Disentangling Cooper-pair formation above the transition temperature from the pseudogap state in the cuprates

Takeshi Kondo^{1*}, Yoichiro Hamaya², Ari D. Palczewski¹, Tsunehiro Takeuchi^{2,3}, J. S. Wen⁴, Z. J. Xu⁴, Genda Gu⁴, Jörg Schmalian¹ and Adam Kaminski^{1*}

The discovery of the pseudogap in the cuprates^{1–3} created significant excitement as it was believed to be a signature of pairing⁴, in some cases above room temperature. Indeed, a number of experiments detected phase-fluctuating superconductivity above the transition temperature T_c (refs 5–9). However, several recent experiments reported that the pseudogap and superconducting state are characterized by different energy scales^{10–14}, and probably compete with each other^{15,16}, leaving open the question of whether the pseudogap is caused by pair formation. Here we report the discovery of a spectroscopic signature of pair formation and demonstrate that in a region commonly referred to as the pseudogap, two distinct states coexist: one that is due to pair formation and persists to an intermediate temperature $T_{\text{pair}} < T^*$ and a second—the ‘proper’ pseudogap—characterized by the loss of spectral weight and anomalies in transport properties that extends up to T^* . T_{pair} has a value around 120–150 K even for materials with very different T_c values and it probably sets a limit on the highest attainable T_c in the cuprates.

The traditional approach of exploring the pairing above T_c by tracking the energy scale of spectral features has so far not yielded convincing results, as these features are poorly defined above T_c . The apparent smooth evolution of the spectral gap from the lowest temperatures up to T^* has previously been interpreted as key evidence for a common origin of the pseudogap and pairing gap^{17–20}. However, very detailed, high-precision data demonstrate that the gap size actually does change across T_c (as seen in Supplementary Fig. S3). Similar behaviour is indeed expected for a system with multiple gaps (in this case a pairing gap and pseudogap), when weights of the features associated with the respective gaps change with temperature. These data provide perhaps the strongest evidence supporting a ‘two gaps’ scenario in the cuprates. A better approach is to investigate the spectral weights, which are easier to quantify and interpret. A key measure of pair formation is the density of states at the Fermi energy $D(E_F)$. In conventional, clean superconductors this weight is zero below T_c , but can be finite if there are strong impurity scattering effects. In such cases $D(E_F)$ reflects the pair-breaking states. A generic ‘density wave state’ in the absence of pairing would also lead to a decrease of the $D(E_F)$ due to the opening of the density wave gap. In addition there is also the possibility of the coexistence of superconductivity and the

density wave state—inhomogeneous superconductors such as the cuprates^{14,21–23}, where superconducting and non-superconducting patches coexist in the sample. One can then expect that the temperature dependence of $D(E_F)$ can be used to distinguish between these scenarios and disentangle the electronic ground states of the cuprates. In our study we use the intensity of the spectral function at E_F , $I(E_F, k)$, which when integrated over all momenta equals $D(E_F)$, so the changes of one quantity with temperature are reflected in the other. This allows us to isolate the behaviour at a specific k -point and avoid smearing due to averaging. A discussion of the relation between $D(E_F)$ and $I(E_F, k)$ is provided in Supplementary Section S3.

In Fig. 1a–c we examine the temperature evolution of the spectral line shape, measured at the antinodal Fermi momentum in optimally doped Bi2212 ($T_c = 90$ K). Symmetrized energy distribution curves²⁴ (EDCs) show the opening of the pseudogap on cooling below T^* (~ 210 K). As the temperature is decreased below T_c , a sharp quasiparticle peak associated with superconductivity appears²⁵. We obtain the spectral changes with temperature by subtracting the spectrum at the highest temperature from all the spectra measured, as shown in Fig. 1b. Now we focus on the loss of spectral weight close to the Fermi level, $W(E_F)$ (hatched area in Fig. 1b). The temperature dependence of $W(E_F)$ is plotted in Fig. 1d. On cooling through T^* , the spectral weight decreases linearly, which is a characteristic behaviour of the pseudogap state. An astonishing feature seen in this plot is the clear deviation from linear behaviour (indicated by the arrow). As the temperature dependence below and above this point is very different, the arrow marks the onset of another distinct state. The onset temperature T_{pair} (~ 150 K) of this transition is considerably higher than T_c ($= 90$ K), but is also significantly lower than the pseudogap temperature T^* (~ 210 K). This state probably arises from pairing of the electrons because the weight loss associated with this state smoothly evolves through T_c . If we extrapolate the linear variation of $W(E_F)$ down to $T = 0$ K, we obtain approximate values of the spectral weight lost as a result of the pseudogap, W_{PG} (blue area), and pairing, W_{pair} (red area), as marked in Fig. 1d.

