

The Flory–Huggins Interaction Parameter and Thermoreversible Gelation of Poly(vinylidene fluoride) in Organic Solvents

Masaru OKABE, Risei WADA, Michiko TAZAKI, and Terutake HOMMA

*Department of Applied Chemistry, Faculty of Engineering, Kanagawa Institute of Technology,
1030 Shimo-ogino, Atsugi, Kanagawa 243–0292, Japan*

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ABSTRACT: The Flory–Huggins interaction parameter (χ_{12}) between poly(vinylidene fluoride) (PVdF) and organic solvent was estimated experimentally over wide range of temperature by an inverse gas chromatography (IGC) using many kinds of solvents such as alkane, alkene, ketone, lactone, and nitrogen-containing solvent. The thermoreversible gelation of PVdF solution was discussed from the magnitude of interaction parameter χ_{12} between PVdF and solvent. The parameter χ_{12} was measured for a concentrated PVdF solution by the usual IGC technique. The parameter χ_{12} obtained for each PVdF/solvent system increased slowly with decreasing temperature. The present systems were divided broadly into three groups according to the magnitude of χ_{12} in the vicinity of room temperature, *i.e.*, group (a) with $\chi_{12} \gg 0.5$, group (b) with $\chi_{12} \approx 0.5$, and group (c) with $\chi_{12} \ll 0.5$. The group (b), to which ketone and lactone belong, converted to thermoreversible gels accompanying with crystallization of polymer. The gelation process of PVdF solution was investigated through measurement of *in situ* Fourier transform infrared (FT-IR) spectroscopy. The time-resolved FT-IR spectra suggested that the gelation took place taking the conformation $T_3GT_3\bar{G}$ for the system where the parameter χ_{12} was nearly equal to 0.5 such as PVdF in γ -butyrolactone. For the system where the parameter χ_{12} became larger than 0.5 such as PVdF in cyclohexanone, 3-pentanone, 3-hexanone, 3-heptanone, or 3-octanone, the gelation occurred taking the conformation $TGT\bar{G}$.

KEY WORDS Thermoreversible Gel / Poly(vinylidene fluoride) / Time-Resolved FT-IR / Flory–Huggins Interaction Parameter / Inverse Gas Chromatography (IGC) / Sol–Gel Transition /

It is well known that the semicrystalline poly(1,1-difluoroethylene) (hereafter named poly(vinylidene fluoride) (PVdF)) takes at least three types of crystalline structures, *i.e.*, α -type (conformation: $TGT\bar{G}$), β -type (T), and γ -type ($T_3GT_3\bar{G}$) structures, depending on the preparation conditions of the polymer such as solution-casting or melt-crystallization techniques. For example, the structure of β -type crystal can be obtained from the solution-cast film of the PVdF/hexamethylphosphorotriamide (HMPTA) system, while the γ -type crystal is obtained by casting from a PVdF/dimethylacetamide (DMA) solution. The α -type is known to be the most stable structure, and can be obtained by casting from a PVdF/acetone solution. Another methods for obtaining these crystalline structures have been also reported.^{1–6}

According to the polarity of the bonds between the relatively electron-rich CH_2 carbon atoms and the relatively electron-poor CF_2 carbon atoms, the repeating unit CF_2CH_2 of PVdF chain has a dipole moment.⁷ As the PVdF polymer shows the ferroelectric behavior,¹ there is much current interest in solution-casting techniques for fabricating this polymer for sonar and acoustic devices.

Recently, PVdF in some ketones or lactones was found to convert to thermoreversible gel when the solution was cooled to room temperature. This gel is now

utilized as binder for positive and negative electrodes in a lithium ion battery. The thermoreversible gelation of crystalline or semicrystalline polymer in solvents is considered to take place in consequence of formation of the network structure whose junction points consist of crystallites. This concept has been widely supported by the X-ray diffraction measurement and kinetics as well as thermodynamics of gel-melting behavior of crystallites.⁸

The structure and physical properties of PVdF gel have been studied by many workers.^{9–13} The present authors investigated gelation process of PVdF homopolymer in many organic solvents from measurements of both time-resolved Fourier transform infrared (FT-IR) spectroscopy and dilatometry.^{14–17} Tashiro *et al.* studied the structural change during the gelation process and the resultant aggregation structure of PVdF polymer and solvent molecules in the gel through measurement of the time-resolved FT-IR.¹⁸ Hong and Chou studied the relation between phase separation behavior and gelation kinetics in PVdF/tetra(ethylene glycol) dimethyl ether (TG) solution.¹⁹ They clarified the effects of the crystallization and phase separation on the gelation of PVdF/TG solution in terms of thermodynamic and kinetic aspects.

