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Giant narrowband twin-beam generation along the pump-energy propagation direction

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Walk-off effects, originating from the difference between the group and phase velocities, limit the efficiency of nonlinear optical interactions. While transverse walk-off can be eliminated by proper medium engineering, longitudinal walk-off is harder to avoid. In particular, ultrafast twin-beam generation via pulsed parametric down-conversion and four-wave mixing is only possible in short crystals or fibres. Here we show that in high-gain parametric downconversion, one can overcome the destructive role of both effects and even turn them into useful tools for shaping the emission. In our experiment, one of the twin beams is emitted along the pump Poynting vector or its group velocity matches that of the pump. The result is markedly enhanced generation of both twin beams, with the simultaneous narrowing of angular and frequency spectrum. The effect will enable efficient generation of ultrafast twin photons and beams in cavities, waveguides and whispering-gallery mode resonators.

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alk-off effects are caused by the difference between the velocities and directions of energy and phase propagation. In particular, transverse (spatial) walkoff is due to the fact that the Poynting vector is, in the general case, non-collinear to the wavevector. Similarly, longitudinal (temporal) walk-off appears because the energy of a pulse travels at a different speed than its phase. Since in nonlinear optical processes it is phase matching that determines the frequency and angular spectrum, interacting pulses are, in the general case, group mismatched and separate in both space and time in the course of propagation. This limits the length of nonlinear interactions for short pulses and focused beams^{1,2}.

This is definitely the case for high-gain parametric down-conversion (PDC), widely used for the generation of bright squeezed vacuum^{3–7}. In particular, twin-beam bright squeezed vacuum has perfect photon-number correlations between two beams, each of which taken separately has a very broad (thermal) photon-number distribution. This non-classical state of light has interesting applications in quantum imaging^{3,8} and sensing⁹, phase super-resolution¹⁰, macroscopic entanglement¹¹, enhanced nonlinear interactions and many other fields. In high-gain PDC, down-converted radiation is exponentially amplified provided that it overlaps in space and time with the pump pulse. This makes certain angles and frequencies of emission distinguished and the emission into the corresponding modes enhanced.

Here we show that if one of the twin beams is emitted along the pump Poynting vector or its group velocity matches that of the pump, the generation of both twin beams can be enhanced by more than two orders of magnitude. Because it is enhanced only in certain directions and at certain frequencies, considerable narrowing of the angular and frequency spectrum is observed. In particular, the angular spectrum of each twin beam contains less than two modes.

Results

High-gain PDC along the pump Poynting vector. For PDC in an anisotropic crystal, if the pump is polarized extraordinarily and the down-converted light ordinarily, the emission will be mainly along the pump Poynting vector (Fig. 1a) as well as along its matching direction. The latter is because every signal photon emitted in the walk-off direction has its idler counterpart, and vice versa. This leads to a high-intensity beamlike PDC.

In our experiment, we focused the Gaussian pump beam (frequency-tripled YAG:Nd laser with the wavelength 355 nm, pulse duration 18 ps and repetition rate 1 kHz) into a 5-mm beta barium borate (BBO) crystal by means of a lens with the focal length 500 mm, which resulted in a waist with full width at half maximum of 60 µm. The crystal was oriented to provide frequency-degenerate collinear type-I phase matching (which occurs at the crystal orientation 32.97° to the optic axis). After the crystal, the pump was cut off by a dichroic mirror. The angular spectra of PDC were first captured using a digital photographic camera (Fig. 1b). We see beamlike strongly enhanced emission in the green spectral range. The colour is modified because of the camera saturation, which is clear from a snapshot with an OD2 neutral-density filter (Fig. 1c). The green beam is only one of the 'twins'; moreover, it is the other beam that propagates along the Poynting vector (4° to the collinear direction inside the crystal), but it belongs to the infrared range and is therefore not visible (Fig. 2a).

By tilting the crystal, one can change the phase matching, so that the beamlike emission is observed in other spectral ranges (Fig. 1d–f). As the wavelength of the enhanced beam approaches the visible range, both left and right parts of the ring become pronounced (Fig. 1f).