We now verify this hypothesis by studying how these quantities vary with doping in related samples of Bi2201, where T_c and T^* are more separated over a wide range of carrier concentrations²⁶. Figure 2a–g shows symmetrized EDCs measured at the antinode for various temperatures and dopings from underdoped (left side)

¹Ames Laboratory and Department of Physics and Astronomy, Iowa State University, Ames, Iowa 50011, USA, ²Department of Crystalline Materials Science, Nagoya University, Nagoya 464-8603, Japan, ³EcoTopia Science Institute, Nagoya University, Nagoya 464-8603, Japan, ⁴Condensed Matter Physics and Materials Science Department, Brookhaven National Laboratory, Upton, New York 11973, USA. *e-mail: kondo@ameslab.gov; kaminski@ameslab.gov.

Figure 1 | Temperature dependence of the spectral weight at the Fermi energy. **a**, Symmetrized EDCs (ref. 24) for various temperatures from deep below T_c to above the pseudogap temperature (T^*). The spectra were measured at the antinode (marked by the red point on the Fermi surface shown in the inset) in optimally doped Bi2212 ($T_c = 90$ K). **b**, Difference spectra. The spectrum measured at the highest temperature is subtracted from each of spectra in **a**. Spectral weight close to the Fermi level ($W(E_F)$, hatched area) is estimated by integrating the spectral intensity in **b** within an energy window of the experimental energy resolution (10 meV). **c**, The same spectra as in **a** with offsets. Spectral gaps are indicated with bars. **d**, The temperature dependence of $W(E_F)$. The pairing temperature, T_{pair} , is defined as the onset temperature of deviation (marked by arrow) from a linear behaviour seen at higher temperatures. The pseudogap temperature, T^* , is defined to be the temperature where the two spectral peaks in the symmetrized EDCs merge into a single peak as seen in **c**. The three temperatures, T_c (green), T_{pair} (red) and T^* (blue), are indicated with dashed lines. The pairing weight (W_{pair} , red area) and the pseudogap weight (W_{PG} , blue area) are separated by a line extrapolated from the linear behaviour of $W(E_F)$ at high temperatures. Errors in EDC data (**a–c**) are statistical and reflected by noise in the data. Maximum measurement errors $\pm 1\%$ in **d** are due to uncertainty in the normalization and are smaller than data markers.

to overdoped (right side) samples. In Fig. 1c the peak positions are marked with short black lines to demonstrate that the spectral gap changes across T_c , as discussed in the second paragraph. The spectral changes of the EDCs with temperature are plotted in Fig. 2h–n and $W(E_F)$ is plotted in Fig. 2o–u for all samples. As in the case of Bi2212 (Fig. 1), $W(E_F)$ is linear below T^* at high temperatures, then suddenly deviates from a straight line—defining a new temperature scale T_{pair} . The temperature dependence of $W(E_F)$ evolves in a surprisingly systematic manner with doping. The linear part becomes longer with underdoping, as both T^* and T_{pair} increase. Eventually, at the lowest dopings, $W(E_F)$ is linear down to the lowest temperature. This is because the quasiparticle residue vanishes at the antinode for heavily underdoped samples¹⁶ causing W_{pair} to become very small. The T_{pair} can be still extracted for such samples by examining $W(E_F, T)$ slightly off the antinode. In case of UD23K T_{pair} is ~ 125 K.

To validate our assertion about the pairing origin of W_{pair} , we extract this quantity for each doping by subtracting the interpolated W_{PG} line from each of the $W(E_F, T)$ curves and compare them in Fig. 3a. Obviously the magnitude and onset temperature of W_{pair} is very different for each doping. To make a fair comparison, we rescale the vertical axis for each curve by its maximum value at the lowest temperature and the horizontal axis by T_{pair} . Surprisingly the curves for all dopings fall on top of each other, demonstrating a universal scaling of W_{pair} , which smoothly evolves through T_c . Clearly, $W(E_F, T)$ in the superconducting state reflects pair formation, which causes it to decrease on cooling. The temperature dependence of W_{pair} does not exhibit significant features at T_c and

