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A fast quantum interface between different spin qubit encodings

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Single-spin qubits in semiconductor quantum dots hold promise for universal quantum computation with demonstrations of a high single-qubit gate fidelity above 99.9% and two-qubit gates in conjunction with a long coherence time. However, initialization and readout of a qubit is orders of magnitude slower than control, which is detrimental for implementing measurement-based protocols such as error-correcting codes. In contrast, a singlet-triplet qubit, encoded in a two-spin subspace, has the virtue of fast readout with high fidelity. Here, we present a hybrid system which benefits from the different advantages of these two distinct spin-qubit implementations. A quantum interface between the two codes is realized by electrically tunable inter-qubit exchange coupling. We demonstrate a controlled-phase gate that acts within 5.5 ns, much faster than the measured dephasing time of 211 ns. The presented hybrid architecture will be useful to settle remaining key problems with building scalable spin-based quantum computers.

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Initialization, single-qubit and two-qubit gate operations, and measurements are fundamental elements for universal quantum computation¹. Generally, they should all be fast and with high fidelity to reach the fault-tolerance thresholds². So far, various encodings of spin qubits into one to three-spin subspaces have been developed in semiconductor quantum dots^{3–15}. In particular, recent experiments demonstrated all of these elements including two-qubit logic gates for single-spin qubits proposed by Loss and DiVincenzo (LD qubits) and singlet-triplet (ST) qubits^{6–8,14}. These qubits have different advantages depending on the gate operations, and combinations thereof can increase the performance of spin-based quantum computing. In LD qubits, the two-qubit gate is fast^{6,7} as it relies on the exchange interaction between neighboring spins. In contrast, the two-qubit gate in ST qubits is much slower as it is mediated by a weak dipole coupling¹⁴. Concerning initialization and readout, however, the situation is the opposite: it is slow for LD qubits, relying on spin-selective tunneling to a lead^{16,17}, while it is orders of magnitude faster in ST qubits relying on Pauli spin blockade^{12,13}. Therefore, a fast and reliable interface between LD and ST qubits would allow for merging the advantages of both realizations.

Here we present such an interface implementing a controlled-phase (CPHASE) gate between a LD qubit and a ST qubit in a quantum dot array^{18,19}. The gate is based on the nearest neighbor exchange coupling and is performed in 5.5 ns. Even though we do not pursue benchmarking protocols here, the gate time being much shorter than the corresponding dephasing time (211 ns) indicates that the fidelity of this type of gates can be very high. Our results demonstrate that controlled coherent coupling of different types of gated spin qubits is feasible, and one can proceed to combining their advantages. Overall, our work pushes further the demonstrated scalability of spin qubits in quantum dot arrays.

Results

A LD qubit and a ST qubit formed in a triple quantum dot (TQD). A hybrid system comprising a LD qubit and a ST qubit is implemented in a linearly-coupled gate-defined TQD shown in Fig. 1a. The LD qubit (Q_{LD}) is formed in the left dot while the ST qubit (Q_{ST}) is hosted in the other two dots. We place a magnet near the TQD to coherently and resonantly control Q_{LD} via electric dipole spin resonance (EDSR)^{20–23,26}. At the same time it makes the Zeeman energy difference between the center and right dots, ΔE_Z^{ST} , much larger than their exchange coupling J^{ST} , such that the eigenstates of Q_{ST} become $|\uparrow\downarrow\rangle$ and $|\downarrow\uparrow\rangle$ rather than singlet $|S\rangle$ and triplet $|T\rangle$. We apply an external in-plane magnetic field $B_{ext} = 3.166$ T to split the Q_{LD} states by the Zeeman energy E_Z as well as to separate polarized triplet states $|\uparrow\uparrow\rangle$ and $|\downarrow\downarrow\rangle$ from the Q_{ST} computational states. The experiment is conducted in a dilution refrigerator with an electron temperature of approximately 120 mK. The qubits are manipulated in the $(N_L, N_C, N_R) = (1,1,1)$ charge state while the $(1,0,1)$ and $(1,0,2)$ charge states are also used for initialization and readout (see Fig. 1b). Here, $N_{L(C,R)}$ denotes the number of electrons inside the left (center, right) dot.

We first independently measure the coherent time evolution of each qubit to calibrate the initialization, control, and readout. We quench the inter-qubit exchange coupling by largely detuning the energies of the $(1,1,1)$ and $(2,0,1)$ charge states. For Q_{LD} , we observe Rabi oscillations⁴ with a frequency f_{Rabi} of up to 10 MHz (Fig. 1d) as a function of the microwave (MW) burst time t_{MW} , using the pulse sequence in Fig. 1e. For Q_{ST} , we observe the precession between $|S\rangle$ and $|T\rangle$ (ST precession) (Fig. 1f) as a function of the evolution time t_e , using the pulse sequence in Fig. 1g (see Supplementary Note 2 for full control of Q_{ST}). We use

a metastable state to measure Q_{ST} with high fidelity¹³ (projecting to $|S\rangle$ or $|T\rangle$) in the presence of large ΔE_Z^{ST} with which the lifetime of $|T\rangle$ is short²⁷.

