

## <sup>13</sup>C NMR Relaxation of Poly(*t*-butyl crotonate) in Solution. Effects of $\beta$ -Substitution on Local Chain Motions

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**ABSTRACT:** Measurement of <sup>13</sup>C spin-lattice relaxation times,  $T_1$ , and nuclear Overhauser effects, NOE, was made as a function of temperature at two magnetic fields for poly(*t*-butyl crotonate), PTBC, and poly(*t*-butyl methacrylate), PTBM, in toluene-*d*<sub>8</sub> to study the effects of  $\beta$ -substitution on local chain motions. For main chain carbons of PTBC and PTBM, experimental  $T_1$  and NOE data were well reproduced by the Dejean–Lauprêtre–Monnerie (DLM) model in the entire temperature range. The model parameters thus obtained differed between PTBC and PTBM. For methyl carbons in the *t*-butyl ester group, the experimental data were analyzed by the models combining the DLM model and multiple internal rotations. The model parameters were almost the same for the two polymers. These results indicate that  $\beta$ -substitution affects the local motion of main chains as well as chain stiffness, but does not significantly affect the local motion of methyl carbons at the ends of side-chains. The correlation between the local dynamics of various polymer chains and chain stiffness is discussed.

**KEY WORDS** <sup>13</sup>C NMR Relaxation / Poly(*t*-butyl crotonate) / Spin-Lattice Relaxation Time / Nuclear Overhauser Effect /  $\beta$ -Substitution / Local Chain Motions / Chain Stiffness /

Static properties such as unperturbed conformation of polymer chains or chain stiffness have been extensively studied theoretically and experimentally,<sup>1,2</sup> whereas, dynamic properties such as local chain motions of polymer chains have been recently studied by various relaxation experiments such as NMR relaxation,<sup>3–5</sup> dielectric relaxation,<sup>6,7</sup> and time-resolved fluorescence.<sup>8</sup> Since both properties are considered closely related,<sup>5,7</sup> it is interesting to study the relationship between them. Previous papers showed by light scattering,<sup>9</sup> intrinsic viscosity<sup>10</sup> and small-angle X-ray scattering measurements<sup>11</sup> that the persistence length of poly(*t*-butyl crotonate), PTBC, is much longer than that of poly(*t*-butyl methacrylate), PTBM. That is, steric hindrance between  $\beta$ -methyl and *t*-butyl ester groups makes polymer chains stiff. Thus, the present work studied the effects of  $\beta$ -substitution on local chain motions, using both PTBC and PTBM.

The NMR relaxation method is quite useful because it provides detailed information about molecular motion of different parts of chain through the spectral density function which is the Fourier transformation of correlation function of the relaxing dipoles in different environments of chains. This work thus studied <sup>13</sup>C NMR relaxation such as spin-lattice relaxation time  $T_1$  and nuclear Overhauser effect, NOE, of PTBC and PTBM at two magnetic field (67.8 and 125.7 MHz) as a function of temperature.

In polymer chains with side-chains, local dynamical processes occur in short segments of both main and side chains. There are various models that describe local chain motion in terms of conformational transition, multiple internal rotation, etc. For main chain motions, Dejean, Lauprêtre, and Monnerie modified the Hall–Weber–Helfand (HWH) model describing the main chain motions in terms of the conformational transitions<sup>12,13</sup>

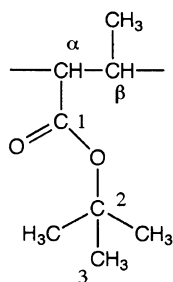
by introducing libration motion of the C–H vector.<sup>14</sup> The Dejean–Lauprêtre–Monnerie (DLM) model is in good agreement with experimental  $T_1$  and NOE data for various polymers in solution or bulk.<sup>14–21</sup> The interesting features of this model include correlation times for damping (single conformational transition), propagation (correlated pair conformational transition) and libration, which can be related with chain stiffness. That is, the degree of damping and propagation along the main chain may be related with the chain stiffness and degree of libration motion may be related to steric environment around a C–H unit. For side-chain motion, the relaxation is more complicated owing to superposition of main chain motions and multiple internal rotations in the side-chain. Several models for multiple internal rotations such as free rotational diffusion, restrict rotational diffusion and three site jump models have been proposed.<sup>22–29</sup> In this work, we analyzed experimental <sup>13</sup>C NMR data of main and side chains by the DLM model and the multiple internal rotations, respectively, to study the effects of  $\beta$ -substitution or chain stiffness on the local chain motions.

