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# Predicting elastic properties of hard-coating alloys using ab-initio and machine learning methods

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Accelerated design of hard-coating materials requires state-of-the-art computational tools, which include data-driven techniques, building databases, and training machine learning models. We develop a heavily automated high-throughput workflow to build a database of industrially relevant hard-coating materials, such as binary and ternary nitrides. We use the high-throughput toolkit to automate the density functional theory calculation workflow. We present results, including elastic constants that are a key parameter determining mechanical properties of hard-coatings, for  $X_{1-x}Y_xN$  ternary nitrides, where  $X,Y \in \{AI, Ti, Zr, Hf\}$  and fraction  $x = 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1$ . We also explore ways for machine learning to support and complement the designed databases. We find that the crystal graph convolutional neural network trained on ordered lattices has sufficient accuracy for the disordered nitrides, suggesting that existing databases provide important data for predicting mechanical properties of qualitatively different types of materials, in our case disordered hard-coating alloys.

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# INTRODUCTION

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Hard-coating materials have a wide range of applications including metal cutting, scratch-resistant coatings, grinding, and aerospace and automotive parts. For metal cutting tools, hard coatings are essential to their machining performance, increasing it by orders of magnitude over uncoated tools in most applications. Since the beginning, high-hardness materials have been developed experimentally, but for a few decades computational tools, such as density functional theory (DFT)<sup>1,2</sup> and molecular dynamics, have been used to support and complement experiments. However, as the design of new coatings moves from binary and ternary systems to quaternary and beyond, the combinatorial complexity increases rapidly, making conventional approaches increasingly difficult.

More recently, machine learning (ML) has been found to be a viable way to reduce the number of experiments, as well as computations, to accelerate the design process<sup>3–7</sup>. Demand for robust ML models is there, but a big hurdle in their adoption is the limited availability of data, either experimental or computational, that ML models need to be trained on. Experimental data has traditionally been relatively scarce, while computational databases, such as Materials Project<sup>8</sup> and AFLOW<sup>9</sup>, have grown to contain tens or hundreds of thousands of entries. For example, Avery et al. used AFLOW and a combined ML and evolutionary search method to predict new superhard phases in carbon<sup>6</sup>. Mazhnik et al. used Materials Project data to train the crystal graph convolutional neural network (CGCNN)<sup>10</sup> model to predict the bulk and shear moduli of ordered compounds using only the structural and chemical information of the system as input<sup>5</sup>, obtaining good results. In this paper, we extend the approach to qualitatively different class of materials, disordered alloys (asdeposited metastable thin films). It is well-known that ML is good at interpolation, but bad at extrapolation, and it is therefore vital to establish how well ML models extrapolate from ordered data to disordered data. We utilize a transfer learning (TL) approach<sup>11</sup> to predict polycrystalline elastic constants of disordered alloys based

on data obtained from ordered compounds. To the best of our knowledge, there are only very few TL studies in predicting properties of alloys. For a broad overview of ML approaches utilized in the case of alloys, see<sup>12</sup>.

From the point of view of practical applications, e.g., to design new hard coatings, however, currently existing databases are lacking for two reasons. Firstly, elastic constants are important: for instance, the intrinsic hardness of a material can be gualitatively assessed from the elastic constants and moduli<sup>13,14</sup>. However, since elastic constants are demanding to calculate, only a limited fraction of the entries in existing databases have elastic constants data included. Secondly, most industrially relevant hard coatings, e.g.,  $Ti_{1-x}AI_xN$ ,  $Cr_{1-x}AI_xN$ , and  $Ti_{1-x}Si_xN$ , are substitutionally disordered<sup>15</sup>, and are often thermodynamically metastable or even unstable, which is possible due to the far-from-equilibrium synthesis techniques of physical vapor deposition. Existing databases, on the other hand, are focused on ordered compounds. Creating databases for disordered systems is therefore an activity that requires more attention. There is a recent effort to enable data-driven study of high-entropy ceramics<sup>16</sup>, and in this paper we work towards a database of disordered hardcoating materials. Because of significant computational costs, direct first-principles calculations for disordered alloys would lead to a relatively small database, which limits the amount of data to train ML models on. On the other hand, there are recent efforts in literature to find ways to make ML useful for small datasets<sup>11,17–20</sup>.

Given the abundance of data for ordered compounds, we investigate how ordered data can help with the lack of disordered data. Using a bigger data set to help the modeling of a smaller data set is one of the goals of TL<sup>18</sup>. In this paper, we use a TL approach, in which the CGCNN model is trained on the data for ordered compounds available in Materials Project, and the model is then used to predict the properties of disordered systems. We are interested in predicting quantities that are known to correlate with the intrinsic hardness of materials, such as bulk and shear moduli<sup>21–24</sup>. We find that even without an explicit inclusion of the

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data for disordered alloys in the model, it is able to predict the bulk and shear moduli of the industrially relevant nitrides with sufficient accuracy.

## RESULTS

# DFT results

We calculate disordered binary and ternary nitrides of the form  $X_{1-x}Y_xN$ , where  $X,Y \in \{AI, Ti, Zr, Hf\}$  and the concentration parameter  $x = 0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, 1$ . The calculations are performed with and without taking atomic relaxations into account, so that we can assess the importance of the atomic relaxation effects. Cell shape and volume are optimized in both cases. Note that in this comparison in the unrelaxed B4 calculations we must fix the one available atomic degree of freedom along the *z*-direction. We fix it by setting the atomic unit cell coordinates as  $z_1 = 0$  and  $z_2 = 0.38$  in terms of the notation of ref.<sup>25</sup>. One can define  $z_1 = 0$  without loss of generality and  $z_2 = 0.38$  represents the average value for the type of systems we consider here. It should be noted that the  $z_2$  coordinate is also called the *u* parameter in some literature sources<sup>26</sup>.