Calibration of the two-qubit coupling. The two qubits are interfaced by exchange coupling J^{QQ} between the left and center dots as illustrated in Fig. 1c. We operate the two-qubit system under the conditions of $E_Z \gg \Delta E_Z^{ST}, \Delta E_Z^{QQ} \gg J^{QQ} \gg J^{ST}$ where ΔE_Z^{QQ} is the Zeeman energy difference between the left and center dots. Then, the Hamiltonian of the system is

$$\mathcal{H} = -E_Z \hat{\sigma}_z^{LD} / 2 - \Delta E_Z^{ST} \hat{\sigma}_z^{ST} / 2 + J^{QQ} (\hat{\sigma}_z^{LD} \hat{\sigma}_z^{ST} - 1) / 4 \quad (1)$$

where $\hat{\sigma}_z^{LD}$ and $\hat{\sigma}_z^{ST}$ are the Pauli z-operators of Q_{LD} and Q_{ST} , respectively¹⁸ (Supplementary Note 3). The last term in Eq. (1) reflects the effect of the inter-qubit coupling J^{QQ} : for states in which the spins in the left and center dots are antiparallel, the energy decreases by $J^{QQ}/2$ (see Fig. 2a). In the present work, we choose to operate Q_{LD} as a control qubit and Q_{ST} as a target, although these are exchangeable. With this interpretation, the ST precession frequency f^{ST} depends on the state of Q_{LD} , $f_{\sigma_{LD}}^{ST} = (\Delta E_Z^{ST} - \sigma_z^{LD} J^{QQ} / 2) / h$. Here σ_z^{LD} represents $|\uparrow\rangle$ or $|\downarrow\rangle$ and $+1$ or -1 interchangeably. This means that while J^{QQ} is turned on for the interaction time t_{int} , Q_{ST} accumulates the controlled-phase $\phi_C = 2\pi J^{QQ} t_{int} / h$, which provides the CPHASE gate (up to single-qubit phase gates; see Supplementary Note 7) in $t_{int} = h / 2J^{QQ}$. An important feature of this two-qubit gate is that it is intrinsically fast, scaling with J^{QQ}/h which can be tuned up to ~ 100 MHz, and is limited only by the requirement $J^{QQ}/h \ll \Delta E_Z^{QQ}/h \sim 500$ MHz in our device.

Before testing the two-qubit gate operations, we calibrate the inter-qubit coupling strength J^{QQ} , and its tunability by gate voltages. The inter-qubit coupling in pulse stage F (Fig. 2b) is controlled by the detuning energy between $(2,0,1)$ and $(1,1,1)$ charge states (one of the points denoted E in Fig. 1b). To prevent leakage from the Q_{ST} computational states, we switch J^{QQ} on and off adiabatically with respect to ΔE_Z^{QQ} by inserting voltage ramps to stage F with a total ramp time of $t_{ramp} = 24$ ns (Fig. 2b)²⁸. The coherent precession of Q_{ST} is measured by repeating the pulse stages from D to H without initializing, controlling and measuring Q_{LD} , which makes Q_{LD} a random mixture of $|\uparrow\rangle$ and $|\downarrow\rangle$. Figure 2c shows the FFT spectra of the precession measured for various interaction points indicated in Fig. 1b. As we bring the interaction point closer to the boundary of $(1,1,1)$ and $(2,0,1)$, J^{QQ} becomes larger and we start to see splitting of the spectral peaks into two. The separation of the two peaks is given by J^{QQ}/h which can be controlled by the gate voltage as shown in Fig. 2d.

We now demonstrate the controllability of the ST precession frequency by the input state of Q_{LD} , the essence of a CPHASE gate. We use the quantum circuit shown in Fig. 2b, which combines the pulse sequences for independent characterization of Q_{LD} and Q_{ST} . Here we choose the interaction point such that $J^{QQ}/h = 90$ MHz. By using either $|\uparrow\rangle$ or $|\downarrow\rangle$ as the Q_{LD} initial state (the latter prepared by an EDSR π pulse), we observe the ST precessions as shown in Fig. 2e, f. The data fit well to Gaussian-decaying oscillations giving $f_{|\uparrow\rangle}^{ST} = 434 \pm 0.5$ MHz and $f_{|\downarrow\rangle}^{ST} = 524 \pm 0.4$ MHz [These are consistent with the values determined by Bayesian estimation discussed in Methods]. This demonstrates the control of the precession rate of Q_{ST} by J^{QQ}/h depending on the state of Q_{LD} .

