ARTICLE OPEN (R) Check for updates A fully coupled Hydraulic Mechanical Chemical approach applied to cementitious material damage due to carbonation

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Coupled Thermal-Hydraulic-Mechanical-Chemical (THMC) approaches may be important for assessing the long-term durability of cementitious materials. We present a multiphysics approach to overcome past limitations of THMC modelling and validate it based on experimental results of accelerated carbonation tests. Our numerical approach rests on a sequential coupling between Hytec and Cast3m. Hytec computes the evolution of hydraulic and mineralogical fields allowing to compute the micromechanical properties (e.g. Young's modulus). The mineral reactions generate tensile stresses and Cast3M computes the associated strain tensors and the damage evolution represented by the opening or sealing of cracks, impacting subsequent reactive transport processes. Our approach manages to qualitatively represent the crack patterns and non-uniform degradation depths observed on microtomographic images of carbonated cement samples, which can only be explained by the coupled dynamics of chemical and mechanical processes. Our approach can be extended to a wide range of cement-concrete pathologies and contexts.

npj Materials Degradation (2023)7:60; https://doi.org/10.1038/s41529-023-00378-x

INTRODUCTION

In recent years, the need for accurate and powerful computational methods has increased for many fields of earth and material science. They constitute powerful tools for decision-making and to understand complex coupled systems. For example, reactive transport modelling has emerged at the end of the 20th century mostly in the context of contaminant transport for groundwater guality¹. Now, this field has grown to tackle more and more applications², including the description of material degradation, for example in radioactive waste repositories^{3,4}. The impact of geochemical reactions within a porous medium can significantly alter its properties^{5,6}, further impacting its response to various perturbations. However, the mechanical response of the material which has undergone microstructural changes^{5,7,8} has almost always been neglected, as were the chemical effects for geomechanical calculations. This is primarily due to the fact that a coupled description of these phenomena significantly increases the complexity of the model formulation.

The degradation of porous reactive materials is a prime example in which mechanical and chemical evolutions are coupled and exert a feedback on each other, often through the appearance or sealing of cracks. As examples, we can cite the chemical induction of fractures within lithium batteries⁹, the durability of geomaterials in the reservoir context^{10,11}, or concrete^{8,12,13}, melting of nuclear pellets¹⁴ or the corrosion and hydrogen transport in steel¹⁵. On a larger scale, we can cite the durability of injection wells for gas reservoirs¹⁶ or concrete dams^{17,18}, the induced seismicity associated with various applications^{19–22}.

In past attempts to model thermo-hydraulic-mechanicalchemical (THMC) effects, several key issues have rarely been addressed. In particular, the dynamic two-way coupling between chemistry and mechanics is generally not described. For example, mineralogical evolutions obtained from reactive transport (RT) simulations were used to evaluate the potential evolution of strains and stresses. This allowed some authors to evaluate whether or not a mechanical failure could occur^{23–26}. The appearance, propagation of cracks and its impact on the subsequent reactive transport processes have rarely been included in such coupled approaches^{10,12,27–30}. Also, RT simulations often neglect one or several processes which may have a significant effect on the mechanical response, such as the porosity evolution or the water balance (consumption, evaporation)^{13,31–33}.

In this research paper, we propose a generic fully dynamicallycoupled THMC approach to predict the appearance and propagation of cracks in deformable porous materials. This approach is suited to describe the generic reactive transport processes (i.e. mineral dissolution and precipitation, drying, porosity evolution, gas transport, heat transfer) and the mechanical damage they exert (i.e. shrinkage, swelling, cracking) under various thermo-hydro-chemomechanical loadings. This approach is based on the numerical coupling of Hytec, a reactive transport simulator³⁴ and Cast3m, a mechanical Finite Element (FE) code³⁵ as depicted in Fig. 1.

We focus our developments on the specific case of the accelerated atmospheric carbonation of cementitious materials, which is a ubiquitous process responsible for important CO2 uptake³⁶. Both Hytec³⁷ and Cast3m have been used^{38,39} to describe this cement pathology. When a cementitious material is in contact with the atmosphere, $CO_2(q)$ diffuses through the pores, dissolves in the pore-water and reacts with dissolved calcium to precipitate CaCO₃. This reaction is known as carbonation and has been extensively studied for decades as it leads to a significant changes in mineralogy (coupled decalcification and precipitation of CaCO₃)^{40,41}, microstructure and transport properties^{42–47}. The densification linked to the fixation of exogenous CO₂ leads to an increase in the mechanical properties of the material (elastic modulus, strength)⁴⁸⁻⁵² but makes it more brittle⁵³⁻⁵⁵. In practice, carbonation is one of the most detrimental degradation phenomenon for concrete durability as it induces uniform corrosion of the reinforcing steel bars⁵⁶⁻⁵⁸. This degradation involves the coupling of several processes: gaseous migration and dissolution; mineral dissolution and precipitation as well as porosity evolution⁵⁹; release, evaporation and transport of water⁶⁰;

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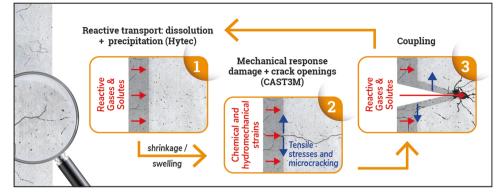


Fig. 1 Schematic representation of the THMC model. Schematic representation of the developed Thermal-Hydraulic-Mechanical-Chemical approach based on a sequential coupling between Hytec and Cast3m softwares.

solid phase shrinkage^{61–63} and tensile stresses leading to the appearance of cracks^{64–66}. Seigneur et al.⁶⁰ have shown that reactive transport modelling alone was not able to reproduce the observed degradation depths and the reaction fronts as soon as a crack pattern was observable. The development of microcracks is attributed to shrinkage induced by both carbonation reactions and drying processes. These mechanisms have not yet been addressed with a fully coupled THMC formulation including either the appearance and propagation of cracks or their effects on transport properties. Therefore, we use our approach to overcome the previous limitations and tackle the THMC problem of unsaturated carbonation in cementitious materials.

