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Symmetry breaking in drop bouncing on curved surfaces

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The impact of liquid drops on solid surfaces is ubiquitous in nature, and of practical importance in many industrial processes. A drop hitting a flat surface retains a circular symmetry throughout the impact process. Here we show that a drop impinging on *Echevaria* leaves exhibits asymmetric bouncing dynamics with distinct spreading and retraction along two perpendicular directions. This is a direct consequence of the cylindrical leaves that have a convex/concave architecture of size comparable to the drop. Systematic experimental investigations on mimetic surfaces and lattice Boltzmann simulations reveal that this novel phenomenon results from an asymmetric momentum and mass distribution that allows for preferential fluid pumping around the drop rim. The asymmetry of the bouncing leads to $\sim 40\%$ reduction in contact time.

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Since Worthington's pioneering work studying the complex dynamics of liquid drops impacting on solid surfaces¹ in 1876, extensive progress has been made in understanding and controlling drop dynamics on various textured surfaces. Recent research, in particular, has shown that the spreading and retraction dynamics of impacting drops is highly dependent on both the roughness and the wettability of the underlying substrate^{2–15}. Progress has been driven by the intrinsic scientific interest and beauty of fluid impacts¹⁶, together with recent advances in the ability to fabricate micro and nanoscale surfaces^{17,18}, and also because drop impact is central to many technological processes including DNA microarrays, digital lab-on-a-chip, water harvesting, dropwise heat removal and anti-icing^{19–25}.

Drops hitting superhydrophobic surfaces can bounce off quickly because of the low friction between drop and the substrate, either at the end of retraction^{26,27} or at their maximum extension in a pancake shape^{28–30}. Normally the drop retains a circular symmetry during the bouncing and the contact time is bounded below by the Rayleigh limit³¹. However, Bird *et al.*⁴ showed that drops impacting on surfaces where asymmetry is introduced with ridges, an order of magnitude smaller than the drop, leave the surface with shortened contact time. Moreover, the contact time of drops bouncing on a superhydrophobic macrotexture can take discrete values depending on the drop impact point relative to the texture and its impact velocity⁵. The left–right symmetry can be also broken by imposing a surface gradient to induce a directional movement^{32–36} or by considering impacts on a moving surface^{37,38}. In these studies, the reported surfaces are still macroscopically flat, with the feature size at the scale of microns or nanometres.

In nature, many plant surfaces have convex or concave architecture with curvature at the millimetre scale, as exemplified by the *Echeveria* surface. We hypothesize that drops on such unusual surfaces might exhibit distinct hydrodynamics. Therefore in this work we design asymmetric surfaces with macrottextures comparable to the drop size. We demonstrate that a drop impacting on such surfaces displays asymmetric bouncing with a

~40% contact time reduction compared with that on the equivalent flat substrate. Further experimental visualization shows that the impacting drop undergoes a preferential spreading in one direction and leaves the surface owing to fast retraction in the perpendicular direction. Evidence from lattice Boltzmann simulations and analytical analysis reveals that the drop hydrodynamics is due to the anisotropic architecture, which engenders an asymmetric momentum distribution and flow coupling.

