

Weight Reduction in Young Obese Children. I. Effects on Adipose Tissue Cellularity and Metabolism

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Summary

A 10-year longitudinal study was conducted on 26 prepubescent youngsters who had undergone successful weight reduction. Their ages ranged from 2 to 10 years when the study began. In all subjects, weight reduction proceeded only by a decrease in adipose cell size (from 0.62 ± 0.02 to 0.46 ± 0.02 μg lipid per cell) and resulted in a corresponding 33% decrease (from 177 ± 6 to $144 \pm 5\%$) in percent ideal body weights. Cell numbers did not change appreciably during the period of weight loss (29.4 ± 2.6 versus $28.7 \pm 2.3 \times 10^9$ total adipocytes). Three years after the start of the study, 14 of 20 youngsters had maintained their reduced percent ideal body weights, including eight who remained below 130% ideal body weight. Ten years later, only four remained below 130% ideal body weight. All four children had total adipose cell numbers below 20×10^9 total adipocytes at the start of the weight reduction program, a value below the lower limit for adult normal weight subjects. Thirteen other children have maintained or decreased their initial percent ideal weights. The remaining nine youngsters have further increased their percent ideal body weights. *In vitro* metabolic studies of the patient's adipocytes revealed a >50% depression of epinephrine-stimulated lipolysis pre- and immediately postweight reduction; this decrease persisted for the entire period of study, irrespective of the maintenance of a normal percent ideal body weight. At the same time, normal 150% increases in the *in vitro* production of $^{14}\text{CO}_2$ from $[1-^{14}\text{C}]\text{glucose}$ in the presence of insulin occurred.

Speculation

Maintaining weight reduction long term is generally unsuccessful except in a small minority of very young obese children. Therefore, if the prevalence of obesity and its associated diseases are to be decreased, very early identification of at-risk youngsters is important. Specific enzymatic and metabolic alterations in these children, e.g., depression of *in vitro* epinephrine-stimulated lipolysis, appear to be useful for early identification of susceptible individuals. In addition, this study indicates that factors such as genetics and gestation may lay the groundwork for the future development of increased adiposity.

Obesity, developing in childhood and persisting into adolescent and adult life, is associated with varying combinations of hypercellularity and enlargement of adipocytes (1, 20, 29, 45). However, weight loss is accomplished solely by a reduction in the size of the adipocytes; significant reductions in cell number have not yet been described. Weight loss, even if substantial, is almost invariably followed by some degree of weight gain to either previous or higher levels. Furthermore, a decrease in insulin insensitivity, a hallmark of the obese state, occurs in fat cells where the lipid content is reduced by dietary intervention. This is reflected by

changes in glucose tolerance, serum insulin concentrations, and numbers and/or affinity of the cell membrane insulin receptors (17, 37, 46). Adipocytes in obese adolescents also display diminished *in vitro* epinephrine responsiveness pre- and immediately postweight reduction (28). Previous experiments in animals have shown that significant reductions in total adult adipose cell number can only be permanently achieved by altering early nutritional intake or by increasing early exercise patterns (26, 30, 39). Thus, it is important to assess if a similar situation in young children exists to determine critical periods for fat cell development. The present investigation was designed to measure adipose cell number, size, *in vitro* responsiveness of adipocytes to insulin and epinephrine, plus the percent ideal weight in young obese children pre- and postweight reduction to assess the relative importance of these parameters on the ability to permanently maintain the reduced state.

MATERIALS AND METHODS

SUBJECTS

Twenty-six prepubescent children, 12 boys and 14 girls, ages 2 to 10 years at the start of the study, were investigated. They were originally referred to our Pediatric Nutrition Clinic because of obvious and significant obesity which was documented before their first birthday. All were tested and examined to exclude the concomitant presence of described endocrinopathies. They were then placed, as outpatients, on weight reduction diets calculated at approximately 50 calories/kg of ideal body weight. Before the start of dietary intervention, adipose tissue studies, described below, were also performed. Five of 26 patients were studied only as outpatients; the remaining 21 were admitted to the Clinical Research Center (CRC) one to four times for periods ranging from 1 to 5½ months.

After admission to the CRC, all patients were placed on calculated food diets containing 40 to 45% carbohydrate. This enabled maintenance of their initial weight for periods ranging from 3 to 5 days. Baseline studies were performed after a 12-hr overnight fast, and all patients were then placed on a constant 400 calorie reduction diet. The diet (Table 1) was calculated to provide 21% of the total energy intake as protein, 45% as fat, and 34% as carbohydrate and was supplemented by 1 mg folic acid daily, multivitamins twice daily, and 324 mg ferrous gluconate every other day. In addition to two cans of diet soda, water was allowed *ad libitum*, and the amount was recorded. No other fluids were given. During the weight reduction period, daily strenuous physical activity was encouraged via the use of a gymnasium at the hospital and facilities at a neighborhood park and playground. Patients were weighed each day, urinalyses were performed daily, and serum uric acid and other blood determinations were made weekly. At the conclusion of the weight reduction period, each