The goal of this application is to study whether or not our approach is suited to the description of such THMC processes. A thorough quantitative validation of simulation results would require accurate 3D data acquisition (e.g. crack distribution) which are intrinscally challenging to extract from microtomographic images. Furthermore, the main objective of our approach is its upscaling and generalization: it is not meant to perform a porescale thorough description of these processes. We mostly focus on describing the macroscopic behaviour of engineering materials with an emphasis on degradation depths and patterns as well as the crack distribution within the studied sample and it consequences on the chemical degradation.

RESULTS

Sample characterization and core degradation

In this study, we focus on a cylindrical cement paste sample (radius R = 15 mm, height H = 110 mm) obtained by the hydration of C₃S described in Kangni-Foli et al.⁶⁶. The mineralogy of this hydrated C₃S paste only consists in Portlandite (calcium hydroxyde) and an amorphous calcium-silicate-hydrate (C-S-H) phase. C-S-H corresponds to the binding phase⁶⁷ of cementitious materials. It is structurally built as a layered structure with polymerized silicate chains whose nanostructure is comparable to tobermorites⁶⁸⁻⁷⁰. Following the calcium over silica atomic ratio (Ca/Si), different degree of polymerization of silicate chains are observed⁷¹⁻⁷³. When subject to leaching or carbonation, the Ca/ Si ratio of the hydrates progressively decreases which leads to a microstructural modification of the C-S-H phase, associated with a reduction in molar volume and thus shrinkage^{66,74-76}. In our sample, the initial calcium over silica atomic ratio (Ca/Si) of the C-S-H is 1.6. The sample initial total porosity is 40%, determined from oven drying at 105 °C, with a 25% volume fraction of portlandite (obtained from thermogravimetric analyses). More details on the miscrostructure and experimental characterizations can be found in Kangni-Foli et al.⁶⁶.

Microtomographic images of the carbonated samples were obtained and revealed three distinct density-zones (Fig. 2a,c and

Supplementary Video): a completely carbonated zone (close to the exposed surface in light-grey on Fig. 2c and Supplementary Video); a transition zone (dark-grey) that was partially carbonated and then the non-carbonated zone (light green). It is noteworthy that the carbonation depth was not uniform and that the partially carbonated zone showed an unexpected bell-like frontier. These features were however supported using phenolphtalein (Fig. 2b) that showed similar pH distribution (note that phenolphtalein is a pH indicator that turns pink at high pH corresponding to sound material, and that is used to probe the extent of carbonation). Figure 2a and the Supplementary Video show the crack distribution within the sample induced by carbonation shrinkage. These cracks modified the carbonation front and induced the bell-like frontier as well as a locally deeper carbonation front. Noted that the 2D microtomographic image in Fig. 2a only highlight the larger crack resulting from the sample deformation, but it does not show the microcrack network which is below microtomographic resolution.

Model formulation

Reactive flow processes include the migration of water, transport of solutes and gaseous species within a porous medium while accounting for the solid-liquid-gas equilibrium. We use the fully coupled reactive transport approach of Hytec^{34,37,77}. Release and consumption of water by chemical reactions are included and coupled with the unsaturated flow, as well as water evaporation, controlled by the sorption isotherm⁴³, described by the Van Genuchten empirical relation⁷⁸. To represent the appearance and local effect of cracks, a double porosity approach has been used⁷⁹⁻⁸². It represents that each gridcell is a combination of two interconnected domains, the matrix (superscript m) with a porosity ω^m and the cracks (superscript c) with a porosity ω^{c} . Transport and reactions can occur independently within each domain but they influence each other through crossdomain fluxes. The crack properties (diffusion D^c , permeability K^c) are evaluated based on their apertures.

Hytec models the evolution of the mineralogy, allowing to evaluate both the evolution of the poro-elastic properties of the material and the carbonation shrinkage Equation (2). The poroelastic properties are computed through the use of the Mori-Tanaka scheme^{5,8,83–85}. For this, the cement system is represented as an evolving matrix phase (the C-S-H phase with its gel porosity) with several spherical inclusions representing portlandite, capillary porosity and calcite.

Then, the poromechanical model includes material deformation and damage induced by the evolution of porosity, mineralogical and pore-pressure fields. The damage model is supposed to be isotropic and the crack density is modelled through a classical damage scalar variable d^{86} , varying between 0 for sound material and 1 for totally degraded one. We assume that the material

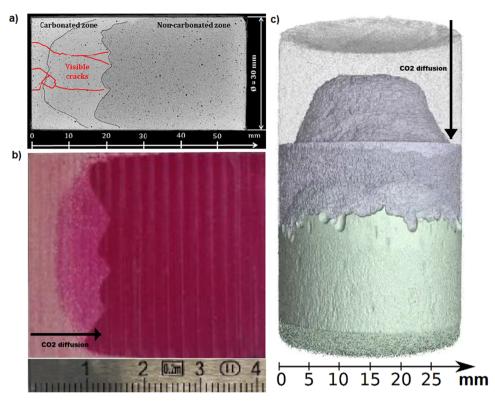


Fig. 2 Experimental observations after 326 days of accelerated carbonation of the hydrated C_3S sample. a 2D section of a microtomographic image showing a non-uniform carbonation front. Largest visible cracks are highlighted in red and are associated to local increased degradation depths. b 2D observation of a phenolphtalein test revealing the carbonation fronts (after 81 days of carbonation). The spatial scale is given in cm. c 3D microtomographic image of the sample. The green zone depicts the sound hydrated C_3S paste, the dark-grey corresponds to the transition zone, while the fully carbonated paste is represented in light grey (top part). These elements can be observed dynamically in the Supplementary Video.