Results

Asymmetric bouncing on natural surfaces. We first consider the impact of drops on a natural *Echeveria* surface. Figure 1a–c shows the optical and scanning electron microscopic (SEM) images of the surface. The *Echeveria* leaves approximate cylinders with a diameter of curvature (D) a few millimetres. The surface of the leaves is covered by waxy nanofibers³⁹ yielding an apparent contact angle over 160° . Our experimental results are very different from those conventionally reported on a flat superhydrophobic surface^{3,6}. Figure 1d presents selected snapshots of a drop of diameter $D_0 = 2.9$ mm impinging on the convex surface of an *Echeveria* leaf with a diameter of curvature of ~ 8.2 mm. The impact velocity is 0.63 ms^{-1} , corresponding to $We = 7.9$ and $Oh = 0.0028$. Here $We = \rho v_0^2 r_0 / \gamma$ is the Weber number, where r_0 is the drop radius, ρ is the liquid density and γ is the liquid–vapour surface tension, and $Oh = \mu / \sqrt{\rho \gamma r_0}$ is the Ohnesorge number, with μ the liquid viscosity. The impacting drop initially spreads isotropically, but the drop spreading becomes increasingly anisotropic as the drop starts to retract (Supplementary Movie 1). Interestingly, when the liquid in the axial (straight) direction has started to retract at ~ 3.8 ms, the liquid in the azimuthal (curved) direction continues to spread, with a sustained fluid transfer from the axial direction. Once the fluid in the axial direction has fully contracted at 11.8 ms ($= 1.73 \sqrt{\rho r_0^3 / \gamma}$), the drop leaves the surface maintaining an elongated shape along the azimuthal direction, indicating that the asymmetric bouncing can be driven by preferential retraction along just one axis. The contact time (t_0) is $\sim 30\%$ faster than that

Figure 1 | The surface morphology of *Echeveria* and drop impact dynamics. (a) Optical image of *Echeveria* showing the curvature of individual leaves. (b) Low-resolution SEM image of an *Echeveria* surface showing protuberances on the scale of $100 \mu\text{m}$. (c) Magnified SEM image of a single protuberance consisting of countless nanofibers. (d) Selected snapshots showing a drop ($D_0 = 2.9$ mm) impacting on an *Echeveria* leaf at $We = 7.9$. The first row is a cross-section parallel to the azimuthal direction and the second is a plan view from above the drop. After spreading to its maximum extension in the axial direction at 3.8 ms, the drop continues its spreading in the azimuthal direction and reaches its maximum spreading at 5.0 ms, while retracting in the axial direction. The drop bounces off the surface at 11.8 ms with a much shortened contact time compared with that on the flat surface (16.1 ms, Supplementary Fig. 1).

on the equivalent flat substrate^{8,9,26} (which is compared in Supplementary Movie 2, right and Supplementary Fig. 1) and sphere (Supplementary Fig. 2). A reduction in contact time due to bouncing asymmetry was first reported by Bird *et al.*⁴ who considered drop break-up on surfaces with ridges of size $\sim 100 \mu\text{m}$.

Symmetry breaking in droplet bouncing on synthetic surfaces. Inspired by this unexpected result we hypothesize that new physics comes into play when symmetry-breaking mechanisms are introduced by the convexity of the surface^{40,41}. To explore these, we fabricated curved surfaces with varying diameters of curvature D between 4 and 20 mm (Supplementary Fig. 3). The surfaces are coated with hydrophobic rosettes of diameter $\sim 5 \mu\text{m}$ to give an intrinsic contact angle of $\sim 160^\circ$.

Drop impact on the fabricated surfaces reveals similar bouncing dynamics to that on the natural surface. Figure 2a shows the time evolution of the spreading diameters in the axial and azimuthal directions on the curved surface with $D=8 \text{ mm}$ at $We=7.9$ (Supplementary Movie 2, left). The maximal spreading diameter in the axial direction is measured to be 4.45 mm, following the scaling⁴² of $\sim We^{1/2}$. To quantify the spreading asymmetry we define k as the ratio of the maximum values of the drop spreading diameters in the azimuthal and axial directions. Figure 2b plots the variation of k as a function of the diameter of curvature normalized by the initial drop diameter (D/D_0). It is apparent that an increase in the structural anisotropy gives rise to a larger k . Note that for the flat or spherical superhydrophobic surfaces, the k is equivalent to unity, suggesting that the asymmetric spreading is modulated by the structural anisotropy. Figure 2c plots the variation of the contact time as a function of normalized diameter of curvature for different We . The contact time is also significantly affected by the anisotropy: at a constant We , the symmetry-breaking surfaces with