Demonstration of a CPHASE gate. To characterize the controlled-phase accumulated during the pulse stage F, we separate the phase of Q_{ST} into controlled and single-qubit contributions as $\phi_{\sigma_z^{LD}} = -\pi \sigma_z^{LD} J^{QQ} (t_{int} + t_0) / h$ and

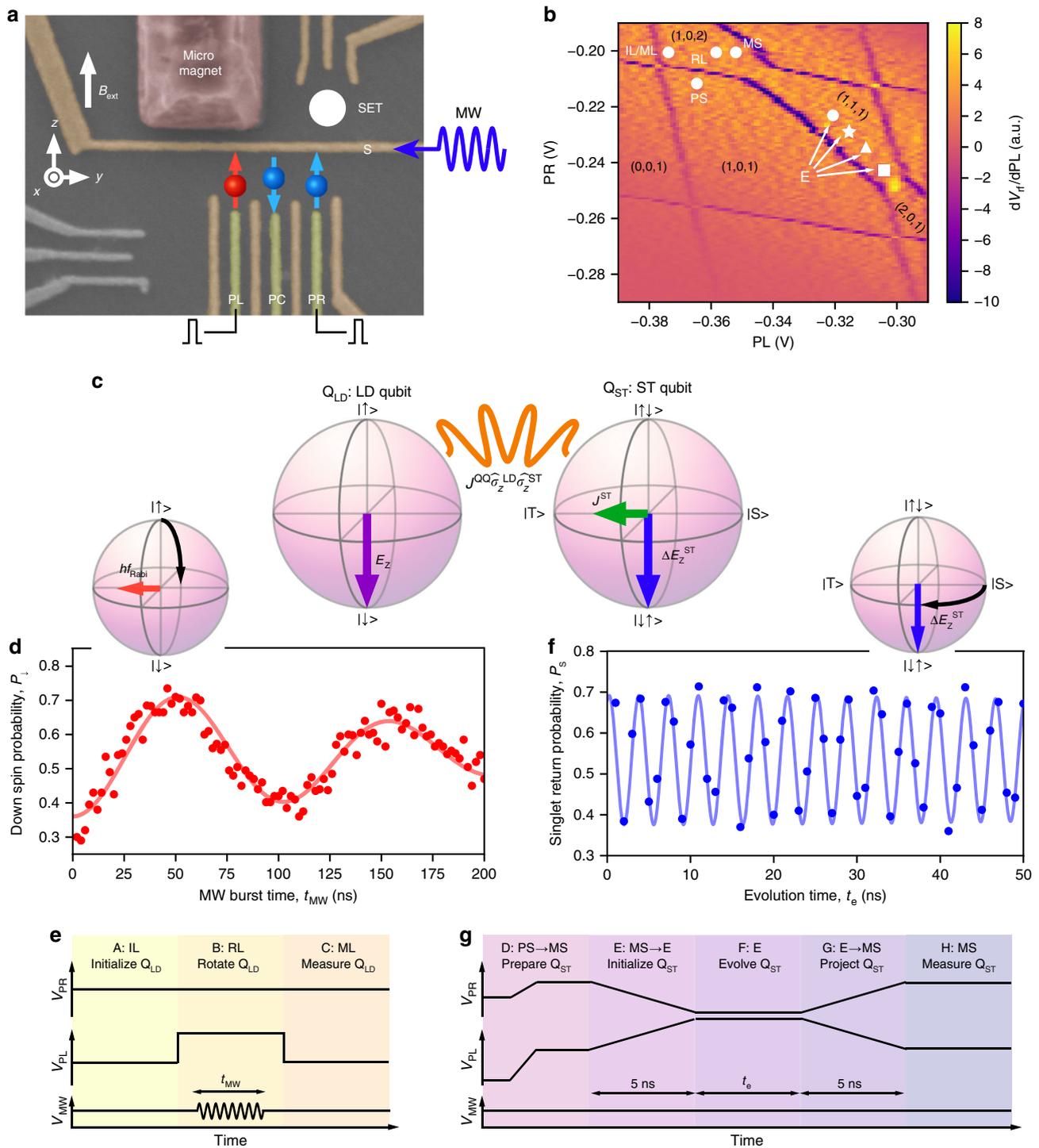


Fig. 1 Hybrid system of a LD qubit and a ST qubit realized in a TQD. **a** False color scanning electron microscope image of a device identical to the one used in this study. The TQD is defined in a two-dimensional electron gas at the GaAs/AIGaAs heterointerface 100 nm below the surface. The upper single electron transistor is used for radiofrequency-detected charge sensing^{24,25}. A MW with a frequency of 17.26 GHz is applied to the S gate to drive EDSR. **b** Stability diagram of the TQD obtained by differentiating the charge sensing signal V_{rf} . **c** Hybrid system of a LD qubit and a ST qubit coupled by the exchange coupling J^{QQ} . **d** Rabi oscillation of Q_{LD} (rotation around x-axis) driven by EDSR with $J^{QQ} = 0$ at point RL in Fig. 1b. The data is fitted to oscillations with a Gaussian decay of $T_2^{Rabi} = 199$ ns. **e** Pulse sequence used to produce Fig. 1d showing gate voltages V_{PL} and V_{PR} applied to the PL and PR gates and a MW burst V_{MW} . **f** Precession of Q_{ST} (rotation around z-axis) with a frequency of $f^T = 280$ MHz due to ΔE_z^{ST} , taken at point E marked by the white circle in (1,1,1) in Fig. 1b, where J^{QQ} and $J^{ST} = 0$. The data follow the Gaussian decay with a decay time of 207 ns (see Supplementary Fig. 2a) induced by the nuclear field fluctuations²⁹. **g** Pulse sequence used to produce Fig. 1f

