

Geographical structure of gene diversity in *Quercus petraea* (Matt.) Liebl. III. Patterns of variation identified by geostatistical analyses

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Geostatistics were used for describing and modelling spatial patterns of gene frequencies at eight allozyme loci in 93 populations of sessile oak well distributed over the natural range of the species. Spatial patterns were summarized by the variogram, a measure of gene frequency variance as a function of distance. They were of three kinds: stationary patterns, clines and random distributions of allele frequencies. The main directions of variation of gene frequencies over Europe were estimated using directional geostatistics. They were shown to reflect postglacial migration routes as well as a genetic divergence among populations from different glacial refugia. A method of spatial interpolation, called kriging, was used to draw synthetic maps for allele frequencies and for multilocus patterns of variation using two canonical variables. It appears from this study that geostatistics are useful tools for the description of complex patterns of genetic variation, and therefore also for the management of natural genetic resources in forest trees.

Keywords: allozymes, geostatistics, isolation-by-distance, postglacial history, *Quercus petraea*.

Introduction

Long-lived woody plant species, particularly those with large geographical ranges and outcrossing breeding systems, maintain higher levels of genetic variation than most other plant species, but have generally very low levels of genetic differentiation among populations (Hamrick *et al.*, 1992). The study of geographical variation in forest trees, which is particularly of interest for the identification and characterization of provenance regions, therefore necessitates large and range-wide sampling as well as accurate descriptive methods (Zanetto & Kremer, 1995).

Most studies conducted over the whole ranges of species have detected geographical patterns, which were most often gradual trends of variation. Among the descriptive methods used have been multivariate or clustering methods (Kinloch *et al.*, 1986; Cheliak *et al.*, 1988; Lagerkrantz & Ryman, 1990), the examination of the relationship between genetic and geographical distances (Li & Adams, 1989) or between allele frequencies and geographical vari-

ables such as latitude or longitude (Zanetto & Kremer, 1995), or the assessment of the variation within and between regional groups of populations (Li & Adams, 1989; Zanetto & Kremer, 1995). Implicit in all these studies is the assumption that there is a spatial autocorrelation among the data, that geographically close populations will share higher genetic similarity than populations located further apart. A stable autocorrelation of neutral gene frequencies may result from limited gene flow ('isolation-by-distance', Sokal & Wartenberg, 1983). Similarly, selection may lead to clines or to local genetic homogeneity (Sokal *et al.*, 1989). Spatial autocorrelation may also arise after range expansions (Sokal & Menozzi, 1982), and is particularly likely to persist in long-lived species like forest trees (Strauss *et al.*, 1992).

However, the classical descriptive methods do not actually take into account spatial autocorrelation, because they all assume statistical independence among samples. Specific statistical tools have been developed that focus on the analysis of spatial dependence (see, e.g., Cressie, 1991, for a review). Among them are geostatistics and spatial autocorrelation analysis. The former approach was initially

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developed in the fields of geology and mining (Matheron, 1963), and has only recently been used in the field of ecology (Rossi *et al.*, 1992), and also, but much more scarcely, in population genetics (Barbujani, 1988a; Monestiez *et al.*, 1994). Conversely, autocorrelation analysis has been extensively used for the study of spatial genetic structures, after it was introduced into the field by Sokal & Oden (1978). The two approaches are closely related, but geostatistics has some advantages. First, it relies on a single, straightforward measure of spatial dependence called the variogram, whereas different expressions exist for the autocorrelation coefficient. Secondly, geostatistics allows the modelling of the spatial dependence, and, subsequently, the prediction (called 'kriging') of the variable everywhere in the studied space to obtain a map. Furthermore, like the correlogram, the variogram has a genetical interpretation within the frame of isolation-by-distance models (Piazza *et al.*, 1981).

We will use geostatistics to describe spatial patterns of genetic variation in a range-wide set of European sessile oak (*Quercus petraea* (Matt.) Liebl.) populations analysed at eight polymorphic allozyme loci. Part of this sampling scheme was previously analysed using classical statistics (Zanetto & Kremer, 1995). In this study, geostatistics are used as a way to confirm and describe in more detail the geographical patterns previously detected. These patterns consisted mainly of the presence at most loci of a west–east cline, which was interpreted as a consequence of the northwards postglacial migration of oaks from separate refugia (located presumably in south Spain, south Italy and the Balkans).

We will describe the spatial patterns of 11 allozymic alleles and two canonical variables using the variogram. The main directions of geographical variation will be determined using directional geostatistics, and kriged maps will be drawn to illustrate patterns of genetic variation.