smaller diameters of curvature corresponds to smaller contact times. To better elucidate the dependence of the contact time on the surface structure, we decompose the contact time into the spreading time t_1 and retraction time t_2 along the axial direction in Fig. 2d. It is apparent that the spreading time is almost independent of surface curvature, partially due to the fact that the spreading is mainly dominated by the inertia. However, the retraction time shows a strong decrease with decreasing D : for $D=6 \text{ mm}$ the total decrease in contact time compared with a flat substrate is $\sim 40\%$ for $We \sim 15$. These results, in conjunction with the spreading dynamics shown in Fig. 2a,b, indicate that the asymmetric bouncing is indeed modulated by the asymmetric curvature whose size is comparable to that of the impacting drop. This argument is also confirmed by our control experiment on the spherical surface where the bouncing is symmetric and the contact time is the same as that on a flat surface (Supplementary Fig. 2).

Mechanisms for symmetry breaking and contact time reduction.

To interpret the mechanism behind the asymmetric bouncing observed in our experiments, we first considered the effect of surface topography on initial drop momentum. Two factors will lead to more momentum being transferred in the azimuthal direction than in the axial direction. First, distinct from the flat surface, the impact area on the curved surface is approximately elliptical. As a result of such an asymmetric footprint, more momentum will be transferred perpendicular to the long axis of the ellipse, that is, along the azimuthal direction. Second, fluid landing on the curved sides of the asymmetric surface has a tangential component of momentum that will continue unperturbed.

To test this interpretation, we modelled the drop impact, using a lattice Boltzmann algorithm to solve the continuum equations of motion of the drop^{43,44}. Details of the equations and the

Figure 2 | Asymmetric bouncing on bio-inspired asymmetric surface. (a) The variations of contact line length in the axial and azimuthal directions as a function of time. The drop continues spreading in the azimuthal direction after it reaches its maximum extension in the axial direction at 3.8 ms. While retracting in the axial direction, the lateral extension in the azimuthal direction remains almost constant. (b–d) The variation of the k (defined as the ratio of the maximum spreading diameters in the azimuthal and axial directions), the contact time, the axial spreading time t_1 (left) and axial retraction time t_2 (right) as a function of surface curvature D (normalized by drop radius D_0) under different We .

numerical algorithm are given in the Methods section. Figure 3a shows snapshots of the time evolution of a drop impacting on the asymmetric surface obtained from the numerics. Comparison of the simulation results with those obtained in the experiments (Fig. 1d and Supplementary Movie 1) shows that the evolution of the drop shape is qualitatively the same during the rebound, with the axial direction starting to retract first. The colour shading represents the relative heights of the fluid at each time, red high to blue low. Note that, in particular, (the third image) a large rim develops in the azimuthal direction. The arrows in the figure show the local fluid velocity field. Consistent with our experimental observation, during the initial spreading stage, the fluid exhibits a radial outwards flow. As spreading progresses, there is a preferential flow to the azimuthal direction that drives the formation of the larger liquid rims. The liquid pumped around the rim to the azimuthal direction acts to amplify the contrast in the drop retraction between the two directions,

leading to a positive feedback that enhances the asymmetry of the bouncing. This scenario is in striking contrast to that on the flat surface.

The simulations allow us to understand how the asymmetric surface topography affects the drop bouncing. Figure 3b displays the variation of the momentum in the horizontal direction relative to the initial impact momentum as a function of time during the impact on the surface with $D/D_0 = 1.2$. In the figure, a positive momentum corresponds to drop spreading while a negative momentum corresponds to drop retraction. From the graph, it can be clearly seen that the momentum in the azimuthal direction is always larger than that in the axial direction. When the momentum in the axial direction starts to reverse its direction, the azimuthal momentum remains positive and indeed increases slightly. This is consistent with our experimental observations that the drop sustains a spreading state without retracting in the azimuthal direction, demonstrating the positive