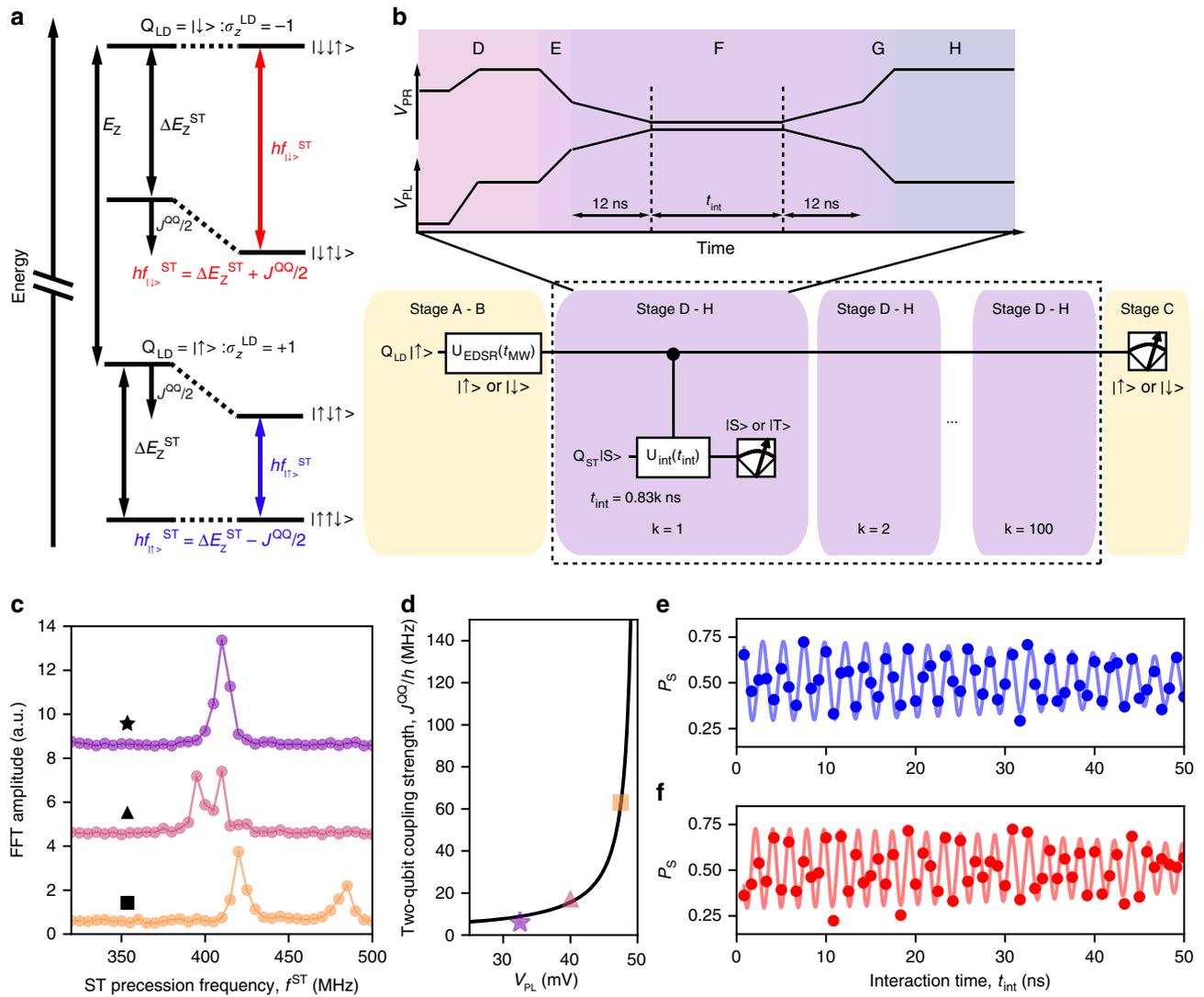


Fig. 2 ST qubit frequency controlled by the LD qubit. **a** Energy diagram of the two-qubit states for $E_Z \gg \Delta E_Z^{ST}$, $\Delta E_Z^{QQ} \gg J^{QQ}$ ($J^{ST} = 0$). The ST qubit frequency is equal to ΔE_Z^{ST} for $J^{QQ} = 0$, and shifts by $\pm J^{QQ}/2$ depending on the Q_{LD} state for finite J^{QQ} . **b** The quantum circuit for demonstrating the phase control of Q_{ST} depending on Q_{LD} . After preparing an arbitrary state of Q_{LD} (stages A and B), we run modified stages from D to H (shown in the upper panel) 100 times with t_{int} values ranging from 0.83 to 83 ns to observe the time evolution of Q_{ST} without reinitializing or measuring Q_{LD} . Stages A, B and C take 202 μ s in total and the part from D to H is 7 μ s long. **c** FFT spectra of f^{ST} with different interaction points shown by the white corresponding symbol in Fig. 1b (traces offset for clarity). In addition to the frequency splitting due to J^{QQ} , the center frequency of the two peaks shifts because ΔE_Z^{ST} is also dependent on the interaction point (Methods). **d** Interaction point dependence of the ST qubit frequency splitting, i.e. the two-qubit coupling strength J^{QQ}/h , fitted with the black model curve (see Supplementary Note 4 for the data extraction and fitting). **e** ST precession for the Q_{LD} input state $|\uparrow\rangle$ fitted with the Gaussian-decaying oscillations with a decay time of 72 ns. **f** ST precession for the Q_{LD} input state $|\downarrow\rangle$ with a fitting curve. The decay time is 75 ns. The total data acquisition time for **e** and **f** is 451 ms