Let us first investigate the effect of atomic relaxations on the elastic constants. Assessment of the computational cost due to atomic relaxation is useful, because computing the elastic constants is time consuming. Thus, if the effect is minor, some computational time could be saved by neglecting atomic relaxations. Several previous studies have investigated the impact that atomic relaxations have on the elastic constant results<sup>27–33</sup>. In summary, the previous studies have found that, in most cases, relaxed and unrelaxed elastic constants are guite similar. Most often, the relative differences are lower than  $\approx 10\%$ . Relaxation effects can also be qualitatively estimated from symmetry arguments. For some lattice symmetries, a uniform deformation (used for elastic-constant calculations) may be sufficient to shift atoms from their equilibrium positions. This implies, in turn, that the resulting elastic tensors strongly depend on the strain matrix used for the calculation.

Table 1 shows the mean absolute errors (MAE) and mean absolute relative errors (MARE) ( $X_{rel} - X_{unrel}$ )/ $X_{unrel}$  between the relaxed and unrelaxed elastic constants and the polycrystalline quantities, calculated for all the alloys that can be found in Table 2, except for those that are marked B4  $\rightarrow$  B<sub>k</sub>. We have not included those B4 structures that relaxed into B<sub>k</sub>, because all unrelaxed calculations remain in the B4 phase and therefore are not directly comparable to the relaxed calculations that end up in the B<sub>k</sub> phase (see Fig. 3). We can see that for the B1, which is a highly symmetric structure, relaxation effects are minor. With the B3 phase, atomic relaxation effects on calculated  $c_{11}$  and  $c_{12}$  are negligible. Conversely, the MAE and MARE values indicate a strong effect of atomic relaxation on  $c_{44}$ . That is due to local B3-symmetry-breaking

Poisso	<b>Table 1.</b> Mean absolute error (MAE) in GPa (except the unitlessPoisson's ratio v) and mean absolute relative error (MARE) $(X_{rel} - X_{unrel})/X_{unrel}$ in % between the relaxed and unrelaxed elastic properties.										
	<b>C</b> <sub>11</sub>	C <sub>12</sub>	C <sub>13</sub>	C <sub>33</sub>	C <sub>44</sub>	В	G	Ε	v		
MAE											
B1	8	6	-	-	9	4	4	10	0.004		
B3	4	3	-	-	38	3	17	38	0.035		
B4	41	34	39	108	11	3	26	57	0.052		
MARE											
B1	2	5	-	-	6	2	3	3	2		
B3	2	2	-	-	28	2	17	15	13		
B4	12	31	46	32	14	2	26	23	21		

induced by shear lattice distortions. Also the B4 phase shows noticeable relaxation effects.

Based on our findings, if one is only interested in the bulk modulus, one might perform only unrelaxed calculations. If the shear modulus, or quantities that depend on the shear modulus, is of interest, the unrelaxed shear modulus will be accurate only for structures such as B1, where the different distortions do not break the symmetry in such a way that there are significant distortion dependent atomic movements.

The calculated elastic properties are shown in Table 2 and the mixing energies  $E[X_{1-x}Y_xN] - (1-x)E[XN] - xE[YN]$  and relative stabilities E[structure] - E[B1] of the B1 and B3 structure types are shown in Fig. 1. The B4 alloys, most of which relaxed into the B<sub>k</sub> setting are not shown. All of the calculated alloys are found to be mechanically stable within a 10% tolerance of e = 1.1 (see "DFT calculations"). Dynamical stability checks, which are based on phonon dispersion calculations, are out of the scope of this work, but based on existing literature some of the calculated alloys can be expected to be dynamically unstable. All two-component systems are ordered and those systems have been checked against available Materials Project data and the two sets have been found to be generally in good agreement. Our results for the well-studied Ti<sub>1-x</sub>Al<sub>x</sub>N system are also in agreement with literature data<sup>15,34-36</sup>.

For the alloys in B1 structure we find good agreement with the elastic constants, bulk modulus, and mixing energy results of refs. <sup>37,38</sup>. Reference <sup>37</sup> calculated the same set of alloys that can be found in Fig. 1, except for  $Hf_{1-x}Zr_xN$ . The mixing energies of Fig. 1 are in general in good agreement with those of ref. <sup>37</sup>, except for the trend found in ref. <sup>37</sup>, whereby the obtained mixing energies that are highly symmetrical in terms of the concentration parameter *x*-axis. Our mixing energies in panel (a) of Fig. 1 show more pronounced asymmetry (except  $Hf_{1-x}Zr_xN$  and  $Zr_{1-x}Ti_xN$ ) with the  $x \approx 1$  side having larger positive mixing energies. The reason for these different trends could be related to differences in the SQS supercells between our study and ref. <sup>37</sup>.

We notice that all alloys, except HfN and Al-rich alloys, prefer the planar  $B_k$  structure. We interpret the tendency to relax toward the planar  $B_k$  structure (*u* parameter ~0.5) as an effect induced by the dynamical instability (imaginary phonon frequencies<sup>39</sup>, see Fig. 3g in ref.<sup>40</sup>) combined with an energetic preference for the  $B_k$ hexagonal polymorph<sup>41</sup>. Additionally, the B4 ZrN and HfN binaries are predicted to be dynamically stable in the  $B_k$  phase<sup>40</sup>.