### EXPERIMENTAL

PTBC and PTBM samples used here were prepared by anionic polymerization in our laboratory. Details of the preparation are described in a previous paper.<sup>30</sup> Molecular weights were  $M_w = 128000$  and  $32000$ , respectively, determined by GPC calibrated with standard polystyrenes of Tosoh Co. Ltd. and tacticity is atactic. The polymer concentration was 10 wt/vol% in toluene-*d*<sub>8</sub>, purchased from Aldrich Chemical Co. In the main chain carbons in the repeating unit of PTBC, a carbon attached with *t*-butyl ester group is identified as  $\alpha$ -methine carbon and another carbon as  $\beta$ -methine carbon (see Figure 1).

<sup>13</sup>C NMR relaxation experiments were performed with

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**Figure 1.** Labeling scheme of carbon atoms in the repeating unit of PTBC.

Varian unity INOVA 500 and JEOL FX-270 NMR instruments operating at 125.7 and 67.8 MHz for carbon resonance frequency, respectively. Temperatures were regulated within  $\pm 1$  K by a controller.  $T_1$  was measured by conventional inversion recovery using  $180^\circ$ - $\tau$ - $90^\circ$  pulse sequence. 2000–4000 acquisitions were accumulated for a set of 12–14 arrayed  $\tau$  and the delay times between pulse cycles were 5 times longer than maximum  $T_1$ .  $T_1$  was determined by fitting the observed data to a nonlinear exponential function. NOE was evaluated as the ratio of <sup>13</sup>C signal intensities obtained by continuous <sup>1</sup>H decoupling to those obtained by inverse gate decoupling. The delay times for NOE experiments were 10 times longer than maximum  $T_1$ . All sample solutions were degassed, though the experimental data were not seriously affected for the system having a short relaxation time such as polymer solution.<sup>31</sup> The relative error of measured  $T_1$  and NOE values was estimated to be lower than 10 and 15%, respectively.

### THEORETICAL BACKGROUND

Assuming a purely <sup>13</sup>C–<sup>1</sup>H dipolar–dipolar relaxation mechanism, we have the following equations for spin-lattice relaxation time,  $T_1$ , and NOE, under the condition of complete proton decoupling.<sup>22</sup>

$$\frac{1}{T_1} = \frac{N}{10} \left[ \frac{\mu_0 \hbar \gamma_H \gamma_C}{4\pi r^3} \right]^2 [J(\omega_H - \omega_C) + 3J(\omega_C) + 6J(\omega_H + \omega_C)] \quad (1)$$

$$\text{NOE} = 1 + \frac{\gamma_H}{\gamma_C} \left[ \frac{6J(\omega_H + \omega_C) - J(\omega_H - \omega_C)}{J(\omega_H - \omega_C) + 3J(\omega_C) + 6J(\omega_H + \omega_C)} \right] \quad (2)$$

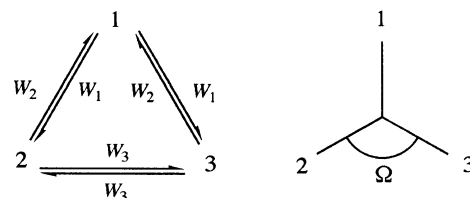
where  $N$ ,  $\mu_0$ , and  $r$  are the number of direct bonded proton, permeability in vacuum, C–H internuclear distance (0.109 nm),<sup>32</sup> respectively,  $\hbar = h/2\pi$  with  $h$  being Planck constant, and  $\gamma_H$ ,  $\gamma_C$ ,  $\omega_H$ , and  $\omega_C$  are the magnetogyric ratios and Larmor frequencies of <sup>1</sup>H and <sup>13</sup>C, respectively. The spectral density function,  $J(\omega)$ , is obtained by the Fourier transformation of the correlation function,  $G(t)$ , derived on the basis of motional models.

$$J(\omega) = \frac{1}{2} \int_{-\infty}^{\infty} G(t) \exp(i\omega t) dt \quad (3)$$

### MOTION MODELS

#### Main Chain Motion

The DLM model<sup>12</sup> describes local chain motions in



**Figure 2.** Schematic illustration of jump model.

terms of conformational transition and libration, which well explain  $T_1$  and NOE data for various polymers in solution and bulk.<sup>12,15–21</sup> The spectral density function,  $J(\omega)$ , of the DLM model is given by

$$J(\omega) = \frac{1-f}{(\alpha + i\beta)^{1/2}} + \frac{f\tau_2}{1 + \omega^2\tau_2^2} \quad (4)$$

with

$$\alpha = \frac{1}{\tau_0^2} + \frac{2}{\tau_0\tau_1} - \omega^2 \quad (5)$$

and

$$\beta = -2\omega \left[ \frac{1}{\tau_0} + \frac{1}{\tau_1} \right] \quad (6)$$

where  $\tau_0$ ,  $\tau_1$ ,  $\tau_2$ , and  $f$  are correlation times for damping, propagation and libration, and relative weight of libration, respectively. According to the theory of Howarth,<sup>33</sup>  $f$  is given by,

$$1-f = \left[ \frac{\cos\theta - \cos^3\theta}{2(1-\cos\theta)} \right]^2 \quad (7)$$

where  $\theta$  is the libration angle of C–H vector.

