

one of the most difficult parts of the subject to present in an elegant manner, on account of the non-symmetrical character of the necessary approximations. The treatment here given seems to leave nothing to be desired.

Chapter VIII. begins with an exposition of the properties of a general system of rays: this with the cardinal result that the rays are all bi-tangents to a focal surface is ascribed to Kummer. They had, however, been previously given by Hamilton in his memoir on "Systems of Rays," in the discussion of ray-systems in a crystalline medium where the wave-surface no longer cuts the rays at right angles; and he in turn refers back to the same papers of Malus which contain the theorem of orthogonality in isotropic media.

The theory of the characteristic function is next applied to the solution of the general problem of the refraction of a narrow beam at a surface of double curvature; and to the analytical determination of the relation between the forms of such beams before and after passing through a general optical instrument whose internal structure is not specified. In these discussions the author has closely followed a series of papers by Clerk Maxwell which appeared about fifteen years ago in the Proceedings of the London Mathematical Society, and which presumably were to find a place in a book on optics then contemplated by their lamented author. It does not seem to have been much noticed in this country that the same formulæ for oblique refraction were developed a long time ago by Sturm and others, in a direct geometrical manner, from Malus's theorem; but the conciseness and precision which arise from defining a beam by means of its characteristic function give them an enhanced importance in optical theory. Their application is here given to some cases which we do not remember having seen published before: thus the modification impressed on a beam by refraction centrally through a single thin lens is expressed by means of very simple formulæ, from which several properties of considerable elegance and some practical value might be directly drawn.

The theory of dispersion and achromatism is treated in the ordinary way. In the chapter on vision are introduced discussions, chiefly from Helmholtz, of the mechanism of accommodation and the principles of binocular vision. Then follows a clear and valuable chapter on telescopes and microscopes, a chapter on miscellaneous optical instruments, and a brief account of atmospheric refraction, mirage, rainbows, and halos.

It may seem ungracious to expect more where so much is given, but we could have wished that the theory of refraction through general systems had been treated more from an historical standpoint. A difficulty often felt in this part of the subject arises from the way in which the geometrical and analytical methods of different writers are liable to be intermixed. The book was probably in the press before a recent note by Lord Rayleigh had brought again into prominence the large share taken by the English opticians of last century, notably Cotes and Smith, in the development of the general theory of this branch of the subject.

The list of treatises and memoirs might be improved by consulting the bibliographies given by Helmholtz and Verdet.

It is a misfortune incident on the scheme of the book

that it is seldom able to say the last word in relation to the more delicate arrangements of telescopes and microscopes, where diffraction plays an important part. This becomes very patent, for example, in the account of immersion objectives. The theory of diffraction as applied to optical construction is for the most part purely geometrical, and it would much increase the value and interest of books on geometrical optics if that theory were explicitly included, and the subject introduced by the consideration of light as wave-motion, instead of the artificial conception of the reflexion and refraction of rays.

As is usual in English text-books, selections of problems have been added at the ends of the chapters. In this case, Cambridge examination-papers of recent years have been largely drawn upon for questions, with the result that some are included which are not of much value as illustrations of the subject, though they may be very useful as tests of mathematical power. Indeed it seems open to question whether the practice of adding large collections of examples is not now overdone in this country; it certainly in some cases tends to unfit the books which contain them for the use of students who do not possess the advantage of tuition, or some guidance in selecting the few that will be of value for them.

The treatise is, on the whole, a most welcome addition to our optical text-books. Much of its contents, though fundamental and elementary, has only hitherto been accessible in English through Mr. Pendlebury's treatise on "Systems of Lenses"; and there is more that now appears in a text-book for the first time. The printing and general appearance of the book reflect great credit on all concerned with it.

J. LARMOR.

#### OUR BOOK SHELF.

*Shores and Alps of Alaska.* By H. W. Seton Karr, F.R.G.S. (London: Sampson Low, 1887).

THIS is a very interesting account of a journey of exploration in a country which, as the author says, is probably destined soon to become better known. The most important part of the book is that which relates to the attempt made by Mr. Seton Karr and his companions upon Mount St. Elias. When this attempt was made, the combined "alpinism" of the climbers was "insignificant." Nevertheless, they achieved considerable success, and the writer has been able to present a vivid and striking record of their observations. The height of Mount St. Elias was differently estimated by the old navigators, and Mr. Seton Karr points out that it is the only mountain the real height of which has exceeded the first estimates made of it. The latest determination taken from Yakatat and from the United States Coast Survey schooner *Yukon*, gives 19,500 and possibly 20,000 feet. From its massive shape the mountain does not convey the impression of being quite so high as this, although "its whole altitude is presented to the eye, from its sharp summit down to the ocean at its foot." Of the scenery of which Mount St. Elias is the most prominent feature, Mr. Seton Karr writes most enthusiastically. He even goes so far as to say that "without a doubt the scenery at Yakatat is the most wonderful of its kind in the whole world." Seen early in the morning, when the air is remarkably transparent, the mountains seem "too ethereal to have any actual existence." The observer feels that "they cannot be anything except some unholy illusion that must dissolve and disperse when the sun rises."