Table 1. 400 calorie constant diet

	Volume (ml)	Wt (gm)	Carbohydrate (gm)	Protein (gm)	Fat (gm)	Energy (calories)
Breakfast						
Orange juice	50		5.2	0.4	0.1	22.5
Rice Krispies		10	8.8	0.6	0.0	39.0
Skim milk	90		4.6	3.2	0.1	32.4
Total	140	10	18.6	4.2	0.2	93.9
Lunch						
American cheese		22	0.4	5.1	6.6	81.4
Unsweetened peaches (drained)		50	4.1	0.2	0.1	15.0
Skim milk	50		2.5	1.8	0.1	18.0
Total	50	72	7.0	7.1	6.8	114.4
Dinner						
Ground sirloin patty (Raw wt.)		50		8.5	13.4	156.5
Unsweetened applesauce		50	5.4	0.1	0.1	20.5
Skim milk	50		2.6	1.8	0.1	18.0
Total	50	100	8.0	10.4	13.6	195.0
Additional: 2 cans diet soda	720		1.0			4.0
Grand total	960	182	34.6	21.7	20.6	407.3
% total calories			33.9	21.2	45.1	

patient's weight was stabilized at the new lower level for 3 to 5 days on a diet calculated at approximately 50 calories/kg of reduced body weight containing 40 to 45% carbohydrate. At the conclusion of this period, all the described baseline studies were repeated.

The patients were discharged and followed for periods ranging from 28 months to 9½ years. All the children were seen in the Pediatric Nutrition or Metabolism Clinics at 3- to 4-wk intervals by the same physician, a social worker, and a dietician from the CRC. No drugs, except for one multivitamin tablet daily, were administered. Recommended energy intakes ranged from 1000 to 1200 calories/day with each patient's diet being based on individual likes and dislikes for particular foods; protein intake was encouraged. Adipose tissue studies, as described below, were repeated at frequent intervals during the follow-up period.

The five outpatients were also seen at frequent intervals by the same physician, the clinic dietician, and social worker at each visit. Their diets ranged from 1200 to 1400 calories per day, and no drugs were used. Their studies were also performed pre- and postweight reduction after a 12-hr overnight fast. Control data for metabolic studies were obtained from identical studies performed on normal weight children with no family history of diabetes mellitus. Informed consent was obtained from both parents of all study participants.

ADIPOSE TISSUE STUDIES

Determination of adipose cell size and number. Adipose tissue samples of the patients were obtained from the subcutaneous tissue of the upper outer gluteal quadrant of the buttocks by needle aspiration; 1% xylocaine was used for local anesthesia (18, 19). The tissue fragments were immediately placed in Krebs-Ringer bicarbonate buffer and kept at 37°C under 95% oxygen and 5% carbon dioxide in a Thermos flask. The fragments were processed according to methods previously described (28). The lipid content per cell (adipose cell size) was measured in triplicate.

Total body adipose cell number was calculated from the follow-

ing equation:

$$\text{Cell number} = \frac{\text{body weight} - \text{lean body mass}}{\text{mean adipose cell size}}$$

where the numerator is a measure of total body fat. Lean body mass was determined in all patients during the weight stabilization periods both from the Friis-Hansen nomograms (10) and from measurements of total body potassium (TBK) pre- and postweight reduction. The value for lean body mass is the mean of these two determinations.

TBK was measured in the whole-body counter located at Brookhaven National Laboratories, Upton, NY. The computer facility has an accuracy of ±3.3% when measuring TBK. A complete description of the 54 detector Brookhaven counter has been published (5). Routine counting procedures involved a 15-min count of the subject. Calibration of the counter was first performed. The whole-body count of the Alderson random phantom, containing a known amount of potassium homogeneously distributed, was obtained in the same geometry as that for the subjects. The count was corrected for geometry and absorption effects. For prepubescent children in this study, lean body mass in kilograms was determined by dividing total body potassium (milliequivalents obtained from the whole-body count) by 89 mEq assuming that 1 kg of lean body mass contains 89 mEq of potassium (4, 8, 9, 15).

Incubation of Tissue. Measurement of glycerol release. Individual fragments of adipose tissue were placed in 25 ml siliconized Erlenmeyer flasks containing 2 ml of Krebs-Ringer bicarbonate buffer (pH 7.4) at 37°C, glucose (0.5 mg/ml) and defatted fat-free albumin (50 mg/ml). Incubations were carried out as previously described (28). Glycerol was determined enzymatically by a modification of the Wieland method (51). Percent change, in the rate of glycerol release on the addition of 1 µg/ml epinephrine, was calculated from the following equation:

$$\frac{(\text{epinephrine} - \text{basal})}{(\text{basal})} \times 100$$

The rate of glycerol release was expressed as $\mu\text{moles glycerol} \times 10^{-6}/\text{cell}/4 \text{ hr}$.

Measurement of $^{14}\text{CO}_2$ production. Measurement of $^{14}\text{CO}_2$ production from $[1-^{14}\text{C}]$ glucose in the presence and absence of 100 $\mu\text{U}/\text{ml}$ insulin was performed by methods previously described using individual fragments of adipose tissue (12).

Other measurements. Weight and height percentiles were obtained from Stuart and Meredith (48) and Center for Disease Control (14) growth charts for infants and children. Percent ideal weight was calculated as the ratio of actual weight to expected weight for height and age $\times 100$ on both charts; the mean of these two values is indicated. Statistical analyses were performed using the paired and unpaired *t* tests; intercorrelation matrix analyses for cell size and cell number versus other parameters of body growth were performed (32).