#### Side-Chain Motion

The relaxation parameters,  $T_1$  and NOE, in side-chain carbons are given by superposing both segmental motions in main chain and multiple internal rotational motions in the side-chain. Motion analysis for methyl carbon in the *t*-butyl ester group was performed by assuming the multiple internal rotations with two axes as described below. Internal rotations around the C<sub>α</sub>–C<sub>1</sub>O and C<sub>1</sub>O–C<sub>2</sub> bonds in the *t*-butyl ester group cannot be evaluated without the following assumption, since there is no hydrogen attached to these bonds as shown in Figure 1, while the rotation around the C<sub>1</sub>–O bond can be neglected because of conjugate nature of the bond. Therefore, we assumed internal rotational motion around C<sub>α</sub>–C<sub>1</sub>O and C<sub>1</sub>O–C<sub>2</sub> bonds as the single rotation around the first axis, which is independent of temperature, *i.e.*, no activation energy, or constant, though, strictly speaking, this assumption may not be valid for relaxation for carbonyl and quaternary carbons in the ester groups because of steric hindrance with the carbonyl groups.

Free rotational diffusion and equivalent three site jump models are useful for describing local motion for end of side-chains<sup>22,23</sup> or internal rotational motion around C<sub>2</sub>–C<sub>3</sub> bonds as the second axis, though the more elaborate analysis was performed for local motions of side-chain.<sup>21</sup> A schematic illustration of jump model is shown in Figure 2, where positions 1, 2, and 3 correspond to the three possible sites which are related to *trans*,

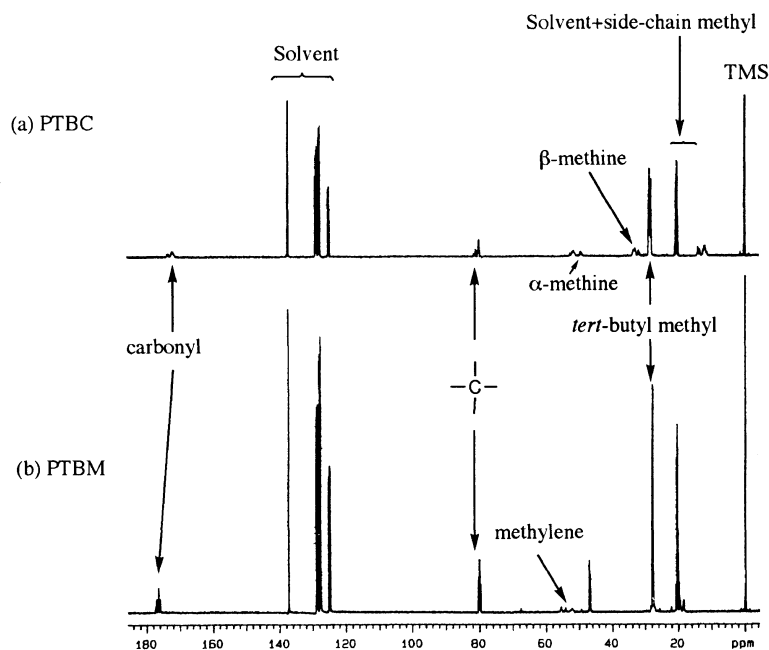


Figure 3.  $^{13}\text{C}$  NMR spectra of PTBC (a) and PTBM (b) at 125.7 MHz.

*gauche*<sup>+</sup>, and *gauche*<sup>-</sup> forms, and  $W_1$ ,  $W_2$ , and  $W_3$  are the respective jump rates (1→2 and 3), (2 and 3→1), and (2↔3) where  $W_i = W_0 \exp(-E_i/RT)$  with  $E_i$ ,  $R$ , and  $T$  the apparent activation energy between sites, gas constant and absolute temperatures, respectively.  $\Omega$  is the angle between site 2 and 3 ( $120^\circ$  for alkyl chain). The jump rates are related with internal correlation time  $\tau_{ir}$  as  $W_i = (6\tau_{ir})^{-1}$  for free rotational diffusion model and  $W_i = (3\tau_{ir})^{-1}$  for an equivalent three site jump model, respectively.