In order to discuss more generally whether a PVdF solution converts to thermoreversible gel or not, and

Table I. Physical properties of PVdF samples

Sample	$\overline{M}_w \times 10^{-4}$ ^a	T_m ^b °C	X_c ^c %	comonomer	HFP ^d content %
Homopolymer					
PVdF850	30.7	177.9	61.7	—	—
PVdF1000	37.2	177.1	60.7	—	—
PVdF1100	42.7	177.2	59.9	—	—
PVdF1600	82.7	176.7	59.0	—	—
Copolymer					
PVdF2100	40.0	154.8	53.6	HFP ^d	8
PVdF2300	25.0	138.2	39.8	HFP ^d	12

^aWeight-average molecular weight determined by the intrinsic viscosity in *N,N*-dimethylacetamide (DMA) at 25 °C, using the following equation:³² $[\eta] = 2.01 \times 10^{-4} \overline{M}_w^{0.675}$. ^bMelting temperature measured by DSC. ^cDegree of crystallinity estimated from DSC using eq 1. ^dHexafluoropropylene.

furthermore to discuss the stability of PVdF/organic solvent gel, it is very important to investigate the gelation phenomenon from the viewpoint of the magnitude of interaction between PVdF and solvent. Such thermodynamic study has not been carried out.

In this study, the Flory–Huggins interaction parameter (χ_{12}) between PVdF and solvent is estimated from an inverse gas chromatography (IGC) measurement using both homopolymer and copolymer. The correlation between thermoreversible gelation of PVdF solution and the magnitude of χ_{12} is then examined using a large number of solvents of chemically different groups such as ketone, lactone, alkane, alkene, or nitrogen-containing solvent. Another purpose of this study is to obtain experimentally both sol→gel and gel→sol transition temperatures as a function of polymer concentration.

EXPERIMENTAL

Materials

Four samples of PVdF homopolymers and two samples of copolymers (comonomer is hexafluoropropylene (HFP)), supplied by Kureha Chemical Industry Co., were used. These copolymers are heterogeneous in composition. Physical properties of the samples are summarized in Table I. Each sample has different molecular weight (\overline{M}_w) and degree of crystallinity (X_c).

The values of X_c were estimated by means of differential scanning calorimetry (DSC) using the following equation:

$$X_c[\%] = [\Delta H_m^s / \Delta H_m^*] \times 100 \quad (1)$$

where ΔH_m^s and ΔH_m^* are the heats of fusion of the present sample and perfectly crystalline PVdF, respectively. A Shimadzu heat flux differential scanning calorimeter (Model DSC-50) was used for measurement of ΔH_m^s after calibration with standard indium

($T_m = 156.6$ °C; $\Delta H_m = 28.5$ J g⁻¹). All DSC experiments were carried out at a heating rate of 10 °C min⁻¹ under a constant flow of N₂ gas. In this study, a value of 104.7 J g⁻¹ was used for ΔH_m^* in eq 1, whose value was reported by Rosenberg *et al.*²⁰

The solvents (probes) used were hexane, *m*-xylene, 3-pentanone, 3-hexanone, 3-heptanone, 3-octanone, cyclohexanone, γ -butyrolactone, *N,N*-dimethylacetamide (DMA), and *N*-methyl-2-pyrrolidinone (NMP). These solvents are reagent grade, and were used without further purification.