RESULTS

Table 2 summarizes the data for each hospitalized patient at the first visit to the Nutrition Clinic and the beginning (period I) and end (period II) of the in-hospital weight reduction program. Means and standard errors of the means are shown at the bottom of each column. Similar data for the five children who lost significant weight as outpatients are shown in Table 3. Fifteen of 21 hospitalized patients increased their percent ideal body weight $11 \pm 6\%$ (from 169 ± 8 to $180 \pm 8\%$) during the mean 10 ± 3 months which elapsed from the time they were first evaluated until the time of their first admission to the CRC. The remaining six of these 21 patients, however, decreased their percent ideal body weights $13 \pm 4\%$ (from 171 ± 7 to $158 \pm 7\%$) during a similar 16 ± 6 month time period. Although the group with such initial weight loss began its inpatient weight reduction program at a significantly lower percent ideal body weight (158 versus 180%; $P < 0.05$), the subsequent rate of weight loss and ultimate per cent ideal body weights were not altered by the initial outpatient weight loss. Thus, one patient in each of these CRC groups (M. C. and M. R.) ultimately remained below 130% ideal body weight. In each case, the weight loss which occurred (either outpatient or on the CRC) was achieved only by a decrease in cell size while cell number remained essentially unchanged. Mean cell number in the hospitalized patients was $29.4 \pm 2.6 \times 10^9$ total adipocytes on admission and $28.7 \pm 2.3 \times 10^9$ adipocytes on discharge. Identical decreases in cell size were seen in the six patients who underwent weight reduction more than once.

In the 21 hospitalized patients, average cell size decreased from 0.62 ± 0.02 to $0.46 \pm 0.02 \mu\text{g}$ lipid per cell over a period of 8.2 ± 0.7 wk, a decrement significant at $P < 0.001$. Similarly, average cell size in the five outpatients decreased from 0.57 ± 0.04 to $0.46 \pm 0.03 \mu\text{g}$ lipid per cell. These facts are depicted graphically in Figures 1 and 2 for two patients who exhibited diametric long-term results after weight reduction. Data for patient M. C. are charted in Figure 1, in which arrows denote the time span of the in-hospital weight reduction program. His initial rapid reduction in weight when total adipocyte number was 15.3×10^9 cells resulted in a 4% decrease in cell size over a period of 1 month although his percent ideal weight fell significantly from 150 to 110%. Over the next 4 months, his percent ideal weight increased to 122%. Over an approximately 7½-year interval, it has not risen above 130%. Concomitantly, total adipose cell number increased slowly to a value of 20×10^9 adipocytes at age 10. In contrast, patient I. G. (Fig. 2) was above 180% of ideal weight when she was first seen in the Nutrition Clinic at age 5 years and 7 months. Fifteen months later, she was admitted to the CRC, and over a 13 wk period, her percent ideal weight decreased from 202 to 172%. Cell size decreased 10%, and cell number remained unchanged at a mean value of 42.2×10^9 total adipocytes. After discharge, she rapidly gained weight and was then readmitted to the CRC at age 9 years and 6 months. This time her percent ideal weight declined to 159% over a period of 3 months. Cell size decreased 30%, whereas cell number remained unchanged at a mean 61.8×10^9

adipocytes. On discharge, she continued to gain weight and, postmenarche, is currently 290% of ideal weight. Her current cell number, 85×10^9 , is 70% greater than the upper limit of normal for adults, 50×10^9 total adipocytes.

As indicated in Table 2, mean weight loss for all patients on the CRC was 8.9 kg over 8.2 wk or 1.1 kg/wk (range, 0.5 to 2.4 kg/wk with younger and lighter patients having the smaller weight loss and older and heavier ones having the larger weight loss). This occurred even though the daily energy intake ranged from 17.2 kcal/kg/day in the lightest patient (M. C.) to as low as 4.3 kcal/kg/day in the heaviest one (I. G.). Of this weight loss, 4.9 kg (55%) was calculated to be body fat loss. We then performed calculations to determine the validity of the two values used to derive total body fat. The correlation coefficient for the value, lean body mass, was the same for both the Friis-Hansen nomograms and TBK counts, namely 0.95 preweight reduction and decreased to 0.84 postweight reduction. As would be expected, the duration of weight loss correlated with the total fat and body weight loss ($P < 0.001$). However, it correlated negatively ($P < 0.01$) with the present percent ideal weight, implying that children who underwent longer periods of weight reduction presently have greater percent ideal body weights. Before the in-hospital weight reduction, these 21 patients averaged $177 \pm 6\%$ of ideal body weight. At the conclusion of the inpatient weight loss program, they had a mean ideal body weight of $144 \pm 5\%$. Thus, they had lost $33 \pm 2\%$ of their ideal weight, a loss significant at the $P < 0.001$ level. At the first follow-up study, 6 months to 4 years after initial weight reduction had occurred, 15 re-evaluated patients had increased their percent ideal weights from $140 \pm 5\%$ to $157 \pm 14\%$, a value significant at the $P < 0.05$ level. It is of interest, that four of these 15 patients were continuing to decrease their percent ideal weights, whereas nine showed increases, and two remained the same.

Furthermore, when these 15 patients were evaluated 4½ to 9½ years after initial weight reduction, their percent ideal weights had increased up to $183 \pm 11\%$, a value significantly above ($P < 0.05$) the value 5 years previously. It exceeded, but not significantly, the value $181 \pm 8\%$ which was calculated before any dietary intervention. From computations by intercorrelation matrix analyses (Table 4), individual total body weight, total body fat, weight loss, and fat loss in all patients correlated (P at least < 0.05) with each other and with the age of the patient, total adipose cell number, and percent ideal body weight. This suggests that patients with the greatest body weights were older, had the largest amount of body fat, the highest total adipose cell numbers and per cent ideal body weights and lost the most weight and body fat during the weight reduction program. On the other hand, adipose cell size, unlike cell number, did not correlate with all the parameters cited above. Positive cell size correlations were consistently found only with total body weight at the beginning and end of the weight reduction period and with age on starting weight reduction. The P values for the adipose cell size correlations were never as great as those for the cell number correlation. Thus, older children had larger fat cells and higher body weights. The percent ideal weight on the first visit to the Nutrition Clinic correlated ($P < 0.05$) with all subsequent percent ideal weights. It was noteworthy that girls came to the Nutrition Clinic at a lower percent ideal weight (166%) than did boys (177%) ($P < 0.01$).