Materials and methods

Sampling of populations

The populations analysed in this study include 81 populations previously sampled and analysed electrophoretically by Zanetto & Kremer (1995), as well as an additional set of 12 populations from eastern Europe. All populations are of putative native origin and are well distributed over the natural range of the species, except that no population from Italy nor from eastern Germany could be

included. Random samples of 120 seeds in each population were taken for allozyme analyses.

Allozyme analyses

Eight polymorphic loci were characterized in all the populations, either as part of the previous work by Zanetto & Kremer (1995) or for the present study. They are: *Aap-A* (alanine aminopeptidase, EC 3.4.11.1), *Acp-C* (acid phosphatase, EC 3.1.3.2), *Dia-A* (diaphorase, EC 1.8.1.4), *Got-B* (glutamic-oxaloacetic transaminase, EC 2.6.1.1), *Lap-A* (leucine aminopeptidase, EC 3.4.11.1), *Mr-A* (menadiolone reductase, EC 1.6.99.2), *Pgi-B* (phosphoglucose isomerase, EC 5.3.1.9) and *Pgm* (phosphoglucose mutase, EC 5.4.2.2). Protein extraction and starch gel electrophoresis were performed as described in Zanetto *et al.* (1994).

For geostatistical analyses, only the most common allele was considered at each locus showing one or two major alleles and several minor alleles (*Acp*, *Got*, *Lap*, *Mr* and *Pgm*). For those loci showing three common alleles, the two most frequent were considered (*Aap*, *Dia* and *Pgi*). A total of 11 alleles was analysed. Their frequency distributions are summarized in Table 1. In addition to the analysis at individual loci, a factorial discriminant analysis (FDA) was carried out on individual multilocus genotypic data, in which the ratio of the variance among populations to the variance within populations was maximized. The first two canonical variables (*FDA1* and *FDA2*), which accounted, respectively, for 20.6 and 13.6% of the total variation, were analysed using geostatistics.

Table 1 Main statistics of the allele frequency distributions at eight allozyme loci in sessile oak populations: allele considered for geostatistical analyses, number of populations (*n*) retained after elimination of the outliers, allele frequency mean, minimum and maximum

Allele	<i>n</i>	Mean	Min.	Max.
<i>Aap4</i>	88	0.589	0.417	0.808
<i>Aap6</i>	89	0.292	0.114	0.474
<i>Acp2</i>	88	0.537	0.358	0.750
<i>Dia2</i>	88	0.515	0.374	0.689
<i>Dia3</i>	90	0.352	0.217	0.596
<i>Got2</i>	88	0.940	0.836	0.964
<i>Lap4</i>	90	0.578	0.292	0.797
<i>Mr2</i>	92	0.798	0.652	0.936
<i>Pgi3</i>	91	0.834	0.652	0.991
<i>Pgi4</i>	86	0.073	0.000	0.165
<i>Pgm3</i>	92	0.918	0.800	1.000

Identification of outliers

Because geostatistics are based on measures of difference between pairs of locations, an unusually large or small value at a given location may strongly influence the results. Hawkins's test (Rossi *et al.*, 1992) provides a way to detect outliers by comparing each value at location x , $z(x)$, to its neighbouring values. Let n be the number of neighbouring values excluding $z(x)$, M the arithmetic mean of the n -values, and σ^2 the average variance measured over all equivalently sized neighbourhoods over the sampling space. Hawkins has shown the statistic $n[z(x)-M]^2/(n-1)\sigma^2$ to be distributed as a χ^2 with one degree of freedom. There is no objective criterion for the choice of the neighbourhood size. We used the smallest size for which most neighbourhoods contained more than five points, 450 km. Outliers were eliminated at the 5% significance level.

Construction of the variogram

The variogram measures the semivariance of the difference between points separated by a given distance h in space. The underlying assumption, called the 'intrinsic hypothesis' is that the difference between the values at any two points is a function of the distance between the points only. The empirical variogram is estimated from the data as a discrete function of given distance classes by:

$$\gamma(h) = (1/2n) \sum_{i=1}^n [z(x+h) - z(x)]^2,$$

where n is the number of points in the distance class h considered (Rossi *et al.*, 1992).

The variogram may be calculated for all directions in space, or for specific directions to test for anisotropy. In the latter case, only the pairs of points connected along a given direction in space (\pm a tolerance angle) are taken into account in the calculations.

Geostatistical analyses consist of describing and modelling the variogram as a function of distance. The variogram usually increases, then reaches a constant value called the sill. The distance at which the sill is attained, called the range, represents the distance beyond which two values may be considered as independent. The variogram theoretically equals zero at the origin, but a discontinuity is often observed, called the 'nugget effect'. This initial variance is caused either by fine-scale structures or by measurement errors. The empirical variogram may

be adjusted to several theoretical models including the exponential, Gaussian and spherical models. The linear model is used for variograms that do not reach a plateau, and characterizes either clinal patterns, or patterns with ranges exceeding the maximum distance considered. Flat variograms, representing the 'pure nugget' effect, characterize random patterns of variation.