behaviour can be described by the behaviour law:

$$\underline{\underline{\sigma}} = (1-d) : \mathbb{C} : \left(\underline{\underline{\varepsilon}} - \underline{\underline{\varepsilon}}^{\underline{\varepsilon}}\right) - (1-\omega^{c})b^{m}\Delta P^{m}\underline{\underline{I}}$$
(1)

where σ , \mathbb{C} , ε and I are the Cauchy stress, stiffness, total strain and identity tensors, respectively. The last term represents the macrostress induced by pore pressure where b^{m} is the Biot coefficient estimated from the elastic properties and $\Delta P^{m} = \Delta(S^{l}P^{l}) + \Delta((1 - S^{l}))$ P^{g}) represents the pore pressure variation from the initial state which plays a significant role on the degradation process^{18,87,88} and for drying shrinkage⁸⁹. S^{f} and P^{f} respectively represent the saturation and pressure in fluid phase f (liquid-gas). The impact of water production/evaporation can significantly modify these values⁹⁰, which is considered in Hytec thanks to its full description of water as a reacting species⁷⁷. The pressure exerted in the crack domain is neglected due to the fact that the cracks are mostly desaturated. ε^{ξ} models the homogenized internal free strain related to chemical reactions. Based on^{66,74}, carbonation shrinkage is assumed to evolve with the variation of the volume fraction of the equivalent C-S-H phase $\Delta \phi^{eq}_{CSH}$ during its decalcification. This volume fraction includes the different Ca/Si ratio as well as the C-S-H intrinsic gel porosity, whose initial value is estimated at 9%. This yields a C-S-H phase initial volume fraction of 44%. For more details about the computation of theses volume fractions from Hytec simulation, see "Governing equations". The homogenized carbonation shrinkage strain $\underline{\varepsilon}^{\xi}$ can then be computed using a shrinkage coefficient α^{ξ} describing the macroscopic effect of the C-S-H phase shrinkage occurring locally in the form:

$$\underline{\boldsymbol{\varepsilon}}^{\boldsymbol{\xi}} = \boldsymbol{\alpha}^{\boldsymbol{\xi}} \Delta \boldsymbol{\varphi}_{\mathsf{CSH}}^{\mathsf{eq}} \underline{\boldsymbol{I}}. \tag{2}$$

The damage estimation is based on the Fichant-Laborderie model^{91,92} (see Table 1). The crack opening displacement vector

 $[\mathbf{u}]$ is calculated from the anelastic tensor⁹¹, which has been applied and validated in several studies involving concrete^{18,93,94} (see "Governing equations"). The damage scalar variable and the normal crack aperture are used to estimate the evolving crack porosity ω^{c} and their transport properties, respectively, which are updated in the reactive transport model.

The study focuses on the simulation of the isothermal accelerated carbonation of a hydrated C_3S paste. Simulations are parametrized with the Thermodem thermodynamic database⁹⁵, and dedicated measurements on the C_3S sample including mineralogy, porosity, initial gas diffusion coefficient, Van Genuchten parameters and water content. More details about the hydrogeochemical description of our materials are given in⁶⁰.

Based on the initial microstructure and phase assemblage, the poroelastic properties estimated using the Mori-Tanaka scheme yields an initial Young Modulus of 14.47 GPa, in agreement with the measured value 15 ± 1 from Kangni-Foli et al.⁶⁶ (see "Governing equations"). The other initial poroelastic properties are given in Table 1. The progressive decalcification of the C-S-H phase is modelled using a discretized set of dissolution-precipitation reactions towards hydrates with lower Ca/Si atomic ratios⁶⁰, ranging from 1.6–1.2–0.8 and amorphous silica.

The simulation of the cylindrical sample by a chemical unilateral loading is modelled through a 2D axisymmetric simulation with a 30 mm diameter and a length of 110 mm (Fig. 3). For the RT simulation, atmospheric cells are used to model gaseous exchange (CO_2 and water vapor)⁶⁰, while the other boundaries do not allow any mass transfer. No external mechanical loading is applied on the sample, but internal stresses are induced by carbonation shrinkage and the variation of pore-pressure associated with the release of water and porosity changes.

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Variables	Symbol	Value - Law	Reference
Transport properties with	nin the crac	k domain	
Crack porosity	ω ^c	$1 - (1 - d)^{1/3}$	117
Phase a diffusion	D_a^c	$D_a^{\text{eff}} \max\left(1, \frac{u_n}{u_{\text{ref}}}\right)$	28
Reference crack	u _{ref}	100 µm	28
Aqueous diffusion	D ^{ref}	$10^{-9} \text{ m}^2 \text{ s}^{-1}$	97
Gaseous diffusion		$3 \times 10^{-4} \text{ m}^2 \text{.s}^{-1}$	
Effective diffusion	$D_g^{ m ref} \ D_a^{ m eff,c}$	$D_{\alpha}^{\rm ref}(\omega^{\rm c})^2 (S_{\rm c}^{\alpha})^2$	109
Permeability	K ^c	$\frac{u_n^2 \mu^l}{12\rho^l q}$	118
Fluid viscosity	μ ^ι	12p g 10 ⁻³ Pa.s	
Gravitational acceleration constant	g g	9.81 m.s ⁻²	
Fluid density	ρ^{l}	1000 kg.m ⁻³	
Total surface area	\mathcal{A}	100 m ² .m ⁻³	
Distance	\mathcal{D}	1 <i>µ</i> m	
Mechanical model behav	viour	- F	
Damage law	d	$1 - \frac{\epsilon_{d0}}{\epsilon_{eq}} \text{exp}\big(\textit{B}_t \big(\epsilon_{d0} - \epsilon_{eq} \big) \big)$	91
	ε _{eq}	$\sqrt{\sum_{i=1}^{3}\left\langle \mathbf{\epsilon}_{i}^{e} ight angle _{+}^{2}}$	92
Damage law parameter	Bt	$(\textit{E}\epsilon_{d0}\textit{I}_c)/(\textit{G}_f-0.5\textit{E}\epsilon_{d0}^2\textit{I}_c)$	91
Strain damage threshold	ε _{d0}	$f_{\rm t}/E~(f_{\rm t}{=}3.3$ MPa)	93,94
Fracture energy	G _f	100 J.m	91
Initial Young's Modulus	Ε	14.47 GPa	
Initial Poisson ratio	v	0.231	
Initial Biot coefficient	Ь	0.548	
Initial shrinkage coefficient	a ^ę	0.42	
Hydrogeochemical mode			
Matrix total porosity	ω^{m}	0.4 (initial)	60
Gel porosity	$arphi_{gel}$	0.09 (initial)	60
Capillary porosity	φ_{cap}	0.31 (initial)	60
Portlandite initial volume fraction	$arphi_{ m portlandite}$		60
Solid C-S-H(1.6) volume fraction	Фсѕн	Initial: 0.35 (solid)	60
C-S-H phase volume fraction	$arphi_{CSH}^{eq}$	0.44 (with gel pores)	
Initial matrix permeability	К ^т	10^{-21} m^2	60
Liquid pressure	P ^I	Richards equation	60
Liquid saturation	SI	Van Genuchten	78
Van Genuchten parameters	а	0.0007685 m ⁻¹	60
Effective diffusion (phase <i>a</i>)	n Da ^{eff,m}	1.6373 $D_{\alpha}^{\rm ref}(\omega^{\rm m})^2 (S_{\rm m}^{\alpha})^2$	60 60,109
Relative humidity	RH	55% (initial and boundary conditions)	66