At the last follow-up, (mean 87 ± 6 months postreduction), the mean percent ideal body weight of all 26 patients, $177 \pm 9\%$, was identical with their weight before dietary intervention, $177 \pm 5\%$. At the initial follow-up, eight hospitalized children and three children treated as outpatients were below 130% ideal body weight. Five years later only four remained at this percentage while two others were between 130 and 140% ideal weight. The four youngsters had initial total adipose cell numbers of 13.2, 13.4, 15.3, and 19.4×10^9 whereas the latter two had values of 18.4 and 27.4×10^9 . These data demonstrate that the two children hospitalized for weight reduction and two who had lost weight as outpatients maintained their lower, relatively normal weights for several years. Moreover, maintenance of nearly normal percent ideal body

Table 2. Studies in hospitalized obese children pre- and postweight reduction: admission to CRC

Patient	Sex	First visit to nutrition clinic						Period I					
		Age (yr/mos.)	Wt (kg)	% ideal wt	Total body fat (kg)	Cell size (μg lipid per cell)	Cell no. ($\times 10^9$)	Age (yr/mos.)	Wt (kg)	% ideal wt	Total body fat (kg)	Cell size (μg lipid per cell)	Cell no. ($\times 10^9$)
R. S.	M	0 ¹⁰	11.9	116	2.9	0.47	6.2	2 ³	24.3	164	7.8	0.54	14.4
M. C.	M	2 ⁴	23.5	153	7.3			2 ⁵	23.2	150	7.2	0.47	15.3
U. L.	F	2 ¹⁰	21.9	133	6.3	0.51	12.4	6 ²	38.6	146	12.4	0.48	25.8
								7 ⁵	41.2	131	12.9	0.67	19.3
D. R.	F	3 ⁷	25.5	155	7.9	0.44	17.9	5 ⁵	33.4	163	9.8	0.66	14.8
J. H.	M	3 ¹¹	34.2	157	9.8			4 ¹	35.1	161	10.3	0.51	20.2
G. N.	M	4 ⁰	28.1	224	10.5			4 ¹	29.3	231	10.9	0.54	20.2
								5 ⁵	32.6	197	11.1	0.52	21.3
								6 ⁹	35.4	200	11.0	0.61	18.0
								9 ¹¹	54.9	244	22.2	0.75	29.6
Y. S.	F	4 ⁴	36.6	149	12.5	0.46	27.0	7 ¹¹	65.0	164	24.6	0.65	37.8
K. B.	F	4 ⁷	32.1	138	9.1			4 ⁸	33.8	140	11.0	0.58	19.0
D. B.	F	4 ⁷	42.4	192				5 ¹	45.6	199	17.5	0.67	26.2
C. P.	M	4 ¹⁰	34.1	166	11.1	0.58	19.2	7 ⁴	52.5	165	19.1	0.63	30.4
M. R.	F	5 ⁴	36.3	172	7.9			5 ⁶	37.4	176	8.3	0.63	13.2
I. G.	F	5 ⁷	45.5	182	16.8	0.46	36.5	6 ¹⁰	57.2	202	22.6	0.51	44.3
								9 ⁶	93.1	210	42.3	0.66	64.1
E. S.	F	5 ⁸	42.7	168	14.5	0.93	15.6	9 ³	52.2	141	17.3	0.63	27.4
L. H.	F	5 ⁹	36.9	156	12.2	0.46	26.6	6 ⁵	45.4	139	15.5	0.42	36.9
J. S.	M	5 ¹⁰	46.4	199	17.3	0.66	26.2	6 ⁹	53.7	182	20.1	0.66	30.5
								7 ¹¹	52.3	157	19.0	0.69	27.5
								9 ¹¹	72.0	164	26.3	0.79	33.3
F. F.	M	6 ²	50.8	227	21.1			6 ⁷	55.8	238	23.0	0.59	38.9
								8 ⁰	52.1	200	20.0	0.52	38.5
N. A.	F	6 ⁴	38.3	182	12.1	0.54	22.4	6 ⁹	40.6	171	12.8	0.43	29.8
A. D.	F	7 ⁸	53.6	174	20.0			7 ⁹	55.9	180	21.1	0.77	27.4
								9 ⁰	64.5	168	25.5	0.99	25.8
C. B.	F	7 ⁸	55.2	176	19.1			8 ⁰	57.1	180	21.2	0.75	28.3
R. G.	F	8 ⁷	56.9	139	18.2			8 ¹¹	57.8	140	20.1	0.76	26.4
V. J.	F	10 ⁰	81.1	204	35.3			10 ⁴	83.6	212	36.8	0.47	78.3
Mean \pm S.E.		5 ²	39.4	178	13.9	0.56	22.2	6 ⁹	49.2	177	18.0	0.62	29.4
		$\pm 0^5$	± 3.1	± 7	± 1.4	± 0.04	± 2.8	$\pm 0^5$	± 3.0	± 6	± 1.5	± 0.02	± 2.6