In this study, variograms were calculated separately for the whole sampling area (93 populations) and for a subarea corresponding to western Europe (67 populations, see Fig. 1). These separate analyses were conducted because the western and the eastern parts of the natural distribution are known to have been colonized from different glacial refugia (Ferris *et al.*, 1993; Petit *et al.*, 1993). The objective was to test whether different migration routes could be detected by different directional variograms. However, the limited number of populations in the eastern part did not allow a separate analysis to be computed for that region.

A classical rule of thumb is to consider only pairs of points separated by less than half the maximum distance observed. Variograms were therefore calculated for 10 distance classes ranging from 0 to 1500 km for the whole area, and from 0 to 1000 km for the western subarea. More than 100 pairs of points were present in each class. Directional variograms were calculated for the following four sectors: 0 ± 22.5 degrees (west-east), 45 ± 22.5 degrees (southwest-northeast), 90 ± 22.5 degrees (south-north), and 135 ± 22.5 degrees (southeast-northwest), and within the same range of distances as the global variograms (but for eight classes only, to ensure that sufficient numbers of pairs were considered). Each variogram was standardized by dividing its values by the overall variance. This transformation will allow comparisons among different variables.

The variograms were adjusted either to the exponential model:

$$\gamma(h) = c + b[1 - \exp(-3h/a)],$$

where c is the nugget, b is the difference between the sill and the nugget, and a is the distance at which 95% of the sill is asymptotically attained, or to the linear model:

$$\gamma(h) = c + b h.$$

A weighted least squares method was used to fit both models to the observed data (Cressie, 1991, p. 99). The model for which the sum of squared residuals was smaller was retained.

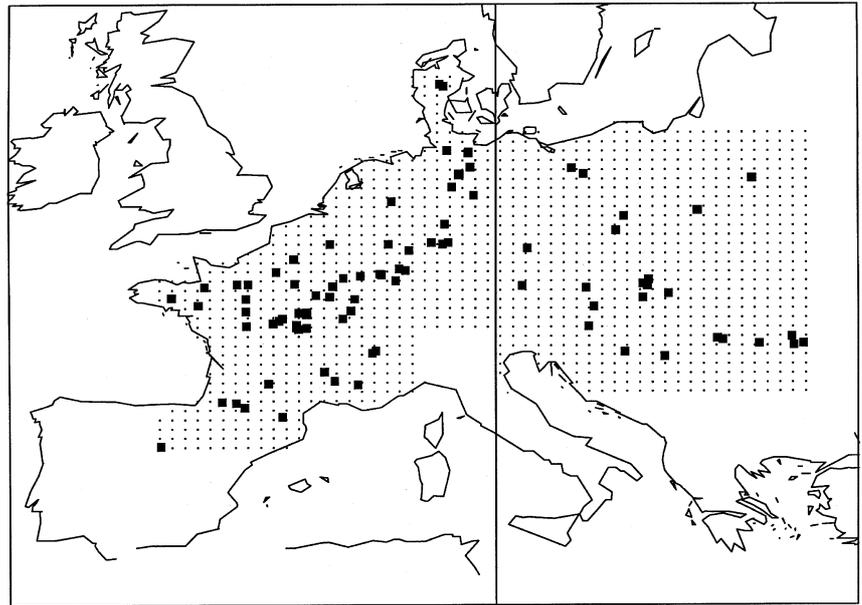


Fig. 1 Geographical map showing the locations of the 93 populations of sessile oak (black squares) with the grid of estimation points used for kriging. The vertical line delineates the western subsample of 67 populations analysed separately.

Genetical interpretation of the variogram

Variograms showing a sill can be interpreted within the frame of isolation-by-distance models. For a linear set of populations, Piazza *et al.* (1981) have shown that, at genetic equilibrium, the expression of the standardized variogram for gene frequencies is:

$$\gamma^*(h) = 1 - \exp\left(-\sqrt{\frac{2k}{\sigma^2}}h\right),$$

where σ is the standard deviation of parent-to-offspring dispersal distances and k is a 'recall' term representing mutation or selection.

This expression has been found to be empirically valid for a wide range of sampling schemes, including two-dimensional ones (Cavalli-Sforza & Feldman, 1990). In our study, it was used to interpret the ranges of the exponential variograms in terms of dispersal variances. For this purpose, we assumed k to be a mutation rate equal to 10^{-7} .