its scaling remains unchanged across T_c , strongly suggesting that pair formation occurs well above T_c . As W_{pair} scales with T_{pair} , this must be the onset temperature of pairing. At the lowest dopings (Fig. 2o), $W(E_F, T)$ is a linear function of temperature. We attribute this behaviour to the pseudogap, because it was demonstrated that the antinode in underdoped samples is dominated by the pseudogap and does not contribute to the superfluid density^{15,16}. This almost perfect scaling behaviour of W_{pair} with T_{pair} not only validates our extraction of the pairing component, but it also gives compelling evidence that T_{pair} is the onset temperature of pairing and that pairing is not the origin of the pseudogap, because the pseudogap persists to the much higher T^* .

We summarize our results in Fig. 4 in the form of a phase diagram. We compare our data to the detection of phase-fluctuating superconductivity by magnetization⁶, the Nernst effect⁵, NMR (ref. 26) and specific heat²⁷. We note the reasonable agreement between these probes and angle-resolved photoemission spectroscopy (ARPES). Note that ARPES reports slightly different temperatures, because the other probes are sensitive to a weighted average over the Fermi surface, whereas with ARPES we can extract these directly for the antinodal areas, where this temperature is expected to be highest. We note that specific-heat results²⁷ were carried out using Bi2212 samples and exhibit slightly higher pairing fluctuation temperatures, in agreement with our Bi2212 results in Fig. 1. The pairing temperature (T_{pair}) (shown in Fig. 4b) increases steadily from the overdoped side of the phase diagram towards optimal doping. For dopings lower than optimal, it levels off at ~ 120 K. This behaviour contrasts with that of the pseudogap

Figure 2 | Doping and temperature dependence of spectral weight at the Fermi energy. a–g, Symmetrized EDCs at various temperatures measured at the antinode (marked by the red point on the Fermi surface shown in the inset of **o**) in Bi2201 over a wide range of doping from underdoping (left) to overdoping (right). An offset is used for clarity. **h–n**, Difference spectra. The spectrum at the highest temperature is subtracted from each of the spectra in **a–g**. **o–u**, Temperature dependence of the spectral weight close to E_F , $W(E_F)$, obtained by integrating the spectra in **h–n** within the energy resolution window (10 meV) about E_F (see Fig. 1b). The three temperatures, T_c (green), T_{pair} (red) and T^* (blue), are indicated with dashed lines. The pairing weight (W_{pair} , red area) and the pseudogap weight (W_{PG} , blue area) are separated by a line extrapolated from the linear behaviour of $W(E_F)$ at high temperatures. Error bars in EDC curves (**a–n**) are statistical and reflected by noise in the data. Maximum measurement errors $\pm 1\%$ in **o–u** are due to uncertainty in the normalization and are smaller than data markers.

Figure 3 | Universal scaling behaviour of the pairing spectral weight. a, Temperature dependence of (W_{pair}) for all samples extracted by subtracting the extrapolated W_{PG} line from the $W(E_F)$ curves in Fig. 2h–n. **b**, W_{pair} from **a** scaled with the pairing temperature (T_{pair}) and the maximum value at the lowest temperature (W_{pair}^{Max}). Maximum measurement errors $\pm 1\%$ in **a** and **b** are due to uncertainty in the normalization and are smaller than the data markers.

temperature (T^*) (Fig. 4c), which monotonically increases up to the lowest doping. We note that the pairing temperature of Bi2201 is similar to that of Bi2212 (see Fig. 1d), despite the large difference of T_c . This strongly suggests that the onset temperature of pairing (120–150 K) is universal and similar to the highest achieved superconducting temperature in the cuprates. Quantitative analysis of the very detailed ARPES data presented here provides clear evidence for a spectroscopic temperature scale T_{pair} , distinct from T_c and T^* . It demonstrates that pairing and the pseudogap are two

fundamentally different states. The competition between the two states may play a key role in the determination of T_c , where bulk superconductivity is established.