Inverse Gas Chromatography (IGC)

The interaction parameter χ_{12} between polymer and solvent was estimated by an IGC measurement. According to the IGC method, the parameter χ_{12} can be obtained easily over wide range of temperature. The column preparation was carried out as follows: A definite amount of PVdF sample was dissolved completely in dimethylformamide (DMF) under stirring. As a support, Chromosorb WAW-DMCS 60/80 mesh was used, which is a good solid support for IGC measurement. The coating with PVdF was carried out by the method recommended by Al-Saigh and Munk.^{21,22} A PVdF/DMF solution was deposited on the Chromosorb. The solution on the Chromosorb was evaporated by gentle stirring and heating on a hot plate.

A solid support (Chromosorb) coated with PVdF sample was dried under reduced pressure at 50 °C for 24 h, and packed tightly into a stainless steel column with 2.2 mm in diameter and 2 m in length. The weight of polymer (W in eq 2) in the column was determined by weighing of the column before and after coating. An IGC experiment was carried out by increasing the column temperature using a GL Science GC-380 type gas chromatograph equipped with a flame ionization detector (FID). Helium gas was used as a carrier, while methane gas was used as a noninteracting marker. The

helium carrier gas was introduced at a flow rate of 25 mL min^{-1} . The retention time (Δt in eq 3) was determined from the difference between maximum peaks of marker t_M (CH_4 gas) and probe t_P (solvent).

Fourier Transform Infrared Measurement

The FT-IR measurement of a PVdF solution was carried out using a JASCO FT-IR spectrometer, Model FT/IR-660. A PVdF solution with the given concentration was poured into a KRS-5 cell placed in the FT-IR spectrometer. The FT-IR spectra were recorded by the ATR (attenuated total reflection) method at intervals of 10 s with the wavelength resolution of 4 cm^{-1} .

Sol→Gel and Gel→Sol Transition Temperatures

Sol→gel transition temperatures were determined as follows: A PVdF solution (170°C) with a given concentration in a sealed glass tube (*ca.* 35 cm in length and 1 cm in diameter) was immersed in a thermobath kept at an appropriate temperature (T_{gel}) for 12 h. A steel ball of *ca.* 30 mg weight with 2 mm in diameter was then put on the surface of the PVdF/solvent system in the glass tube to examine whether it would ride or not. If so, such a system was defined as a gel. When the steel ball moved downwards, such a system was defined as a sol and the system was heated once more at 170°C in order to dissolve the polymer. The same measurement was then repeated lowering the gel-forming temperature T_{gel} of the thermobath.

Gel→sol transition (gel-melting) temperature (T_{m}^{g}) was measured by the ball-drop method using a steel ball of *ca.* 30 mg weight, whose size did not influence T_{m}^{g} . A PVdF solution at elevated temperature (170°C) in a sealed glass tube was cooled at 30°C for 12 h to prepare a gel. The gel in the glass tube was heated at *ca.* $0.3^\circ\text{C min}^{-1}$, while the height of the steel ball placed on the surface of gel layer was recorded by a cathetometer as a function of temperature. The gel-melting temperature T_{m}^{g} was determined by the method proposed by Takahashi.²³

RESULTS AND DISCUSSION

The Flory–Huggins Interaction Parameter

The retention volume (V_g) at polymer loading W in the column was calculated using the following equation²⁴:

$$V_g = \frac{\Delta t \times F \times (P_0 - P_w) \times (273.15)}{W \times P_0 \times T_r} \times \frac{3[(P_i/P_w)^2 - 1]}{2[(P_i/P_w)^3 - 1]} \quad (2)$$

with

$$\Delta t = t_P - t_M \quad (3)$$

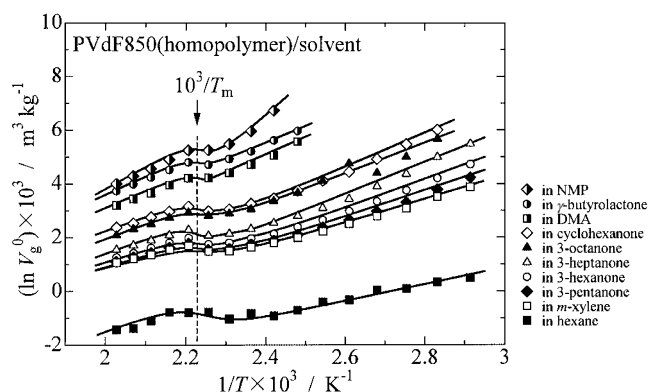


Figure 1. Relation between $\ln V_g^0$ and reciprocal of temperature ($1/T$), where V_g^0 is the specific retention volume.