Previous ab initio results<sup>41</sup> and Fig. 1 suggest that  $X_{1-x}Al_xN$  (X = Ti, Zr, Hf) solid solutions energetically favor the B1 structure for Al contents  $x \leq 0.5$ , whereas the wurtzite B4 alloy phase becomes the most stable for high  $x \geq 0.7$ ). At ambient conditions, the ordered TiN, HfN, and ZrN favor the B1 structure, which is also their ground state. Other recent ab initio results indicate that TiN can be metastable in the B4 structure (see Fig. 3g in ref.<sup>40</sup>). Our calculations, however, do not find TiN to be stable in the B4 structure. Note, indeed, that ref.<sup>40</sup> reports phonon dispersion results only along a few high-symmetry directions. Evaluation of the B4 TiN phonon-density of states may be necessary to reveal imaginary frequencies.

## Machine learning results

Given that it is relatively resource heavy to calculate the elastic tensor of disordered structures, a large amount of supercomputer time would be needed to amass a sizable database of such materials. We are therefore interested in different strategies to supplement or augment the database using ML techniques. One way to tackle the problem of low data availability is to train the ML model to a part of the available data that is related to the problem at hand, and then appropriately modifying and verifying the model with the smaller dataset. This is the basic idea behind TL<sup>18</sup>. In this work, we use an approach that might be considered a

Alloy	SB	C <sub>11</sub>	C <sub>12</sub>	C <sub>13</sub>	C <sub>33</sub>	C44	В	G	Ε	ν
AIN	B1	432	167	_	_	307	256	219	511	0.167
HfN	B1	598	112	-	-	129	274	166	414	0.248
Hf <sub>0.75</sub> Al <sub>0.25</sub> N	B1	524	124	-	-	147	258	166	410	0.235
Hf <sub>0.50</sub> Al <sub>0.50</sub> N	B1	460	142	-	-	174	248	168	411	0.224
Hf <sub>0.25</sub> Al <sub>0.75</sub> N	B1	429	158	-	-	221	248	182	439	0.205
Hf <sub>0.75</sub> Ti <sub>0.25</sub> N	B1	581	113	-	_	134	269	168	417	0.242
Hf <sub>0.50</sub> Ti <sub>0.50</sub> N	B1	567	119	-	_	142	268	171	423	0.237
Hf <sub>0.25</sub> Ti <sub>0.75</sub> N	B1	577	122	-	-	153	274	180	443	0.231
Hf <sub>0.75</sub> Zr <sub>0.25</sub> N	B1	584	109	-	-	128	267	165	410	0.244
Hf <sub>0.50</sub> Zr <sub>0.50</sub> N	B1	569	108	-	-	128	262	162	403	0.244
Hf <sub>0.25</sub> Zr <sub>0.75</sub> N	B1	554	107	-	-	127	256	159	395	0.243
TiN	B1	584	136	-	-	166	285	187	460	0.231
Ti <sub>0.75</sub> Al <sub>0.25</sub> N	B1	535	139	-	_	181	271	187	456	0.22
Ti <sub>0.50</sub> Al <sub>0.50</sub> N	B1	492	155	-	-	214	268	194	469	0.208
Ti <sub>0.25</sub> Al <sub>0.75</sub> N	B1	443	161	-	-	250	255	199	474	0.19
ZrN	B1	544	110	_	_	125	255	156	389	0.246
Zr <sub>0.75</sub> Al <sub>0.25</sub> N	B1	477	124	-	-	139	242	153	379	0.239
Zr <sub>0.50</sub> Al <sub>0.50</sub> N	B1	427	141	-	-	166	236	156	384	0.229
Zr <sub>0.25</sub> Al <sub>0.75</sub> N	B1	411	157	_	_	215	242	174	421	0.21
Zr <sub>0.75</sub> Ti <sub>0.25</sub> N	B1	538	111	_	_	130	253	159	394	0.24
Zr <sub>0.50</sub> Ti <sub>0.50</sub> N	B1	540	116	_	_	138	257	164	406	0.237
Zr <sub>0.25</sub> Ti <sub>0.75</sub> N	B1	568	122	_	_	150	271	176	434	0.233
AIN	B3	285	152	_	_	178	196	120	299	0.246
HfN	B3	292	152	_	_	93	199	83	219	0.317
Hf <sub>0.75</sub> Al <sub>0.25</sub> N	B3	272	144	_	_	100	188	84	219	0.306
Hf <sub>0.50</sub> Al <sub>0.50</sub> N	B3	261	144	_	_	106	183	84	219	0.301
Hf <sub>0.25</sub> Al <sub>0.75</sub> N	B3	263	144	_	_	127	183	94	241	0.281
Hf <sub>0.75</sub> Ti <sub>0.25</sub> N	B3	205	150	_	_	93	196	82	216	0.316
Hf <sub>0.50</sub> Ti <sub>0.50</sub> N	B3	286	150	_	_	92	195	82	216	0.316
Hf <sub>0.25</sub> Ti <sub>0.75</sub> N	B3	289	150	_	_	92	198	82	216	0.318
Hf <sub>0.75</sub> Zr <sub>0.25</sub> N	B3	281	148	_	_	91	193	80	210	0.318
Hf <sub>0.50</sub> Zr <sub>0.50</sub> N	B3	272	148	_	_	90	189	78	206	0.319
Hf <sub>0.25</sub> Zr <sub>0.75</sub> N	B3	263	147		_	88	189	78	198	0.321
TiN	B3	203	155	_	_	91	201	81	214	0.322
Ti <sub>0.75</sub> Al <sub>0.25</sub> N	B3	295	155			103	197	85	214	0.322
Ti <sub>0.50</sub> Al <sub>0.50</sub> N	B3	282	154	-	-	116	197	89	223	0.301
Ti <sub>0.25</sub> Al <sub>0.75</sub> N			154	-	-	138	194			
ZrN	B3	271		-	-			98 73	251	0.282
	B3	258	144	-	-	87	182	73	193	0.32
Zr <sub>0.75</sub> Al <sub>0.25</sub> N	B3	247	140	-	-	92	176	74	195	0.31
Zr <sub>0.50</sub> Al <sub>0.50</sub> N	B3	240	142	-	-	98	175	74	195	0.31
Zr <sub>0.25</sub> Al <sub>0.75</sub> N	B3	253	146	-	-	123	182	88	227	0.292
Zr <sub>0.75</sub> Ti <sub>0.25</sub> N	B3	262	144	-	-	87	184	74	196	0.323
Zr <sub>0.50</sub> Ti <sub>0.50</sub> N	B3	269	148	-	-	88	188	76	201	0.322
Zr <sub>0.25</sub> Ti <sub>0.75</sub> N	B3	282	154	-	-	89	197	78	207	0.325
AIN	B4	376	129	98	352	112	194	121	301	0.242
HfN	B4	253	161	162	220	47	188	44	122	0.39
Hf <sub>0.75</sub> Al <sub>0.25</sub> N	$B4 \rightarrow B_k$	296	204	113	359	107	201	79	210	0.326
Hf <sub>0.50</sub> Al <sub>0.50</sub> N	$B4 \rightarrow B_k$	298	176	145	110	109	135	51	136	0.332
Hf <sub>0.25</sub> Al <sub>0.75</sub> N	B4	305	140	124	216	87	175	79	206	0.304
Hf <sub>0.75</sub> Ti <sub>0.25</sub> N	$B4 \rightarrow B_k$	298	210	106	493	113	214	85	225	0.325
Hf <sub>0.50</sub> Ti <sub>0.50</sub> N	$B4 \rightarrow B_k$	304	210	103	491	120	214	90	237	0.316
Hf <sub>0.25</sub> Ti <sub>0.75</sub> N	$B4 \rightarrow B_k$	311	212	106	500	128	218	94	247	0.31
Hf <sub>0.75</sub> Zr <sub>0.25</sub> N	$B4 \rightarrow B_k$	292	211	105	495	106	212	81	216	0.33