Detecting mean directions of variation

The directional variograms were used to compute for each variable its mean direction of spatial variation following the method of Barbujani (1988b). Briefly, this method estimates the components of variation along each direction as the correlation coefficient (Kendal's τ) between each directional variogram value and the lag distance. The mean direction of variation is then computed as the

average over the directional components. The significance of the mean direction may be assessed using Rayleigh's test (Greenwood & Durand, 1955), as described in Barbujani (1988b).

Kriging

Kriging uses the observed values of the variable in conjunction with the information provided by the

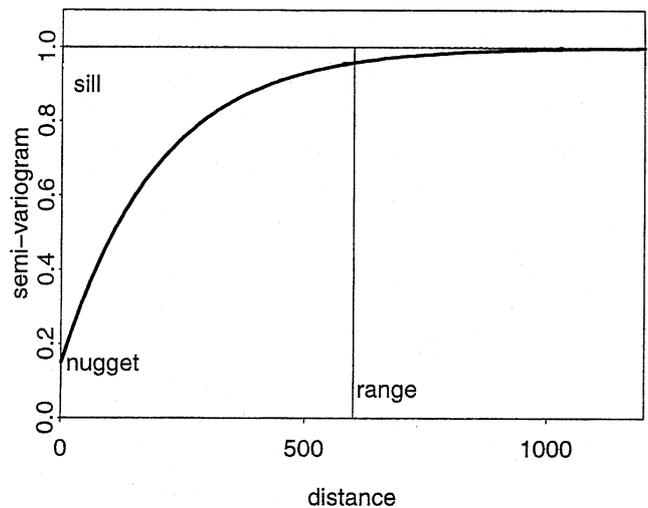


Fig. 2 Shape of an exponential variogram. The nugget effect is equal to 0.15 and the sill is equal to 1. At a practical range equal to 600, the model has approached 95% of the sill.

variogram to predict values at unsampled locations. The estimates are linear combinations of the observed values taken within a given search neighbourhood. They are both optimal (the estimation variance is minimized) and unbiased (the mean of the estimation errors equals zero). Kriging was performed on a regular grid of 1517 equally spaced points (one point each 50 km) covering the sampling area. The search neighbourhoods were the ellipsoids defined by the ranges of the directional variograms for the variable studied (Wackernagel, 1995, p. 46).

Results

Between one and seven points (mean: 4.33) were eliminated as outliers for each variable, so that the variograms were calculated from 86 to 92 data points for the whole sampling area, and from 62 to 67 data points for the western subarea.

Variograms for the whole sampling area (Fig. 3 and Table 2)

Among the 11 alleles analysed, four (*Aap4*, *Aap6*, *Pgi3* and *Dia2*), showed empirical variograms that fitted better to the exponential model. The adjusted ranges were 565 km, 623 km, 995 km and 776 km, respectively. The corresponding estimates of the standard deviation of dispersal distances, obtained by fitting an isolation-by-distance model, varied between 84 m (for *Aap4*) and 148 m (for *Pgi3*).

The other variograms fitted better to the linear model. The nugget effect accounted for more than 50% of the variation for *Dia3*, *Got2*, *Mr2*, *Pgi4* and *Pgm3*. Although a clinal trend was present, the spatial variation for these five alleles was therefore predominantly random. Conversely, a clinal pattern was predominant for *Acp2*, and, to a lesser extent, for *Lap4*.

The empirical variogram for the first canonical variable, *FDA1*, showed two distinct spatial structures. From 0 to 700 km, the variogram fitted an exponential model with a range of 750 km. From 700 to 1500 km, the variogram showed a rapid linear increase, indicative of a strong clinal pattern. The variogram for the second canonical variable, *FDA2*, fitted a linear model with a high random component.

Variograms for the western subarea

The same four alleles as for the whole area showed exponential variograms. However, except for *Pgi3*, very long ranges (of the order of thousands of kilo-

metres) were found, which indicates rather clinal patterns of variation, and nugget effects were higher than before. In particular, the patterns of variation at the alleles *Dia3*, *Got2* and *Pgm3* may be considered as purely random.

Mean directions of variation

Rayleigh's tests were all significant, indicating the presence of some anisotropy for all the variables, over the whole area as well as over the western subarea. Over the whole sampling area (Fig. 4a), the mean variation for most alleles is roughly along a west–east direction. The two exceptions are the alleles *Pgi3* and *Dia2*, whose mean directions of variation are in the south–north direction. The first canonical variable, *FDA1*, varies mainly along a west–east direction, whereas the mean direction of variation of the second canonical variable, *FDA2* is rather south–north. Over the western subarea, the mean directions of allelic variation showing a nonrandom pattern and the variation for *FDA1* are approximately all distributed between the southwest–northeast and the south–north directions (Fig. 4b).