where

- V_g [mL g^{-1}]: retention volume;
- F [mL s^{-1}]: flow rate of carrier gas;
- P_0 [Pa]: pressure of outlet;
- P_w [Pa]: vapor pressure of water at room temperature T_r ;
- P_i [Pa]: pressure of inlet;
- W [g]: weight of polymer;
- T_r [K]: room temperature;
- t_P [s]: retention time of probe;
- t_M [s]: retention time of marker.

The retention volume V_g calculated by eq 2 was extrapolated to infinite loading in order to obtain the specific retention volume (V_g^0). The retention diagram was obtained as shown in Figure 1 by plotting logarithm of V_g^0 vs. reciprocal of the absolute temperature ($1/T$). As seen in Figure 1, a Z-shaped curve was obtained for each PVdF/solvent system and a retention diagram was nearly linear before and after the reciprocal of melting temperature of the sample ($10^3/T_m$ shown in Figure 1). It is well known that this behavior is characteristic for crystalline or semicrystalline polymers.^{24,25}

The Flory–Huggins interaction parameter χ_{12} was calculated by the following equation²⁴ using the data V_g^0 in Figure 1:

$$\chi_{12} = \ln \frac{(273.15) \times R \times V_2}{V_g^0 \times V_1 \times P_1^0} - 1 - \frac{P_1^0}{R \times T} (B_{11} - V_1) \quad (4)$$

where

- V_1 [$\text{m}^3 \text{ mol}^{-1}$]: molar volume of probe;
- P_1^0 [J m^{-3}]: vapor pressure of probe;
- V_2 [$\text{m}^3 \text{ kg}^{-1}$]: specific volume of polymer at column temperature;
- R [J K mol^{-1}]: gas constant;
- B_{11} [$\text{m}^3 \text{ mol}^{-1}$]: the second virial coefficient of probe in a gaseous state;
- V_g^0 [$\text{m}^3 \text{ kg}^{-1}$]: specific retention volume.

The values of V_1 , P_1^0 , and B_{11} in eq 4 were calculated

using the method reported by Daubert and Danner.²⁶ The parameter χ_{12} thus obtained for many kinds of solvents was plotted against temperature T as shown in Figure 2, which is the data of copolymer (PVdF2300). As seen in Figure 2, the parameter χ_{12} increased slowly with decreasing temperature for any solvent. That is, each solvent behaves as a poor solvent for PVdF with decreasing temperature.

The characteristic result is that the present systems are classified broadly into three groups, *i.e.*, group (a), (b), and (c), according to the magnitude of χ_{12} in the vicinity of room temperature as shown in Figure 2:

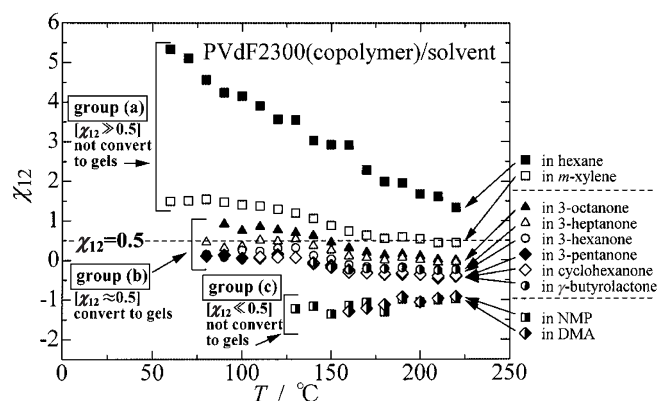


Figure 2. Relation between the Flory-Huggins interaction parameter (χ_{12}) and temperature (T), which was measured for the sample PVdF2300 (copolymer) in ten kinds of organic solvents.