### FITTING PROCEDURE

Experimental  $T_1$  and NOE data were analyzed by motional models as above. According to Helfand,<sup>34</sup> who applied the theory of Kramer<sup>35</sup> for the diffusion of a particle over a potential barrier to conformational transitions of polymer chains, the temperature dependence of the correlation time  $\tau(T)$  is given by the Arrhenius type as,

$$\tau(T) = A \exp(E_a/RT) \quad (8)$$

with  $A = \eta c$  where  $\eta$ ,  $c$ , and  $E_a$  are solvent viscosity, molecular constant and apparent activation energy, respectively. In the fitting procedure,  $A$  and  $E_a$  were treated as adjustable parameters.

$T_1$  and NOE are fitted simultaneously at both magnetic fields as a function of temperature. At first the parameters,  $A$ ,  $E_a$ ,  $f$ ,  $\tau_0/\tau_1$ , and  $\tau_1/\tau_2$  in the DLM model were fitted manually for main chain carbons, and then the parameters of the internal rotation models,  $W_0$  and  $E_i$ , were fitted for the side-chain carbons while the fitting parameters obtained for the main chain carbons were fixed.

### RESULTS

Figure 3 shows the  $^{13}\text{C}$  NMR spectra of PTBC (a) and PTBM (b) in toluene- $d_8$  at 125.7 MHz. Chemical shift

was measured from tetramethylsilane (TMS) resonance as an internal reference and the peaks were assigned as reported previously.<sup>36</sup> Since the peak of  $\beta$ -methyl carbon in the side-chain of PTBC is overlapped by the solvent peaks at about 10–20 ppm,  $T_1$  and NOE of this carbon could not be accurately determined. In this work, therefore, we examined only segmental motion of main chain carbons and multiple internal rotational motion of methyl carbons in *t*-butyl ester groups.

Tables I and II summarize  $^{13}\text{C}$   $T_1$  and NOE data as a function of temperature at the two magnetic fields for PTBC and PTBM, respectively. The data were obtained for the major component of stereo-sequence. The values obtained for minor components almost agree with those of major one within experimental errors. The data in these tables indicate the following specific features. For the main chain carbons of both PTBC and PTBM,  $T_1$  lies on the higher correlation time side of the  $T_1$  minimum, and this is remarkable at the higher magnetic field.  $T_1$  increases with decreasing temperature at both magnetic fields. NOE is significantly smaller than the maximum value (3.0) obtained at the extreme narrowing limit and seem to have a minimum at the lower magnetic field. This implies that the segmental motion in the main chain cannot be explained by the correlation function having a single correlation time.<sup>21</sup>

For side-chain carbons,  $T_1$  of PTBC and PTBM are larger than those of main chain carbons at the entire temperature range. This implies that there is a contribution of multiple internal rotations to the side-chain motions in addition to the segmental motion in the main chain.  $T_1$  of both PTBC and PTBM increase with temperature, but the former is larger. NOE of PTBC is slightly smaller than for PTBM.

### DISCUSSION

Figures 4, 5, and 6 show the best fitting curves of  $T_1$  and NOE vs. temperature, calculated by the parameters

**Table I.** Experimental  $T_1$  (ms) and NOE<sup>a</sup> data of PTBC as a function of temperature in two magnetic fields

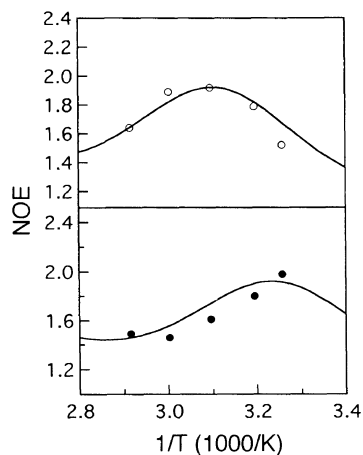
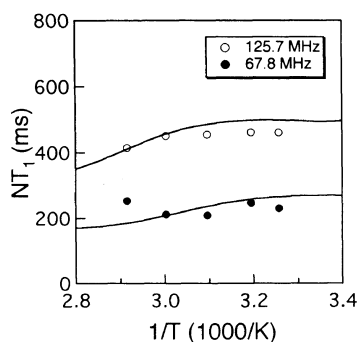
Temp/K	Main chain carbon				Side-chain carbon	
	$\alpha$ -CH		$\beta$ -CH		<i>t</i> -Butyl CH <sub>3</sub>	
	125.7 MHz	67.8 MHz	125.7 MHz	67.8 MHz	125.7 MHz	67.8 MHz
307	461 (1.52)	230 (1.98)	449 (1.67)	231 (1.94)	482 (2.40)	359 (2.40)
313	462 (1.79)	246 (1.80)	438 (1.72)	238 (1.86)	498 (2.40)	373 (2.44)
323	455 (1.92)	208 (1.61)	437 (1.98)	214 (1.65)	569 (2.44)	383 (2.47)
333	451 (1.89)	211 (1.46)	452 (1.75)	229 (1.62)	604 (2.48)	512 (2.44)
343	415 (1.64)	253 (1.49)	416 (1.64)	222 (1.45)	693 (2.48)	601 (2.40)

<sup>a</sup> Values in parentheses.

