Studies on Formaldehyde Resin. XVI. Hydroxymethylation of Melamine with Formaldehyde in Weakly Acidic Region and without Additional Catalyst

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ABSTRACT: Early stage hydroxymethylation of melamine with formaldehyde to form monomethylolmelamine in the weakly acidic region of $0 < S < 1.0$, and in the absence of the catalyst, $S=0$ (pH, *ca.* 3-8) was investigated kinetically at 40°C in aqueous media; here S denotes $[\text{hydrochloric acid}]_0/[\text{melamine}]_0$. As a result, the hydroxymethylation rate in the region of $0 \leq S < 1.0$ was found to be dependent on the concentration of the melamine molecule (base species) MH and its conjugate acid MH_2^+ in the following manner: $\text{rate} = k_{\text{H}_2\text{O}}[\text{MH}][\text{HCHO}] + k_{\text{H}^+}[\text{MH}_2^+][\text{HCHO}] + k_{\text{MH}_2^+}[\text{MH}_2^+][\text{MH}][\text{HCHO}] + k_{\text{MH}}[\text{MH}]^2[\text{HCHO}]$. In particular, the rate at $S=0$ was represented by $\text{rate} = k_{\text{H}_2\text{O}}[\text{MH}][\text{HCHO}] + k_{\text{MH}}[\text{MH}]^2[\text{HCHO}]$. The values of the rate constants ($k_{\text{H}_2\text{O}}$, k_{H^+} , $k_{\text{MH}_2^+}$, and k_{MH}) were obtained, and then the relative contributions of these four reactions at pH 3-8 were made clear in connection with the initial concentration of melamine.

KEY WORDS Melamine / Formaldehyde / Hydroxymethylation / Formaldehyde Resin / Amino Resin / General Base Catalysis / General Acid Catalysis /

In a preceding paper,¹ we reported that the kinetic study of hydroxymethylation of melamine with formaldehyde to form monomethylolmelamine in the strongly acidic region of $S=1 \sim 5$ (pH 2.5-0.6), where S denotes $[\text{hydrochloric acid}]_0/[\text{melamine}]_0$. The present work summarizes a kinetic study of the early stage hydroxymethylation of melamine in the weakly acidic region of $0 < S < 1.0$ and in the absence of the catalyst, $S=0$ (pH, *ca.* 3-8).

Okano and Ogata,² on the basis of their extensive study of the hydroxymethylation of melamine with formaldehyde, reported that hydroxymethylation in the region between the absence of the catalyst and pH 4.5 takes place only by a reaction of melamine molecules with formaldehyde molecules ($k_{\text{H}_2\text{O}}$ -reaction in eq 15); other investigators³ have carried out further research by the use of this mechanism for melamine hydroxymethylation. This mechanism was discussed as follows.

Addition of hydrochloric acid to a mixture

of melamine and formaldehyde results in the dominant addition reaction of hydrochloric acid to melamine to form the conjugate acid of melamine because the base constant of melamine⁴ is much greater than that of formaldehyde⁵ (*cf.* eq 1 and 2). Consequently, the concentration of melamine molecules at $S=1/2$ (pH 5.0) is one-half of that of melamine molecules at $S=0$. Thus, according to this mechanism, the rate at $S=1/2$ should be one-half of that at $S=0$, but our preceding paper¹ indicated that the hydroxymethylation rate at $S=1/2$ is slightly larger than that at $S=0$. Accordingly, this experimental result can not be explained by this mechanism. Therefore, in order to elucidate the mechanism of hydroxymethylation of melamine with formaldehyde in the region of $0 \leq S < 1.0$, a kinetic investigation was made in the present work.

In this paper, $[]$ expresses the concentration (mol l^{-1}) and $[]_0$, the initial concentration (mol l^{-1}).

EXPERIMENTAL

Materials

Commercially available melamine and para-formaldehyde were purified by the method described in a preceding paper.¹

Kinetics

In a thermostat adjusted to the reaction temperature, an appropriate quantity of melamine and sodium perchlorate were dissolved and brought to 1 l with distilled water; there also a suitable concentration of formaldehyde was brought to 200 ml with distilled water. These two solutions were mixed, aliquots were taken out at certain intervals, and the amount of unreacted formaldehyde was determined by the sulfite method.² The pH was measured with a glass electrode pH-meter. The reaction temperature was 40°C and ionic strength of the media was adjusted to 0.07 with the above sodium perchlorate. Since the early stage hydroxymethylation was examined in this work, the formation of the methylene linkage would be small, and its effect was neglected in this paper.

RESULTS AND DISCUSSION

Reaction-Order

For the hydroxymethylation of melamine with formaldehyde in the strongly acid region of $S > 1.0$, a preceding paper¹ showed that the hydroxymethylation follows the second-order kinetics *i.e.*, $R_0 = k[\text{melamine}]_0[\text{formaldehyde}]_0$, where R_0 is the initial rate.

In the region of $0 \leq S \leq 1.0$, the reaction-order was determined.