Table 3. Adipose tissue studies pre- and postweight reduction in ambulatory obese children

Patient	Initial age	Sex	Period I				Period II			
			kg initial wt.	Initial % ideal wt.	Cell size μg lipid/cell	Cell no. $\times 10^9$	Cell size μg lipid/cell	Cell no. $\times 10^9$	Final % ideal wt.	Present % ideal wt.
J. P.	3 ⁶	M	23.7	139	0.48	13.4	0.43	16.6	127	119
W. G.	5 ⁸	M	39.1	146	0.56	19.4	0.42	24.6	131	125
W. M.	6 ¹	M	55.4	197	0.52	46.9	0.47	44.2	165	206
R. R.	6 ⁸	M	38.4	192	0.73	18.6	0.57	22.9	175	181
M. N.	10 ⁸	M	61.5	203	0.58	41.9	0.42	42.0	167	182
				175 \pm 14 ¹	0.57 \pm 0.04		0.46 \pm 0.03		153 \pm 10	163 \pm 17

¹ Mean \pm S.E.

weight was not dependent on the weight at the time of completion of the weight reduction program. Six patients who were reduced to below 130% ideal weight later again became obese.

Figure 3 and Table 5 summarize the data on *in vitro* responsiveness of aspirated adipocytes to epinephrine (1 $\mu\text{g}/\text{ml}$) which was measured by glycerol release during a 4 hr incubation period. Our previously reported data on obese adolescents and adults are

included for comparison (28). The mean age of 14 control children, 6.6 ± 0.7 years, was similar to that of our obese children. The mean *in vitro* responsiveness averaged $127 \pm 21\%$ over baseline values for controls whereas the mean for obese children before weight reduction was only $49 \pm 9\%$ ($P < 0.05$). Furthermore, this defect was not corrected by weight reduction, even in the youngest patients. Immediately postweight reduction, epinephrine-stimu-

Period II											
Wt (kg)	% ideal wt	Total body fat (kg)	Wt loss (kg)	Calculated fat loss (kg)	Duration of wt reduction (wk)	Cell size (μg lipid/cell)	Cell no. ($\times 10^9$)	First follow-up 1973 (% ideal wt)	Present % ideal wt	Total mos. follow-up	
21.6	139	6.6	2.7	1.2	5	0.42	15.7	134	154	115	
20.4	110	6.3	2.8	0.9	4	0.45	13.9	119	127	93	
32.1	124	9.2	6.5	3.2	8	0.45	20.4	114	160	116	
33.3	114	8.9	7.9	4.0	9	0.45	19.8				
27.4	138	6.5	6.0	3.3	8	0.42	15.4	124	160	90	
28.4	123	6.9	6.7	3.4	7	0.35	19.7		155	28	
27.1	215	9.4	2.2	1.5	4	0.36	26.1	186	202	98	
28.2	174	9.0	4.4	2.1	8	0.35	25.7				
30.3	173	8.6	5.1	2.4	7	0.48	17.9				
50.4	224	19.6	4.5	2.6	9	0.63	31.1				
52.3	128	17.5	12.7	7.1	9	0.46	38.0	128	176	117	
25.9	129	6.9	7.9	4.1	9	0.37	18.6		155	52	
35.2	156	11.5	10.4	6.0	9	0.45	25.6		178	53	
44.2	141	14.2	8.3	4.9	8	0.46	30.9	141	174	108	
26.0	133	5.8	11.4	2.5	9	0.41	14.1		115	56	
50.3	172	18.4	6.9	4.2	13	0.46	40.0	220	290	119	
73.2	159	27.3	19.9	15.0	14	0.46	59.4				
46.6	105	14.0	5.6	2.3	5	0.57	24.6	109	135	116	
42.6	131	13.2	2.8	2.3	4	0.38	34.7	142	225	110	
42.0	135	13.3	11.7	6.8	8	0.45	29.6	125	172	91	
43.4	131	12.7	7.9	6.3	6	0.49	25.9				
60.1	137	21.9	11.9	4.4	5	0.62	35.3				
41.3	172	14.2	14.5	8.8	7	0.41	34.6	245	270	79	
40.7	157	16.6	11.4	3.4	6	0.33	37.0				
32.1	138	8.9	8.5	3.9	8	0.34	26.2	144	176	70	
46.9	149	16.0	9.0	5.2	8	0.62	25.8	125	186	89	
47.6	131	15.8	16.9	9.7	9	0.65	24.3				
45.4	124	15.3	11.7	5.9	9	0.52	29.5		202	53	
50.0	109	15.9	7.8	4.2	6	0.60	26.5		138	51	
61.6	157	22.9	22.0	13.9	25	0.31	73.9	290	288	109	
40.2	144	13.1	8.9	4.9	8.2	0.46	28.7	156	183	87	
± 2.3	± 5	± 1.0	± 1.1	± 0.6	± 0.7	± 0.02	± 2.3	± 14	± 11	± 6	