Figure 3 | Asymmetric bouncing verified by simulation. (a) Selected snapshots obtained using the lattice Boltzmann simulation showing the time evolution of a drop bouncing on an asymmetric surface for $We = 10.6$ and $Oh = 0.0028$. The top panel corresponds to the cross-section view parallel to the azimuthal direction, and the bottom panel is the plan view from above the drop. The colours in the plan view are indicative of the relative height of the liquid at each time (Fig. 4e for quantitative data) and arrows indicate the velocity flux. (b) The time evolution of the momentum normalized by the total initial momentum along the axial (red) and azimuthal (black) directions on the curved surface ($D/D_0 = 1.2$), and for any direction on a flat surface (blue), under the same $We = 10.6$ and $Oh = 0.0028$. The positive values correspond to the spreading stage while the negative values correspond to drop retraction. (c) The ratio between the maximum momentum transferred into the azimuthal direction and the axial direction as a function of normalized surface curvature D/D_0 . (d) Simulations of the variation of the contact time relative to that for a flat superhydrophobic surface showing a different dependence on D/D_0 in different regimes. (e) Experimental results for the variation of the critical We for drop break-up (We_c) with D/D_0 . Error bars denote the range of the measurements.

feedback from the axial direction that enables this to occur. As a comparison, we also plotted the variation of momentum on a flat surface (blue curve in Fig. 3b), which shows that the momentum along any given direction for a flat substrate lies between the two curves for the asymmetric surface. To quantify how the momentum anisotropy is dictated by the surface topography, we calculated the ratio between the maximal momentum in the azimuthal direction and that in the axial direction. As shown in Fig. 3c, the momentum anisotropy decreases with increasing diameter of curvature.

To further validate that the momentum asymmetry is responsible for the asymmetric bouncing, we simulated drop impact on a flat surface by introducing a momentum asymmetry into the simulation manually immediately after the initial collision. The momentum in the azimuthal direction was increased by a factor of 2 while the momentum in the axial direction was reduced by a factor of 2. Indeed, as shown in Supplementary Fig. 4, the drop shows qualitatively the same bouncing pathway as that in Fig. 3a. In particular, the drop retraction in the axial direction is much faster than that in the azimuthal direction, which is consistent with our experimental results. Moreover, to validate that a momentum asymmetry can be induced by an elliptical drop footprint, we also simulated an initially elliptical drop impacting a flat substrate which, again, led to a very similar asymmetric bouncing (Supplementary Fig. 5).

For surface obstacles much smaller than the drop, such as those used in Bird *et al.*⁴, the initial momentum asymmetry is largely suppressed. Notably, the plot of the variation of the contact time relative to that on a flat surface as a function of D/D_0 (Fig. 3d) displays a minimum at $D/D_0 \sim 1$. This is expected since, as the obstacle size decreases the surface becomes more comparable to a flat surface and the momentum anisotropy starts to get smaller and has less effect. However, in this regime, the critical Weber number for drop splitting (We_c) is low (Fig. 3e) and drops in the experiments tend to break-up giving the mechanism for contact time reduction described by Bird *et al.* The drop retracts faster along the ridge than perpendicular to it. As a result it tends to fragment and the newly formed inner rims retract away from the obstacle resulting in the contact time reduction. These two regimes for contact time reduction serve to emphasize the richness of the physics underlying bouncing on curved and irregular surfaces.

We perform a simple hydrodynamic analysis to explain the contact time reduction associated with the asymmetric bouncing. Since the drop spreading is mainly governed by the inertia, we consider the drop retraction process here. The drop retraction is primarily driven by the decrease in surface energy of the thinner central film, which leads to a force pulling the rim of the drop inwards. For conventional bouncing, the drop retraction is symmetric and the surface energy of a central film of radius r is $E_s \approx \pi r^2 \gamma (1 - \cos\theta)$, where θ is the apparent contact angle, giving a retraction force⁴⁵, $F_s = \frac{\partial E_s}{\partial r} \approx 2\pi r \gamma (1 - \cos\theta)$. Fast drop detachment requires not only a large driving force in the central film, but also a small inertia of the rim. However, due to the symmetric retraction and mass conservation, these two processes are mutually exclusive, since a reduction in the central film radius r leads to an increase in the mass of the liquid rim as is apparent in Supplementary Fig. 1.