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Alloy	SB	C <sub>11</sub>	C <sub>12</sub>	C <sub>13</sub>	C <sub>33</sub>	C <sub>44</sub>	В	G	Ε	v
Hf <sub>0.50</sub> Zr <sub>0.50</sub> N	$B4 \rightarrow B_k$	288	206	102	483	107	208	81	215	0.328
Hf <sub>0.25</sub> Zr <sub>0.75</sub> N	$B4 \rightarrow B_k$	286	201	101	470	107	205	82	217	0.324
TiN	$B4 \rightarrow B_k$	322	219	111	524	138	227	100	262	0.308
Ti <sub>0.75</sub> Al <sub>0.25</sub> N	$B4 \rightarrow B_k$	311	212	120	438	138	218	93	244	0.313
Ti <sub>0.50</sub> Al <sub>0.50</sub> N	$B4 \rightarrow B_k$	314	196	128	363	148	211	98	255	0.29
Ti <sub>0.25</sub> Al <sub>0.75</sub> N	B4	315	136	136	214	88	181	80	209	0.30
ZrN	$B4 \rightarrow B_k$	284	195	101	458	106	202	82	217	0.32
Zr <sub>0.75</sub> Al <sub>0.25</sub> N	$B4 \rightarrow B_k$	277	195	108	320	101	188	72	192	0.33
Zr <sub>0.50</sub> Al <sub>0.50</sub> N	$B4 \rightarrow B_k$	287	177	125	202	110	176	74	195	0.31
Zr <sub>0.25</sub> Al <sub>0.75</sub> N	B4	302	147	122	190	89	169	76	198	0.30
Zr <sub>0.75</sub> Ti <sub>0.25</sub> N	$B4 \rightarrow B_k$	288	200	101	453	110	203	83	219	0.32
Zr <sub>0.50</sub> Ti <sub>0.50</sub> N	$B4 \rightarrow B_k$	297	205	102	461	116	207	87	229	0.31
Zr <sub>0.25</sub> Ti <sub>0.75</sub> N	$B4 \rightarrow B_k$	307	210	105	485	125	215	92	242	0.31

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zeroth-order approximation to TL. In this approach, we train an ML model using Materials Project data, which are ordered compounds, and see how well that model predicts the disordered alloys simulated in the present study. In other words, we check how well the patterns learned from the ordered dataset, without modifications, transfer or generalize to the disordered dataset. If the ML model generalizes well, one can employ the network to predict, or at least estimate the properties of disordered systems outright, as the case may be, or use it as a basis for further training with the disordered dataset<sup>11</sup>. Performing more sophisticated TL, such as fine-tuning and layer freezing<sup>11,18</sup>, is out of the scope of this study and will be addressed in future work.

Throughout the ML section, the B4 phase is not included because most of the studied B4 alloys turns out to be unstable and transform into Bk structure upon structural relaxation. At the same time, information on compounds with Bk structure in the databases is insufficient to build reliable ML models: hexagonal systems (and the Bk in particular) are underrepresented in the training set (only ~1000 compounds are hexagonal out of the total 8000). One may view the inability to describe B4/Bk alloys as a limitation of the applicability of the ML and TL that requires further in-depth study. Additionally, those ordered binary compounds (concentration parameter x = 0 or 1) that can be found in the Materials Project data are excluded, because for those data points the error would be biased as they were part of the training set.