First, the reaction-order with respect to $[\text{formaldehyde}]_0$ was determined. The value of R_0 was calculated from the initial slope of the plots of formaldehyde consumed and reaction time. Figure 1 shows the plots of $\log R_0$ against $\log [\text{formaldehyde}]_0$ at constant $[\text{melamine}]_0$ and pH, giving a linear relation with a slope of 1.0, irrespective of the pH of the media. It follows first-order kinetics with respect to $[\text{formaldehyde}]_0$.

Next, the reaction-order for $[\text{melamine}]_0$ was investigated. At constant $[\text{formaldehyde}]_0$, $[\text{melamine}]_0$ was varied and S was made constant with hydrochloric acid. (Since the values of S were made constant in each series of Table

Figure 1. Linear dependence of $\log R_0$ on $\log [\text{formaldehyde}]_0$ at $[\text{melamine}]_0 = 0.07 \text{ mol l}^{-1}$ and 40°C: $\triangle$, 0 (pH 8.0); $\circ$, 0.25 (pH 5.5); $\square$, 0.80 (pH 4.4) for S .

Figure 2. Relationship between $\log R_0$ and $\log [\text{melamine}]_0$ at $[\text{formaldehyde}]_0 = 0.07 \text{ mol l}^{-1}$ and 40°C: $\circ$, 0; $\triangle$, 0.10; $\square$, 0.25; $\diamond$, 0.50; $\bullet$, 0.70; $\triangle$, 0.80; $\blacksquare$, 1.0 for S ; dotted line, slope. Points refer to Table I.

Hydroxymethylation of Melamine with Formaldehyde

Table I. Dependence of initial rates (R_0) and the second-order rate constants (k) of the hydroxymethylation of melamine on $[\text{melamine}]_0$ at 40°C and ionic strength of 0.07

Run	$[\text{Melamine}]_0$, mol l^{-1}	$[\text{Formaldehyde}]_0$, mol l^{-1}	$\frac{[\text{HCl}]_0}{[\text{Melamine}]_0}$ ($\equiv S$)	pH	$R_0 \times 10^5$, $\text{mol l}^{-1} \text{min}^{-1}$	$k \times 10^2$, $\text{l mol}^{-1} \text{min}^{-1}$
1	0.07	0.07	0.00	8.0	15.04	3.14
2	0.04	0.07	0.00	7.6	7.05	2.52
3	0.02	0.07	0.00	7.4	2.98	2.12
4	0.01	0.07	0.00	7.3	1.32	1.88
5	0.07	0.07	0.10	5.9	18.15	3.69
6	0.04	0.07	0.10	5.9	7.92	2.83
7	0.02	0.07	0.10	5.9	3.08	2.20
8	0.01	0.07	0.10	5.9	1.34	1.91
9	0.07	0.07	0.25	5.6	19.80	4.02
10	0.04	0.07	0.25	5.6	8.40	2.98
11	0.02	0.07	0.25	5.5	3.15	2.24
12	0.01	0.07	0.25	5.5	1.30	1.85
13	0.07	0.07	0.50	5.0	19.48	3.97
14	0.04	0.07	0.50	5.0	7.80	2.78
15	0.02	0.07	0.50	4.9	2.79	1.99
16	0.01	0.07	0.50	4.9	1.12	1.59
17	0.07	0.07	0.70	4.6	14.35	2.90
18	0.04	0.07	0.70	4.6	6.20	2.21
19	0.02	0.07	0.70	4.6	2.24	1.61
20	0.01	0.07	0.70	4.6	0.91	1.30
21	0.07	0.07	0.80	4.5	13.14	2.64
22	0.04	0.07	0.80	4.4	5.28	1.90
23	0.02	0.07	0.80	4.4	1.94	1.39
24	0.01	0.07	0.80	4.4	0.82	1.15
25	0.07	0.07	1.0	3.1	3.75	0.77
26	0.04	0.07	1.0	3.1	2.08	0.74
27	0.02	0.07	1.0	3.1	1.10	0.77
28	0.01	0.07	1.0	3.2	0.51	0.72

I, the values of pH were also kept nearly constant.) Table I summarizes R_0 and k together with the reaction conditions, where k is the second-order rate constant if $R_0 = k[\text{melamine}]_0$ $[\text{formaldehyde}]_0$ were to be assumed. With the use of data in Table I, $\log R_0$ were plotted against $\log [\text{melamine}]_0$ as shown in Figure 2. As is seen from Figure 2, slight upward curvatures with the slope increasing from 1.25 to 1.45 were obtained with increasing $[\text{melamine}]_0$ at constant S of 0, 0.10, 0.25, 0.50, 0.70, and 0.80; but for $S=1.0$, a straight line with a slope of *ca.* 1.0 was obtained and this result is the same as that of the strong acid region of $S > 1.0^1$. In addition, plots of R_0 against $[\text{melamine}]_0$ are shown

in Figure 3, in which a linear dependence of R_0 on $[\text{melamine}]_0$ was approximately observed at $S=1.0$, whereas the decided upward curvatures were observed in the region of $0 \leq S < 1.0$; viz., $R_0 \propto [\text{melamine}]_0^n$ ($n > 1$) was, undoubtedly, established in the region of $0 \leq S < 1.0$.