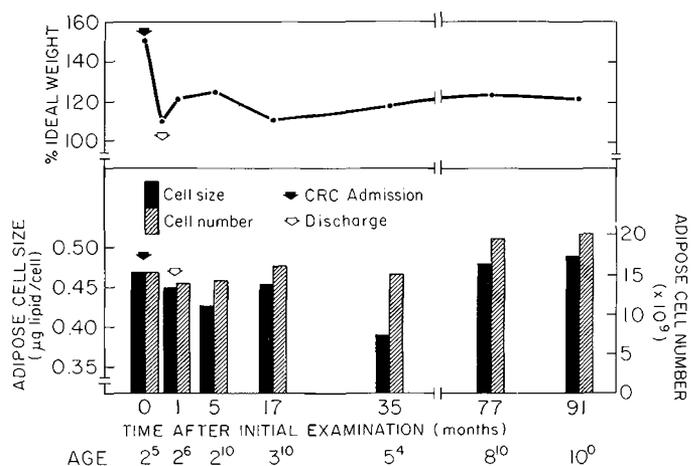


Fig. 1. Percent ideal body weight, adipose tissue cell size, and cell number over 93 months time span in patient M. C.

lated lipolysis decreased slightly, to a mean value of $40 \pm 13\%$. It was maintained 19.4 ± 8.2 months later at an average of $52 \pm 7\%$ and at 6.4 ± 2.4 years the mean was $45 \pm 6\%$. Epinephrine-stimulated lipolysis did not return to normal in any of the patients irrespective of their age or maintenance of ideal body weight

below 130%. Mean basal glycerol release declined 22% after weight reduction as mean cell size decreased 25%. This confirms the fact that basal glycerol release correlates with cell size ($r = 0.78$; $P < 0.0002$). Basal glycerol release was increased during both study periods in the obese children; however, its postreduction release was only minimally above the control children's value at the same time when mean fat cell sizes in the obese were identical to those in the controls. Both the percent increase in lipolysis and the absolute glycerol release in the presence of epinephrine were consistently decreased in the obese patients during all study periods. Absolute levels of epinephrine-stimulated lipolysis did not correlate with cell size in either study period but as cell size decreased with weight reduction these levels also fell.

"Normal" *in vitro* responses of adipocytes from obese subjects to $100 \mu\text{U/ml}$ of insulin were measured by conversion of $[1-^{14}\text{C}]$ -glucose to labeled carbon dioxide (Fig. 4). Conversion occurred even though the cell size of these obese patients decreased significantly to $0.48 \pm 0.02 \mu\text{g}$ lipid per cell after weight loss ($P < 0.001$). These values of the obese patients during both study periods were also similar to those of the control patients whose cell size averaged $0.48 \pm 0.04 \mu\text{g}$ lipid per cell in this study.

DISCUSSION

The onset of obesity in children described in this paper occurred before their first birthday. They displayed hyperplastic fat depots when compared with normal children of the same age and height

(27). The significance of adipose tissue hyperplasia and the techniques for calculating the total number of fat cells in a given individual have been the subject of intensive debate. Nonetheless, our previous cross-sectional and longitudinal studies of adipose cell development and body composition in children and adolescents have confirmed that obese children can be identified by fat cell characteristics as early as age two, if not earlier (29, 32). These studies demonstrate conclusively that obese children, when followed longitudinally, continue to exhibit adipose tissue hypercellularity. Although the buttock area has been used for adipose tissue sampling in these studies, it has been shown that correlations exist between fat cell sizes of different regions of the body. It may be inferred that samples obtained at a single site from a large group of subjects can provide a reasonable estimate of the variation among individuals in fat cell sizes in all depots (7). Fat cells isolated by needle aspiration from the buttocks have been shown by Khan *et al.* (25) to be about 7% smaller than those from the abdomen. Errors in calculating total body fat cell number may then occur, but such differences only change absolute values, not trends. Thus, although the number of adipocytes calculated cannot be determined exactly, ranges for different degrees of obesity can be extrapolated. Furthermore, in such longitudinal studies, it is

impractical, if not impossible, to frequently sample multiple sites for adipose tissue.

The concept of hypercellularity has been challenged on the basis that empty fat cells cannot be counted using the osmium tetroxide method of fixation (50). Although some "preadipocytes" may be missed using these methods, it has never been shown conclusively that such precursors exist in humans. If precursors do exist, our longitudinal data from obese and normal children provide no evidence that they are filled with fat at different rates. We conclude that groups increase their fat cell numbers during adolescence, but the distinct differences in fat cell number persist between normal and obese adolescents. Retrospective studies, which have not been able to demonstrate these relationships, (22) are obviously not as reliable as prospective longitudinal ones.

These longitudinal data strongly indicate that it is very difficult to reduce and maintain weight reduction in very young grossly obese youngsters. Furthermore, the results of this study question the efficacy of various short-term weight reduction programs and suggest that these programs be reassessed. Our data support the early work of Lloyd *et al.* (33) who demonstrated that 80% of obese children who underwent weight reduction relapsed 9 years later. Ours is the first long-term study of obese children undergoing early intervention which includes *in vitro* metabolic and cellular studies of adipocytes. It seems logical that the earlier dietary intervention occurs, the more likely it would be to decelerate the development of new fat cells and achieve positive long-term results. For example, no statistical increase in cell number was noted in patient M. C. over a 3 year period (from age two years, five months to age five years, 4 months). It is during this same time that other obese children of identical age increased their cell numbers (32). Previous studies on adipose cell number in nonobese