Interestingly, for the symmetry-breaking surface this conflict is resolved by the preferential fluid flows around the drop rim (Figs 3a and 4a). To demonstrate this, in Fig. 4c we showed selected plan-view images of drop retraction on the asymmetric surface. The panels just above (Fig. 4b) and below (Fig. 4d) this figure correspond to the side view of drop retraction in the axial direction and azimuthal direction, respectively. It is clear that owing to the preferential liquid pumping to the azimuthal direction

(blue arrows), the size of rim in the axial direction is almost unchanged throughout the retraction stage, whereas that in the azimuthal direction shows a significant increase. This is confirmed by the simulation results in Fig. 4e, which plots the time evolution of the rim heights in the two directions and the height of the central film. Notably, the mass per unit length of the rim along the azimuthal direction is more than twice of that in the axial direction when the rims from opposite sides of the drop meet just before bouncing, confirming the apparent symmetry breaking in the mass distribution. Moreover, the desirous reduction in the mass of rim in the axial direction is achieved without compromising the retraction force. Owing to the preferential spreading on the curved surface, the central film can be approximated by an ellipse with a major axis b (in the azimuthal direction) and minor axis a (in the axial direction). Thus, the surface energy of the central film is $E_a \approx \pi a b \gamma (1 - \cos\theta)$. As the asymmetric retraction proceeds the length of the major axis b remains constant while there is a continuous reduction in a . Hence, the retraction force is now $F_a \approx \pi b \gamma (1 - \cos\theta)$, and the ratio of the force acting on the rim on the curved surface to that on the flat surface is $b/2r$. Experimentally, the drop diameter $2r$ on the symmetric surface continually decreases while the azimuthal diameter b on the curved surface remains unchanged. Thus, the synergy of the enhanced retraction force and reduced mass of rim rendered by the symmetry-breaking structure results in a remarkably efficient pathway for fast drop retraction. The convergence of liquid in the axial direction translates into motion perpendicular to the surface and drives the drop upwards. Moreover, as shown in Fig. 4d, as the drop retracts on the curved surface, the surface tension energy converts to kinetic energy with a velocity component in the vertical direction (red arrows), which will aid the bouncing. By contrast, on the flat surface, the drop transition from the oblate shape (7.6 ms) to a prolate one (16.1 ms) before its jumping takes a longer time (Supplementary Fig. 1).

Discussion

In a broad perspective, we expect that rapid bouncing driven by an asymmetric momentum transfer occurs on many surfaces that have asymmetric structure on the order of the drop size. The most obvious extension is to a surface that is concave in one direction and flat in the perpendicular direction. Figure 5 shows snapshots of a water drop hitting a concave surface with a diameter of curvature $D = -8$ mm at $We = 7.9$. By contrast to the impact on the convex surface, there is a preferential fluid flow from the azimuthal direction to the axial direction. After the drop reaches its maximum spreading in the azimuthal direction at ~ 3.0 ms, the liquid in the axial direction continues to spread and finally leaves the surface in a shape elongated along the axial direction at ~ 10.3 ms ($= 1.58 \sqrt{\rho r_0^3 / \gamma}$) (Supplementary Movie 3). Indeed the contact time reduction is even more pronounced than that on the convex surface, suggesting that corrugated surfaces may be excellent candidates for enhanced water repellency and other applications. For example, many pathogens and diseases are transmitted through drops^{46,47}, and thus the fast drop detachment from natural plant and our synthetic surfaces might significantly decrease the likelihood of virus and bacteria deposition. In addition, the presence of large-scale curved topography on corrugated surfaces could offer promise for enhanced heat transfer performances and anti-icing^{19,22,23}. Moreover, these corrugated surfaces with such millimetre-scale features are scalable in manufacturing. Thus, we envision that the asymmetric bouncing discovered on curved surfaces not only extends our fundamental understanding of classical wetting phenomenon, but also offers potential for a wide range of applications^{19,21,24,46,47}.