The ML architecture that we use is the CGCNN, and Mazhnik et al. have shown that it can be succesfully harnessed, together with Materials Project data, to predict simultaneously both the bulk and shear moduli of an input crystal structure. One could always train separate ML models for the bulk and shear moduli, but in the approach of Mazhnik et al. both quantities are treated on equal footing. Based on their good results, we are encouraged to implement a similar approach here. We employ a typical trainvalidate-test workflow to build the optimal CGCNN model from the Materials Project data.

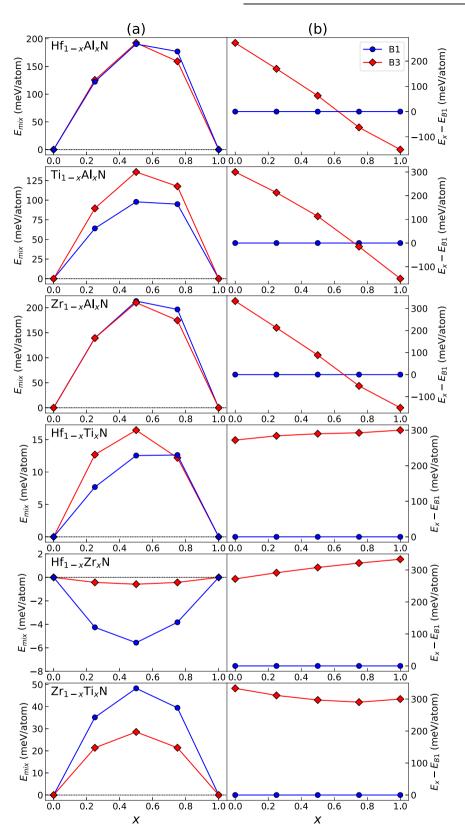
The performance of the finished model is depicted in Table 3 in terms of MAE and MARE for the test set and the disordered dataset, with and without atomic relaxations. In the Table, the B1 + B3 means the combination of the B1 and B3 structure sets. We can see that the predictions made by the ML model for the disordered alloys with B1 and B3 crystal structure are quite accurate, even though no actual TL was done to the model. We notice that for the B3 structures the shear modulus prediction error is noticeably better for the relaxed data compared to

unrelaxed data. This difference reflects the differences in unrelaxed and relaxed shear moduli in Table 1. There are two possible reasons that could explain this behavior. Firstly, the ML prediction error is smaller for the relaxed data, which makes sense since the model was trained on Materials Project data, for which atomic relaxation is used systematically. It is reasonable to assume that the bonding lengths of the unrelaxed structures appear unphysical to the ML model. That would explain why the model performs poorly for unrelaxed structures. Secondly, the CGCNN construction includes a certain cutoff parameter (8 Å in this work) that is used to make the descriptor of each atomic site finite; neighboring atomic sites that fall outside the cutoff radius are neglected. When the structure is relaxed, some atomic sites may move beyond the cutoff radius while others may move within the radius. The descriptors between relaxed and unrelaxed structures are therefore slightly different, which could create discrepancies in the ML results for relaxed and unrelaxed structures.

An interesting observation is that the test set and disordered nitrides MAEs show opposite qualitative trends; for the test set, the shear modulus MAE is smaller than the bulk modulus MAE, while for the disordered data this trend is reversed. Overall, the average ML prediction error for the disordered nitrides is good for the bulk modulus and somewhat worse for the shear modulus. We can say that the CGCNN architecture generalizes quite well from ordered systems to disordered ones even without explicit finetuning of the ML model.

To get a clearer picture of the performance of the ML model, Fig. 2 shows a parity plot of the DFT versus ML predicted values (B4/B<sub>k</sub> not included). Panel (a) of Fig. 2 shows the performance of the network for the test set (green round markers), as well as for the training set (blue cross markers). The figure also shows ML predictions for Young's modulus *E* and Poisson's ratio *v*, which are not directly produced by the ML model, but can be calculated from the predicted bulk and shear moduli. Our results for the test set are comparable to those of Mazhnik et al.<sup>5</sup>. The prediction accuracy for the disordered nitrides falls within the accuracy range of the Materials Project test set.

Panel (b) of Fig. 2 shows how well the ML model with the lowest loss function performs for the disordered nitrides. We can see a fairly tight clustering around the diagonal and an absense of major outliers. Clear outliers or significant scatter for the nitrides is not expected anyway, because the disordered dataset is very homogeneous (in terms of the variety of structures and chemical elements) compared to the Materials Project training set, so the ML model should work similarly for all the data points the



**Fig. 1** Calculated mixing energies and structural stability. a Calculated DFT mixing energies  $E[X_{1-x}Y_xN] - (1-x)E[XN] - xE[YN]$ . **b** Structural stability with respect to B1 with the same composition E[structure] - E[B1]. B4 alloys, most of which relaxed into the B<sub>k</sub> setting (see Table 2) are not shown.

**Table 3.** The MAE (in GPa) and MARE (in %) of the bulk modulus *B* and the shear modulus *G* for the Materials Project test set and the disordered nitrides.

Dataset	MAE(B)	MARE(B)	MAE(G)	MARE(G)				
Mat. Proj. test set	11.6	18.4	9.0	21.7				
unrelaxed B1	15.8	6.0	28.3	16.4				
unrelaxed B3	3.9	2.1	23.6	23.7				
unrelaxed B1+B3	9.7	4.0	25.9	20.2				
relaxed B1	14.0	5.3	23.9	13.9				
relaxed B3	5.3	2.9	7.9	9.8				
relaxed B1+B3	9.5	4.1	15.7	11.8				
The B1 $+$ B3 means the combination of the B1 and B3 structure sets.								

disordered data. We can identify some structure specific trends in the ML prediction accuracy. While the bulk and shear moduli of the B3 structures are especially well predicted, the B1 shear moduli show a lower accuracy. For the B1 phase the shear modulus is consistently underestimated and the largest single underestimation is  $\approx$  50 GPa. It is not easy to give a simple reason for the inconsistent shear modulus, as evidenced by Table 1, is a more sensitive quantity than the bulk modulus. It is the aim of future studies to see how much fine-tuning the current ML network will improve the prediction accuracy.