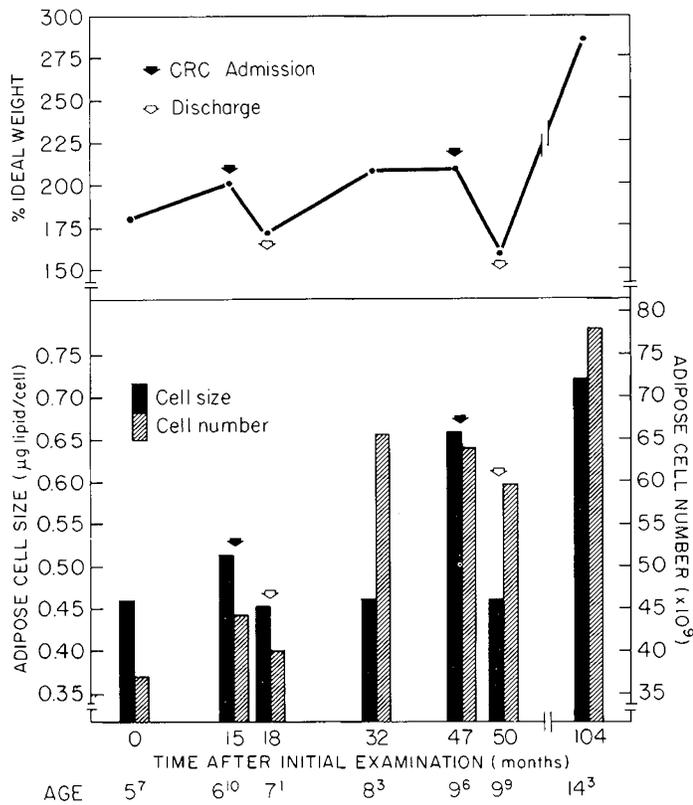


Fig. 2. Percent ideal body weight, adipose tissue cell size, and cell number over 104 months time span in patient I. G.

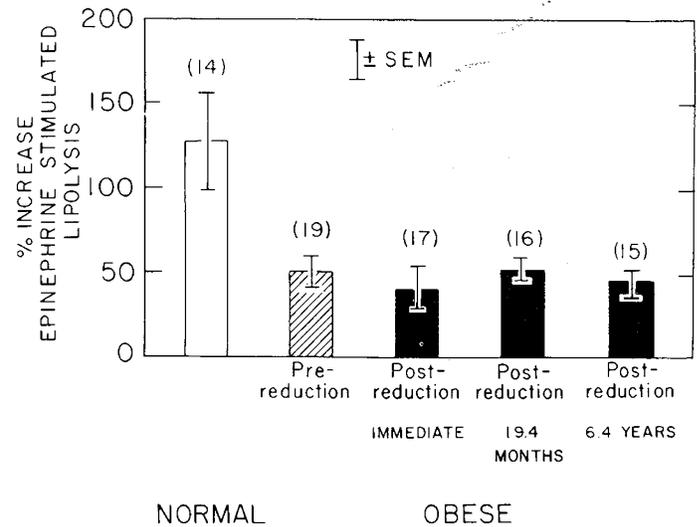


Fig. 3. *In vitro* percent increase over baseline of epinephrine-stimulated lipolysis in adipocytes of control and obese children preweight reduction and at various time intervals postweight reduction.

Table 4. Correlation analysis of adipose cell size and cell number with other parameters pre- and postweight reduction

	Period I				Period II			
	Adipose cell size		Adipose cell no.		Adipose cell size		Adipose cell no.	
	Correlation coefficient	P	Correlation coefficient	P	Correlation coefficient	P	Correlation coefficient	P
Age	0.49	0.006	0.62	0.0003	0.50	0.005	0.62	0.0003
Total body wt.	0.39	0.03	0.84	0.0001	0.42	0.02	0.81	0.0001
% ideal body wt.	-0.008	0.96	0.38	0.04	-0.10	0.60	0.27	0.15
Total body fat	0.34	0.07	0.88	0.0001	0.37	0.02	0.85	0.0001

wk (42). If they ingested only 2800 kilocalories per wk, then they had a deficit of 19,586 kcal which should result in a mean loss of 2.55 kg/wk compared to the observed 1.1 kg. Even if we calculate the body's needs based on providing a caloric intake of 65 kcal/kg/day to the patients' lean body mass plus 15% (the average value for percent body fat for normal children over the age of two) (36), we would have expected a weight loss of 1.8 kg/wk as opposed to the 1.1 kg observed.

Similar decreased rates of weight reduction in nine fasting obese adults when compared with normal weight adults have recently been reported by Forbes and Drenick (10). Further support for reduced caloric needs (34) and energy use in the cells of obese persons has very recently been provided by DeLuise, *et al.* (6). They demonstrated the presence of reduced numbers of sodium pump units and reduced activity of the pump in erythrocytes of obese adults. Sodium- and potassium-dependent adenosine triphosphatase, the enzymatic expression of the sodium pump, uses 20 to 50% of total cellular thermogenesis. This results in decreased activity, which is not increased by weight reduction, and may account for the reduced metabolic rates in obesity. In addition, impaired thermogenetic responses to rises in circulating catecholamines have been demonstrated *in vivo* in human obese subjects (23). Our observation that *in vitro* epinephrine-stimulated lipolysis is depressed in obese children may be related to these reductions in sodium-potassium ATPase. Longitudinal studies of the sodium pump activity in both red cells and other tissues of obese children must now be performed to validate these hypotheses.