The remaining open question is the origin of the pseudogap. Recent results from scanning tunnelling microscopy (STM) suggested^{23,28} that the pseudogap is associated with a ‘checkerboard’ pattern²⁹. Although direct evidence for this (for example, vanishing of the ‘checkerboard’ pattern at T^*) is still missing, our data seem to support this scenario. Figure 3d of ref. 30 shows the relation

Figure 4 | Phase diagrams obtained using pairing and pseudogap spectral weights. a, $W(E_F)$ versus T plots for OD31K, the same as Fig. 2r. **b**, Phase diagram obtained using the pairing spectral weight (W_{pair} , red area in **a**). The onset temperature of pair formation estimated from our ARPES data (T_{pair}), the onset temperature of the Nernst effect⁵ (T_v), the diamagnetic effect⁶ (T_M) and specific heat²⁷ (T_{mf}) are plotted for comparison. As the specific-heat measurements were carried out using Bi2221, the horizontal axis for T_{mf} plots was scaled by the ratio of T_c values for Bi2212 and Bi2201. Note that T_{pair} for UD23K was extracted from data around 13° off the antinode because both quasiparticle peaks and W_{pair} are very small at the antinode. **c**, Phase diagram obtained using the pseudogap spectral weight (W_{PG} , blue area in **a**). The pseudogap temperature estimated from our ARPES data (T^*), our resistivity results (T_p , see Supplementary Fig. S1) and NMR (T_{NMR} ; ref. 26) are plotted. Error bars in **b** represent uncertainty in estimating the temperatures at which deviation from linear behaviour occurs (obtained by interpolation from errors in $W(E_F)$). Error bars in **c** represent uncertainty in estimating the temperature at which the pseudogap closes (that is, two peaks merge into a single peak at E_F). Experimental errors in **a** are the same as in Fig. 1d.

between a ‘checkerboard’ wave vector and pseudogap energy. The average binding energies (represented by black data points), for which the ‘checkerboard’ is observed in STM measurements agrees with the values of the pseudogap we find for the same samples with ARPES. There is also no STM evidence for a ‘checkerboard’ pattern in overdoped samples, where the pseudogap is absent.

The fact that we observe perfect scaling of W_{pair} with T_{pair} , regardless of the doping, implies that the only two relevant energy scales are the order parameter of the pseudogap state and the magnitude of the pairing potential, making the existence of the three temperature scales $T_c < T_{pair} < T^*$, a universal aspect of underdoped cuprates. The observed scaling behaviour with respect to T_{pair} indicates a breakdown of the classical picture of phase fluctuations in the cuprates and gives an important clue as to the nature of the Cooper-pair fluctuations: it is not sufficient to solely consider phase fluctuations of the pairing field. T_{pair} is the temperature where the amplitude of the pairing field melts, that is, where the strength of incoherent pairing disappears. The

emergence of T_{pair} as the relevant temperature of the scaling requires that the pair-amplitude and phase fluctuation are equally crucial below T_{pair} . A pairing interaction that is in the extreme strong-coupling limit, reminiscent of Mott physics, was shown to lead to simultaneous amplitude and pair modes that separate coherent and local pairing³⁰.

Methods

Optimally doped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ (Bi2212) single crystals with $T_c = 90$ K (OP90K) and $(\text{Bi,Pb})_2(\text{Sr,L a})_2\text{CuO}_{6+\delta}$ (Bi2201) single crystals with various T_c values were grown by the conventional floating-zone technique (see Supplementary Information on the sample characterization). To precisely analyse the ARPES spectra, we partially substituted Pb for Bi for all Bi2201 samples, and suppressed the modulation in the BiO plane, which usually contaminates the ARPES signal. ARPES data were acquired using a laboratory-based system consisting of a Scienta SES2002 electron analyser and a GammaData helium ultraviolet lamp. All data were acquired using the He I line with a photon energy of 21.2 eV. The angular resolution was 0.13° and $\sim 0.5^\circ$ along and perpendicular to the direction of the analyser slits, respectively. The energy resolution was set at ~ 10 meV—confirmed by measuring the energy width between the 90% and 10% of the Fermi edge

from the same Au reference. Custom-designed refocusing optics enabled us to accumulate high-statistics spectra in a short time without effects of sample surface ageing. In the analysis we used symmetrized EDCs normalized to the total area over the whole energy range ($-0.4 \text{ eV} \leq E \leq 0.4 \text{ eV}$) for each spectrum. We verified that the choice of normalization scheme does not affect the results of our analysis (see Supplementary Information on the details). The results were reproduced on several samples and on temperature cycling.

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Author contributions

T.K. and A.K. designed the experiment. T.K., Y.H., T.T., J.S.W., Z.J.X. and G.G. grew the high-quality single crystals. T.K. and A.D.P. acquired the experimental data and T.K. carried out the data analysis. T.K., A.K. and J.S. wrote the manuscript. All authors discussed the results and commented on the manuscript.

Additional information

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