(1) Solvents in the group (a) are alkane and alkene such as hexane and *m*-xylene, and this group shows $\chi_{12} \gg 0.5$; (2) Solvents in the group (b) are ketones and lactone such as 3-octanone, 3-heptanone, 3-hexanone, 3-pentanone, cyclohexanone, and γ -butyrolactone, and this group shows $\chi_{12} \approx 0.5$; (3) Solvents in the group (c) are polar solvents such as NMP and DMA, and this group shows $\chi_{12} \ll 0.5$. According to the measurement by the ball-drop method, PVdF/organic solvent systems in the group (b) were found to convert to thermoreversible gels near room temperature. The group (a) caused macroscopically the liquid/solid phase separation and crystalline precipitates were separated from a solution with cooling, while the group (c) showed one phase solution even if the PVdF/NMP and PVdF/DMA solutions were cooled to room temperature.

In situ FT-IR Spectra

In the above section, we reported that the PVdF/organic solvent systems with $\chi_{12} \approx 0.5$ converted to thermoreversible gels. It is very interesting to investigate the gelation process of the PVdF/solvent systems having different values of χ_{12} . The gelation process was investigated by *in situ* FT-IR method. Figure 3 shows the time-resolved FT-IR spectra obtained for the sample PVdF850 (homopolymer) in (a) cyclohexanone and (b) γ -butyrolactone. In Figure 3c, PVdF850 in hexane, *m*-xylene, NMP, and DMA did

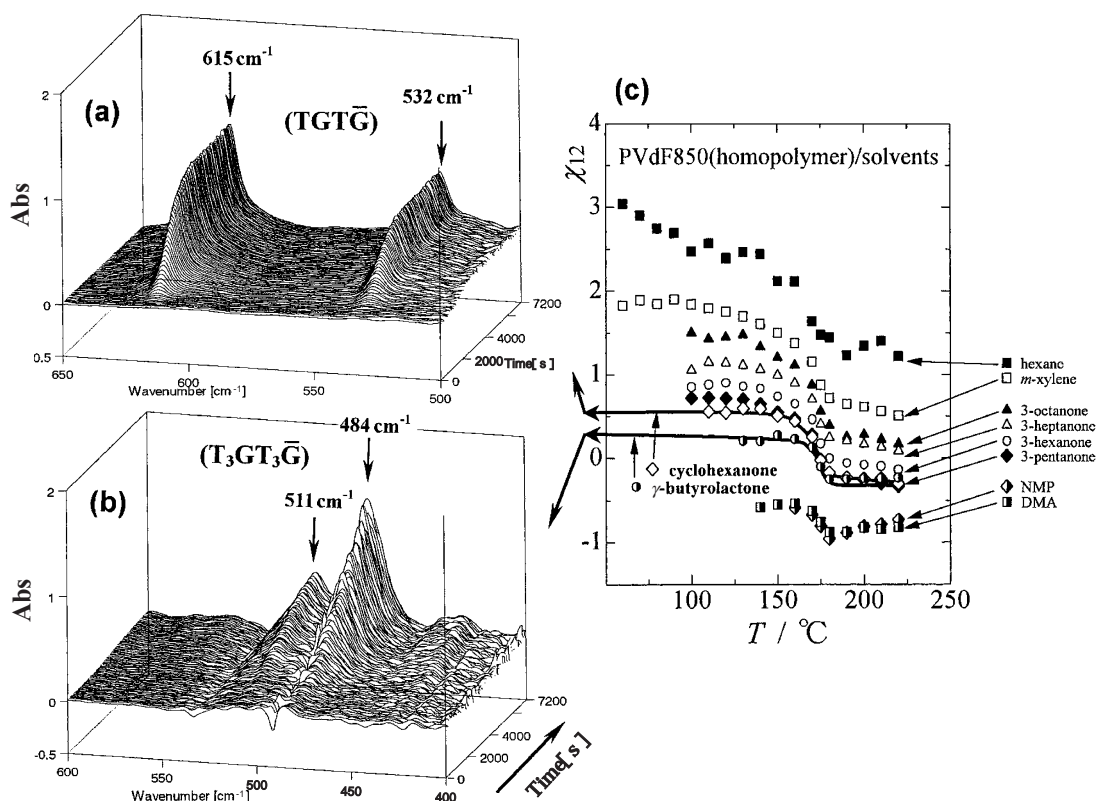


Figure 3. Time dependence of FT-IR spectra obtained for the sample PVdF850 (homopolymer) in (a) cyclohexanone and (b) γ -butyrolactone; and (c) relation between χ_{12} and temperature (T) of PVdF850 in various solvents.

