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Q in cosmology

THE following example in classical mechanics yields the key equations of relativistic cosmology, including the new equations by Harrison¹. The argument given here develops that of an earlier note².

A set of n gravitating particles of masses m_i are at positions $\mathbf{r}_i(0) = \mathbf{a}_i$ relative to a fixed origin at the time $t = 0$, when an explosion gives a radial motion $\mathbf{r}_i(t) = R(t)\mathbf{a}_i$ to all the particles. The scale factor R is the same for all the particles. The kinetic energy of the system at time t is a sum of terms of the type $\frac{1}{2}m_i v_i^2$, and the gravitational potential energy is a sum of terms of the form $(|\mathbf{a}_i - \mathbf{a}_j| = a_{ij})$

$$-G \frac{m_i m_j}{r_{ij}(t)} = -G \frac{m_i m_j}{a_{ij}} \frac{1}{R(t)}$$

Accordingly, the energy equation of the system is

$$E = A\dot{R}^2 - B/R, \quad A = \frac{1}{2} \sum_i m_i a_i^2, \quad B = \frac{G}{2} \sum_{i \neq j} \frac{m_i m_j}{a_{ij}} \quad (1)$$

To attain a formal analogy with relativistic cosmology, write

$$E/A = -kc^2, \quad B/A = C,$$

and add a cosmological energy term $A\lambda R^2/3$. This gives the following energy equation and its first and second time derivatives

$$\frac{\lambda}{3} = H^2 + \frac{kc^2}{R^2} - \frac{C}{R^3} \quad (H \equiv \dot{R}/R) \quad (2)$$

$$\frac{\lambda}{3} = \frac{C}{2R^3} - qH^2 \quad (q \equiv -\ddot{R}R/\dot{R}^2) \quad (3)$$

$$\frac{\lambda}{3} = QH^2 - \frac{C}{R^3} \quad (Q \equiv R^2 \ddot{R}/\dot{R}^3) \quad (4)$$

The importance of the Q parameter has already been noted¹. One obtains the basic cosmological differential equation in two forms which are independent of the experimentally little known parameter λ , by equating equations (2) and (3) or by equating (2) and (4)

$$\frac{kc^2}{R^2} = \frac{3C}{2R^3} - (q+1)H^2 \quad (5)$$

$$\frac{kc^2}{R^2} = (Q-1)H^2 \quad (6)$$

Adding twice (3) to (4) and taking (3) from (4):

$$\lambda = (Q-2q)H^2, \quad \frac{3C}{2R} = (Q+q)H^2 \quad (7,8)$$

In a Newtonian context, the system is ever expanding if E is positive; that is, if k is negative. By equation (6), the appropriate condition is $Q < 1$, and for $\lambda = 0$ models, it is equivalent to $q < \frac{1}{2}$ (equation (7)). The inequalities are reversed if the system is to collapse again. Note that only if one puts (ρ is the mass density)

$$C = \frac{8\pi}{3} G\rho R^3 \quad (9)$$

do these become the equations given by Harrison¹. The simplicity of the example given here is illuminating: the role of q , which determines whether a ($\lambda = 0$)-model is closed or open, can clearly be taken over by Q if $\lambda \neq 0$. A continuous distribution of gravitating matter, which is needed to obtain equation (9) in general relativity, and which was used in ref. 1, is clearly not needed here. A discrete distribution of galaxies with sufficient symmetry to ensure the continued validity of Hubble's Law is all that is required. It is to be emphasised that in Newtonian cosmology it is possible to give discussions of interacting particles and discrete matter distributions which give Hubble's Law, though the corresponding general relativistic problems remain unsolved.

This possibility has been noted already^{2,3}, but no example has been given before. The simplest distribution to verify this possibility is a set of eight galaxies, each of mass m , on the vertices of a cube of side $2a_0$, which are given velocities, v , radially away from the centre of the cube. Because of the seven other galaxies each galaxy is then subject to a deceleration in the direction of the centre. Its magnitude is

$$\frac{D}{2a(t)^2}, \quad D = \left[1 + \frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{9} \right] \frac{Gm}{2}$$

where $2a(t)$ is the side of the cube at time t . If the escape velocity $v_{\text{esc}} = \sqrt{(D/a_0)}$ has been exceeded, the Hubble parameter is

$$\frac{\theta^3(1+w^2)^{\frac{1}{2}}}{Dw^3}, \quad \theta \equiv (v^2 - v_{\text{esc}}^2)^{\frac{1}{2}}$$

$$w \equiv \theta\sqrt{[a(t)/D]}.$$

Essentially, a topic for so far undiscovered theorems in Newtonian physics is raised here: the classification of (usually unstable) particle configurations which, for a given interaction, are consistent with a Hubble type expansion; and expressions for the Hubble parameter should also be found in each case.

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Anomalous M₁ tide at Lagos

I HAVE recently described¹ the phenomenal appearance in the seas off western Europe of a tidal component with a period of exactly one mean lunar day, namely the "M₁ tide". Although only a few mm in amplitude, it is about ten times larger than one would expect from comparison with ordinary diurnal tides, and suggests a resonant response of