$\phi^{ST} = 2\pi\Delta E_Z^{ST}(t_{int} + t_{ramp})/h + \phi_0$, respectively. Here t_0 ($\ll t_{ramp}$) represents the effective time for switching on and off J^{QQ} (Supplementary Note 5). A phase offset ϕ_0 denotes the correction accounting for nonuniform ΔE_Z^{ST} during the ramp (Supplementary Note 5). Then the probability of finding the final state of Q_{ST} in singlet is modeled as

$$P_{S,model} = a \cos(\phi_{\sigma_z^{LD}} + \phi^{ST}) \exp(-(t_{int}/T_2^*)^2) + b \quad (2)$$

where a , b and T_2^* represent the values of amplitude, mean and the dephasing time of the ST precession, respectively. We use maximum likelihood estimation (MLE) combined with Bayesian estimation^{29,30} to fit all variables in Eq. 2, that are a , b , t_0 , J^{QQ} , T_2^* , ϕ_0 , and ΔE_Z^{ST} , from the data (Methods). This

allows us to extract the t_{int} dependence of $\phi_{\sigma_z^{LD}}$ (Fig. 3a) (Methods) and consequently $\phi_C = \phi_{|\downarrow\rangle} - \phi_{|\uparrow\rangle}$ (Fig. 3b). It evolves with t_{int} in the frequency of $J^{QQ}/h = 90$ MHz, indicating that the CPHASE gate time can be as short as $h/2J^{QQ} = 5.5$ ns (up to single-qubit phase). On the other hand, T_2^* obtained in the MLE is 211 ns, much longer than what is observed in Fig. 2e, f because the shorter data acquisition time used here cuts off the low-frequency component of the noise spectrum²⁹. We note that this T_2^* is that for the two-qubit gate while J^{QQ} is turned on⁸, and therefore it is likely to be dominated by charge noise rather than the nuclear field fluctuation (Supplementary Note 6). The ratio $2J^{QQ}T_2^*/h$ suggests that 38 CPHASE operations would be possible within the two-qubit dephasing time. We anticipate that this ratio can be further enhanced by adopting approaches used to reduce

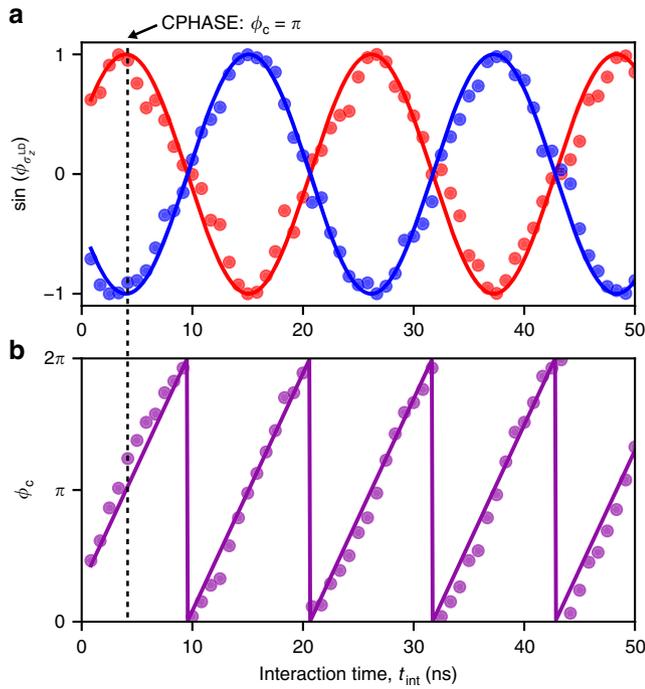


Fig. 3 Controlled-phase evolution. **a** Interaction time t_{int} dependence of $\phi_{\sigma_z^{\text{LD}}}$ controlled by Q_{LD} . The blue and red data are for $Q_{\text{LD}} = |\uparrow\rangle$ and $|\downarrow\rangle$, respectively. The solid curves are $\sin(\pi J^{\text{QQ}}(t_{\text{int}} + t_0)/h)$ (red) and $\sin(-\pi J^{\text{QQ}}(t_{\text{int}} + t_0)/h)$ (blue) where the values of J^{QQ} and t_0 are obtained in the MLE. The curves are consistent with the data as expected. **b** Controlled-phase $\phi_c = \phi_{|\downarrow\rangle} - \phi_{|\uparrow\rangle}$ extracted from Fig. 3a. Including the initial phase accumulated during gate voltage ramps at stage F, ϕ_c reaches π first at $t_{\text{int}} = 4.0$ ns and increases by π in every 5.5 ns afterwards

the sensitivity to charge noise in exchange gates such as symmetric operation^{31,32} and operation in an enhanced field gradient³³.