Kriged maps

An example of an allele frequency map is shown in Fig. 5, for the allele *Aap4*. There is a clear east–west trend of variation superimposed with some patches.

The kriged map for the first canonical variable, *FDA1*, was constructed using the exponential model fitted to its first component of variation. The resulting map (Fig. 6) clearly shows a gradual west–east cline, with a few patches of contrasting values. For *FDA2*, kriging was performed using a linear model. The map (Fig. 7) shows mainly the presence of a south–north cline throughout Europe. Although the two variables *FDA1* and *FDA2* follow different patterns, their kriged maps exhibit some similarities. For example, oak stands from France, Belgium, the Netherlands, northern Germany and Denmark are clearly separated from others.

Discussion

This study is the third report of range-wide variation at allozyme loci in sessile oak. In the first study (Zanetto & Kremer, 1995), it was shown that despite a very low level of genetic differentiation (mean F_{ST} -value over eight loci: 0.025), the allozyme variation was organized geographically. A majority of the allele frequencies was significantly correlated with longitude, whereas some were correlated with lati-

tude. These trends were reinforced when multilocus and multivariate methods of analysis were applied (Kremer & Zanetto, 1997).

The enlargement of the sampling scheme for this study did not modify the observed level of genetic differentiation (mean F_{ST} -value over the same eight loci: 0.024). The use of geostatistics largely confirmed the geographical patterns previously observed by showing the presence of significant anisotropies at all allele frequencies, with a

predominance of variations in the west–east direction. However, geostatistics provided a much more detailed insight into these geographical patterns. First, mean directions of variation were defined more precisely and were compared between the total sampling area and the western part of the species range. Secondly, the variograms indicated the presence of three kinds of spatial patterns: stationary patterns characterized by a finite range, clines and random patterns. Thirdly, the kriging