**Table II.** Experimental  $T_1$  (ms) and NOE<sup>a</sup> data of PTBM as a function of temperature in two magnetic fields

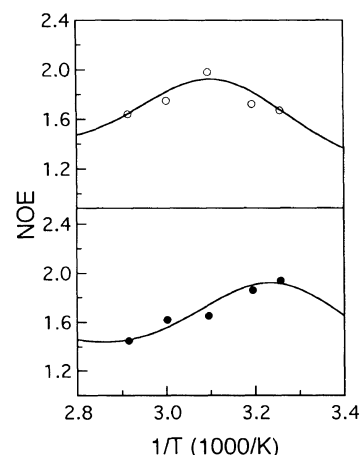
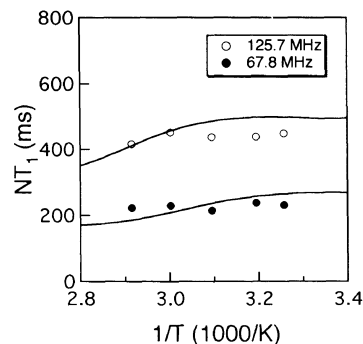
Temp/K	Main chain carbon		Side-chain carbon	
	CH <sub>2</sub>		<i>t</i> -Butyl CH <sub>3</sub>	
	125.7 MHz	67.8 MHz	125.7 MHz	67.8 MHz
303	207 (1.68)	98 (1.75)	383 (2.35)	267 (2.52)
313	196 (1.69)	122 (1.70)	431 (2.45)	282 (2.56)
323	184 (1.75)	94 (1.54)	482 (2.55)	315 (2.56)
333	163 (1.60)	88 (1.58)	542 (2.59)	482 (2.58)
343	158 (1.55)	71 (1.65)	614 (2.49)	558 (2.53)

<sup>a</sup> Values in parentheses.



**Figure 4.** Temperature dependence of  $T_1$  and NOE for  $\alpha$ -methine carbon of PTBC. Solid lines calculated by the DLM model with the parameters listed in Table III.

of the DLM model listed in Table III for  $\alpha$ -,  $\beta$ -methine carbons of PTBC, and methylene carbon of PTBM, respectively. In the entire temperature range, experi-

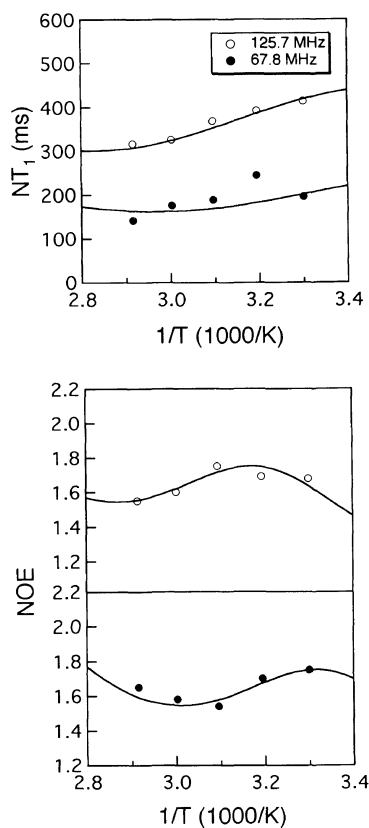


**Figure 5.** Temperature dependence of  $T_1$  and NOE for  $\beta$ -methine carbon of PTBC. Solid lines calculated by the DLM model with the parameters listed in Table III.

mental  $T_1$  and NOE are in good agreement with the DLM model for both polymers. As shown in Table III, there is no significant difference between the model parameters obtained for  $\alpha$ - and  $\beta$ -methine carbons of PTBC. This implies that the segmental motions of  $\alpha$ - and  $\beta$ -methine carbons are governed by the same mechanism of local dynamics. This is reasonable because there is no significant difference in neighboring environments for  $\alpha$ - and  $\beta$ -methine carbons.

Let us compare the parameters of PTBC and PTBM in Table III. The correlation time ratio  $\tau_0/\tau_1$  of the former (1.7) is smaller than that of the latter (2.0). Since the difference in molecular architecture between the two polymers is in the position of methyl unit on the main chains and the former chain is stiffer than the latter chain due to the steric hindrance between  $\beta$ -methyl and *t*-butyl ester groups, this implies that PTBC having the stiffer chain has smaller correlation time ratio.