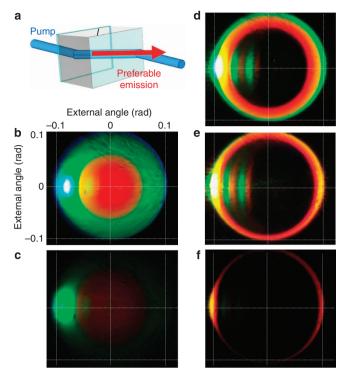


Figure 1 | Beamlike PDC along the pump spatial walk-off. The highest gain is achieved for emission along the pump Poynting vector, which inside the crystal is non-collinear to the wavevector (**a**). The optic axis direction is schematically shown on top of the crystal. Snapshots with a photographic camera (**b-f**) show the spectra of high-gain PDC at different crystal orientations: 32.97° (**b**, c), 33.4° (**d**), 33.7° (**e**) and 34° (**f**). The angular scale is shown in panel **b**; the grid is the same for all panels. Additional stripes in **d**, **e** are due to the reflections in the crystal. Emission at the walk-off angle and in the phase-matched direction is enhanced. This occurs, at different crystal orientations, for different colours (**d**-**f**). A snapshot with a neutral-density filter (**c**) shows colours without the saturation.

To demonstrate both twin beams emitted at the degenerate wavelength, we installed a bandpass filter (bandwidth 10 nm centred at 710 nm) after the crystal and tilted the crystal to the orientation 34.9° (see Supplementary Fig. 1). The resulting angular distribution was recorded by a charge-coupled device camera (Fig. 2b). One can hardly see the whole ring of emission at 710 nm (in fact it is seen with a much larger exposure time) but there is a strong peak in the direction corresponding to the walk-off angle in the crystal, as well as in the direction symmetrical with respect to the pump.

At other orientations of the crystal, the emission at the degenerate wavelength is much weaker, as shown in Fig. 2c, which presents one-dimensional cuts of the obtained twodimensional (2D) spectra (Supplementary Fig. 2). In agreement with the theory (Fig. 2d), the PDC peak observed in the walk-off direction exceeds the near-collinear emission by more than two orders of magnitude.

As seen in Fig. 2b, the angular divergence of both beams is very small. This is because amplification occurs within the angle a/L, where *a* is the pump beam waist and *L* is the crystal length. Because the pump divergence, λ_p/a , is on the same order of magnitude, the beams are nearly single-mode. This effect is similar to the generation of spatially single-mode PDC from two separated crystals¹². Indeed, in experiment we measured the effective number of spatial modes m = 1.4 at the maximal parametric gain G = 15, corresponding to the pump power of 30 mW (Supplementary Fig. 1). This measurement relies on the

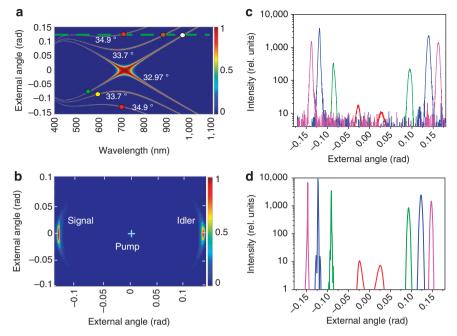


Figure 2 | Giant amplification of twin beams along the spatial walkoff. Frequency-angular spectra of type-I PDC from 355 nm pump in a 5-mm BBO crystal (**a**) show that at orientation 32.97° (as in Fig. 1b,c), only the infrared beam (white dot) propagates along the Poynting vector (green dashed line), but its twin is in the green spectral range (green dot). At orientation 33.7°, the enhanced twin beam is at wavelength 590 nm (yellow dot and Fig. 1e). At orientation 34.9°, the emission at the degenerate wavelength 710 nm is along the walk-off (red dots), and the 2D intensity distribution obtained by a charge-coupled device camera (**b**) shows hugely enhanced low-divergence twin beams. The rest of the PDC ring is faint and not seen in the linear scale. At other orientations, emission at 710 nm is much weaker, which is shown by logarithmic-scale one-dimensional angular intensity distributions measured (**c**) and calculated (**d**) for orientations 33° (red), 34° (green), 34.9° (blue) and 36° (magenta). Slight angular displacement of the right-hand experimental peaks is caused by the large (up to 10°) tilt of the crystal.