Therefore, it is important to note that all of the obese children in this study, similar to the adolescents previously reported (28), displayed a distinct blunting of *in vitro* adipocyte epinephrine-stimulated lipolysis. Although preweight reduction, basal- and epinephrine-stimulated glycerol release values were higher in our younger obese patients than in the obese adolescents, they did not decrease to the low values seen in the older subjects postweight reduction. Postreduction, obese children still displayed a 75% increase in basal lipolysis over values obtained from data on reduced obese adolescents and adults at identical cell sizes (0.46 μg lipid per cell). Whereas the basal rate, prereduction, for the obese children was 49% greater, the mean cell size was 19% smaller. Similarly, absolute levels of epinephrine-stimulated lipolysis in the obese children as compared with the mature obese subjects were 29% higher preweight reduction and 69% postweight reduction. It can be speculated that age (and perhaps years of obesity) may be important factors in the metabolic responses of adipocytes. That age may be important is suggested by the work of Nyberg *et al.* (35) who reported increased rates of both basal lipolysis and absolute epinephrine-stimulated lipolysis in normal children 1 to 15 years. Our own unpublished data also reveal that both basal and epinephrine-stimulated glycerol release decrease in children as their age increases. Control children with a mean age of 6½ years have a basal glycerol release 50% above that of children whose mean age is 11 years. Reported increases in the percent epinephrine-stimulated lipolysis in children and adults also concur with our data (35). That percent increase in epinephrine-stimulated lipolysis does not change after weight reduction in obese adults was also documented by Ostman *et al.* (40).

Inasmuch as this defect in epinephrine-stimulated lipolysis does not disappear with weight reduction, even in the youngest patients, it is suggested that cyclic AMP formation via the enzyme adenylyl cyclase (49) may be altered. Defects in this mechanism may be important factors in the development of the obese state. Defective lipolysis might then contribute to establishing and enlarging the adipose tissue depot by signaling for a greater production of adipocytes as a compensatory mechanism. Alternatively, growth hormone and/or insulin or somatomedin C (43) may play a role in the production of added number of fat cells. Growth hormone initially increases the number of fat cells in growth hormone-deficient children treated with exogenous hormone (31). However, all studies to date, conducted only on older children, have indicated low growth hormone levels in obese subjects (41). Unpub-

lished studies from our laboratory indicate that growth hormone responses to insulin-induced hypoglycemia may be increased in very young obese subjects. Insulin, as a growth hormone, has long been discussed, but its role still remains to be proven (3, 47). In this connection, it is noteworthy that the obese youngsters in this study have plasma hyperinsulinemia in response to glucose stimulation. Therefore, several factors may be important in the pathogenesis of the documented hypercellularity. Of additional note is that our previously reported data (31) as well as that of Hager *et al.* (15) suggest that there may be an important coupling between fat cell size and adipocyte multiplication in man. We have previously shown (32) that when percent body fat exceeded 25% (as in all obese patients reported here), cell number rose dramatically. Furthermore, percent fat strongly correlates with cell size in all our patients ($r = 0.58$; $P < 0.05$). This suggests a "triggering" of fat-cell proliferation at a set level of body fatness and/or cell lipid content (32). In addition, fat cell size in children destined to be of normal weight falls between ages one and two, whereas this decrease in the change of size fails to occur in those children who become obese (29).

Normal *in vitro* response of obese children's adipocytes to insulin (mean cell size, 0.62 μg lipid cell prereduction) is comparatively greater than the responsiveness previously reported in obese adults (46). This contrast may reflect the fact that obese adults have adipose cell sizes greater than 0.7 μg of lipid per cell, and insulin responsivity at this size level decreases sharply. Although four of our patients also had cell sizes above 0.7 μg of lipid per cell prereduction, only one (A. D., whose cell size was 0.99 μg lipid per cell) displayed any significant decrement in fat cell responsivity to insulin. This reduction, 23% below the mean for the other children, suggests that age is also an important factor in determining hormonal responsivity. Furthermore, insulin secretion, as well as action, can quantitatively change with increasing age. These data are compatible with the hypothesis that insulin insensitivity is secondary to obesity and not a primary factor in its development (24, 38, 46).

Other factors are also determinants of adipocyte metabolism. The state of nutrition and adipose cell size have been shown to be important components in the patterns of basal- and insulin-stimulated glucose metabolism (13, 21). During high carbohydrate intake in adults, Salans *et al.* (44) demonstrated increased levels of basal glucose metabolism within adipocytes. Insulin sensitivity of such cells could also be altered such that in states of increased caloric intake, increased insulin sensitivity was induced in large fat cells whereas in states of decreased caloric intake, smaller adipose cells showed decreased insulin sensitivity. It is well to note that in the children studied, such differences were not demonstrated and insulin sensitivity was normal (although not as carefully studied as in patients of Salans *et al.*). Thus, such changes may also be related to the increasing age of patients studied. Whether dietary changes have any effect on epinephrine-stimulated lipolysis cannot be answered from this study. However, during high carbohydrate intakes (the usual diet of the patients described) or high fat intake (during the in hospital weight reduction period), no differences could be evoked. Therefore, it appears that reduction of epinephrine-stimulated lipolysis within adipocytes is a permanent feature of the hypercellular state in obese children. Furthermore, preliminary data in our laboratory have now documented such reductions in infants as young as 1 month of age, suggesting that genetic or *in utero* factors may be important. These influences are presently under intensive investigation.

It is not surprising that fat cells do not disappear in these children after weight reduction. Animal studies suggest that number can only be permanently decreased via *in utero* or preweaning reductions in diet. Projected, this time interval corresponds to the first 2 years of a child's life. It is well to note that none of the children reported here had nutritional intervention before their second birthday. Thus, total adipose tissue cell number appears to be the primary factor in estimating the ultimate risk for lifelong obesity. Early determination of this parameter in children deviat-

ing significantly from expected percent ideal body weights for height and age is obviously of importance.

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