## DISCUSSION

We have developed an automated high-throughput workflow for building a computational database of disordered hard-coating materials and presented results of our calculations. The reliability of our data is verified by comparing to the Materials Project data and existing literature. Moreover, we have trained the CGCNN ML model on ordered compounds from the Materials Project and demonstrated that this model is able to readily predict the bulk and shear moduli of disordered nitrides with sufficient accuracy. The CGCNN architecture seems to be able to learn such fundamental patterns in the data that these patterns hold regardless of the degree of order, indicating good generalizability of CGCNN from ordered to disordered systems. Prediction accuracy for disordered systems can be further improved by using the ML model trained on ordered data as the starting point for TL. Our findings open new ways to gain insight into disordered hard-coating materials, as well as to support and possibly speed up the investigations of disordered hard-coating materials, which are computationally demanding to calculate and thus slow to accumulate into a large database.

## **METHODS**

## **DFT calculations**

The DFT calculations were performed using the Vienna Ab initio Simulation Package (VASP)<sup>42,43</sup>. The exchange and correlation effects were treated at the generalized gradient approximation (GGA) level<sup>44-46</sup> using the Perdew–Burke–Ernzerhof (PBE)<sup>47</sup> functional. Energy cutoff is set to 500 eV in the preliminary relaxation phase and to 700 eV in subsequent phases. The precision mode is set to Accurate (PREC = Accurate). The Gaussian smearing scheme with a smearing width of 0.05 eV is used. Ionic relaxations are stopped when all forces are below the threshold 0.01 eV/Å. In cases where the threshold 0.01 eV/Å is difficult to reach, the threshold is increased to 0.03 eV/Å or 0.05 eV/Å. The elastic constants calculations include the support grid for augmentation charges (ADDGRID=.TRUE.).

The VASP calculations were managed with The High-Throughput Toolkit  $(httk)^{48,49}$ . The *httk* software offers workflows to create input files, manage calculations on computing clusters, automatically fix broken calculations

by adjusting VASP input settings, and organize results in databases. The automatic computation of elastic constants is implemented in *httk*.

In this work, we consider disordered binary and ternary nitrides in cubic rocksalt (B1)<sup>50</sup>, cubic zincblende (B3)<sup>51</sup>, and hexagonal wurtzite (B4)<sup>21</sup> structures. These structure types are illustrated in Fig. 3. Disorder is modeled using the special guasirandom structures (SQS) technique<sup>52,53</sup>. The SQS supercells that are used in this study are listed in Supplementary Methods. Here, substitutional disorder is considered only on the metallic sublattice, i.e., the nitrogen sublattice is ordered because it is fully occupied by nitrogen atoms. All SQS supercells had size of 96 atoms. This size has been found to be within the optimal range for ternary nitrides from the standpoint of accuracy versus computational speed<sup>35</sup>. The B1  $X_{0.5}Y_{0.5}N$  SQS cell is taken from the supplementary materials of ref.<sup>35</sup>, where it is referred to as the  $(4 \times 4 \times 3)$  cell. In ref. <sup>35</sup> the  $(4 \times 4 \times 3)$  cell was found to model disorder at a high-quality level, that is, comparable to SQS cells of bigger sizes. The B3  $X_{0.5}Y_{0.5}N$  SQS can be easily derived from the B1  $X_{0.5}Y_{0.5}N$  SQS by noting that the B1 conventional unit cell turns into B3 when the N atom is shifted from the high-symmetry position  $\frac{1}{2}\vec{a}_1 + \vec{a}_2$  $\frac{1}{2}\vec{a}_2 + \frac{1}{2}\vec{a}_3$  to another high-symmetry position  $\frac{1}{4}\vec{a}_1 + \frac{1}{4}\vec{a}_2 + \frac{1}{4}\vec{a}_3$ . All the other SQS supercells are generated with the stochastic Monte-Carlo SQS program mcsqs<sup>54</sup>, which is part of the Alloy Theoretic Automated Toolkit (ATAT) program package<sup>55</sup>

Although the SQS scheme is an efficient way to simulate disorder, the downside is that the proper (macroscopic) symmetry is broken and the generated SQS cells typically only have triclinic symmetry. For the calculation of elastic constants this poses a problem, because we are interested in elastic constant tensors of cubic (B1 and B3) or hexagonal (B4) classes instead of triclinic-structure elastic tensors. In order to derive properly symmetrized elastic constants from the full triclinic elastic tensor, we employ the projection technique that has been discussed in ref.<sup>35</sup> and references therein. For the unprojected triclinic elastic constants, see Supplementary Tables. We can see that the deviations between the different crystallographic directions are small, even though the disordered SQS supercells do not respect the proper macroscopic symmetry. As ref.<sup>35</sup> shows, the projected elastic constants have the desirable property that they converge fast to the correct value as a function of supercell size, faster than the unprojected elastic constants. To facilitate automated calculations, we have implemented the symmetrization technique in httk. The elastic constants in VASP are calculated using the stress-strain method in the same general way that was used, e.g., in ref.<sup>56</sup>. Four distorted structures are generated for each strain component (in terms of Voigt notation) and the range of distortion are -3%, -1.5%, 1.5%, 3% for nonshear components and -6%, -3%, 3%, 6% for shear components. All polycrystalline quantities are calculated using the Hill averaging scheme<sup>56</sup>. The mechanical stability is checked based on the Born-Huang stability criteria<sup>57</sup>. In addition to the normal stability check, we also use the stricter tolerance based check of ref.<sup>56</sup>. For example, cubic systems must fulfill a condition  $C_{11} > |C_{12}|$  to be mechanically stable. In the tolerance based check, a more rigorous condition  $C_{11} > \epsilon |C_{12}|$  ( $\epsilon > 1$ ) must be fulfilled. All of the calculated alloys are found to be mechanically stable. Dynamical stability checks, which are based on phonon dispersion calculations, are out of the scope of this work, but based on existing literature some of the calculated alloys can be expected to be dynamically unstable.