Consideration on the Reaction Mechanism Reported Previously

In the presence of an acid catalyst, the melamine molecules MH form conjugate acids MH_2^{+4} and also MH_3^{2+6} according to the equilibrium of eq 1, while the formaldehyde molecules form methylol cations according to eq 2. Clearly, eq 1 and 2 are both fast pre-equilibria, and K_1 , K_2 , and K_3 are the respective equilibrium constants.

Figure 3. Relationship between R_0 and $[\text{melamine}]_0$ at $[\text{formaldehyde}]_0 = 0.07 \text{ mol l}^{-1}$ and 40°C : $\circ$, 0; $\blacktriangle$, 0.10; $\square$, 0.25; $\diamond$, 0.50; $\bullet$, 0.70; $\triangle$, 0.80; $\blacksquare$, 1.0 for S .

$$\left(\begin{array}{l} K_1 = \frac{K_{b1}}{K_w} = 10^5 \text{ mol}^{-1} \text{ l}^4, \\ K_2 = \frac{K_{b2}}{K_w} = 1 \text{ mol}^{-1} \text{ l}^6 (25^\circ\text{C}), \\ K_w = 10^{-14} \text{ mol}^2 \text{ l}^{-2} (25^\circ\text{C}) \end{array} \right)$$

Thus, the rate law would be expressed generally by eq 3, then transformed to eq 4, and then derived to eq 5 because of "ambiguities in kinetics"; in eq 3, a_1 , a_2 , b , and c are such constants as those

$$\begin{aligned} \text{rate} &= c([\text{MH}] + a_1[\text{MH}_2^+] + a_2[\text{MH}_3^{2+}]) \\ &\quad \times ([\text{HCHO}] + b[\text{CH}_2\text{OH}^+]) \quad (3) \\ &= k_1[\text{MH}][\text{HCHO}] + k_2[\text{MH}][\text{CH}_2\text{OH}^+] \end{aligned}$$

$$\begin{aligned} &+ k_3[\text{MH}_2^+][\text{HCHO}] + k_4[\text{MH}_2^+][\text{CH}_2\text{OH}^+] \\ &+ k_5[\text{MH}_3^{2+}][\text{HCHO}] \\ &+ k_6[\text{MH}_3^{2+}][\text{CH}_2\text{OH}^+] \quad (4) \end{aligned}$$

in the kinetic study of the reaction of acetone with iodine.⁷

$$\begin{aligned} \text{rate} &= k_1[\text{MH}][\text{HCHO}] + k_3'[\text{MH}_2^+][\text{HCHO}] \\ &\quad + k_4'[\text{MH}_2^+][\text{CH}_2\text{OH}^+] \\ &\quad + k_6[\text{MH}_3^{2+}][\text{CH}_2\text{OH}^+] \quad (5) \\ &\left(k_3' = \frac{K_3}{K_1}k_2 + k_3, \quad k_4' = k_4 + \frac{K_2}{K_3}k_5 \right) \end{aligned}$$

A preceding paper stated that the main reaction of the hydroxymethylation in the strongly acid region of $S \div 1.3 \sim 5.0$ (pH 1.7–0.6) is a k_4' -reaction¹ of eq 5, and that the main reaction in the region of $S \div 1.02 \sim 1.2$ (pH, ca. 2.9–2.0), where the rate vs. pH profile shows the minimum rate, would be a k_3' -reaction.^{1,2} For the above reason, in the region of $0 \leq S < 1.0$ examined in the present work, k_4' - and k_6 -reactions are clearly of insignificant magnitude, so that eq 5 can be approximately derived to eq 6.

$$\text{rate} \div k_1[\text{MH}][\text{HCHO}] + k_3'[\text{MH}_2^+][\text{HCHO}] \quad (6)$$

As pointed out in the introduction, it is not appropriate that the reaction in the region of $0 \leq S < 1.0$ is assumed to proceed only by the k_1 -reaction proposed by Okano and Ogata,² i.e., the first term on the right-hand side of eq 6. Next, let us assume that hydroxymethylation is the parallel reaction to the k_1 - and k_3' -reactions,⁸ i.e., the first and second terms on the right-hand side of eq 6. When hydrochloric acid is added to a mixture of melamine and formaldehyde, the concentration of MH_2^+ at $S=1/2$ would be one-half of that of MH_2^+ at $S=1$. Consequently, the size of the k_3' -reaction at $S=1/2$ would be one-half of that of the k_3' -reaction at the minimum rate, and accordingly, the contribution of k_3' -reaction to the rate at $S=1/2$ is quite small. Hence, the parallel reaction of the k_1 - and k_3' -reactions is not coincident with the experimental result¹ that the rate at $S=1/2$ is slightly larger than that at $S=0$.

Moreover, the upward curvatures given in Figure 3 mean that R_0 is dependent on a higher power of $[\text{melamine}]_0$ than one, and this result

cannot be explained by either of the above two mechanisms reported previously.

Rate Equation

The decided upward curvature in Figure 3 suggests that the melamine molecule (base species), MH, itself acts as a general base catalyst and its conjugate acid, MH_2^+ , acts as a general acid catalyst for the hydroxymethylation of melamine. In this case, the reaction catalyzed by MH_3^{2+} is neglected, because K_2 is markedly smaller than K_1 (eq 1) and the concentration of MH_3^{2+} is remarkably small at the $\text{pH} > 3$ values studied in this paper.