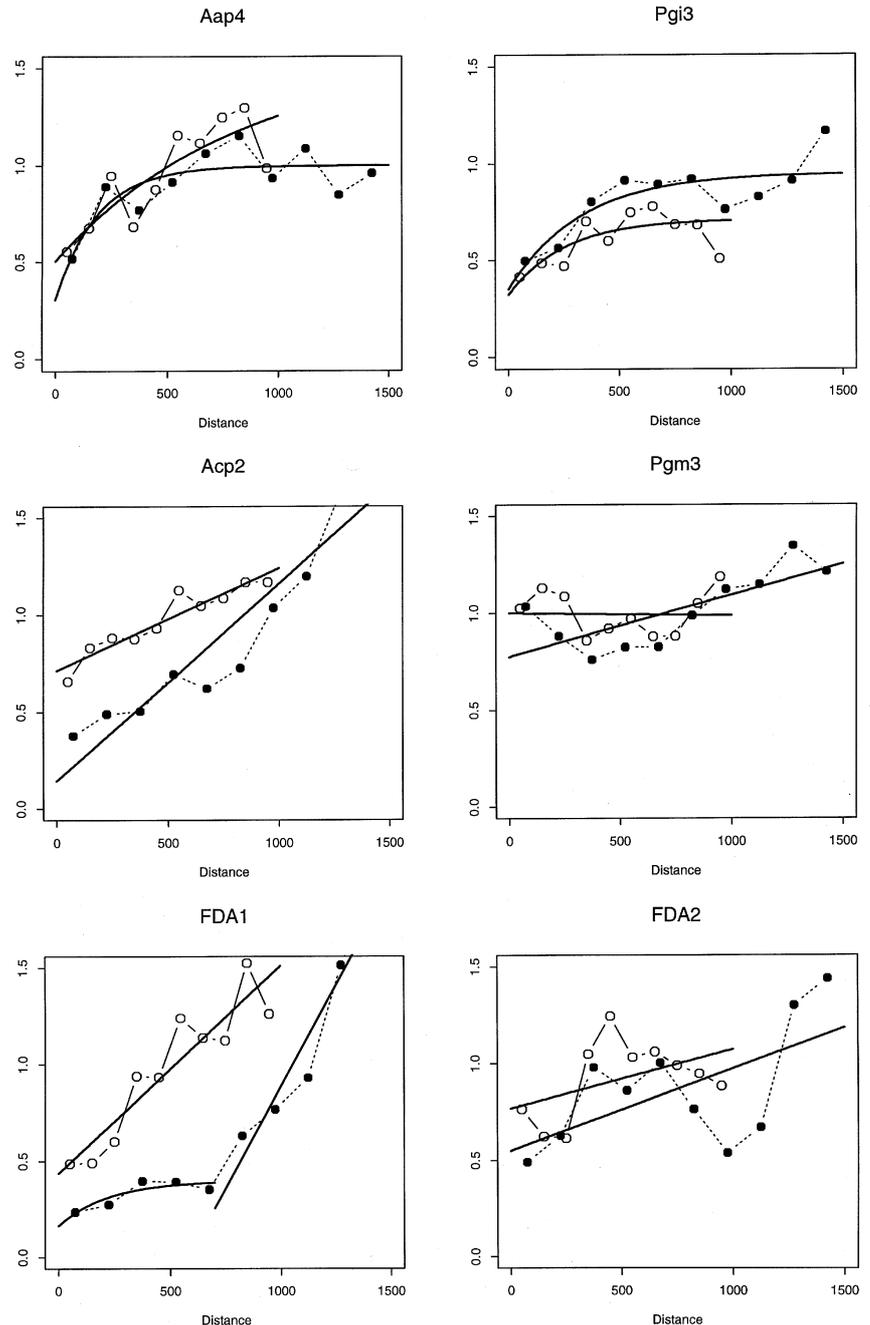


Fig. 3 Main types of experimental variograms and their adjusted models. Black circles represent estimated variogram values over the whole sampling area. Values estimated over the western subarea are represented by open circles. The variograms for the alleles *Aap6*, *Dia2* and *Pgi3* were similar to that for *Aap4* (exponential model). The variogram for the allele *Lap4* was similar to that for *Acp2* (linear model with a small nugget effect). The variograms for *Dia3*, *Got2*, *Mr2* and *Pgi4* were similar to that for *Pgm3* (predominance of the nugget effect).

method provided synthetic visual representations of the genetic variation of *Q. petraea* over its natural range.

These additional results offer new perspectives for the interpretation of the geographical patterns of genetic diversity. On account of the recent colonization history and present range-wide distribution of sessile oak, clinal trends of variation may result from three causes. First, the south-to-north postglacial range expansion may have caused a parallel cline in allele frequencies (Wijsman & Cavalli-Sforza, 1984). Secondly, clines may result from the contact between populations arising from different refugia (Zanetto & Kremer, 1995). Thirdly, selection acting along ecological gradients may also account for the presence of range-wide clines. Stationary patterns are known to result from isolation-by-distance among populations (Barbujani, 1988a), but they may also be caused by local selection (Sokal *et al.*, 1989). Random patterns may be attributable to noise resulting from the sampling of populations or loci. Because of the high number of individuals analysed

per population (120) the standard deviation of allele frequencies amounts in the worst case to 3.2%. Similarly, the high number of pairs of populations within each distance class ensures a good precision in the estimation of the variograms. The presence of a nugget effect would therefore indicate the presence of spatial structures occurring at a scale too small to be analysed with the present sampling scheme.

Heterogeneity of variograms among loci

Differences in the geographical patterns of variation at different unlinked loci are often taken as evidence of the action of natural selection (Barbujani, 1988b). However, Eastaer (1989) also invoked the possible role of independent genetic drift events during range expansion in shaping different patterns of variation at different loci.

Among the eight allozyme loci analysed, only two pairs (*Lap-Aap* and *Mr-Dia*) exhibited significant linkage disequilibrium (Kremer & Zanetto, 1997). The different types of variogram observed (exponen-

Table 2 Modelling of the variograms for the whole sampling area. Details (nugget and range for the exponential (Exp.) model or nugget and slope for the linear (Lin.) model) are given for the best fitted model. The sum of squared residuals (SSR) obtained with the other model is given in parentheses. σ is the standard deviation of dispersal distances estimated from the ranges of exponential variograms according to a one-dimensional continuous model of isolation-by-distance

Allele	Model	SSR	Nugget	Range (km) or slope	σ
<i>Aap4</i>	Exp.	0.101 (0.206)	0.304	565 km	84 m
<i>Aap6</i>	Exp.	0.093 (0.147)	0.360	623 km	93 m
<i>Acp2</i>	Lin.	0.234 (0.325)	0.143	1.017×10^{-3}	
<i>Dia2</i>	Exp.	0.065 (0.169)	0.370	776 km	116 m
<i>Dia3</i>	Lin.	0.080 (0.270)	0.691	0.319×10^{-3}	
<i>Got2</i>	Lin.	0.506 (0.974)	0.570	0.501×10^{-3}	
<i>Lap4</i>	Lin.	0.079 (0.916)	0.316	0.671×10^{-3}	
<i>Mr2</i>	Lin.	0.026 (0.174)	0.610	0.470×10^{-3}	
<i>Pgi3</i>	Exp.	0.105 (0.125)	0.350	995 km	148 m
<i>Pgi4</i>	Lin.	0.041 (0.042)	0.650	0.226×10^{-3}	
<i>Pgm3</i>	Lin.	0.146 (0.151)	0.777	0.317×10^{-3}	