not convert to gel, but did so in γ -butyrolactone, cyclohexanone, 3-pentanone, 3-hexanone, 3-heptanone, and 3-octanone. As seen in Figure 3c, the Flory–Huggins interaction parameter χ_{12} of PVdF850 in cyclohexanone is larger than that in γ -butyrolactone. That is, cyclohexanone behaves as more poor solvent than γ -butyrolactone.

The region 400–600 cm^{-1} is known to be sensitive to the PVdF conformation.^{1,27} In Figure 3a, strong vibrational bands near 615 cm^{-1} and 532 cm^{-1} are observed, and become larger with increasing time. These bands are known to be due to the formation of the conformation TGT \bar{G} . Besides the PVdF850/cyclohexanone system, the same absorption bands were also observed for PVdF850 in other ketones such as 3-pentanone, 3-hexanone, 3-heptanone, or 3-octanone. On the other hand, the absorption bands at 511 cm^{-1} and 484 cm^{-1} in Figure 3b are known to be due to the formation of the conformation T₃GT₃ \bar{G} .

Therefore, it was found from both χ_{12} and *in situ* FT-IR measurements that the thermoreversible gelation of PVdF took place taking the conformation T₃GT₃ \bar{G} for the system where the interaction between PVdF and solvent is relatively large such as the PVdF/ γ -butyrolactone system. While, gelation took place taking the conformation TGT \bar{G} for the system where the interaction becomes smaller ($\chi_{12} > 0.5$) such as PVdF in cyclohexanone, 3-pentanone, 3-hexanone, 3-heptanone, or 3-octanone.

In the previous study,¹⁴ the present authors measured the gelation times (t_{gel}) of two systems: PVdF/ γ -butyrolactone and PVdF/cyclohexanone. In that study, t_{gel} of PVdF in cyclohexanone was found to be smaller than that in γ -butyrolactone. That is, the completion of gelation in cyclohexanone was faster than that in γ -butyrolactone. Taking account of these results, it may be possible to suppose that PVdF random coil chains in a relatively poor solvent such as cyclohexanone gather quickly to crystallize because of small interaction between PVdF and solvent. It is expected, therefore, that the formation of TGT \bar{G} conformation is induced rapidly and, as a result, gelation accompanying with crystallization takes place fast. On the contrary, crystallization of polymers is delayed in γ -butyrolactone because the interaction between PVdF and solvent is large. Accordingly, it is considered that gelation accompanying with crystallization of polymers in γ -butyrolactone takes place slowly.

Sol→Gel and Gel→Sol Transition Temperatures

Figures 4 and 5 show sol→gel transition (gel-forming) and gel→sol transition (gel-melting) temperatures as a function of PVdF concentration in γ -

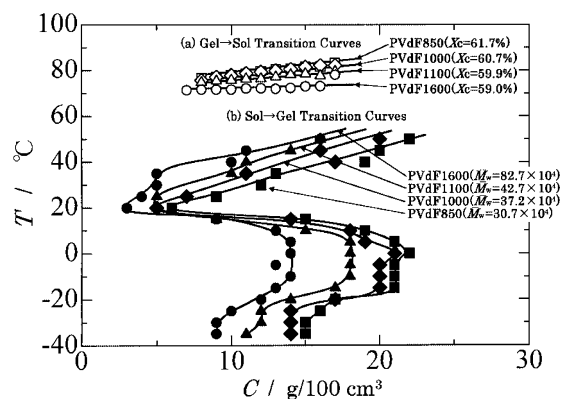


Figure 4. (a) Gel→sol transition curves and (b) sol→gel transition curves measured in γ -butyrolactone.