Finally we show that the CPHASE gate operates correctly for arbitrary Q_{LD} input states. We implement the circuit shown in Fig. 4a in which t_{int} is fixed to yield $\phi_c = \pi$, while a coherent initial Q_{LD} state with an arbitrary σ_z^{LD} is prepared by EDSR. We extract the averaged $\phi_{\sigma_z^{\text{LD}}}$, $\langle \phi_{\sigma_z^{\text{LD}}} \rangle$ by Bayesian estimation^{29,30}, which shows an oscillation as a function of t_{MW} in agreement with the Rabi oscillation measured independently by reading out Q_{LD} at stage C as shown in Fig. 4b (see Methods for the estimation procedure and the origin of the low visibility, i.e., $\max|\langle \phi_{\sigma_z^{\text{LD}}} \rangle| < \pi/2$). These results clearly demonstrate the CPHASE gate functioning for an arbitrary Q_{LD} input state.

Discussion

In summary, we have realized a fast quantum interface between a LD qubit and a ST qubit using a TQD. The CPHASE gate between these qubits is performed in 5.5 ns, much faster than its dephasing time of 211 ns and those ratio (~ 38) would be high enough to provide a high-fidelity CPHASE gate (Supplementary Note 8). Optimizing the magnet design to enhance the field gradient would allow even faster gate time beyond GHz with larger J^{QQ} . At the same time, this technique is directly applicable to Si-based devices with much better single-qubit coherence^{5–9}. Our results suggest that the performance of certain quantum computational tasks can be enhanced by adopting different kinds of qubits for different roles. For instance, LD qubits can be used for high-fidelity control and long memory and the ST qubit for fast initialization and readout. This combination is ideal for

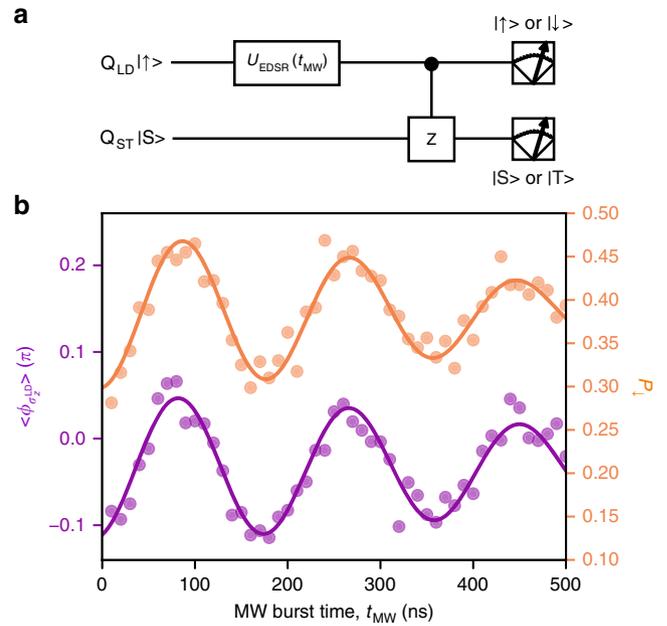


Fig. 4 Demonstration of the controlled-phase gate for arbitrary control qubit states. **a** The circuit for CPHASE gate demonstration. Here t_{int} is fixed at 4.2 ns where $\phi_c \approx \pi$ (Fig. 3b). **b** t_{MW} dependence of the spin-down probability of Q_{LD} , P_{\downarrow} (yellow) and the averaged $\phi_{\sigma_z^{\text{LD}}}$, $\langle \phi_{\sigma_z^{\text{LD}}} \rangle$ (purple) obtained by the circuit shown in Fig. 4a. $\langle \phi_{\sigma_z^{\text{LD}}} \rangle (= -\pi \langle \sigma_z^{\text{LD}} \rangle / 2)$ is expected to be proportional to P_{\downarrow} . We see $\langle \phi_{\sigma_z^{\text{LD}}} \rangle$ oscillates depending on the input Q_{LD} state. The oscillation visibility of $\langle \phi_{\sigma_z^{\text{LD}}} \rangle$ is most probably limited by low preparation fidelity of the input Q_{LD} state as the visibility of the oscillation in P_{\downarrow} is also low (see Methods)

example, the surface code quantum error correction where a data qubit must maintain the coherence while a syndrome qubit must be measured quickly³⁴. Furthermore, the fast (~ 100 ns²⁵) ST qubit readout will allow the read out of a LD qubit in a quantum-non-demolition manner³⁵ with a speed three orders of magnitude faster than a typical energy-selective tunneling measurement^{16,17}. Viewed from the opposite side, we envisage coupling two ST qubits through an intermediate LD qubit, which would boost the two ST qubit gate speed by orders of magnitude compared to the demonstrated capacitive coupling scheme¹⁴. In addition, our results experimentally support the concept of the theoretical proposal of a fast two-qubit gate between two ST qubits based on direct exchange³⁶ which shares the same working principle as our two-qubit gate. Our approach will further push the demonstrated scalability of spin qubits in quantum dot arrays beyond the conventional framework based on a unique spin-qubit encoding.