Thus, let us examine the relationship between the correlation time ratio and the chain stiffness for other polymers having similar molecular architectures, *i.e.*, polyacrylate or polymethacrylate derivatives and vinyl polymers. The chain stiffness can be represented by the characteristic ratio,  $C_\infty = \langle r^2 \rangle_0 / nl^2$ , where  $\langle r^2 \rangle_0$ ,  $n$  and  $l$  are the unperturbed mean square end-to-end distance, degree of polymerization and monomer length, respectively. Table IV lists the correlation time ratios and



**Figure 6.** Temperature dependence of  $T_1$  and NOE for methylene carbon of PTBM. Solid lines calculated by the DLM model with the parameters listed in Table III.

characteristic ratios of the polymers. Here, the characteristic ratio of PTBC was evaluated from the persistence length (*ca.* 1.9–3.1 nm) measured by small angle X-ray scattering.<sup>11</sup> Although the characteristic ratios are unknown for poly(isobutyl methacrylate) (PIBM), poly(naphthyl acrylate) (PNA), and poly(1-naphthylmethyl acrylate) (PNMA), the values of PIBM and PNA may be close to that of PTBM because they have bulky groups similar to *t*-butyl ester, while PNMA may be smaller because a methyl unit intervenes between a carboxyl group and a naphthalene unit. Figure 7 shows a comparison between the correlation time and characteristic ratios. Roughly speaking, this implies that the stiffer the chain is, the smaller the correlation time ratio is. This is understandable because the smaller correlation time ratio means that the propagation of local motion associated with  $\tau_1$  is more restricted by damping associated with  $\tau_0$ .

We compared the activation energy  $E^*$  associated with a potential barrier for conformational transition with the chain stiffness. If eq 8 is valid for the conformational transitions,  $E^*$  is given by

$$E^* = E_a - E_\eta \quad (9)$$

where  $E_\eta$  is the activation energy of solvent viscosity, expressed as  $\eta = B \exp(E_\eta/RT)$  with  $B$  a constant. As reported by Gisser *et al.*,<sup>40</sup> eq 8 is not valid for ordinary flexible chains, and the correlation times are proportional to  $\eta^\alpha$  ( $\alpha = 0.41$ ). In this case we have

$$E^* = E_a - \alpha E_\eta \quad (10)$$

In Table IV  $E_a$  and  $E^*$  are listed, and a comparison

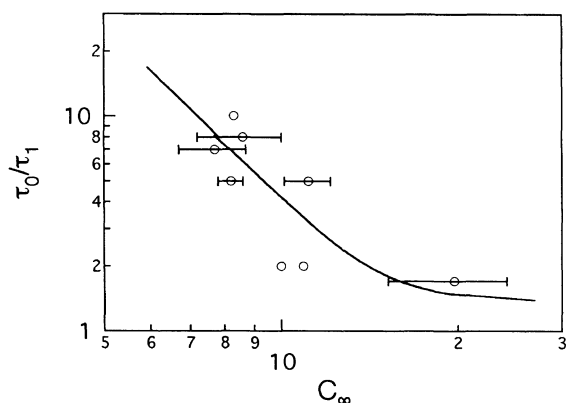
**Table III.** Fitting parameters of the DLM model for main chain carbons of PTBC and PTBM

	$\tau_0/\tau_1$	$\tau_1/\tau_2$	$E_a/\text{kJ mol}^{-1}$	$10^{15} A/s$	$\theta$
PTBC- $\alpha$	1.7	60	38.9	7.4	30.5
PTBC- $\beta$	1.7	60	38.9	7.4	30.5
PTBM	2.0	30	36.4	7.4	30.5

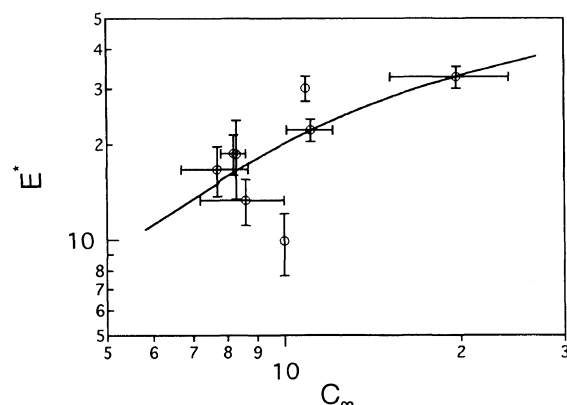
**Table IV.** Correlation time ratio, activation energy, and characteristic ratio for various polymers