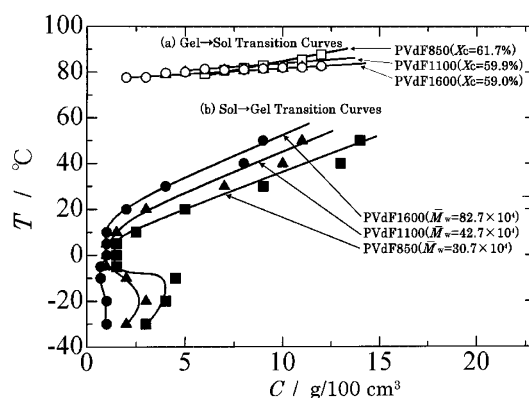


Figure 5. (a) Gel→sol transition curves and (b) sol→gel transition curves measured in cyclohexanone.

butyrolactone and cyclohexanone. As seen in Figure 4b, the sol→gel transition curve obtained for each sample showed an S-shaped curve. In the temperature region $T > 20^\circ\text{C}$, the sol→gel transition temperature showed the lowest value near 20°C without regard to the difference in sample. In other words, a gel having the lowest concentration was formed in the vicinity of 20°C . As a whole, the sol→gel transition curve shifted to lower concentration with increasing molecular weight of \bar{M}_w of sample. In Figure 5b, the similar tendency was obtained as in Figure 4b.

The gel→sol transition (gel-melting) temperatures are shown in Figure 4a and 5a. The gel-melting temperature (T_m^g) of each sample increases gradually with increasing polymer concentration similar to highly crystalline polymer gel such as polyethylene or isotactic polypropylene gel.^{28–30} The molecular weight dependence of T_m^g is not observed in Figure 4a and 5a. It is likely seen that the gel→sol transition curve becomes higher with increasing X_c of sample, though the difference in X_c of the present PVdF samples is not so large.

As seen in Figures 4b and 5b, the sol→gel transition curve of PVdF sample showed a unique behavior. Kaji *et al.* measured the sol→gel transition curves of atactic poly(vinyl alcohol) (at-PVA) in a mixture of dimethyl

sulphoxide (DMSO) and water (60/40 vol/vol) as a function of at-PVA molecular weight.³¹ The transition curves of at-PVA are very similar to the present curves of PVdF/organic solvent systems.

As a PVdF sample is a semicrystalline polymer, the sol→gel transition temperatures may be influenced by the effect of crystallization of polymer. Moreover, the present system is cooled near room temperature and thus it is expected that liquid/liquid phase separation caused by the spinodal decomposition may take place at the early stage of crystallization. Therefore, it is strongly suggested that the sol→gel transition of PVdF/organic solvent system takes place through competition between liquid/liquid phase separation and crystallization. In order to discuss more detail the sol→gel transition curve of PVdF, spinodal decomposition as well as binodal lines must be measured. These problems are left for future study.

CONCLUSION

The present study clarified the following results for the sol–gel transition of PVdF in organic solvents through measurements of time-resolved FT-IR spectrum and polymer/solvent interaction parameter:

1. The Flory–Huggins interaction parameter χ_{12} estimated for PVdF/organic solvent systems were divided into three groups according to the magnitude of χ_{12} in the vicinity of room temperature, *i.e.*, $\chi_{12} \approx 0.5$, $\chi_{12} \gg 0.5$, and $\chi_{12} \ll 0.5$. The thermoreversible gelation took place taking the conformation $T_3GT_3\bar{G}$ in a system where the parameter χ_{12} was nearly equal to 0.5. In a system where the parameter χ_{12} became larger than 0.5, the gelation occurred taking the conformation $TGT\bar{G}$. In a system where $\chi_{12} \gg 0.5$ or $\chi_{12} \ll 0.5$, no gelation occurred.

2. The sol→gel transition (gel-forming) curve shifted to lower concentration with increasing molecular weight, while the gel→sol transition (gel-melting) curve became higher with increasing degree of crystallinity of PVdF sample.

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