Accordingly, as is clear from Scheme 1, the over-all kinetic expression would be represented by eq 7 at controlled pH, which becomes eq 8 and then eq 9 for initial stage hydroxymethylation. Comparison between eq 9 and 10 gives eq 11 for k , and eq 11 shows that k is given as a sum of zero, first, and second order terms relative to $[\text{melamine}]_0$. Parameters α , β , and γ of eq 11 are expressed by eq 12, 13, and 14, respectively, where $1 + K_3$ was taken as 1 since $K_3 \ll 1$ (eq 2).

$$\text{rate} = [\text{MH}][\text{HCHO}] \sum_i k_i [\text{HA}_i] \sum_j k_j [\text{B}_j] \quad (7)$$

$$\begin{aligned} &= k_{\text{H}_2\text{O}}[\text{MH}][\text{HCHO}] + k_{\text{H}}[\text{MH}_2^+][\text{HCHO}] \\ &+ k_{\text{MH}_2^+}[\text{MH}_2^+][\text{MH}][\text{HCHO}] \\ &+ k_{\text{MH}}[\text{MH}]^2[\text{HCHO}] \\ &+ k_p[\text{MH}_2^+][\text{MH}]^2[\text{HCHO}] \end{aligned} \quad (8)$$

$$\begin{aligned} &= \left\{ \frac{k_{\text{H}_2\text{O}} + k_{\text{H}} + K_1[\text{H}^+]}{(1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2)(1 + K_3[\text{H}^+])} \right. \\ &+ \frac{[\text{MH}]_0(k_{\text{MH}} + k_{\text{MH}_2^+} + K_1[\text{H}^+])}{(1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2)^2(1 + K_3[\text{H}^+])} \\ &+ \left. \frac{[\text{MH}]_0^2 k_p K_1[\text{H}^+]}{(1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2)^3(1 + K_3[\text{H}^+])} \right\} \\ &\times [\text{MH}]_0[\text{F}]_0 \end{aligned} \quad (9)$$

$$= k[\text{MH}]_0[\text{F}]_0 \quad (10)$$

$$k = \alpha + \beta[\text{MH}]_0 + \gamma[\text{MH}]_0^2 \quad (11)$$

$$\alpha = \frac{k_{\text{H}_2\text{O}} + k_{\text{H}} + K_1[\text{H}^+]}{1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2} \quad (12)$$

$$\beta = \frac{k_{\text{MH}} + k_{\text{MH}_2^+} + K_1[\text{H}^+]}{(1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2)^2} \quad (13)$$

$$\gamma = \frac{k_p K_1[\text{H}^+]}{(1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2)^3} \quad (14)$$

Calculation of Rate Constants

Equation 11, by plotting the relationship between k and $[\text{melamine}]_0$, gives an upward curvature with α as an intercept and $\beta + 2\gamma[\text{MH}]_0$ as the slope, and gives a straight line with a slope of β when $\gamma = 0$, i.e., $k_p = 0$. Plots of k against $[\text{melamine}]_0$, using the data in Table I, are shown in Figure 4. As a result, a linear dependence was approximately established, and the following values were obtained: $k_p \approx 0$ (The slopes of 1.25–1.45 in Figure 2 may suggest that γ is negligible.); the values of α are 1.72×10^{-2} , 1.62×10^{-2} , 1.52×10^{-2} , 1.20×10^{-2} , 0.99×10^{-2} , and $0.91 \times 10^{-2} \text{ l mol}^{-1} \text{ min}^{-1}$, respectively at

Figure 4. Linear dependence of k on $[\text{melamine}]_0$ at $[\text{formaldehyde}]_0 = 0.07 \text{ mol l}^{-1}$ and 40°C : $\circ$, 0; $\blacktriangle$, 0.10; $\square$, 0.25; $\diamond$, 0.50; $\bullet$, 0.70; $\triangle$, 0.80; $\blacksquare$, 1.0 for S .

Figure 5. Linear dependence of $\alpha(1+K_1[H^+]+K_1K_2[H^+]^2)$ or $\beta(1+K_1[H^+]+K_1K_2[H^+]^2)$ on $K_1[H^+]$: O, $\alpha(1+K_1[H^+]+K_1K_2[H^+]^2) \times 10^2$; ●, $\beta(1+K_1[H^+]+K_1K_2[H^+]^2)$.

Table II. A tabulation of rate constants at 40°C determined in this study

k_{H_2O} , l mol ⁻¹ min ⁻¹	1.72×10^{-2}
k_{H^+} , l mol ⁻¹ min ⁻¹	6.97×10^{-3}
k_{MH} , l ² mol ⁻² min ⁻¹	0.20
$k_{MH_2^+}$, l ² mol ⁻² min ⁻¹	1.45

$S=0$, 0.10, 0.25, 0.50, 0.70, and 0.80; and the corresponding β values are 0.20, 0.30, 0.36, 0.40, 0.31, and 0.25 l² mol⁻² min⁻¹.