Parameters for the reactive transport model (porosity, thermodynamic constants for the liquid-gas-solid equilibrium, water retention parameters, diffusion coefficients and permeability) are described in⁶⁰. The poroelastic parameters of the cement paste (Biot coefficient and bulk modulus k_{cp}), and the localisation coefficient A_{CSH} of the C-S-H phase, are estimated using the Mori-Tanaka scheme^{5,116} and the material properties described in⁸⁴. \Box properties are computed from the initial microstructure depicted in⁶⁰.

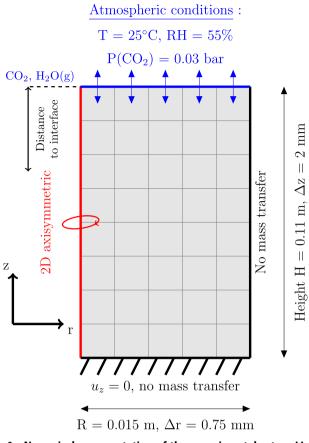


Fig. 3 Numerical representation of the experimental setup. Mesh and boundary conditions of the reactive flow and mechanical systems. We model a 2D-axisymmetric domain whose dimensions correspond to the experimental samples (R = 15 mm, Height = 110 mm). A rectangular grid was used with cell dimensions of $\Delta r = 0.75$ mm along the radius and $\Delta z = 2$ mm along the cylinder axis.

Thus, this approach constitutes a physical two-way dynamic description of the coupled THMC processes. Its numerical implementation is detailed below (Fig. 6). In addition, the use of the fully-coupled nature of Hytec, allows our approach to overcome the previous past limitations.

Simulation results

Results of our THMC simulation are presented with 2D profiles along the sample diameter. For visualization purposes, profiles focus on the first 35 mm of the sample near the atmospheric boundary.

Figure 4 shows the evolution of chemical and mineralogical maps after 40, 160 and 326 days of accelerated carbonation. As carbonation proceeds, portlandite (Fig. 4a) and C-S-H (Fig. 4b) are progressively dissolved and replaced by calcite (Fig. 4c) and amorphous silica (Fig. 4d). A more detailed analysis of the amorphous silica precipitation and C-S-H decalcification obtained with our reactive transport model is provided in our previous work⁶⁰. These reactions result in a decrease of the pore-water pH (Fig. 4f) and porosity from 0.4 to 0.3 (Fig. 4e) in accordance with experimental results, where the porosity measured in the carbonated area is around 0.28 ± 0.05^{66} . Furthermore, the solid mass density estimated in the carbonated zone (not shown) is equal to 2.06 g.cm⁻³, which is comparable to the experimental measurement of 2.11 g.cm⁻³ ⁶⁶.

The modelled carbonation depth, associated with Portlandite dissolution, is also consistent with observation. At the early stages

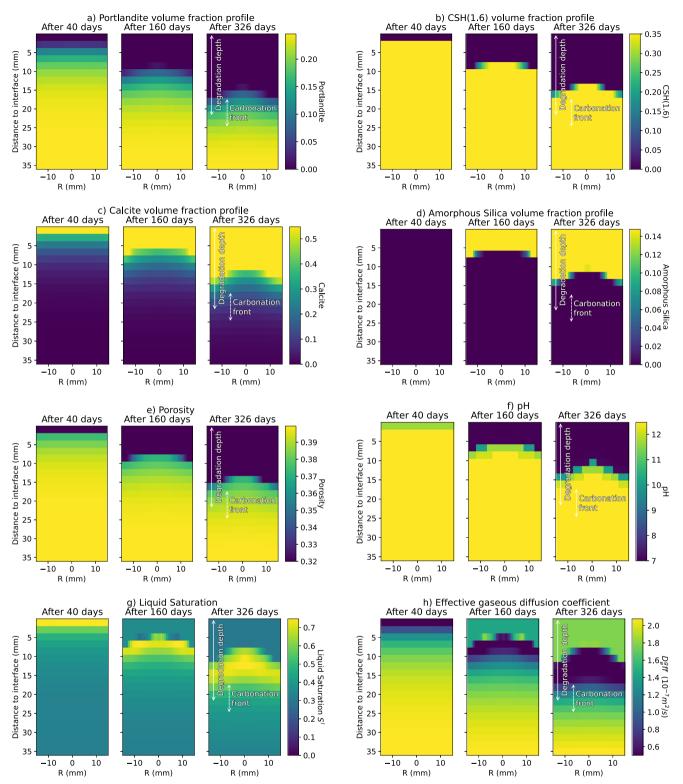


Fig. 4 Spatial maps after 40, 160 and 326 days of accelerated carbonation of the hydrated C₃S paste. Displayed maps focus on the first 35 mm close to the atmospheric carbonation, and show mineralogical, geochemical and hydraulic profiles along the sample diameter. **a** Portlandite volume fraction. **b** C-S-H volume fraction with a Ca/Si of 1.6. **c** Calcite volume fraction. **d** Amorphous silica volume fraction. **e** Matrix porosity evolution. **f** pore-water pH (initial value: 12.5). **g** Liquid saturation. **h** Effective gaseous diffusion coefficient.