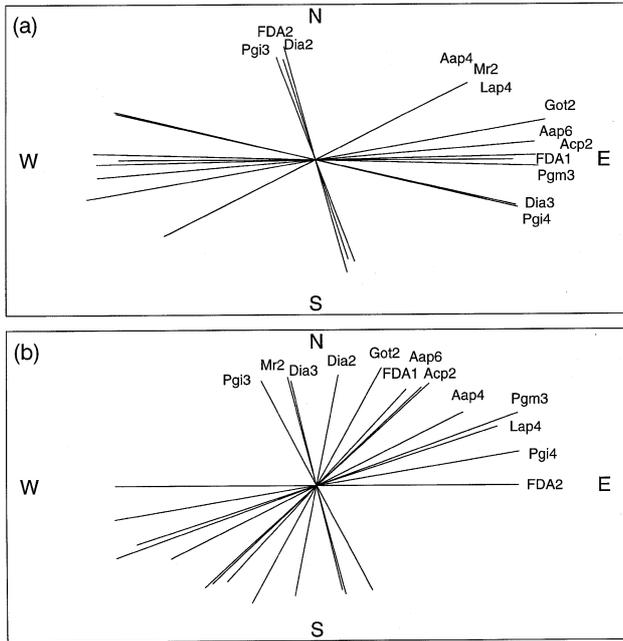


Fig. 4 Main directions of variation for each variable, computed using the method of Barbuji (1988a), over (a) the whole sampling area, and (b) the western subarea.

tial, linear or random), as well as the different main directions of variation, were therefore shared by different independent loci. This suggests the combined action of a few systematic forces rather than the action of selection. The heterogeneity among variograms may result from the presence of different allele frequency patterns at the different

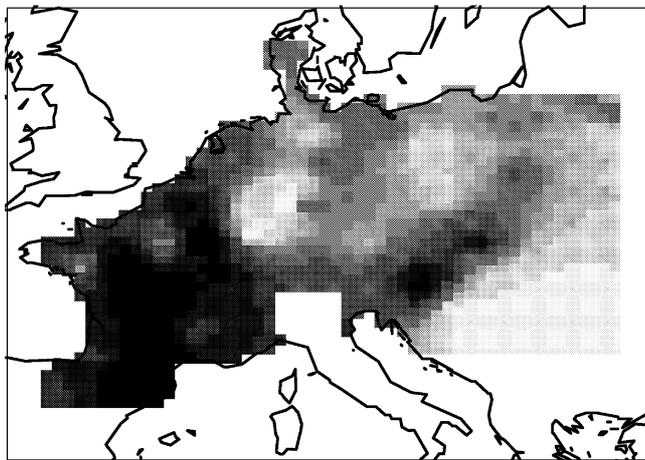


Fig. 5 Kriged map for the frequency of allele *Aap4*. The different levels of grey shading correspond to 10 equally spaced intervals covering the range of the variable (from 0.42 for the lighter to 0.91 for the darker).

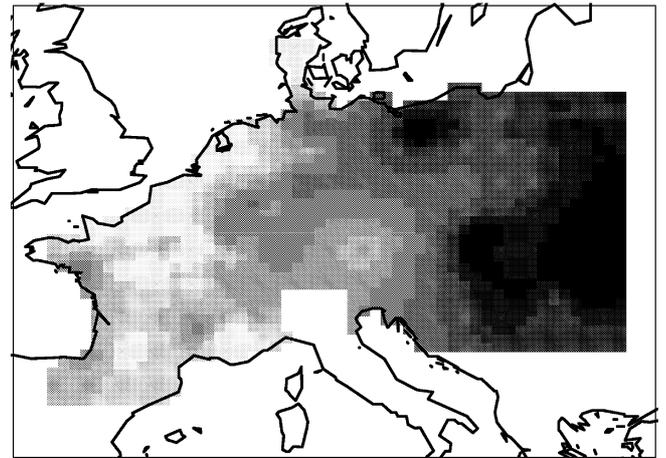


Fig. 6 Kriged map for the first canonical variable *FDA1*. The different levels of grey shading correspond to 10 equally spaced intervals covering the range of the variable (from 4.91 for the lighter to 8.24 for the darker).

loci before the postglacial expansion took place (Le Corre *et al.*, 1997).