As is anticipated from eq 12, the plots of $\alpha(1+K_1[H^+]+K_1K_2[H^+]^2)$ against $K_1[H^+]$ give a straight line with an intercept= k_{H_2O} and a slope= k_{H^+} . Figure 5 shows the plots obtained by the substitution of the above values of α and the values of K_1 and K_2 of eq 1 into eq 12, where $[H^+]$ is computed from the pH shown in Table I; the plots indicate a good linearity, and the values of the second-order rate constants of k_{H_2O} and k_{H^+} are presented in Table II.

From eq 13, the plotting of $\beta(1+K_1[H^+]+K_1K_2[H^+]^2)$ and $K_1[H^+]$ is expected to give a straight line with an intercept= k_{MH} and a slope=

$k_{MH_2^+}$. Figure 5 shows the plots obtained by substitution of the above values of β and the values of K_1 and K_2 into eq 13. A linear dependence was observed and the values of the third-order rate constant, $k_{MH_2^+}$, and k_{MH} are listed in Table II.

Since $k_p \neq 0$ as mentioned above, eq 8 can be simplified to eq 15 in the region of $0 \leq S < 1.0$; viz., the rate in the region of $0 \leq S < 1.0$ was found to be dependent on $[MH]$ and $[MH_2^+]$ in the manner given by eq 15.

$$\begin{aligned} \text{rate} = & k_{H_2O}[MH][HCHO] + k_{H^+}[MH_2^+][HCHO] \\ & + k_{MH_2^+}[MH_2^+][MH][HCHO] \\ & + k_{MH}[MH]^2[HCHO] \end{aligned} \quad (15)$$

In particular, the rate at $S=0$ is speculated to be representable by eq 16, because $[MH_2^+] \neq 0$ at $S=0$ and both k_{H^+} - and $k_{MH_2^+}$ -reactions of eq 15 may be less probable. (This speculation is demonstrated in the following section.)

$$\text{rate} = k_{H_2O}[MH][HCHO] + k_{MH}[MH]^2[HCHO] \quad (16)$$

Comparison between Observed Profiles (k vs. pH and log k vs. pH) and Corresponding Calculated Profiles, and Their Dependence on [Melamine]₀

As indicated above, hydroxymethylation in the region of $0 \leq S < 1.0$ is a parallel reaction to the k_{H_2O} -, k_{H^+} -, $k_{MH_2^+}$ -, and k_{MH} -reactions, so that the use of parameters A , B , C , and D shown in each portion of eq 18 gives eq 17 for k .

$$k = A + B + C + D \quad (17)$$

$$A = \frac{k_{H_2O}}{1 + K_1[H^+] + K_1K_2[H^+]^2} \quad (18-1)$$

$$B = \frac{k_{H^+}K_1[H^+]}{1 + K_1[H^+] + K_1K_2[H^+]^2} \quad (18-2)$$

$$C = \frac{k_{MH_2^+}K_1[H^+][MH]_0}{(1 + K_1[H^+] + K_1K_2[H^+]^2)^2} \quad (18-3)$$

$$D = \frac{k_{MH}[MH]_0}{(1 + K_1[H^+] + K_1K_2[H^+]^2)^2} \quad (18-4)$$

As is clear from eq 18-1 to 18-4, A , B , C , and D show the dependence of k_{H_2O} -, k_{H^+} -, $k_{MH_2^+}$ -, and k_{MH} -reactions on $[H^+]$ and $[melamine]_0$, respectively. Substitution of the values of K_1 and K_2 (eq 1) and the rate constants (Table II) into eq 18-1 to 18-4 gives the cal-

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Figure 6. Calculated profiles of A , B , C , D , and $(A+B+C+D)$ at 40°C as function of pH and $[\text{melamine}]_0$: (a), for $[\text{melamine}]_0 = 0.07 \text{ mol l}^{-1}$; (b), for $[\text{melamine}]_0 = 0.04 \text{ mol l}^{-1}$; $\circ$, $A \times 10^2$; $\triangle$, $B \times 10^2$; $\diamond$, $C \times 10^2$; $\square$, $D \times 10^2$; $\bullet$, $(A+B+C+D) \times 10^2$.

culated profiles illustrated in Figure 6, in which (a) and (b) show the calculated profiles of A , B , C , D and $(A+B+C+D)$ at $[\text{melamine}]_0 = 0.07$ and 0.04 mol l^{-1} , respectively.

As shown by the calculated profiles of Figures 6(a) and (b), A and D are constant in the region from $\text{pH } 8$ to $\text{pH } 7$, and decrease with increasing acidity in the strongly acid region; C exhibits a striking maximum at $\text{pH } 5.0$. From $dC/d\text{pH} = 0$, this maximum point is calculated

as $\text{pH} = \log K_1 (=5.0)$ irrespective of $[\text{melamine}]_0$, where K_2 was taken as zero or, in other words, the $k_{\text{MH}_2^+}$ -reaction attains a maximum rate when the concentration of melamine molecules is equal to that of MH_2^+ (half-neutralization point of melamine); B is constant ($B \doteq 0$) in the region of $\text{pH } 8-7$, and increases with increasing acidity in the more strongly acid region.