of carbonation (40 days), most mineralogical fronts are uniform, in accordance with results obtained without accounting for the mechanical response of the material⁶⁰. However, a crucial improvement of our THMC approach is that it captures the non-uniform development of the carbonation front with a deeper

carbonation near the sample edges. The pH map as well as the other reaction fronts can be compared to the phenolphtalein test shown in Fig. 2b. Furthermore, the model simulated correctly the three area described in the Fig. 2c and supplementary video, comprising a completely carbonated zone (only calcite and

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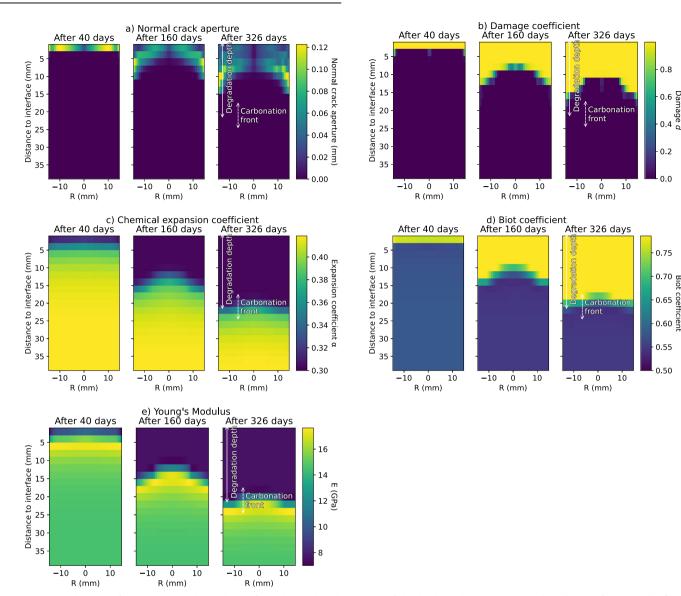


Fig. 5 Spatial maps after 40, 160 and 326 days of accelerated carbonation of the hydrated C₃S paste. Displayed maps focus on the first 35 mm close to the atmospheric carbonation, and show profiles of mechanical properties along the sample diameter. **a** Normal fracture aperture. **b** Damage coefficient. **c** Chemical expansion coefficient a^{ξ} . **d** Biot coefficient. **e** Young's Modulus.

amorphous silica), a transition zone (partly dissolved portlandite, calcite and C-S-H 1.6) and then the non-carbonated zone (initial mineralogy).

In addition to porosity reduction, mineral reactions exert several feedbacks on the carbonation progress which are highlighted in Fig. 4. First of all, the important release of water associated with the dissolution of C-S-H and portlandite induces a significant saturation front (Fig. 4g) yielding an increase in fluid pressure, relative permeability and a decrease in gas transport (Fig. 4h). These effects act together against an in-depth carbonation and should therefore homogenize the carbonation front along the sample diameter as radial diffusion may be favoured over axial migration. However, as carbonation proceeds, the extent of the carbonation front increases, predominantly along the edges, due to localized mechanical damage, as shown in Fig. 5.

As sound C-S-H (with a Ca/Si ratio of 1.6) evolves towards amorphous silica, significant shrinkage occurs (Fig. 5c) in parallel to an important release of water, inducing tensile stresses and increasing pore-pressure within the material (Equation (1)). These local strain induces the sample deformation that mainly occur at the edges of the sample, resulting in localized damage (Fig. 5b) and larger microcracks along the edges (Fig. 5a). These constitute preferential diffusive pathways for CO₂ within the material, accelerating the degradation predominantly near the edges of the sample. This leads to a non-uniform carbonation front and carbonation shrinkage. It must be acknowledged that the carbonation fronts are relatively smooth compared to what is usually expected. This is due to the fact that we allowed the simulation to use a rather high timestep. This results in a deeper CO₂ ingress, slightly diluting the portlandite dissolution front. However, carbonation shrinkage is function of the equivalent C-S-H volume fraction (2), and is maximum at the transition towards amorphous silica, whose front remains sharp (Fig. 4d). Thus, the impact of this timestep on the relevant coupled chemomechanical processes is minimal. Furthermore, it is important to note that cracking, which is the main mechanical impact on the reactive transport, is mesh independent due to our use of Hillerborg regularization techniques (see "Governing equations").

These results highlight the ability of the model to tackle chemomechanical coupling effect²⁸, where damage increases the material diffusivity and permeability and induces preferential diffusion paths, triggering in turn a localization and an acceleration of the chemical degradation as reported in⁹⁶ and⁹⁷.