#### Machine learning

The ML part of this work is done using the PyTorch package. The CGCNN<sup>10</sup> architecture is applied using the code available at GitHub as the basis<sup>58</sup>. In the CGCNN model the input crystal structure is transformed into a crystal graph, which is constructed from node feature vectors  $\mathbf{v}_i$  and edge feature vectors  $\mathbf{u}_{ij}$ . The node feature vector encodes information about the type of atom located at atomic site *i*. The atomic information is encoded in an integer vector using one-hot or dummy encoding. For example, if the training data includes elements N, Al, and Ti, then the elements can be encoded as N  $\Rightarrow$  [1, 0, 0], Al  $\Rightarrow$  [0, 1, 0], and Ti  $\Rightarrow$  [0, 0, 1]. The edge feature vector encodes information is encoded by discretizing a Gaussian distribution function centered around the nearest neighbors *j* is then calculated as

$$\mathbf{u}_{ij} = \exp\left(-\frac{\left(d_{ij} - \boldsymbol{a}\right)^2}{h^2}\right),\tag{1}$$

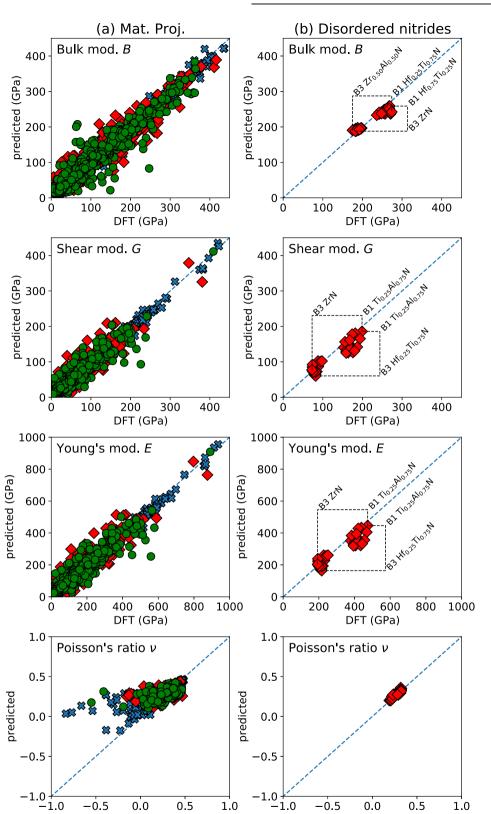
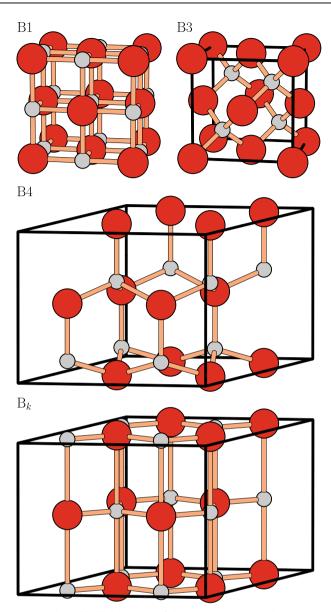


Fig. 2 Parity plot comparing DFT and ML predicted results. a Materials Project training, validation, and test sets. Blue cross markers indicate training set, red diamonds validation set, and green disks test set. b Disordered nitrides test set. The minimum and maximum DFT and ML prediction values for the disordered nitrides are also labeled by chemical formulas and dashed lines.

DFT

DFT



**Fig. 3** Stick and ball drawings of the B1, B3, B4, and Bk structures. The larger red spheres indicate metallic sublattice and the smaller gray spheres the nitrogen sublattice.

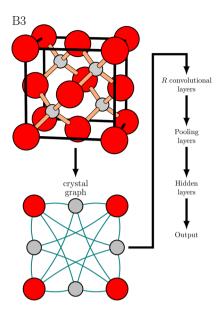
where  $d_{ij}$  is the distance between sites *i* and *j*, *h* is a discretization step size, and *a* is a vector of discretized trial distances

$$\boldsymbol{\alpha} = [0, h, 2h, 3h, \dots, R_{\text{cut}}], \tag{2}$$

where  $R_{cut}$  is a cutoff radius to make the vector finite in length. We can see that when a is close to  $d_{ij}$ ,  $\mathbf{u}_{ij}$  has values close to one, and when a deviates from  $d_{ij}$ ,  $\mathbf{u}_{ij}$  is close to zero. The crystal graph is then fed into a convolutional neural network, which consists of convolutional layers and pooling layers. The convolutional layers iteratively modify the node feature vector of site *i* by convolving it with the edge feature vector  $\mathbf{u}_{ij}$  and node feature vectors of surrounding sites *j*. The convolution is described by the equation