Similarly, the calculated profiles of $\log A$, $\log B$, $\log C$, $\log D$, and $\log(A+B+C+D)$ at $[\text{melamine}]_0 = 0.07 \text{ mol l}^{-1}$ are shown in Figure 7, together with their slopes against pH .

Figures 8(a) and (b) demonstrate the coincidence of the observed profiles of k vs. pH and $\log k$ vs. pH (Table I) with the corresponding calculated profiles in the pH region of $3-8$. Figure 8 also shows that the observed values of k increase with the increasing of $[\text{melamine}]_0$ at constant pH and have a maximum at pH , ca. 5.2; these results are in accord with the fact that A and B at a given pH are constant regardless of $[\text{melamine}]_0$, whereas C and D at a given pH increase with the increasing of $[\text{melamine}]_0$ (eq 18-1 to 18-4 and Figure 6).

However, the calculated profile of Figure 8 is not entirely coincident with the corresponding observed one in the strongly acidic region ($\text{pH} < \text{ca. } 1.7$), since the observed rate in this region increases with increasing acidity (slope, $d \log k / d\text{pH} \doteq -0.7$)¹. Hence, this result is com-

Figure 7. Calculated profiles of $\log A$, $\log B$, $\log C$, $\log D$, and $\log(A+B+C+D)$ at $[\text{melamine}]_0 = 0.07 \text{ mol l}^{-1}$ and 40°C as function of pH : $\circ$, $\log A$; $\triangle$, $\log B$; $\diamond$, $\log C$; $\square$, $\log D$; $\bullet$, $\log(A+B+C+D)$; dotted line, slope.

Figure 8. Comparison between observed profiles and corresponding calculated profiles for the hydroxymethylation of melamine at 40°C: (a) solid line, calculated profiles of $(A+B+C+D) \times 10^2$; (b) solid line, calculated profiles of $\log(A+B+C+D)$. The observed values of k : $\bigcirc$, 0.07 mol l^{-1} ; $\triangle$, 0.04 mol l^{-1} ; $\diamond$, 0.02 mol l^{-1} ; $\square$, 0.01 mol l^{-1} for $[\text{melamine}]_0$; dotted line, slope.

patible with the result of the preceding paper¹ that the main reaction is the k_4' -reaction of eq 5 (the reaction of MH_2^+ with CH_2OH) and not $k_{\text{H}_2\text{O}}$ -, k_{H^+} -, $k_{\text{MH}_2^+}$ -, and k_{MH} -reactions (eq 15) for this strongly acidic region.

Effect of pH and $[\text{Melamine}]_0$ on Relative Contributions of $k_{\text{H}_2\text{O}}$ -, k_{H^+} -, $k_{\text{MH}_2^+}$ -, and k_{MH} -Reactions

Equation 19 follows from eq 18, and $A:B:C:D$ of eq 19 corresponds to the relative con-

tribution among $k_{\text{H}_2\text{O}}$ -reaction, k_{H^+} -reaction, $k_{\text{MH}_2^+}$ -reaction, and k_{MH} -reaction.

$$A:B:C:D = k_{\text{H}_2\text{O}} : k_{\text{H}^+}K_1[\text{H}^+] : \frac{k_{\text{MH}_2^+}K_1[\text{H}^+][\text{MH}]_0}{1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2} : \frac{k_{\text{MH}}[\text{MH}]_0}{1 + K_1[\text{H}^+] + K_1K_2[\text{H}^+]^2} \quad (19)$$

As is evident from eq 19, the relative contributions of these four reactions depend on pH and $[\text{melamine}]_0$, so that they are not constant even if pH is constant. But, the relative contributions of $k_{\text{H}_2\text{O}}$ - and k_{H^+} -reactions and those of k_{MH} - and $k_{\text{MH}_2^+}$ -reactions at controlled pH are respectively constant, because $A/B = k_{\text{H}_2\text{O}}/k_{\text{H}^+}K_1[\text{H}^+]$ and $C/D = k_{\text{MH}_2^+}K_1[\text{H}^+]/k_{\text{MH}}$ (eq 19).

At $[\text{melamine}]_0 = 0.07 \text{ mol } l^{-1}$, relative contri-

Table III. Effect of pH on the relative contributions of $k_{\text{H}_2\text{O}}$ -, k_{H^+} -, $k_{\text{MH}_2^+}$ -, and k_{MH} -reactions at $[\text{melamine}]_0 = 0.07 \text{ mol } l^{-1}$ and 40°C