Another important aspect of our approach is that it allows to estimate the evolution of the mechanical properties (Young's modulus, Biot coefficient and α^{ξ}) of the cement paste sample, whose evolutions are also displayed in Fig. 5c-e. The Young's modulus increases in the carbonation front zone due to a progressive replacement of portlandite by calcite, which results in a porosity decrease while leaving the C-S-H phase intact. Then, upon carbonation, as portlandite locally disappears, the C-S-H is in turn subject to decalcification which decreases its stiffness, as expressed by Equation (11). The Young's modulus admits its maximum value near the carbonation front, with the presence of both portlandite and calcite. Interestingly, the porosity does not exhibit its minimum value in the corresponding zone (see Fig. 4). In that way, there is not a direct link between the stiffness and the porosity of the cement paste. The heterogeneity of the carbonation front induces a heterogeneity of the material properties that impacts the global mechanical response. Then, the damage variation is influenced by the local chemical strain and macroscopic sample deformation, as described in^{8,13}. Finally, due to the complex mechanical behaviour and the method used to estimate the crack opening, no direct and simple relationship between the normal crack opening and the damage fields can be identified. This highlights the necessity to estimate the crack opening to model the crack transport properties⁹⁷.

DISCUSSION

The good qualitative representation of the carbonation fronts, the generated crack patterns and the correct evolution of various properties (porosity, density) is a validation of our approach to the THMC processes involved in the carbonation of a hydrated C₃S paste. While not immediately transposable, our process-based approach has the potential to accurately represent the carbonation and/or other pathologies to various cement formulations, e.g. high-Al content with C-A-S-H phases⁹⁸. Such verification constitutes the important following step of our study. Then, the following developments in the context of cementitious material durability will focus on studying various chemo-mechanical loadings and boundary conditions as well as including coupled transient thermal and hydraulic gradients. For example, chemical degradation of concrete from sensitive civil engineering facilities (e.g. nuclear reactor containment building, dam) can be tackled by including the transient drying mechanisms, which may themselves trigger delayed strain induced by chemical reactions. In the case of carbonation, the competing effect of chemical strains and drying will be more deeply analyzed to better capture the respective importance of these phenomena on microcracking development. Our approach could be extended to account for swelling reactions, which constitute another chemo-mechanical pathology of concrete of major relevance for the industry⁹⁹. Further, the complex coupled THMC nature of hydration processes, which have an essential impact on the durability of concrete structures, could also be described by this approach. Note that the aforementioned chemical degradations necessitate in general the development of specific chemical strain models, depending in particular on the overall mineralogy evolution.

Further, a more representative mechanical behaviour of the material will be obtained by accounting for long-term creep phenomena. This would be of particular importance when our method will be used for more complex materials. For example, in concrete, viscous phenomena induce a redistribution of stresses and strains at the mesoscale (e.g. between aggregates and cement paste) with important structural consequences. Thus, a mesoscale concrete description should explicitly model aggregates and interfaces and include the creep phenomea^{30,97,100}.

Last, the description of microcracking and fracturing remains a challenging topic especially in coupled physical phenomena not necessarily occurring at the same characteristic scale. In this regard, alternative approaches could be tested to better reproduce some key features of crack modelling; for instance, an orthotropic description of discrete crack planes is likely to improve the whole model results, compared to the current more diffuse representation related to the damage continuous approach and the isotropic diffusion and permeability tensor.

Our approach allows to dynamically model processes whose coupled description has been a challenge for decades. Considering its physical and phenomenological roots, this approach can be generalized and extended. It opens perspectives for THMC modelling in various contexts, including corrosion and cracking induced by the precipitation of expanding phases (sulfate attack or alkali-silica reactions). Given the multiphase capacities of the reactive transport simulator, it can be used in the context of gas repositories to predict the durability of injection wells. Also, it can be of particular interest for hydrogen reactivity, either in the context of hydrogen storage¹⁰¹ or during the transient hydraulic phase of nuclear waste repositories^{102,103}. On a larger scale, coupled chemo-mechanical reactions are linked to induced seismicity¹⁰⁴ which could constitute another exciting perspective of this work.

METHODS

Experimental conditions

Post-hydration and prior to carbonation, C_3S samples were equilibrated in a climatic chamber with 25°C and 55% relative humidity (RH) to maximize the effect of carbonation^{105,106}. Accelerated carbonation was then triggered by setting a CO_2 partial pressure of 0.03 bar, which was found to be representative of natural carbonation⁷⁶. The lateral and bottom surfaces of the samples were covered with adhesive aluminium foils to obtain a one-dimensional degradation along the axis. Several carbonated samples were collected after 30, 80 and 326 days to characterize the carbonation depth and the crack patterns.

X-ray computed microtomography (XCT) was used to observe the microstructural changes induced by carbonation. XCT is a nondestructive technique that is sensitive to differences in density (linked in our case to CO₂ incorporation). The scans were carried out using a General Electric (GE) V|tome|x M device (see⁶⁶ for details about the operating conditions). The image reconstruction was done using GE proprietary software resulting in volumes that were post-processed using VG Studio Max (Volume Graphics) with a voxel size of 29.7 μ m.

Governing equations

Parameter definition and values are listed in Table 1.

Reactive transport. Richards equation is solved to compute water migration through the porous medium:

$$\frac{\partial \omega^{\nu} S_{\nu}^{l}}{\partial t} = \operatorname{div}\left(\frac{k_{rl}(S_{\nu}^{l})K^{\nu}}{\mu^{l}} \left(\nabla P_{\nu}^{l}(S^{l}) + \rho \mathbf{g}\right)\right) + Q^{\nu} + J_{dual}^{\nu} \text{ with } \nu = \{\mathsf{c},\mathsf{m}\}.$$
(3)

where μ^{l} is the liquid viscosity and P_{v}^{l} is the liquid pressure within continuum *v*. The unsaturated properties of the porous medium (relative permeability $k_{rl}(S^{l})$, sorption isotherm $P^{l}(S^{l})$) are described using Van Genuchten relations⁷⁸. Q^{v} is the chemical source term of water in domain *v* and J_{dual}^{v} is the water flux towards domain *v*:

$$J_{\text{dual}}^{\text{m}} = -\mathcal{A} \frac{k_{\text{rl}}^{\text{c,m}} K^{\text{c,m}}}{\mu^{\text{l}}} \frac{P_{\text{m}}^{\text{l}} - P_{\text{c}}^{\text{l}}}{\mathcal{D}}$$
(4)

where A represents the total surface area of the crack domain (m².m⁻³), D is a characteristic length (m), and the superscript c, m

represents the harmonic average between the properties of the two media. Solutes and gasesous species migrate by advection (following Darcy velocity \mathbf{u}_{i}) and diffusion in the fluid phases following the traditional reactive transport equations⁷⁷.

