book reviews

Hooke's law (otherwise known as earthquakes). Then they set out methods for quantifying the free oscillations of a spherically symmetrical Earth model, and show how these oscillations can be classified into groups that are affected by particular regions of the Earth's interior. Finally, they show how ellipticity and other forms of lateral variability can be handled.

Although the book's main emphasis is on normal modes, asymptotic methods are given to explain the principal features of body and surface waves. Most applications of seismology, including many of our discoveries about the Earth's internal structure, have been based on such asymptotic methods.

The book's presentation is authoritative, and graduate students and their supervisors for years to come will turn with gratitude to *Theoretical Global Seismology* to learn how to handle such complications as the effect of high initial deviatoric stress on the body force equivalent of an earthquake, or to interpret an accelerometer record at low frequencies when there can be significant contributions from changes in elevation (free air) and the overall gravity field.

Dahlen and Tromp's book shows us that seismology is a highly specialized science in that it focuses just on the internally generated motions of our planet. But, on the other hand, because we can study the Earth year after year and century after century, seismology also forces us to generalize our understanding of linear wave propagation. This we do in order to quantify the effects of inhomogeneity, high initial internal stress and discontinuities across a fault. Our new understanding is then available for other fields, for example waves in layered semiconductors.

The theoretical seismology in this book is not merely an intellectual achievement of a very high order, it is driven by the need to understand our planet and will be the basis of applied seismology and other practical studies of wave generation and propagation for decades to come.

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Science in culture

 π -fetishism

 π : A Darren Aronofsky film Artisan Entertainment: 1998 Graham Farmelo

is, I believe, the first film to be named after a mathematical symbol. This is a sign of the times: mathematics is seeping into popular culture, notably through books that have made Andrew Wiles's proof of Fermat's last theorem and the life of the number theorist Paul Erdös the stuff of recreational chatter.

No sooner have the educational Jeremiahs convinced us that mathematical standards in schools are both low and falling, at least in the West, than the subject becomes a big-business leisure activity among people who cheerfully admit they cannot cope with long division.

Hollywood discovered the new appeal of mathematics two years ago in the box-office hit *Good Will Hunting*, director Gus Van Sant's engaging tale of a delinquent mathematical genius. Set in Boston, the Athens of America, this was a surprisingly unsentimental portrayal of academic life in which mathematicians were for once played as more-or-less normal people and not as unkempt sociopaths with foreign accents as thick as treacle.

 π is more challenging fare, cinematically and mathematically. Like *Good Will Hunting*, it features a mathematician, but is — superficially at least — more concerned with how mathematics might be applied to the world. However, π is not another crowd-pleasing blockbuster from the dream factory, but an accessible art-house film, produced from the independent sector. It first shot to notoriety after winning a Directing Award at the 1998 Sundance Film Festival.

Director and co-writer Darren Aronofsky sets his film in some of the more unsavoury parts of New York. The action revolves around the misanthropic number theorist Max Cohen (played by Sean Gullette), a certifiable π -fetishist and, of course, a genius (why do film-makers seem to think that all mathematicians are brilliant?). He works alone at home in his seedy little apartment, an Alfred Brendel of the computer keyboard,

 $\pi\text{-fetishist}\operatorname{Max}\operatorname{Cohen}$ (Sean Gullette).



looking as if he's recovering from a lobotomy.

Cohen is convinced that the (almost random) digit sequence of π holds the key to understanding the pattern of daily changes in the New York stock market, which he monitors obsessively during his forays into the real world. "Mathematics is the language of nature," the narrator repeatedly intones, but Cohen does not bind himself to the rigours of scientific analysis, and so, as his mentor warns him, he is in danger of practising mere numerology.

As Max closes in on his solution, he is pursued by Wall Street hustlers intent on financial domination and by a Kabbalah sect trying to unlock the secrets behind their ancient holy texts. So we are in strange territory here, in the nether world of impure mathematics, tenuously connected to the real world via a 24-carat eccentric and a host of gargoyles. You can't help feeling sorry for Cohen's neighbour: would you like to live next to someone whose work involves washing a human brain down his bathroom sink?

Aronofsky does not aim to give us a mathematics lesson, so he does not consider in any detail what has made the number π such a rewarding mystery for mathematicians over the past 4,000 years. But he does gently try to interest us in the possibility of understanding the patterns we see around us. In one scene, Cohen looks out across a beach and we are invited to consider with him what might underlie the pattern of waves on the shore, of sea shells and of the light shimmering on the ocean.

Such quiescent moments are rare; π is in the main a sharply cut thriller, suffused with a bleakness intensified by grainy black-and-white photography and the menacing electronic soundtrack. The script is taut, the production inventive and the direction striking. It all amounts to the most imaginative début for a writer–director since Quentin Tarantino gave us *Reservoir Dogs*.

But π is not really about mathematics. Like Bertolt Brecht's *Life of Galileo*, which is less concerned with science than with the inability of a scientist to cope with the moral consequences of his work, Aronofsky's film uses his theme of mathematics-inspired hokum as a backdrop for something different — an off-beat analysis of paranoia.

Now that mathematics is 'cool', its ideas have new currency in the arts. For me, this is both welcome and surprising. When I was an undergraduate, I attended an entertaining lecture on *Principia Mathematica*, Bertrand Russell and Alfred North Whitehead's mind-stretching account of the foundations of mathematics. But if Russell and Whitehead were so smart, our professor mused, why didn't they have the wit to sell the film rights? In 1973, that remark brought the house down. It wouldn't surprise me now if the laugh turns out to be on us.

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