

sources, an interference-field would begin to be possible until, at a certain large value of v , the breadth of bands would correspond to that actually observed. The immediate neighbourhood of $\theta = 45^\circ$ is a region of extraordinary sensitiveness, in which $(\delta_2 - \delta_1)$ passes twice through a zero value. Very minute changes in θ make very great changes in the value of $(\delta_2 - \delta_1)$.

The numerical data do not lend themselves to any general statement as to the value of v ; but they point towards an actual value of v much greater than $c \times 10^{-4}$, however this may be accounted for. So far for the single-ray scheme, with the assumption required by it.

I prefer to deal not with a single incident ray but with an incident plane wave-front, and to study the kind of interference-field necessarily formed where the two reflected moiety-wave-fronts cross one another. Each virtual "image" of the previous working now appears as a point on a virtual plane wave-front, which is at right angles to the corresponding "single reflected ray" of the previous working. The working out is straightforward and unforced; and it again leads to remarkable and unexpected results.

Assuming θ to be an exact 45° , and $l = 1100$ cm. in an apparatus of ideal construction as above; then with yellow light ($\lambda = 0.0005892$ cm.) we have in the first orientation a band-breadth of 11784 cm. if $v = c \times 10^{-4}$; 117.84 cm. if $v = c \times 10^{-3}$; 1.1784 cm. if $v = c \times 10^{-2}$; and 0.011784 cm. if $v = c \times 10^{-1}$.

Assuming v to be $c \times 10^{-4}$, we similarly have band-breadths 0.0059 cm. if $\theta = 45^\circ + 1024''$; 0.59 cm. if $\theta = 45^\circ + 10'' \cdot 3$; 3928 cm. if $\theta = 45^\circ + 0'' \cdot 001$; 11784 cm. if $\theta = 45^\circ$; ∞ if $\theta = 45^\circ - 0'' \cdot 0005$; 11784 cm. if $\theta = 45^\circ - 0'' \cdot 001$; 59.22 cm. if $\theta = 45^\circ - 0'' \cdot 103$; 0.59 cm. if $\theta = 45^\circ - 10'' \cdot 3$; 0.0059 cm. if $\theta = 45^\circ - 1036'' \cdot 43$.

Working out and tabulating combinations of various θ 's and v 's and orientations we might hope, if we had an extraordinarily accurate knowledge of the lengths and angles involved, to be able to reach a conclusion as to the operative value of v from the band-breadths alone. The comparative shift of bands as between two orientations is not helpful in this respect; it depends upon a remainder in decimal places only, where we do not know either l or λ to a sufficient number of working figures. ALFRED DANIELL.

P.S.—By the courtesy of the Editor I have seen Sir Oliver Lodge's comment on the above letter. May I explain further that no bands would or ought to appear unless the instrument be in sufficiently rapid motion when the semi-transparent mirror is set at an exact $\theta = 45^\circ$; if at any other angle, there will always be a certain amount of separation of the virtual images which may not be sufficient to produce an interference-field until aided by a sufficient velocity of movement (smaller than in the former case) producing a farther separation of the virtual images. The breadth of bands is a function of θ and v .

THE Michelson-Morley experiment looked for a shift of well-known interference-bands, about the formation of which there was no doubt or controversy. Ordinary wave theory explains the appearance of these bands with ease. Dr. Daniell, however, claims that no bands would or ought to appear unless the instrument was in motion, and that the width of the bands is itself an indication of the rapidity of motion, which is thereby proven to have a high value. This view is so hopelessly unorthodox that it is difficult to regard it with equanimity. Probably he is attending to one single precise ray—whatever that may be—and not to a small portion of a wave-front, with its inevitable slight obliquities. OLIVER LODGE.

The Theory of Hearing.

IN his letter in NATURE of February 14, p. 228, Prof. Scripture directs attention to the valuable work on the theory of hearing done at the New York research laboratories of the American Telephone and Telegraph Company. He refers to the papers of Fletcher, and of Wegel and Lane. The results obtained by these experimenters, in his opinion, completely confute the resonance theory, though he considers that "The simple facts of the accelerated toothed wheel and of portamento speech . . . ought to have been enough to convince any one."

All minds do not function alike, and those propositions which appear self-evident to one are by no means so to another. As an illustration of this truism one finds that Prof. Scripture, though he avails himself readily of the experimental results in question, rejects at once as unworthy of serious consideration the interpretation of those results given by the experimenters themselves. To him it appears self-evident that the results are wholly inconsistent with the resonance theory, though the experimenters state their conclusions in terms of that modification of the resonance theory to which they give the name, the "dynamic theory."

The cochlea as conceived by Wegel and Lane is a highly damped resonating organ giving more or less localised responses to simple tones conveyed to it. The pitch of the tones heard is determined by the maximum points of the disturbances in the basilar membrane. By the term "non-linear" response they imply (as seems to the writer) that the relation at various pitch levels between the intensity of the impulse and the loudness of the tone heard cannot be expressed graphically by a straight line. From this they deduce the generation of combination tones and subjective harmonics in the cochlea. Their theoretical deductions from the results of their experiments are perhaps vitiated by reason of their having left out of consideration the progressive graduation in tension of the basilar fibres by the spiral ligament. In any case there is nothing in them inconsistent with the resonance theory.

Fletcher's results are indeed startling at first sight. The elimination of the fundamental and the first four upper partials from a clarinet tone produced no alteration of the pitch of the tone, the fundamental still appearing as the characteristic pitch. He explains this as being due to the difference tone generated by the remaining partials. To Prof. Scripture this explanation appears so surprising that he can only express his feelings by a note of exclamation. To the writer the suggestion appears rational, and indeed inevitable. Are we to understand that Prof. Scripture does not believe in the existence of the subjective difference tone? Prof. D. C. Miller has analysed the clarinet tone. He states that it may have twenty or more partials, with the seventh to the tenth predominating. This latter group of partials are even stronger than the fundamental, and it is they which are chiefly concerned with giving the characteristic quality to the tone of the instrument. The difference tone of each successive pair of partials would, of course, have the same pitch as the fundamental. Even after the elimination of the five lowest partials, there would still remain fourteen pairs of generators to supply this difference tone. Possibly not all the partials would have sufficient intensity to act as generators, but the four predominant partials probably would. All these experimenters ascribe the generation of the difference tone to the cochlea, and not to the middle ear, as Helmholtz suggested. The writer has advocated the same view elsewhere, though not on the same grounds.