$$\frac{\partial \omega^{v} S_{v}^{l} T_{i,l}^{v}}{\partial t} + \frac{\partial \omega^{v} S_{g}^{v} T_{i,g}^{v}}{\partial t} = \operatorname{div} \left(D_{l}^{v} \nabla T_{i,l}^{v} + D_{g}^{v} \nabla T_{i,g}^{v} - T_{i,l}^{v} \mathbf{u}_{l} \right) + J_{\mathsf{dual}}^{v} T_{i,l}^{c,\mathsf{m}} + \phi_{a}^{v} + R_{i}^{v}$$
(5)

where $T_{i,a}^{v}$ is the total concentration of species *i* within fluid phase *a* in continuum *v* (mol.L⁻¹ of phase *a*). R_i^{v} is the chemical source term for species *i* in domain *v*. The solid-liquid-gas equilibrium is solved with a thermodynamic database under the assumption of a thermodynamic equilibrium between the three phases. ϕ_a^{v} is the cross-domain diffusive flux of species *i* towards *v*

$$\phi_a^{\rm m} = -D_a^{\rm c,m} \mathcal{A} \frac{T_{i,a}^{\rm c} - T_{i,a^m}}{\mathcal{D}}$$
(6)

where²⁸

$$D_{a}^{c,m} = \max\left(1, \frac{u_{n}}{u_{ref}}\right) D_{a}^{eff,c}$$
⁽⁷⁾

Equation (7) is based on the experimental work of Djerbi et al.¹⁰⁷ and it is assumed that the diffusion coefficient evolves linearly with the crack opening until a critical value u_{ref} . This kind of model has been used in several works^{57,97,108}. The effective diffusion coefficient for phase α is described by a Millington-Quirk relation¹⁰⁹:

$$D_a^{\text{eff},\nu} = D_a^{\text{ref}} (\omega^{\nu})^2 (S_{\nu}^a)^2.$$
(8)

with D_a^{ref} represents the free-phase diffusion coefficient (m².s⁻¹).

Poromechanics. There exists several mechanical approaches to describe the appearance and propagation of deformation-induced cracks. Cracks can be explicitly described through fracture mechanics models such as XFEM¹¹⁰ or frictional cohesive zone models¹³, or can be included through a continuum approach such as damage mechanics⁸. However, with the perspectives of upscaling our approach to large structures or geological settings, continuum models accurately describing the evolution of macro-scale properties and structural damage are required. For these reasons, we have chosen a continuous porous medium approach where the mechanical fracture is simulated using a damage model, which has already yielded satisfactory results for leaching¹² and corrosion³⁹.

Using a damage behaviour requires a dedicated regularization method in order to avoid a mesh dependency. The damage is modelled through Fichant-Laborderie model^{91,92,111} and its regularization is performed using Hillerborg's energetic method^{91,112}. The associated equations are depicted in Table 1. The mechanical system is solved using the finite element Cast3m software³⁵ and the behaviour law is implemented in the code generator MFront^{111,113,114}.

The crack openings are estimated from the anelastic strain tensor $\underline{\varepsilon}^{ane}$ defined by:

$$\underline{\underline{\varepsilon}}^{ane} = \mathbb{C}^{-1} : \underline{\underline{\sigma}}^{ane} = \mathbb{C}^{-1} : \left(\underline{\underline{\sigma}} - \underline{\underline{\sigma}}^{e}\right)$$
(9)

where $\underline{\sigma}^{e}$ is the elastic part of the stress tensor. Normal crack aperture u_{n} is computed using the largest eigenvalues of the anelastic tensor ε_{l}^{ane} and the mesh element characteristic length l_{c} :

$$u_{\rm n} = \varepsilon_{\rm l}^{\rm ane} I_{\rm c}; \tag{10}$$

As mentioned above, the cement paste poroelastic properties required in Equation (1) are estimated using a micromechanics method, where the matrix is modelled through an equivalent C-S-H phase (comprising C-S-H solid phase and gel pores)^{13,85}. In order to capture the decalcification effect of the C-S-H resulting from chemical degradation on the matrix properties, the evolution of the Young modulus of the binding C-S-H phase with the Ca/Si

ratio follows the relation⁷:

$$E_{\text{CSH}} = \left(1 - \frac{\text{Ca/Si} - 0.8}{1.65 - 0.8}\right) E_{\text{gel}} + \left(\frac{\text{Ca/Si} - 0.8}{1.65 - 0.8}\right) E_{\text{CSH}(1.6)}$$
(11)

where $E_{CSH(1.6)}$ and E_{gel} are the Young modulus of the C-S-H phase with a Ca/Si ratio of 1.6 and of the amorphous silica gel corresponding to a totally decalcified phase, respectively.

