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Spin-Hall nano-oscillator with oblique magnetization and Dzyaloshinskii-Moriya interaction as generator of skyrmions and nonreciprocal spin-waves

A. Giordano¹, R. Verba², R. Zivieri³, A. Laudani⁴, V. Puliafito⁵, G. Gubbiotti⁶, R. Tomasello⁷, G. Siracusano¹, B. Azzerboni⁵, M. Carpentieri⁸, A. Slavin⁹ & G. Finocchio¹

Spin-Hall oscillators (SHO) are promising sources of spin-wave signals for magnonics applications, and can serve as building blocks for magnonic logic in ultralow power computation devices. Thin magnetic layers used as “free” layers in SHO are in contact with heavy metals having large spin-orbital interaction, and, therefore, could be subject to the spin-Hall effect (SHE) and the interfacial Dzyaloshinskii-Moriya interaction (*i*-DMI), which may lead to the nonreciprocity of the excited spin waves and other unusual effects. Here, we analytically and micromagnetically study magnetization dynamics excited in an SHO with oblique magnetization when the SHE and *i*-DMI act simultaneously. Our key results are: (i) excitation of nonreciprocal spin-waves propagating perpendicularly to the in-plane projection of the static magnetization; (ii) skyrmions generation by pure spin-current; (iii) excitation of a new spin-wave mode with a spiral spatial profile originating from a gyrotropic rotation of a dynamical skyrmion. These results demonstrate that SHOs can be used as generators of magnetic skyrmions and different types of propagating spin-waves for magnetic data storage and signal processing applications.

Spin-orbitronics combined with other sub-fields of spintronics, such as magnonics and spin-caloritronics, has created a novel paradigm in information processing which could become a viable alternative to Si-based electronics¹.

Recent experimental and theoretical developments in spin-orbitronics have clearly shown a great potential in generation of spin-currents able to compensate damping in magnetic materials^{2–6}. The spin-Hall effect (SHE) plays a dominant role in the above-mentioned experiments, as it converts the input *charge current*, flowing in a heavy metal, into a *spin-current*, diffusing perpendicularly into the adjacent ferromagnet, and creating a spin-transfer torque (STT) that acts on the ferromagnet magnetization⁷. Another interesting and highly non-trivial spin-orbital effect is the interfacial Dzyaloshinskii-Moriya interaction (*i*-DMI)⁸. Both SHE and *i*-DMI have been used to improve the performance of “racetrack” device prototypes in magnetic storage^{9,10}, to add a new degree of freedom in the design of magnetoresistive memories^{3,11}, to create nonreciprocity in the spin-wave (SW) propagation for signal processing applications^{12–14}, to excite coherent magnetization self-oscillations^{4,5}, and for the manipulation of skyrmions in ultrathin ferromagnetic materials^{15,16}. However, to the best of our knowledge, the influence of *i*-DMI on the performance of a spin-Hall oscillator (SHO) has not been studied so far^{4,5}.

¹Department of Mathematical and Computer Sciences, Physical Sciences and Earth Sciences, University of Messina, Messina, Italy. ²Institute of Magnetism, National Academy of Sciences of Ukraine, Kyiv, Ukraine. ³Department of Physics and Earth Sciences and CNISM Unit of Ferrara, University of Ferrara, Ferrara, Italy. ⁴Department of Engineering, University of Roma Tre, Roma, Italy. ⁵Department of Engineering, University of Messina, Messina, Italy. ⁶Istituto Officina dei Materiali del CNR (CNR-IOM), Sede Secondaria di Perugia, c/o Dipartimento di Fisica e Geologia, University of Perugia, Perugia, Italy. ⁷Department of Engineering, Polo Scientifico Didattico di Terni, University of Perugia, Terni, Italy. ⁸Department of Electrical and Information Engineering, Politecnico di Bari, I-70125 Bari, Italy. ⁹Department of Physics, Oakland University, Rochester, MI 48309, USA. Correspondence and requests for materials should be addressed to G.F. (email: gfinocchio@unime.it)