Methods

Device design. Our device was fabricated on a GaAs/Al_{0.3}Ga_{0.7}As heterostructure wafer having a two-dimensional electron gas 100 nm below the surface, grown by molecular beam epitaxy on a semi-insulating (100) GaAs substrate. The electron density n and mobility μ at a temperature of 4.2 K are $n = 3.21 \times 10^{15} \text{ m}^{-2}$ and $\mu = 86.5 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ in the dark, respectively. We deposited Ti/Au gate electrodes to define the TQD and the charge sensing single electron transistor. A piece of Co metal (micro-magnet, MM) is directly placed on the surface of the wafer to provide a local magnetic field gradient in addition to the external magnetic field applied in-plane (along z). The MM geometry is designed based on the numerical simulations of the local magnetic field²³. The field property is essentially characterized by the two parameters²³, dB_x/dz at the position of each dot and the difference in B_z between the neighboring dots, ΔB_z (see Fig. 1a for the definition of the x and z axes). dB_x/dz determines the spin rotation speed by EDSR and is as large as $\sim 1 \text{ mT nm}^{-1}$ at the left dot (Supplementary Fig. 5a) allowing fast control of Q_{LD} ($f_{\text{Rabi}} > 10 \text{ MHz}$)^{20,23}. At the same time ΔB_z between the left and center dots, ΔB_z^{LC} , is designed to be $\sim 60 \text{ mT}$ (Supplementary Fig. 5b) to guarantee the selective EDSR

control of Q_{LD} without rotating the spin in the center dot^{20,23}. Furthermore, ΔB_z between the center and right dots, ΔB_z^{CR} , is designed to be ~ 40 mT (Supplementary Fig. 5b) to make the eigenstates of Q_{ST} $|\uparrow\downarrow\rangle$ and $|\downarrow\uparrow\rangle$ rather than $|S\rangle$ and $|T\rangle$ by satisfying $\Delta E_z^{ST} \gg J^{ST}$. Note that $\Delta E_z^{ST} = |g|\mu_B\Delta B_z^{CR}$ where $g \sim -0.4$ and μ_B are the electron g -factor and Bohr magneton, respectively. From the design we expect a large variation of ΔB_z^{CR} when the electron in the center dot is displaced by the electric field. Indeed, we observe a strong influence of the gate voltages on ΔB_z^{CR} , which reaches ~ 100 mT ($\Delta E_z^{ST}/h \sim 500$ MHz) in the configuration chosen for the two-qubit gate experiment.

Estimation of the ST precession parameters. Here we describe the estimation of the ST precession parameters in Eq. 2 under the influence of a fluctuating single-qubit phase of Q_{ST} . Out of the parameters involved, $\phi_{\sigma_{LD}}$ is the only parameter assumed to be Q_{LD} state-dependent, and the rest is classified into two types. One is the pulse-cycle-independent parameters, a, b, J^{QQ}, T_2^* and t_0 which is constant during the experiment, and the other is the pulse-cycle-dependent parameters, $\sigma_z^{LD}, \Delta E_z^{ST}$ and ϕ_0 , which can change cycle by cycle. Each pulse cycle consists of pulse stages from A to C as shown in Fig. 2b. We run the pulse cycle consecutively with a MW frequency fixed at 17.26 GHz and collect the data while Q_{LD} drifts between on-resonances and off-resonances with the MW burst due to the nuclear field fluctuation. To decrease the uncertainty of the estimated parameters, we choose the cycles during which the spin flip of Q_{LD} is unlikely in the following manner. The cycles throughout which Q_{LD} is likely to be $|\downarrow\rangle$ are post-selected by the condition that Q_{LD} is on-resonance (i.e., Rabi oscillation of Q_{LD} is observed in ensemble-averaged data from nearby cycles) and the final state of Q_{LD} is measured to be $|\downarrow\rangle$ at pulse stage C. Similarly, the cycles for $Q_{LD} = |\uparrow\rangle$ are post-selected by the condition that Q_{LD} is off-resonance and the final state of Q_{LD} is measured to be $|\uparrow\rangle$. The data structure and the index definitions for MLE are summarized in Supplementary Table 1. k is the index of the interaction time such that $t_{int} = 0.83 \times k$ ns with k ranging from 1 to 100. m is the pulse-cycle index ranging from 1 (2001) to 2000 (4000) for Q_{LD} prepared in $|\uparrow\rangle$ ($|\downarrow\rangle$). The estimation procedure is the following. From all the readout results of Q_{ST} (stage H) obtained in the cycles, we first estimate the five pulse-cycle-independent parameters by MLE. Note that J^{QQ} may have a small pulse-cycle-dependent component due to charge noise but this effect is captured as additional fluctuation in ΔE_z^{ST} and ϕ_0 in our model. We apply MLE to 100×4000 readout results of Q_{ST} , $r_m^k = 1$ (0) for $Q_{ST} = |S\rangle$ ($|T\rangle$). To this end, we first introduce the likelihood P_m defined in the eight dimensional parameter space as

