scientific correspondence

- 7. Ridley, R. G. Trends Microbiol. 4, 253-254 (1996).
- 8. Bendrat, K., Berger, B. J. & Cerami, A. Nature 378, 138 (1995).
- 9. Dansa-Petretski, M., Ribeiro, J. M. C., Atella, G. C., Masuda, H.
- & Oliveira, P. L. J. Biol. Chem. 270, 10893-10896 (1995).
- Graça-Souza, A. V., Petretski, J. H., Demasi, M., Bechara, E. J. H. & Oliveira, P. L. *Free Rad. Biol. Med.* 22, 209–214 (1997).

'Raise the stakes' evolves into a defector

To understand how cooperation can evolve by reciprocal altruism when individuals can make variable investments, Roberts and Sherratt¹ have introduced a new strategy, 'raise the stakes' (RTS), for a continuous version of the iterated 'prisoner's dilemma'. An individual investing I bears a cost I, while the recipient gets a benefit kI. For k > 1, this generalizes the standard prisoner's dilemma²⁻⁵. Over *R* alternating encounters^{6,7}, RTS is defined as follows: on the first move, invest a, subsequently raise your investment by 2b (or b) if your partner's previous investment bettered (or equalled) your last move, otherwise match your partner's last move. This strategy is denoted by $\sigma = (a,b)$. Roberts and Sherratt¹ reported that the strategy $\sigma = (1,1)$ performs well in computer simulations against various alternative strategies but did not consider how a population of RTS strategies with different a and b values evolves. We find that selection within RTS populations always acts to lower the values of a and b, hence RTS cooperation is not a robust phenomenon.

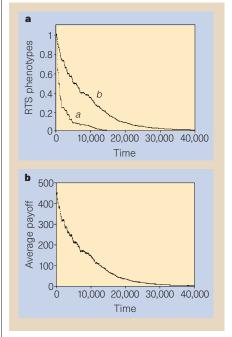


Figure 1 Simulation of the evolution of RTS strategies in the game studied in ref. 1. **a**, Changes in the population mean values of the RTS parameters *a* and *b* (starting values, a=1 and b=1). **b**, Change in the mean payoff. In this simulation, k=2, R=20 (the same as in all figures in ref. 1).

Assuming that mutations are small and rare, evolution in a population of RTS strategies can be understood analytically by using adaptive dynamics⁸. If the population consists of individuals using the strategy $\hat{\sigma} = (\hat{a}, \hat{b})$, then the vector field $\xi = \{ [\partial S(\sigma, \hat{\sigma}) / \partial a]_{\sigma = \delta}, [\partial S(\sigma, \hat{\sigma}) / \partial b]_{\sigma = \delta} \}$ determines the direction that optimizes the increase in payoff of a mutant strategy $\sigma = (a,b)$ (ref. 8), where S is the payoff from an iterated interaction. S, and hence ξ , can be calculated analytically and it can be shown that evolution acts to lower the (a,b)parameters of the population. This yields the general prediction that the (a,b) parameters in a population of RTS strategies evolve to zero under natural selection.

This prediction is verified by evolutionary simulations. Consider a population of RTS strategies, with new mutants introduced at a certain rate. In every generation, each strategy plays against all the others and their frequencies in the next generation are calculated using standard game dynamics⁸. Any strategy whose frequency falls below a given threshold is eliminated. A typical simulation (for parameter values used in ref. 1) is shown in Fig. 1. As predicted, the (*a,b*) parameters evolve to zero. Extensive simulation has confirmed the analytical result for all parameter values studied (including extreme cases, such as k = 100, R = 1,000).

Thus, in general, RTS evolves under natural selection into an unconditional defector (a=0, b=0). The lack of robustness of RTS arises because, although it is essential from an evolutionary perspective to allow the strategies $\sigma = (a,b)$ to vary continuously (as mutations can, in principle, result in arbitrary changes in a and b), the definition of RTS is discontinuous. From a biological viewpoint, the discontinuous nature of RTS is unrealistic as it is implausible that two strategies that are arbitrarily close would have qualitatively different behaviour.