pH	Relative contributions, %			
	$k_{\text{H}_2\text{O}}$ -reaction	k_{H^+} -reaction	$k_{\text{MH}_2^+}$ -reaction	k_{MH} -reaction
2.50	0.7	94.9	4.3	0.0
3.00	2.1	85.6	12.3	0.0
3.25	3.4	77.0	19.6	0.0
3.50	5.1	65.6	29.2	0.1
3.75	7.3	52.1	40.3	0.3
4.00	9.6	38.7	51.0	0.7
4.25	11.9	27.1	59.5	1.5
4.50	14.5	18.5	64.6	2.5
4.75	17.3	12.5	65.1	5.1
5.00	21.1	8.5	61.9	8.6
5.25	25.9	5.9	54.7	13.5
5.50	31.7	4.1	44.7	19.5
5.75	37.8	2.7	33.5	26.0
6.00	43.3	1.7	23.1	31.9
6.25	47.5	1.1	14.9	36.5
6.50	50.5	0.6	9.1	39.7
6.75	52.4	0.4	5.4	41.8
7.00	53.6	0.2	3.1	43.1
7.25	54.3	0.1	1.8	43.8
7.50	54.7	0.1	1.0	44.2
7.75	54.9	0.0	0.6	44.5
8.00	55.0	0.0	0.3	44.6
8.25	55.1	0.0	0.2	44.7
8.50	55.1	0.0	0.1	44.7
8.75	55.2	0.0	0.1	44.8

Hydroxymethylation of Melamine with Formaldehyde

Figure 9. Effect of pH and [melamine]₀ on relative contributions of k_{H_2O} -, k_{H^+} -, $k_{MH_2^+}$ -, and k_{MH^-} -reactions at 40°C according to rate = $k_{H_2O}[MH][HCHO] + k_{H^+}[MH_2^+][HCHO] + k_{MH_2^+}[MH_2^+][MH][HCHO] + k_{MH}[MH]^2[HCHO]$: (a) for [melamine]₀ = 0.07 mol l⁻¹; (b) for [melamine]₀ = 0.04 mol l⁻¹.

Contributions of these reactions were calculated by the use of eq 19 and are given in Table III. Moreover, the relative contributions at [melamine]₀ = 0.07, and 0.04 mol l⁻¹ are shown graphically in Figures 9(a) and (b) in the region of pH 3–8.

First, the region of $0 < S < 1.0$ would be described as follows. For example, the relative contributions at $S = 1/2$ (pH 5.0) and [melamine]₀ = 0.07 mol l⁻¹ are as follows: k_{H_2O} -reaction 21%; k_{H^+} -reaction 9%; $k_{MH_2^+}$ -reaction 62%; k_{MH^-} -reaction 9% (Table III). Consequently, the $k_{MH_2^+}$ -reaction would be regarded as the main reaction in this case. But, the k_{H^+} -reaction becomes the main reaction as the pH tends toward stronger acidity than $S = 1/2$, and this result is in agreement with the result of the preceding papers^{1,2} that the main reaction at $S \div 1.02$ –1.2 would be the k_{H^+} -reaction.

Second, the case of $S = 0$ would be mentioned. At [melamine]₀ = 0.07 mol l⁻¹ and $S = 0$ (pH 8.0), the relative contribution of the k_{H_2O} -reaction is 55%, that of k_{MH^-} -reaction is 45%, and those of k_{H^+} - and $k_{MH_2^+}$ -reactions are negligible; those of the latter two reactions are negligible irrespective of [melamine]₀ (Table III and Figures 9(a) and (b)). Therefore, eq 15 at $S = 0$ could be reduced by eq 16, as predicted above.

Reaction Mechanism

Reaction	H—N	B	HA
k_{H_2O} -reaction	MH	H ₂ O	H ₂ O
k_{H^+} -reaction	MH ₂ ⁺	H ₂ O	H ₂ O
$k_{MH_2^+}$ -reaction	MH ₂ ⁺	MH	H ₂ O
	(or MH	H ₂ O	MH ₂ ⁺)
k_{MH^-} -reaction	MH	MH	H ₂ O

Scheme 2.

The foregoing kinetic results may be summarized as follows. At $0 \leq S < 1.0$, a complex such as Scheme 2 seems to be formed by a series of the prior equilibrium steps followed by the slow step in which the displacement of the

leaving H (proton-transfer) of H—N by the electrophile HCHO is assisted by the general base B and general acid HA catalysis, which may involve concerted mechanisms; the above complex may be analogous to those of the nitrogen bases themselves,⁹ nitrogen bases with the conjugate acids,¹⁰ and nitrogen bases with carbonyl compounds.⁹

In Scheme 2, the k_{MH} -reaction is the hydroxymethylation of MH with HCHO assisted by the general base catalyst MH; on the other hand, $k_{\text{MH}_2^+}$ -reaction is the hydroxymethylation of MH_2^+ with HCHO assisted by the general base catalyst MH, and/or that of MH with HCHO assisted by the general acid catalyst MH_2^+ , and these two reaction paths would not be kinetically distinguishable because these have identical rate equations.

At $S=1.0$, $[\text{MH}]$ is negligible so that hydroxymethylation may mainly proceed through the only remaining one, $\text{MH}_2^+\cdot\text{HCHO}$ (I) among the complexes of Scheme 2, where the structure⁴ of MH_2^+ has been formulated by the study of UV spectra. It follows from this that the reaction is represented by a more than first-order dependence on $[\text{melamine}]_0$ at $0 \leq S < 1.0$, whereas it is of an approximately first-order dependence on $[\text{melamine}]_0$ at $S=1.02\text{--}1.2$, where the k_{H^+} -reaction would be the main reaction.