	$\tau_0/\tau_1$	$E_a/\text{kJ mol}^{-1}$	$E^*/\text{kJ mol}^{-1}$	$C_\infty^b$	ref
PTBC	1.7	38.9	29.9–35.2	$19.7 \pm 4.5$	This work
PTBM	2	36.4	27.4–32.7	10.9	This work
Poly(isobutyl methacrylate)	2	36.4	27.4–32.7	Unknown	21
PIBM					
Poly(vinyl methyl ether)	2	15.1	7.7–12.1	10.0	12
PVME					
Poly(naphthyl acrylate)	3	24.0	12.0–19.1	Unknown	37
PNA					
Poly(butyl methacrylate)	5	25.0	16.0–21.3	$8.2 \pm 0.4$	38
PBMA					
Poly(hexyl methacrylate)	5	33.0	24.0–20.3	$11.1 \pm 1.0$	38
PHMA					
Poly(1-naphthylmethyl acrylate)	7	25.0	11.3 <sup>c</sup>	Unknown	39
PNMA					
Poly(vinyl chloride)	7	23.9	13.7–19.7	$7.7 \pm 1.0$	18
PVC					
Poly(2-vinyl pyridine)	8	18.5	11.1–15.5	$8.6 \pm 1.4$	19
P2VP					
Poly(vinyl alcohol)	10	30.9	13.4–23.7	8.3	20
PVA					

<sup>a</sup> Largest and smallest values evaluated by eq 9 and 10, respectively. <sup>b</sup> Reference 2 except for PTBC. <sup>c</sup> Equation 9 is valid for this polymer.



**Figure 7.** Plots of the correlation time ratio  $\tau_0/\tau_1$  vs. characteristic ratio  $C_\infty$ . A solid line is drawn as eye guide.



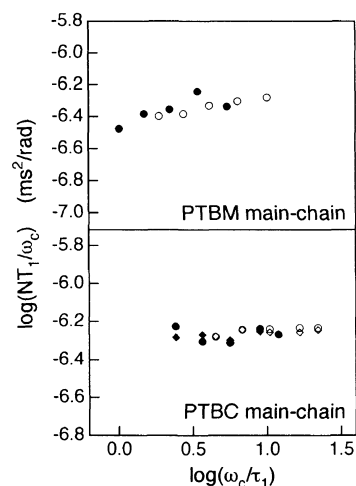
**Figure 8.** Plots of activation energy  $E^*$  for conformational transition vs. characteristic ratio  $C_\infty$ . A solid line is drawn as eye guide.

between  $E^*$  and  $C_\infty$  is shown in Figure 8. It is of much interest that there is a correlation between local chain motion and chain stiffness as shown in Figures 7 and 8 though the origins are different. The former is associated with activation energy of rotation of bonds, while the latter, with difference in the potential minimum.

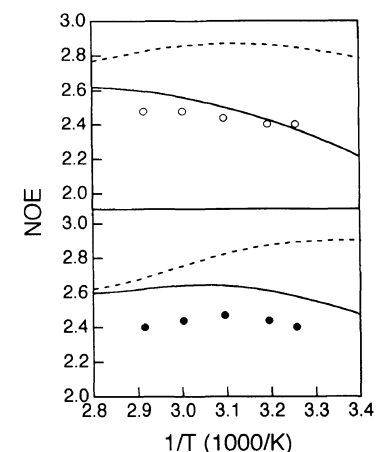
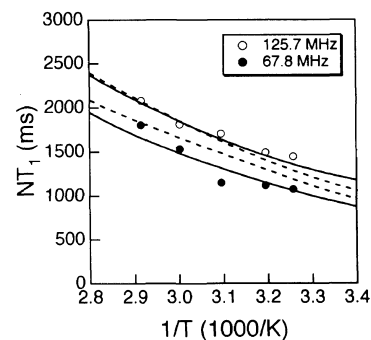
The libration angle  $\theta$  in Table III is the same for  $\alpha$ -,  $\beta$ -methine carbons of PTBC and methylene carbon of PTBM, *i.e.*,  $30.5^\circ$ . This implies that libration motion is not affected by the segmental motions as the former is much faster than the latter.<sup>21</sup> As shown in Table III, another correlation time ratio  $\tau_1/\tau_2$  of PTBC (60) is larger than that of PTBM (30). The propagation may thus be more suppressed for PTBC than for PTBM if we assume that the libration motion is the same for both polymers as above.

Following the method of Guillermo *et al.*,<sup>41</sup>  $\log(NT_1/\omega_c)$  is plotted against  $\log(\omega_c\tau_1)$  for PTBC and PTBM at the two Larmor frequencies in Figure 9.  $T_1$  data superpose fairly well for both polymers. The superposition implies that the mechanism of local motions as reflected in the correlation function,  $G(t)$ , is independent of temperature, and justifies the above analysis.