Directions of allelic variation and the past history of sessile oak populations

Palynological data (Huntley & Birks, 1983) provide evidence for the existence of three main glacial refugia for deciduous oaks: southern Spain, southern Italy and the Balkans. Moreover, the phylogeographical distribution of chloroplast DNA variation in deciduous oak species (Petit *et al.*, 1993; Dumolin-Lapègue *et al.*, 1997) attests to the distinct glacial

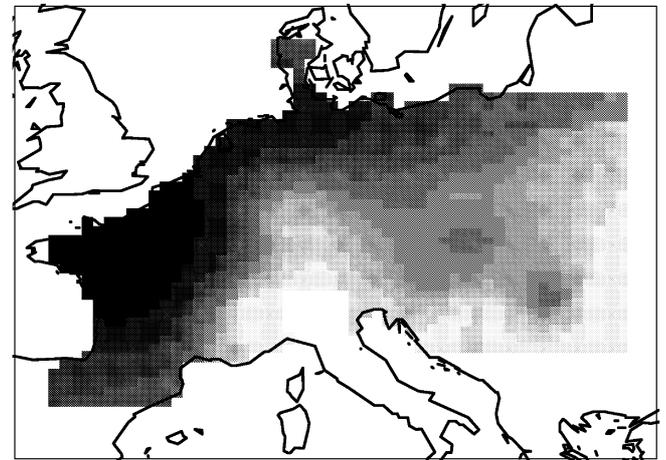


Fig. 7 Kriged map for the second canonical variable *FDA2*. The different levels of grey shading correspond to 10 equally spaced intervals covering the range of the variable (from -2.82 for the lighter to 0.40 for the darker).

origins of the present populations, and suggests that most populations in western Europe originated from Spain as a result of migration in a southwest to north-east direction. The main directions of allelic variation detected over the western part of the range are in agreement with this supposed direction of postglacial expansion. Clinal trends of variation were present for seven alleles among the 11 analysed. This indicates that founding events during the northwards expansion of sessile oak still have persistent effects on its present genetic structure at allozyme loci.

Over Europe, only two allele frequencies varied in a south–north direction. All other alleles showed a mean west–east direction of variation, which is in agreement with the hypothesis of a cline occurring after the populations that originated from south Spain and those that originated from Italy or the Balkans came into contact. The establishment of such a cline implies that allele frequencies in different refugia diverged in opposite directions during the glacial period, a situation which seems to have occurred more often than expected by chance. A bias may have been introduced by considering only alleles with intermediate frequencies, upon which genetic drift can act towards fixation or loss with equal probability. On the other hand, genetic divergence between the different refugia may have been reinforced by the action of divergent selection pressures at some loci, if environmental conditions differed among the different refugia during the glacial period. This hypothesis is in agreement with the fact that the patterns of variation for allozymes are more correlated with the glacial origin of populations than those for presumably neutral nuclear DNA markers (Le Corre *et al.*, 1997).

Stationary patterns of variation

Stationary patterns of variation were found for only four alleles among the 11 analysed, but it is likely that such patterns were masked for other alleles by the presence of clinal trends of variation. The estimates of standard deviation of dispersal distances obtained by fitting an isolation-by-distance model to the stationary variograms have only an illustrative value, because genetic patterns are probably not at equilibrium, and also because of the uncertainty about the mutation rate used for estimation. The values obtained are, however, in agreement with the modes of dispersal of oaks (bird dispersal for the seed, wind dispersal for the pollen).

The ranges of the stationary variograms (found to vary roughly between 500 and 1000 km) can also be

compared with the distances at which autocorrelation becomes negative in spatial autocorrelation analyses of natural populations. The two values are analogous and indicate the approximate size of homogeneous patches for the variable studied. In their study of 81 sessile oak populations, Zanetto & Kremer (1995) found distances that varied roughly between 400 and 650 km. Distances of about 700 km and 800 km were found, respectively, in *Quercus ellipsoidalis* (Jensen, 1986) and *Quercus ilex* (Michaud *et al.*, 1995). These results and the present data suggest that the genetic structure of forest tree populations over their natural ranges is characterized by very large scales of variation.

Application of geostatistics to the management of natural genetic resources in forest trees

Geostatistics appear to be useful tools for the description of complex range-wide patterns of genetic variation in forest trees. The method of kriging applied to canonical variables provided synthetic and visual representations which summarized well the spatial genetic structures in sessile oak. More generally, geostatistics will probably be useful for the management of genetic resources of forest trees. Kriged maps of genetic diversity or the numbers of alleles within populations may be of direct interest for conservation purposes. Geostatistical analysis and mapping of adaptive traits may be used for the elaboration of collecting strategies for breeding, as proposed by Monestiez *et al.* (1994) in their study of perennial ryegrass populations. Kriged maps for sufficiently discriminant genetic markers may also be useful in forest management, particularly for the assessment of the native or introduced origin of populations.

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