Poisson ratio is assumed independent of the Ca/Si ratio and is taken as 0.25¹¹⁵; this allows calculating the bulk modulus k_{CSH} of the C-S-H phase as a function of the Ca/Si ratio. These C-S-H properties are used to compute both shear g_{cp} and bulk k_{cp} moduli of the cement paste, and then its Young's modulus, using the Mori-Tanaka scheme, which gives^{5,83,84,116}:

$$\begin{cases} k_{\rm cp} = \left(k_{\rm CSH} + \frac{4g_{\rm CSH}}{3} \sum_{i=1}^{N^{\rm ph}} \varphi_i \frac{k_i - k_{\rm CSH}}{k_i + 4/3g_{\rm CSH}}\right) \left(1 - \sum_{i=1}^{N^{\rm ph}} \varphi_i \frac{k_i - k_{\rm CSH}}{k_i + 4/3g_{\rm CSH}}\right)^{-1} \\ g_{\rm cp} = \left(g_{\rm CSH} + H_{\rm CSH} \sum_{i=1}^{N^{\rm ph}} \varphi_i \frac{g_i - g_{\rm CSH}}{g_i + H_{\rm CSH}}\right) \left(1 - \sum_{i=1}^{N^{\rm ph}} \varphi_i \frac{g_i - g_{\rm CSH}}{g_i + H_{\rm CSH}}\right)^{-1} \\ H_{\rm CSH} = \left(g_{\rm CSH}(3/2k_{\rm CSH} + 4/3g_{\rm CSH})\right) (k_{\rm CSH} + 2g_{\rm CSH})^{-1} \\ E_{\rm cp} = \frac{9k_{\rm cp}g_{\rm cp}}{3k_{\rm cp} + g_{\rm cp}} \end{cases}$$
(12)

where $\varphi_{ii} g_i$ and k_i are the volume fraction, the shear modulus and the bulk modulus of phase $i \in [1, N^{ph}]$, respectively. The cement paste is assumed to be composed of N^{ph} phases including portlandite, calcite, silica gel and capillarity pores. The volume fraction of the minerals is computed by Hytec. The volume fraction of the equivalent C-S-H φ_{CSH}^{eq} and the capillary porosity φ_{cap} are deduced from the total porosity ω^{m} the volume fraction of C-S-H computed by Hytec, and the parameter γ , which represents the ratio of gel pore in the volume fraction of C-S-H^{13,85}:

$$\begin{cases} \varphi_{CSH}^{eq} = \frac{\varphi_{CSH}}{1 - \gamma}; & \varphi_{cap} = \omega^{m} - \frac{\gamma \varphi_{CSH}}{1 - \gamma}; \\ \omega^{m} = \varphi_{cap} + \varphi_{gel} = \varphi_{cap} + \gamma \varphi_{CSH}^{eq} \end{cases}$$
(13)

The shrinkage coefficient α^{ξ} used to compute the carbonation shrinkage (Equation (2)) and the Biot coefficient (Equation (1)) are calculated from the volumetric strain localization coefficient of the inclusive mineral phases:

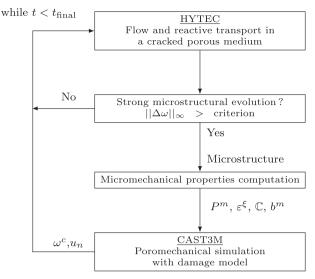
$$\alpha^{\xi} = \frac{k_{\text{CSH}}}{3k_{\text{cp}}} A^{\text{h}}_{\text{CSH}}; \quad b^{\text{m}} = 1 - \sum_{i=1}^{N^{\text{pn}}} \varphi_i A^{\text{h}}_i - \varphi^{\text{eq}}_{\text{CSH}} A^{\text{h}}_{\text{CSH}}$$
(14)

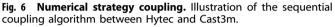
with:

$$A_{i}^{h} = \left(1 + \frac{3k_{CSH}}{3k_{CSH} + 4g_{CSH}} \left(\frac{k_{i}}{k_{CSH}} - 1\right)\right)^{-1} \left[\sum_{i}^{N^{eh}} \varphi_{i} \left(1 + \frac{3k_{CSH}}{3k_{CSH} + 4g_{CSH}} \left(\frac{k_{i}}{k_{CSH}} - 1\right)\right)^{-1}\right]^{-1}$$
(15)

Numerical methodology

The numerical methodology rests on a Sequential Non Iterative coupling between Hytec and Cast3m. At each timestep, Hytec solves the heat transfer and the reactive flow problem^{34,77}. The mechanic solver is called whenever the maximum evolution of porosity (over the whole domain) has gone over a user-defined threshold compared to the last mechanical solver call. Then, the hydrogeochemical data provided by Hytec are used to estimate the pore pressure P^m , the chemical strain tensor $\underline{\varepsilon}^{\xi}$ and the poroelastic properties of the geomaterial. These fields are used together with the damage value by Cast3m to compute the crack porosity ω^{c} (Table 1). Then, the feedback towards the reactive flow problem is performed by adjusting the double porosity and its transport properties (Table 1) within the Hytec simulation. This approach constitutes a complete, thorough and dynamic two-way coupling between chemical and mechanical effects and is depicted in Fig. 6.





DATA AVAILABILITY

All data generated or analysed during this study are included in this published article. More details about the experimental data and numerical methods can be found in cited references, mainly Kangni-Foli et al. 2021⁶⁶, Seigneur et al. 2018, 2020 and 2022^{37,60,77}. Cast3m is a publicly available mechanical code. Hytec software for this research is not publicly available due to intellectual and industrial property.

Received: 17 February 2023; Accepted: 7 July 2023; Published online: 27 July 2023

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ACKNOWLEDGEMENTS

The project leading to this work has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement n847593, in particular from the EURAD/MAGIC workpackage. We want to thank the Institut de Radioprotection et de Sureté Nucléaire (IRSN, France) and in particular Alexandre Dauzères for their participation in the data acquisition.

AUTHOR CONTRIBUTIONS

The respective contributions of the different authors are listed here below A.S.: development, methodology, simulations, microtomographic images analysis, figure, writing and edition of the article N.S.: methodology, funding, supervision, simulations, figure, writing and edition of the article B.B.: methodology, funding, supervision, simulations, writing and edition of the article S.P.: supervision, microtomographic images analysis, experimental results, writing and edition of the article G.T.: microtomographic images analysis, writing and edition of the article.

COMPETING INTERESTS

The authors declare no competing financial or non-financial interests.

ADDITIONAL INFORMATION

Supplementary information The online version contains supplementary material available at https://doi.org/10.1038/s41529-023-00378-x.

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