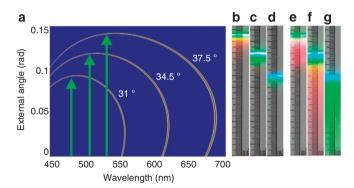


Figure 3 | Group matching for type-II PDC in a BBO crystal pumped by 0.9 ps pulses at 400 nm. Tuning curves for the ordinary down-converted radiation are shown for positive angles for crystal orientations 31°, 34.5° and 37.5° (**a**). For each orientation, at some wavelength the group velocity of the 'ordinary' photon matches that of the pump (green arrows). The PDC ring at this wavelength is hugely enhanced if the crystal is long enough (we used four 5-mm BBO crystals stacked together). (**b**-**d**) Snapshots of the intensity distributions on a screen placed in the far field, with the angular scale and the crystal orientations the same as in panel **a**. For comparison, spectra of a single 5-mm crystal with the same orientations show much broader emission spectra (**e-g**).

dependence of the normalized second-order intensity correlation function on the number of modes, see the Methods section.

Note that at low-gain PDC no such beamlike emission can be observed, only asymmetry in the angular spectrum¹³. The effect at high gain is known and widely used in parametric amplification¹⁴ but, to the best of our knowledge, has been never observed in twin-beam generation. A very special feature of the current configuration is that high directionality of radiation is

achieved without using a cavity, and that the wavelength of the enhanced radiation is tunable within a broad range. The idler beam can serve as a source of tunable broadband diffractionlimited infrared radiation, especially convenient because its copy is maintained in the visible-range signal beam.

High-gain PDC with group-velocity matching. While spatial walk-off can be, in principle, eliminated by using non-critical phase-matching, double-crystal configuration^{15,16} or periodically poled materials, temporal walk-off is inevitable whenever PDC or four-wave mixing is pumped by ultrashort pulses. Owing to the group-velocity difference between the pump and the twin-beam radiation, the pump pulse is delayed from the signal and idler pulses in the course of propagation through the nonlinear material, and only short crystals¹⁷ or fibres^{18,19} can be used for coherent generation of twin beams. Double-pass schemes²⁰ allow one to increase the interaction length but only twice. For instance, in the common case of collinear frequency-degenerate type-I PDC generated in a BBO crystal from the frequency-doubled Ti-sapphire laser (400 nm), a 180 fs delay emerges in a 1 mm crystal. However, at some other wavelength of the signal radiation, its group velocity can be equal to that of the pump. The phase matching can then be fulfilled by using non-collinear emission. The same situation can be realized for type-II PDC. Note that only one pulse, signal or idler, has to propagate together with the pump pulse. Its twin will be amplified as well, similarly to the spatial walk-off case. Hence, giant amplification of both twin beams should be expected.

In our experiment, we used type-II PDC in a BBO crystal pumped at 400 nm. Tuning curves of the 'ordinary' beam for positive angles are shown in Fig. 3a for the orientations 31°, 34.5° and 37.5°. Green arrows mark the positions of group-velocity matching. One should expect considerable amplification of

emission at these wavelengths in the case of a long crystal and high gain.

PDC was pumped by 0.9 ps pulses of frequency-doubled Mai Tai/Spitfire radiation with the repetition rate 5 kHz and the energy per pulse up to 0.1 mJ. To demonstrate the temporal walkoff, we reduced the spatial walk-off by focusing the pump beam only in the plane orthogonal to the principal one by means of cylindrical optics. In the principal plane, the beam full width at half maximum was 3.4 mm but in the orthogonal plane, 130 µ or 680 µ depending on the configuration. The spectra obtained from a single 5-mm crystal were compared with the ones of four 5-mm crystals placed one after another at a minimal distance of 3 mm (Supplementary Fig. 3). The effect is easily observable on a screen (Fig. 3). For PDC generated by 20 mm of BBO, there is huge amplification within a relatively narrow spectral range (Fig. 3b-d), while in the case of a 5-mm crystal the spectrum is more uniform over frequency (Fig. 3e-g). The angle at which amplification occurs is different depending on the orientation; this clearly shows that it is not related to the spatial walk-off.