Figures 10 and 11 show the temperature dependence of  $T_1$  and NOE data for side-chain methyl carbons in *t*-butyl ester group of PTBC and PTBM, respectively. The solid and broken lines are theoretical values calculated by free rotational diffusion and equivalent

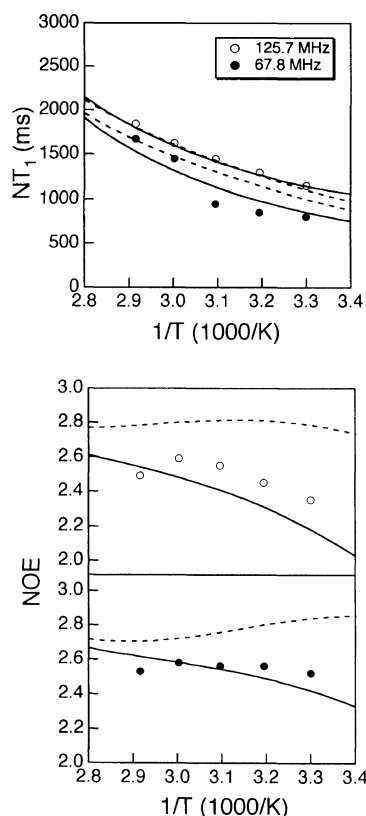


**Figure 9.** Frequency-temperature superposition of  $^{13}\text{C } NT_1$  for the main chain carbons of PTBC and PTBM. Open and filled symbols denote data of 125.7 and 67.8 MHz, respectively. Circle and diamond symbols are data of  $\alpha$ -methine and  $\beta$ -methine carbons, respectively.  $\tau_1$  was evaluated using the DLM model.



**Figure 10.** Temperature dependence of  $T_1$  and NOE for methyl carbon in *t*-butyl ester group of PTBC. Solid and broken lines denote theoretical values of the free rotational diffusion model and three site jump model, respectively.

three site jump models, respectively. Here, we assume that the jump rate for the first axis, *i.e.*, around  $C_\alpha-C_1O$  and  $C_1O-C_2$  bonds is  $W_0 = 3.30 \times 10^{11} \text{ s}^{-1}$  for both PTBC and PTBM, determined so that the experimental data can be reproduced by the model. Even if this value is modified within  $\pm 2.0 \times 10^{11} \text{ s}^{-1}$ , the fitting results would hardly be affected. The model parameters thus obtained are listed in Table V. As shown in Figures 10 and 11,  $T_1$  data of both polymers are more satisfactorily



**Figure 11.** Temperature dependence of  $T_1$  and NOE for methyl carbon in *t*-butyl ester group of PTBM. Solid and broken lines denote theoretical values of the free rotational diffusion model and three site jump model, respectively.

**Table V.** Fitting parameters of free rotational diffusion and three site jump models for side-chain carbons of PTBC and PTBM

	PTBC		PTBM	
	$E_i$	$W_0$	$E_i$	$W_0$
	$\text{kJ mol}^{-1}$	$\text{s}^{-1}$	$\text{kJ mol}^{-1}$	$\text{s}^{-1}$
Free rotational diffusion	19.0	$2.60 \times 10^{12}$	20.8	$3.80 \times 10^{12}$
Three site jump	15.4	$1.57 \times 10^{12}$	14.0	$7.20 \times 10^{11}$

reproduced by the free rotational diffusion model than the equivalent three site jump model, while the NOE data for PTBC at low fields and for PTBM at high fields somewhat deviate from the theoretical values of the free rotational diffusion model having the same parameters as those for fitting  $T_1$  data, but the deviations are within experimental error and the temperature dependence is very similar to the experimental one. As shown in Table V,  $E_i$  and  $W_0$  in the free rotational diffusion model are not much different between two polymers. This implies that the carbons themselves at the ends of side-chains rather freely move irrespective of chain stiffness if we assume that the side-chain rotates freely without the activation energy around the first axis. The overall side-chain motion is affected by the stiffness of main chain through the main chain motion.

## CONCLUDING REMARKS

$^{13}\text{C}$  NMR relaxation measurement of PTBC and PTBM in toluene- $d_8$  was carried out as a function of temperature at two magnetic fields. For main chain carbons of PTBC and PTBM, the  $T_1$  and NOE data were well reproduced by the DLM model, and it was concluded that local motion of main chains is closely related to chain stiffness. For side-chain carbons, the free rotational diffusion model was suitable to describe the experimental data for PTBC and PTBM and this suggests that the ends of side-chains themselves rather freely move irrespective of chain stiffness.

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