$$P_m(a, b, t_0, J^{QQ}, T_2^*, \sigma_z^{LD}, \phi_0, \Delta E_z^{ST}) = \prod_{k=1}^{100} (r_m^k P_{S,model} + (1 - r_m^k)(1 - P_{S,model})) \quad (3)$$

where $P_{S,model}$ is defined in Eq. (2). We calculate P_m on a discretized space within a chosen parameter range (Supplementary Table 2) using a single cycle data. Then we obtain P_m for the target five parameters as a marginal distribution by tracing out the pulse-cycle-dependent parameters,

$$P_m(a, b, t_0, J^{QQ}, T_2^*) = \sum_{\sigma_z^{LD}} \sum_{\phi_0} \sum_{\Delta E_z^{ST}} P_m(a, b, t_0, J^{QQ}, T_2^*, \sigma_z^{LD}, \phi_0, \Delta E_z^{ST}). \quad (4)$$

Repeating this process for all pulse cycles, we obtain the likelihood P as

$$P(a, b, t_0, J^{QQ}, T_2^*) = \prod_m P_m(a, b, t_0, J^{QQ}, T_2^*). \quad (5)$$

We choose the maximum of P as the estimator for a, b, t_0, J^{QQ} and T_2^* , obtaining $a = 0.218 \pm 0.005$, $b = 0.511 \pm 0.003$, $t_0 = 1.53 \pm 0.17$ ns, $J^{QQ}/h = 90.2 \pm 0.3$ MHz, $T_2^* = 211 \pm 37$ ns.

Once these values are fixed, we estimate the pulse-cycle-dependent parameters, σ_z^{LD}, ϕ_0 and ΔE_z^{ST} , for each cycle m . Note that σ_z^{LD} could be prepared deterministically if the state preparation of Q_{LD} were ideal, but here we treat it as one of the parameters to be estimated because of a finite error in the Q_{LD} state preparation. We again evaluate the likelihood $P_m(\sigma_z^{LD}, \phi_0, \Delta E_z^{ST})$ defined in a discretized three dimensional space of its parameters using Eq. 3 and find their values that maximize the likelihood.

Based on the values of a, b, T_2^* and ϕ^{ST} determined above, we can directly estimate $\phi_{\sigma_{LD}}$ controlled by Q_{LD} for each t_{int} without presumptions on the value of J^{QQ} . To this end, we search for the parameter $\phi_{\sigma_{LD}}$ that maximizes the likelihood

$$P^k(\phi_{\sigma_{LD}}) = \prod_m (r_m^k P_{S,model} + (1 - r_m^k)(1 - P_{S,model})). \quad (6)$$

The obtained estimators for $\phi_{|\downarrow\rangle}$ and $\phi_{|\uparrow\rangle}$ are consistent with the expected values $\pm\pi J^{QQ}(t_{int} + t_0)/h$ calculated from J^{QQ}/h and t_0 found above (see Fig. 3a).

The ensemble-averaged phase $\langle \phi_{\sigma_{LD}} \rangle$ is obtained based on a similar estimation protocol. Here we estimate $\phi_{\sigma_{LD}}$ for each m with fixed $k = 5$ ($t_{int} = 4.2$ ns) to yield

$\phi_C \approx \pi$ from the likelihood $P_m^{k=5} = r_m^{k=5} P_{S,model} + (1 - r_m^{k=5})(1 - P_{S,model})$ and then take the average of the estimated values for 800 pulse cycles. The oscillation visibility of $\langle \phi_{\sigma_{LD}} \rangle$ in Fig. 4b is limited by three factors, low preparation fidelity of the input Q_{LD} state, estimation error of $\phi_{\sigma_{LD}}$ and CPHASE gate error. The first contribution is likely to be dominant as the visibility of the oscillation in P_{\downarrow} is correspondingly low. Note that the effect of those errors is not visible in Fig. 3 because the most likely values of $\phi_{\sigma_{LD}}$ are plotted.

Data availability

The data that support the findings of this study are available from the corresponding authors upon reasonable request.

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Author contributions

A.N. and J.Y. conceived the experiment. A.N. and T.N. performed the measurement with the assistance of K.K., Y.K., M.R.D., T.O., K.T., S.A., and G.A. A.N. and T.N. conducted data analysis with the inputs from J.Y., P.S., and D.L. A.N. and T.N. fabricated the device on the heterostructure grown by A.L. and A.D.W. A.N. and T.N. wrote the manuscript with inputs from other authors. All authors discussed the results. The project was supervised by S.T.

Additional information

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