For the quantitative characterization of the effect, we recorded the frequency spectra at different angles, with the crystals oriented at 37.5°. According to the tuning curve (Fig. 3a), each angle corresponds to a peak at a different wavelength. For PDC from 20 mm BBO, the peak at the group-velocity-matching wavelength 533.5 nm exceeds the one at 637.5 nm 250 times (Fig. 4). Because this difference is influenced by many frequencydependent factors^{21,22}, we also recorded spectra for a 5-mm crystal. Although the temporal walk-off is not negligible also in this case, the spectral distribution is much more uniform. Note that in both cases, the parametric gain was made the same (G = 8.6) at the wavelength 637.5 nm, by stronger focusing the pump in the case of a 5-mm crystal. The focusing was performed by a cylindrical lens (focal length 500 mm) or a cylindrical telescope (30:2.5) to avoid the transverse walk-off.

Discussion

This effect can be especially useful for generating twin beams in cavities²³ and whispering-gallery mode resonators²⁴ where, due to the large quality factor, nonlinear interaction occurs on a very large distance. This requires pump beams with large coherence length; however, if the group velocity of down-converted radiation at a certain wavelength coincides with that of the

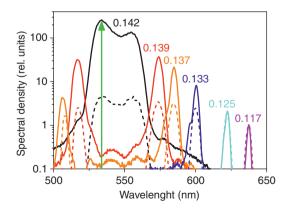


Figure 4 | Quantitative characterization of group matching. Frequency spectra of PDC are recorded at external angles 0.142, 0.139, 0.137, 0.133, 0.125 and 0.117 rad for one (dashed line) and four (solid line) BBO crystals of length 5 mm oriented at 37.5°. In 20 mm of BBO crystal, the emission at the group-matched wavelength 533.5 nm (shown by green arrow) is enhanced 250 times compared with the wavelength 637.5 nm, where there is no group-velocity matching. In a 5-mm crystal, the enhancement is not so dramatic.

pump, strong twin-beam generation can be realized even from short pulses. Under certain conditions, this radiation will be single mode.

The effect will have interesting consequences for low-gain PDC. Indeed, the condition of temporal walk-off compensation, in combination with a large crystal length, will provide the absence of frequency correlations for femtosecond-pulsed PDC^{25,26}. At the same time, signal and idler photons will have very different spectral widths and, consequently, different pulse durations.

In periodically poled crystals or waveguides²⁷, phase matching can be satisfied also in the collinear regime by a proper poling. Near resonance, one can have the pump group velocity very different from the signal/idler group velocity. This could provide additional possibilities for engineering the spectrum.

In conclusion, we have shown that, in contrast to the common opinion, spatial and temporal walk-off is not necessarily degrading the generation of twin beams. When properly used, it can lead to the generation of bright, tunable and diffractionlimited twin-beam radiation. So far we have demonstrated the amplification of down-converted radiation by more than two orders of magnitude under the condition that the signal or idler pulses propagate in the same direction or with the same velocity as the pump pulse energy. More dramatic amplification can be expected for PDC or four-wave mixing in long nonlinear media (fibres, waveguides) or resonators.

Methods

Calculation of high-gain PDC spectra. Our model^{12,28} is based on the Bloch–Messiah reduction. Because the anisotropy manifests itself significantly only in the principal plane of the crystal, the Hamiltonian can be calculated using one Cartesian dimension^{16,28}. By passing to collective photon creation operators A_n^{\dagger} , B_n^{\dagger} corresponding to the Schmidt modes $u_n(\vartheta_s)$, $v_n(\vartheta_i)$, where ϑ_s and ϑ_i are the signal and idler angles, respectively, inside the crystal, we diagonalize the Hamiltonian:

$$H = i\hbar\Gamma\sum_{n}\sqrt{\lambda_{n}} \left(A_{n}^{\dagger}B_{n}^{\dagger} - A_{n}B_{n}\right), \qquad (1)$$

where λ_n are the Schmidt eigenvalues. We assumed here the absence of losses inside the crystal (which do not exceed 0.1%) and the undepleted pump approximation, which indeed holds true in our experiment. Further, we write time-depending differential equations for the new operators in the Heisenberg representation, and find their solutions given by the Bogolyubov transformations (see Supplementary Methods). The equations for the plane-wave operators can be obtained and solved analytically in the Heisenberg picture using the expression for the Schmidt operators. Then the mean photon number in the signal beam can be calculated by averaging over the vacuum state, which yields

$$\langle N_{\rm s} \rangle = \sum_{n} |u_n(\vartheta_{\rm s})|^2 \left(\sinh\left[\sqrt{\lambda_n}\tilde{G}\right] \right)^2,$$
 (2)