Although reciprocal altruism with variable investments is an important approach to understanding the evolution of cooperation, our results indicate that new strategies are required to give a satisfactory theoretical account of this process. We have found, both analytically and by simulation, that investment strategies based on an individual's payoff in the previous round (see those used to study mutualism in ref. 9), rather than on the partner's investment, are evolutionarily robust and show how intraspecific cooperation can emerge with variable investments. We believe that these payoffbased strategies represent a more fertile area for future research than RTS strategies.

Timothy Killingback, Michael Doebeli

Zoology Institute, University of Basel, Rheinsprung 9, 4051 Basel, Switzerland e-mail: killingback@ubaclu.unibas.ch

Roberts, G. & Sherratt, T. *Nature* **394**, 175–179 (1998).
 Axelrod, R. & Hamilton, W. D. *Science* **211**, 1390–1398 (1981)

🚧 © 1999 Macmillan Magazines Ltd

- 3. Axelrod, R. The Evolution of Cooperation (Basic, New York, 1984).
- 4. Nowak, M. & Sigmund, K. Nature 355, 250–253 (1992).
- 5. Nowak, M. & Sigmund, K. Nature 364, 56–58 (1993).
- Nowak, M. & Sigmund, K. J. Theor. Biol. 168, 219–226 (1994).
 Frean, M. Proc. R. Soc. Lond. B 257, 75–79 (1994).
- Hofbauer, J. & Sigmund, K. Evolutionary Games and Population
- Dynamics (Cambridge Univ. Press, 1998). 9. Doebeli, M. & Knowlton, N. Proc. Natl Acad. Sci. USA 95,
- 8676–8680 (1998).

Sherratt and Roberts reply — Killingback and Doebeli argue that our cooperative strategy 'raise the stakes'¹ (RTS) can be continually undermined by selection for less generous strategies. They suggest that the "lack of robustness of RTS" arises from our use of a discontinuous strategy. However, this cannot be the case because the instability they report was in their reformulation of our model in continuous terms. Whether a continuous model is "essential" is debatable. Discontinuous strategies can be more realistic, particularly when resources are not infinitely divisible, hence our notion of a minimal non-zero investment of one unit.

We have also considered the relative success of rare, mutant continuous RTS strategies, but our analyses show that the mean initial investment parameter *a* will always evolve upwards. Simulations confirm this. Therefore, after trying to replicate their approach, we can find no evidence that even the continuous form of RTS-based cooperation can be eroded in the way they suggest. From this, we cannot exclude the possibility that they have misinterpreted the way RTS operates.

Killingback and Doebeli appear to agree that cooperation can thrive in variable investment systems and that successful strategies would tend to exhibit some initial build up of 'trust'. However, they claim that a strategy that depends on responding to the payoff would be more stable, which we question for two reasons. First, payoff dependency can lead to unnecessary investment in a sucker. Second, in a recent payoff-dependent model², negative payoffs always resulted in the end of cooperation, whereas RTS can rebuild relationships. These sources of instability are highlighted by the need for spatial structuring before payoff-dependent mutualism could evolve². Such assumptions are not required when cost-dependent mutualistic strategies are considered (unpublished data). (Further details are available from T.N.S.)

Thomas N. Sherratt*, Gilbert Roberts†

* Department of Biological Sciences, University of Durham, South Road, Durham DH1 3LE, UK e-mail: t.n.sherratt@durham.ac.uk †Evolution and Behaviour Research Group, Department of Psychology, University of Newcastle upon Tyne, Newcastle upon Tyne NE1 7RU, UK

^{1.} Roberts, G. & Sherratt, T. N. Nature 394, 175-179 (1998).

Doebeli, M. & Knowlton, N. Proc. Natl Acad. Sci. USA 95, 8676–8680 (1998).