Finally, the reaction mechanism at $S=0$ can be discussed in further detail as follows.

The pH value increases somewhat (7.3→8.0) with the increase of $[\text{melamine}]_0$ at $S=0$, unlike the cases of the other S values (Table I). Therefore, the fact that the reaction-order at $S=0$ is higher than first-order for $[\text{melamine}]_0$ may be owing to the contribution of the reaction catalyzed by hydroxide ions (k_{OH^-} -reaction), because $[\text{OH}^-] = K_{\text{b}_1}^{1/2}[\text{MH}]^{1/2}$ at $S=0$ (from $\text{MH} + \text{H}_2\text{O} \xrightleftharpoons{K_{\text{b}_1}} \text{MH}_2^+ + \text{OH}^-$) and $\text{rate} = k_{\text{OH}^-}[\text{OH}^-]$

$[\text{MH}][\text{HCHO}] = k_{\text{OH}^-} K_{\text{b}_1}^{1/2} [\text{MH}]^{3/2} [\text{HCHO}]$ (i.e., $\text{rate} \propto [\text{MH}]^{3/2}$) is given for the k_{OH^-} -reaction. Accordingly, eq 20 is given instead of eq 16 if the k_{OH^-} -reaction also

$$\text{rate} = k_{\text{H}_2\text{O}}[\text{MH}][\text{HCHO}] + k_{\text{MH}}[\text{MH}]^2[\text{HCHO}] + k_{\text{OH}^-}[\text{OH}^-][\text{MH}][\text{HCHO}] \quad (20)$$

participates, and becomes eq 21 at $S=0$.

$$\text{rate} = k_{\text{H}_2\text{O}}[\text{MH}][\text{HCHO}] + k_{\text{MH}}[\text{MH}]^2[\text{HCHO}] + k_{\text{OH}^-} K_{\text{b}_1}^{1/2} [\text{MH}]^{3/2} [\text{HCHO}] \quad (21)$$

At $S=0$, $[\text{MH}] = [\text{MH}]_0 / (1 + K_1[\text{H}^+] + K_1 K_2 [\text{H}^+]^2) \doteq [\text{MH}]_0$ is obtained, and hence eq 21 gives eq 22 for k at $S=0$.

$$k = k_{\text{H}_2\text{O}} + k_{\text{MH}}[\text{MH}]_0 + k_{\text{OH}^-} K_{\text{b}_1}^{1/2} [\text{MH}]_0^{1/2} \quad (22)$$

Equation 22 shows that k is given as a sum of zero, first, and square root order terms for $[\text{melamine}]_0$. As is clear from eq 22, plots of k vs. $[\text{melamine}]_0$ shows the downward curvature (the slope $= k_{\text{MH}} + (1/2)k_{\text{OH}^-} K_{\text{b}_1}^{1/2} [\text{melamine}]_0^{-1/2}$) if the k_{OH^-} -reaction participates rather strongly, but shows a straight line when the k_{MH} -reaction predominates over the k_{OH^-} -reaction. The approximate linear dependence of k on $[\text{melamine}]_0$ (Figure 4) would suggest that the k_{OH^-} -reaction is of insignificant magnitude.

In details, plots of k against $[\text{melamine}]_0^{1/2}$ give an upward curvature (the slope $= 2k_{\text{MH}}[\text{melamine}]_0^{1/2} + k_{\text{OH}^-} K_{\text{b}_1}^{1/2}$), but give a straight line with the slope of $k_{\text{OH}^-} K_{\text{b}_1}^{1/2}$ if the k_{OH^-} -reaction were predominates over the k_{MH} -reaction, as eq 22 shows. This speculation may be associated with ammonolysis of methyl phenylacetate and

Figure 10. Plots of k vs. $[\text{melamine}]_0^{1/2}$ in the absence of catalyst; taken from Run 1—4 in Table I.

its derivatives with ammonia,¹¹ because this reaction follows a more than first-order dependence on $[\text{ammonia}]_0$ and plots of k vs. $[\text{ammonia}]_0^{1/2}$ are linear, where k is the second-order rate constant if $R_0 = k[\text{ester}]_0[\text{ammonia}]_0$ is assumed. The slight upward curvature between k and $[\text{melamine}]_0^{1/2}$ given in Figure 10 shows that the contribution of the k_{OH^-} -reaction may be small. Even if the plots in Figure 10 were to be linear within experimental error, the value of $k_{\text{OH}^-} \doteq 1.89 \times 10^8 \text{ l}^2 \text{ mol}^{-2} \text{ min}^{-1}$ can be evaluated at 40°C, since the k_{OH^-} -reaction predominates over k_{MH} -reaction in this case and the slope entails $k_{\text{OH}^-} K_{b1}^{1/2}$ as indicated above; but the k_{OH^-} value has been reported as $38 \text{ l}^2 \text{ mol}^{-2} \text{ min}^{-1}$ ¹² at 30°C for the hydroxymethylation of melamine with formaldehyde in the presence of sodium hydroxide catalyst. This marked difference for k_{OH^-} values may be explicable from the fact that the enhancement of rate with the increase of hydroxide ions due to increase of $[\text{melamine}]_0$ is small at $S=0$.

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