 $\tilde{G} \equiv \int 2\Gamma dt$, and similarly for the idler beam. The parametric gain measured in experiment is $G \approx \sqrt{\lambda_0} \tilde{G}$. Thus, the total intensity distribution results from incoherent contributions of Schmidt modes with new weights that differ dramatically from the initial Schmidt eigenvalues λ_n and strongly depend on the parametric gain. The renormalized new weights of different Schmidt modes are

$$\Lambda_n = \frac{\left(\sinh\left[\tilde{G}\sqrt{\lambda_n}\,\right]\right)^2}{\sum\limits_n \left(\sinh\left[\tilde{G}\sqrt{\lambda_n}\,\right]\right)^2}.\tag{3}$$

Measurement of angular spectra. For recording the angular spectra, we placed an aspheric lens with the focal length f = 26 mm and numerical aperture 0.5 at a distance about 3 cm from the crystal (Supplementary Fig. 1, Supplementary Methods) and a charge-coupled device camera into the focal plane of the lens. The 2D spatial intensity distributions recorded by the camera corresponded then to the angular distributions of PDC radiation, with the external (outside of the crystal) angle θ given by the coordinate *x* as $\theta = \arctan(x/f)$. The relation between the internal angles $\vartheta_{i,s}$ and the external ones $\theta_{i,s}$ is given by Snell's law, $\sin \theta_{i,s}/\sin \vartheta_{i,s} = n_{i,s}$, with $n_{i,s}$ being the refractive indices for the idler and signal radiation. The one-dimensional spectra were obtained as cross-sections of the 2D distributions.

Measurement of frequency spectra. The frequency spectra were recorded by means of an Ocean Optics HR4000 spectrometer connected to a 400-µm

multimode fibre placed at 87 cm from the crystals (Supplementary Fig. 3, Supplementary Methods).

Measurement of the number of modes. The number of spatial modes was determined in the following way. One of the twin beams was collected, using a lens with the focal length 30 mm, into the 20- μ m input slit of a monochromator, with the collection efficiency exceeding 90%. The monochromator filtered a bandwidth of 0.1 nm, which led to the selection of 1.25 frequency modes. The output beam was collimated and sent into a Hanbury Brown–Twiss interferometer for measuring the normalized second-order correlation function $g^{(2)}$. The total number of frequency and angular modes *m* was found from the relation $g^{(2)} = 1 + 1/m$ (ref. 12) and turned out to be m = 1.75. Taking into account that 1.25 frequency modes was 1.4.