$$\begin{aligned} \mathbf{v}_{i}^{(t+1)} &= \mathbf{v}_{i}^{(t)} &+ \sum_{j} \sigma \Big( \mathbf{z}_{ij}^{(t)} \mathbf{W}_{f}^{(t)} + \mathbf{b}_{f}^{(t)} \Big) \\ & \odot g \Big( \mathbf{z}_{ij}^{(t)} \mathbf{W}_{S}^{(t)} + \mathbf{b}_{S}^{(t)} \Big), \end{aligned} \tag{3}$$

where  $\mathbf{z}_{ij}^{(t)} = \mathbf{v}_i^{(t)} \oplus \mathbf{v}_j^{(t)} \oplus \mathbf{u}_{ij}$  is the concatenation of the node and edge feature vectors,  $\sigma$  is the sigmoid activation function, g is the softplus activation function, and  $\mathbf{W}_{\mathbf{S}}^{(t)}, \mathbf{W}_{\mathbf{f}}^{(t)}, \mathbf{b}_{\mathbf{S}}^{(t)}, \mathbf{b}_{\mathbf{f}}^{(t)}$  are the weights and biases of



**Fig. 4 Diagram of the CGCNN architecture.** A high-level representation of how a prediction is made for an input crystal structure (e.g. B3), by converting it into a crystal graph and then passing it through a series of purpose-build ML layers.

the *t*th convolutional layer<sup>10</sup>. After *R* convolutional layers (three in this work), a pooling layer is applied to produce the overall feature vector of the crystal  $\mathbf{v}_c$ . The pooling layer is implemented as a normalized summation of all the feature vectors  $\mathbf{v}_1^{(0)}, \mathbf{v}_2^{(0)}, \dots, \mathbf{v}_1^{(R)}, \mathbf{v}_2^{(R)}, \dots, \mathbf{v}_N^{(R)}$ . Finally,  $\mathbf{v}_c$  is inputed to fully connected hidden layers (two in this work) that predict the output. A diagram of the CGCNN architecture is presented in Fig. 4.

Following ref.<sup>5</sup>, the network is trained to predict bulk and shear moduli using Materials Project data as the training and test datasets. At the time of writing, Materials Project contains a little over 8000 systems that have elasticity data available. We randomly split the data into training, validation, and test sets in a 8:1:1 ratio. While the training set is used to optimize the model parameters, the difference between the validation and test has to do with avoiding biases in the final estimation of the accuracy of the ML model. Here validation set is used to minimize overfitting in a way that is described below. This means that the validation set is part of the model optimization process and the model accuracy for the validation set is slightly biased. Hence we need a test set that only contains data that the final ML model has never seen before. By evaluating model performance on the test set is therefore a way to minimize biases and maximize the trustworthiness of the model accuracy estimate.

Before training, the target values (bulk and shear moduli) are normalized using the formula

$$\widetilde{\mathbf{y}} = \frac{\mathbf{y} - \overline{\mathbf{y}}}{\sigma(\mathbf{y})},\tag{4}$$

where  $\overline{\mathbf{y}}$  is the mean and  $\sigma(\mathbf{y})$  is the standard deviation of the target vector  $\mathbf{y}$ . The loss function to be minimized is defined in terms of the normalized bulk modulus  $\widetilde{\mathbf{B}}$  and shear modulus  $\widetilde{\mathbf{G}}$  as

$$\mathcal{L} = \frac{\sum_{i} (\widetilde{B}_{i}^{\text{pred}} - \widetilde{B}_{i}^{\text{DFT}})^{2} + (\widetilde{G}_{i}^{\text{pred}} - \widetilde{G}_{i}^{\text{DFT}})^{2}}{N},$$
(5)

where *N* is the number of data points. Based on the information of refs.  $^{5,10,18}$  and their supplementary materials, as well as our own testing, we can infer reasonable values for the hyperparameters without performing extensive hyperparameter tuning. The crystal structure descriptor-related settings are the same as those reported in ref.  $^5$ . The training process uses the Adam optimizer with a learning rate of 0.005 and weight decay 0.0. Training is continued for a minimum of 500 epochs to give the randomly initialized model parameters enough time to develop. Training is stopped after 1500 epochs, as it is unlikely that any significant progress will happen after that point. In order to avoid the training process getting stuck in a suboptimal local minimum, 30 instances were trained. To reduce random variance, an ensemble of five networks with

the lowest validation loss is used to make predictions. The validation set is used to decide the final model parameters by extracting the parameters from the epoch that yields the loss function minimum for the validation set. This is one form of the early stopping technique and the purpose is to mitigate overfitting issues<sup>59</sup>. Finally, an unbiased estimate of the performance of the finished model is obtained by evaluating the model using the unseen test set (see Table 3). For further details about the CGCNN architecture and the training process, the reader is referred to refs. <sup>5,10,18</sup>.

# DATA AVAILABILITY

Relevant calculated DFT data and instructions to download the Materials Project data, as well as the trained ML model to reproduce the results of this paper can be downloaded from https://doi.org/10.6084/M9.FIGSHARE.17129045.V2.

# CODE AVAILABILITY

The code to reproduce the results of this paper can be downloaded from https://doi. org/10.6084/M9.FIGSHARE.17129045.V2.

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## **AUTHOR CONTRIBUTIONS**

H.L., R.A., and I.A.A. conceived the project. H.L. performed the calculations and analyzed the results. H.L., F.T., D.G.S., L.J.S.J., R.A., and I.A.A. discussed the results and wrote the manuscript.

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#### **COMPETING INTERESTS**

The authors declare no competing interests.

# ADDITIONAL INFORMATION

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