Figure 4 | Drop retraction and bouncing dynamics. (a) Schematic drawings of the rim and central film on the symmetric and asymmetric surfaces, respectively. On the symmetric surface, the rim retracts uniformly inwards towards the central film. On the asymmetric surface, the central film is an ellipse with major axis b (in the azimuthal direction) and minor axis a (in the axial direction) and retraction is primarily along the axial direction. (b) Selected side-view images of drop retracting on the asymmetric surface in the axial direction. The drop rim is drawn inwards by the central film and the size of rim remains almost unchanged in the majority of retraction process. (c) Selected plan-view images of drop retracting on the asymmetric surface. (d) Selected side-view images of drop retracting in the azimuthal direction. Owing to preferential liquid pumping around the rim (blue arrows), there is a continuous increase in the height of the azimuthal rim. Moreover, as the drop retracts on the curved surface, the surface tension energy converts to kinetic energy with a velocity component in the vertical direction (red arrows). (e) Comparison of the time evolution of the normalized rim heights in the axial and azimuthal directions based on the simulation. The height is scaled by the drop diameter D_0 and time by the contact time t_0 . During the retraction stage the axial rim height stays roughly constant while the azimuthal rim height increases greatly owing to the preferential flow and mass transfer. The reduced mass of the axial rim rendered by the symmetry-breaking flows results in a remarkably efficient pathway for fast drop retraction.

Figure 5 | Drop bouncing behaviour on a concave surface. Selected snapshots showing a drop ($D_0 = 2.9$ mm) impacting on the concave surface (with a diameter of curvature $D = 8.0$ mm) at $We = 7.9$ both from the side view (a) and plan view (b). After spreading to its maximum extension in the azimuthal direction at 3.0 ms, the drop continues its spreading in the axial direction and reaches its maximum spreading at 6.6 ms. It finally bounces off the surface after a contact time of 10.3 ms, reduced by $\sim 40\%$ compared with that on a symmetric surface. More details are shown in Supplementary Movie 3.

Methods

Preparation of the asymmetric surfaces. The asymmetric convex surfaces were fabricated on copper plate by combined mechanical wire cutting and chemical etching. A series of convex surfaces were first cut with arc diameters ranging from 6 to 20 mm. Then the as-fabricated surfaces were coated with hydrophobic rosettes of average diameter ~ 5.0 μm to render them superhydrophobic. More specifically, after ultrasonic cleaning in ethanol and deionized water for 10 min, respectively, the surfaces were washed by diluted hydrochloric acid (1 M) and deionized water,

followed by drying in nitrogen stream. They were then immersed in a freshly mixed aqueous solution of 2.5 mol l^{-1} sodium hydroxide and 0.1 mol l^{-1} ammonium persulphate at room temperature for ~ 60 min, after which they were fully rinsed with deionized water and dried again in nitrogen stream. After the oxidation process, the surfaces were uniformly coated by CuO flowers of diameter ~ 5.0 μm . All the surfaces were modified by silanization by immersion in a 1 mM *n*-hexane solution of trichloro-(1H, 1H, 2H, 2H)-perfluorooctylsilane for ~ 60 min, followed by heat treatment at ~ 150 $^{\circ}\text{C}$ in air for 1 h to render superhydrophobic.

Characterization of the surfaces. The optical images of *Echeveria* were recorded by a Nikon digital camera (Digital SLR Camera D5200 equipped with a Micro-Nikkor 105 mm f/2.8G lens). The micro/nano structures of protuberances and nanofibers were characterized by a field-emission SEM (Quanta 250 FEG). Owing to the extremely low conductivity of the *Echeveria* surface, a thin layer of carbon was coated on the surface before the SEM measurement.

