19</sub>Fe clusters, respectively. Since the Au<sub>19</sub>M and Au<sub>20</sub> systems have nearly identical geometries and similar  $E_b$  values, it could be suggested that the incorporation of transition metal dopants tends to stabilize the gold host and the stability of Au<sub>19</sub>M system can be relatively comparable to that of the robust Au<sub>20</sub>. We further examine the bonding nature between the dopant and Au host by analyzing the electron localizability indicator (ELI-D)<sup>68</sup>. The ELI-D isosurface of Au<sub>19</sub>M clusters produced at the bifurcation value of 1.0 are presented in Fig. S1 in the Supplementary Information file (Supplementary Information: The electron localizability of ground-state Au<sub>19</sub>M clusters). No localization domain is observed in the region between the dopant and Au<sub>19</sub> host, implying that the dopant likely connects with Au moiety via ionic and/or highly polarized covalent bonds. A similar picture was also reported for Re@Au<sub>11</sub>Pt and Ta@Au<sub>11</sub>Hg superatomic systems, in which the energy decomposition analysis (ETS-NOCV) is used to emphasize the importance of electrostatic and covalent interaction between metal dopant and host in stabilizing clusters<sup>69</sup>. To measure the chemical stability of the clusters, we examine the energy gaps between the LUMO of the minority (beta) spin and the HOMO of the majority (alpha) spin [ $\delta_1 = -(\epsilon_{\text{HOMO}}^{\text{alpha}} - \epsilon_{\text{LUMO}}^{\text{beta}})$ ] and between the LUMO of the majority (alpha) spin and the HOMO of the minority (beta) spin [ $\delta_2 = -(\epsilon_{\text{HOMO}}^{\text{beta}} - \epsilon_{\text{LUMO}}^{\text{alpha}})$ ]. These values suggest the required amount of energy for an electron to jump from the HOMO of majority (minority) spin channel to the LUMO of minority (majority) one. The larger gap means the less reactive and more stable clusters<sup>70–72</sup>. Table 2 lists the HOMO and LUMO energies for the majority and minority spin channels and the values of  $\delta_1$  and  $\delta_2$  calculated for the ground states. Both energy gaps  $\delta_1$  and  $\delta_2$  take positive values, again confirming the inertness of all studied clusters. Notably, Au<sub>19</sub>Cr has the largest gaps of  $\delta_1$  and  $\delta_2$ , which means that it is the most stable and least reactive species compared to the others and can be assigned as a magnetic superatom. Among clusters with higher doping concentration, Au<sub>16</sub>M<sub>4</sub> would be a promising system due to its potential as a giant magnetic and highly symmetric superatom. Although the dopant atom apparently prefers substituting one Au atom in the surface center of singly doped species, the situation for Au<sub>16</sub>M<sub>4</sub> clusters could be more puzzling. It is worth to mention that the unique stability of the golden pyramid Au<sub>20</sub> can be understood in term of a superatomic molecule Au<sub>16</sub>Au<sub>4</sub>, where its superatomic core Au<sub>16</sub> binds with four vertex Au atoms<sup>42</sup>. This approach has been supported by the recent findings of the golden pyramid's smaller sisters, the tetrahedral Au<sub>17</sub><sup>+</sup> and Au<sub>10</sub><sup>2+</sup>. These two systems were found highly stable in form of Au<sub>13</sub> and Au<sub>6</sub> octahedral cores, respectively, and the other four gold atoms are above four their triangular faces<sup>37,73,74</sup>. In this scenario, Au<sub>16</sub>M<sub>4</sub> and its smaller magnetic counterparts, Au<sub>13</sub>M<sub>4</sub><sup>+</sup> and Au<sub>6</sub>M<sub>4</sub><sup>2+</sup>, might be considered as a core in -4 charge state and four vertex M atoms. A careful examination of this interesting issue is perhaps warranted for future research.

## Conclusions

In summary, we have investigated structure, stability, and magnetic properties of singly doped Au<sub>19</sub>M (M=Cr, Mn, and Fe) clusters using DFT calculations. The most interesting point of our results is that all studied Au<sub>19</sub>M clusters favorably form magnetic copies of the golden pyramid Au<sub>20</sub>. The dopant atom is found to substitute for a gold atom on the surface center. The coexistence of both delocalized and localized electronic states in these clusters allows to fill the supershell orbitals and to simultaneously promote local magnetic moments, leading to stable magnetic systems. Au<sub>19</sub>Cr is the most stable species that can be assigned as a magnetic sister of the golden pyramid Au<sub>20</sub>.

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## Author Contributions

N.M.T. and N.T.T. conceived the calculations, N.M.T. and H.P.T. conducted the calculations, N.T.C. and N.T.T. analysed the results. All authors prepared and reviewed the manuscript.

## Additional Information

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