References

- 1. Boyd, R. W. Nonlinear Optics (Elsevier, 2008).
- 2. Agrawal, G. Nonlinear Fiber Optics (Elsevier, 2013).
- 3. Jedrkiewicz, O. *et al.* Detection of sub-shot-noise spatial correlation in high-gain parametric down conversion. *Phys. Rev. Lett.* **93**, 243601 (2004).
- Bondani, M. et al. Sub-shot-noise photon-number correlation in a mesoscopic twin beam of light. Phys. Rev. A 76, 013833 (2007).
- 5. Brida, G. et al. Measurement of sub-shot-noise spatial correlations without background subtraction. Phys. Rev. Lett. 102, 213602 (2009).
- Iskhakov, T. Sh., Chekhova, M. V. & Leuchs, G. Generation and direct detection of broadband mesoscopic polarization-squeezed vacuum. *Phys. Rev. Lett.* 102, 183602 (2009).
- Agafonov, I. N., Chekhova, M. V. & Leuchs, G. Two-color bright squeezed vacuum. *Phys. Rev. A* 82, 011801 (2010).
- 8. Brida, G., Genovese, M. & Ruo Berchera, I. Experimental realization of sub-shot-noise quantum imaging. *Nat. Photonics* **4**, 227–230 (2010).
- Lopaeva, E. D. et al. Experimental realization of quantum illumination. Phys. Rev. Lett. 110, 153603 (2013).
- Agarwal, G. S. *et al.* Quantum states of light produced by a high-gain optical parametric amplifier for use in quantum lithography. *J. Opt. Soc. Am. B* 24, 270–274 (2007).
- Iskhakov, T. Sh., Agafonov, I. N., Chekhova, M. V. & Leuchs, G. Polarizationentangled light pulses of 10⁵ photons. *Phys. Rev. Lett.* **109**, 150502 (2012).
- 12. Pérez, A. M. et al. Bright squeezed vacuum source with 1.1 spatial mode. Opt. Lett. 39, 2403–2406 (2014).
- Fedorov, M. V. *et al.* Anisotropically and high entanglement of biphoton states generated in spontaneous parametric down-conversion. *Phys. Rev. Lett.* 99, 163901 (2007).
- Gale, G. M., Cavallari, M., Driscoll, T. J. & Hache, F. Sub-20-fs tunable pulses in the visible from an 82-MHz optical parametric oscillator. *Opt. Lett.* 20, 1562–1564 (1995).
- Grangier, P. R., Slusher, E., Yurke, B. & La Porta, A. Squeezed-light-enhanced polarization interferometer. *Phys. Rev. Lett.* 59, 2153–2156 (1987).
- Perez, A. et al. Compensation of anisotropy effects in a nonlinear crystal for squeezed vacuum generation. Laser Phys. Lett. 10, 125201–125206 (2013).
- Lamas-Linares, A., Howell, J. C. & Bouwmeester, D. Stimulated emission of polarization-entangled photons. *Nature* 412, 887–890 (2001).
- Fan, J., Migdall, A. & Wang, L. A twin photon source based on optical fiber. Opt. Photonics News 3, 26–33 (2007).

- Smith, B. J. et al. Photon pair generation in birefringent optical fibers. Opt. Express 17, 23589–23602 (2009).
- Eisenberg, H. S. et al. Quantum entanglement of a large number of photons. Phys. Rev. Lett. 93, 193901 (2004).
- 21. Klyshko, D. N. Photons and Nonlinear Optics (Gordon and Breach, 1988).
- Spasibko, K. Y., Iskhakov, T. Sh. & Chekhova, M. V. Spectral properties of high-gain parametric down-conversion. *Opt. Express* 20, 7507–7515 (2012).
- 23. Wolfgramm, F. et al. Atom-resonant heralded single photons by interaction-free measurement. Phys. Rev. Lett. 106, 053602 (2011).
- Fürst, J. U. et al. Quantum light from a whispering-gallery-mode disk resonator. Phys. Rev. Lett. 106, 113901 (2011).
- Grice, W. P., U'Ren, A. B. & Walmsley, I. A. Eliminating frequency and space-time correlations in multiphoton states. *Phys. Rev. A* 64, 063815 (2001).
- 26. Mosley, P. J. *et al.* Heralded generation of ultrafast single photons in pure quantum states. *Phys. Rev. Lett.* **100**, 133601 (2008).
- Eckstein, A., Christ, A., Mosley, P. J. & Silberhorn, C. Highly efficient single-pass source of pulsed single-mode twin beams of light. *Phys. Rev. Lett.* 106, 013603 (2011).
- Sharapova, P. R., Pérez, A. M., Tikhonova, O. V. & Chekhova, M. V. Schmidt modes in the angular spectrum of bright squeezed vacuum. *Phys. Rev. A* **91**, 043816 (2015).

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Author contributions

A.M.P. and K.Yu.S. carried out the experimental work; A.M.P., K.Yu.S and M.V.C. contributed to the analysis of the data; P.R.Sh. and O.V.T. provided the theoretical background; M.V.C. and G.L. initiated and supervised the project; all authors discussed the results and contributed to the writing of the manuscript.

Additional information

Supplementary Information accompanies this paper at http://www.nature.com/ naturecommunications

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