Contact angle measurements. Owing to the asymmetric structure, it is difficult to measure the contact angle of the as-fabricated asymmetric surfaces. For the flat surface coated with rosettes (subject to the same treatment), the apparent, advancing (θ_a) and receding contact angles (θ_r) are $163.4^\circ \pm 2.6^\circ$, $165.1^\circ \pm 2.1^\circ$ and $161.9^\circ \pm 1.5^\circ$, respectively. These values are the average of five measurements.

Impact experiments. Impact experiments were performed in ambient environment, at room temperature with 60% relative humidity. Briefly, the Milli-Q water drop of $\sim 13 \mu\text{l}$ (with drop diameter $\sim 2.9 \text{ mm}$) was released from a fine needle equipped with a syringe pump (KD Scientific Inc.) at different heights to vary the impact velocity on the substrate. The impact dynamics of drop was captured simultaneously from side view and plan view by using two synchronous high-speed cameras (Fastcam SA4, Photron limited) at a frame rate of 10,000 fps with a shutter speed 1/93,000 s. The configuration of the drops during impact was measured using ImageJ software (version 1.46, National Institutes of Health, Bethesda, MD).

Simulations. The hydrodynamic equations of motion of the fluid are

$$\frac{\partial p}{\partial t} + \rho c_s^2 \nabla \cdot \mathbf{u} = 0, \quad (1)$$

$$\rho \left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right) = -\nabla p - C \nabla \mu + \nabla \left[\rho c_s^2 \lambda \cdot \left(\nabla \mathbf{u} + (\nabla \mathbf{u})^T \right) \right], \quad (2)$$

where p is the pressure, ρ is the density, c_s is the speed of sound, $\mathbf{u}$ is the velocity, λ is the mean free path, C is the composition and μ is the chemical potential. The chemical potential term in equation (2) leads to phase separation between liquid and gas, creating a diffuse interface between the two phases. C , the phase field, which tracks the two phases, evolves according to

$$\frac{\partial C}{\partial t} + \nabla \cdot (\mathbf{u} C) = M \nabla^2 \mu, \quad (3)$$

where M is the mobility and the bulk chemical potential follows by minimizing the free energy functional

$$E_b = \int_V \left(E_0(C) + \frac{\kappa}{2} [\nabla C]^2 \right) dV. \quad (4)$$

Here $E_0(C)$ is the bulk energy density and κ controls the surface tension and interface width. The density ρ is then related to the composition by $\rho = C\rho_1 + (1-C)\rho_2$, where ρ_1 and ρ_2 are the densities of the liquid and gas, respectively.

The equations of motion were solved using the lattice Boltzmann algorithm described by Lee and Liu⁴³. The simulation box was made up of $150 \times 150 \times 200$ lattice points. The surface curvature was modelled by a set of steps whose size is small compared with the interface width and the wetting boundary conditions were implemented following Conington and Lee⁴⁴. No slip velocity boundary conditions were used on the solid surface and mirror image boundary conditions on the box sides. The simulation parameters in lattice units are given in Supplementary Table 1, and correspond to the dimensionless variables given in the same table. Note that the bond number was chosen to be zero so any gravity-driven effects could be excluded.

Also of note, the Ohnesorge number in our simulations (0.0068) is higher than that in the experiments (0.0028), corresponding to drop radius ~ 6 times smaller in the simulations. This is required for the simulations to run in a reasonable time. Although the smaller drops lose a larger fraction of their energy as viscous dissipation during bouncing, their behaviour is qualitatively unchanged.

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Author contributions

Y.L. and Z.W. conceived the research. Z.W. and J.M.Y. supervised the research. Y.L. and J.L. designed and carried out the experiments. Y.L. and M.A. analysed the data. M.A. and J.M.Y. ran the simulations. Z.W., J.M.Y., Y.L. and M.A. wrote the manuscript. Y.L. and M.A. contributed equally to this work.

Additional information

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