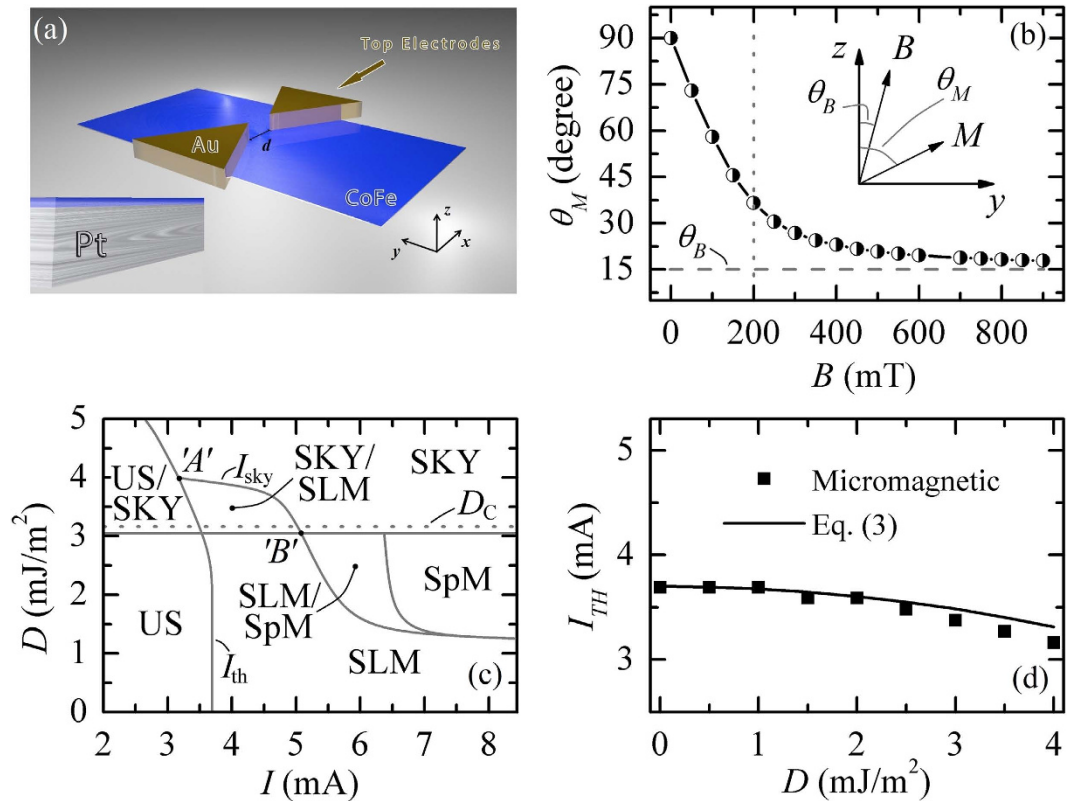


Figure 1. Sketch of the SHO device under investigation and dynamical phase diagram of this device.

(a) Sketch of a bilayer composed of a CoFe ferromagnetic layer and a heavy metal layer (Pt) with a rectangular cross-section. The thick Au electrodes carry the charge current everywhere, except the inter-electrode gap of the width d , where the charge current flows inside the bilayer and excites perpendicular (vertical) spin current going into the CoFe ferromagnetic layer. A rectangular coordinate system for the above described SHO geometry is shown. (b) The angle θ_M characterizing the equilibrium direction of the static magnetization in the CoFe ferromagnetic layer as a function of the magnitude of the external bias magnetic field B . The vertical line at $B = 200$ mT separates the regions where it is possible to excite localized and propagating spin-wave modes, respectively. Inset: Cartesian coordinate reference system where the angles θ_M and θ_B are shown explicitly. (c) The phase diagram of the SHO excitations on the D vs. I plane. Seven different regions can be distinguished in this phase diagram: uniform states (US), Slonczewski linear modes (SLM), spiral modes (SpM), skyrmions (SKY), and the bistability regions uniform states/skyrmions (US/SKY), Slonczewski linear modes/spiral modes (SLM/SpM) and Slonczewski linear modes/skyrmions (SLM/SKY). The amplitude of the external field is $B = 400$ mT. The Oersted field is included in the model. D_C is the critical value of the i -DMI parameter (see explanations below), I_{th} is the threshold current, I_{sky} is the current needed to nucleate skyrmions (line between the points 'A' and 'B'); (d) Comparison between the threshold current of the SLM excitation obtained by means of micromagnetic simulations (symbols) and using the analytical formula (3) (solid line).

Here, we present the magnetization dynamics induced by the SHE in a realistic SHO structure, taking into account the influence of the i -DMI⁸. We have chosen a state-of-the-art SHO geometry (Fig. 1a) where the charge current I flows in the Pt layer along the x -axis between the golden electrodes and, due to the SHE in Pt, a spin-current is locally injected into the ultrathin extended CoFe ferromagnet (SHO “free” layer). The CoFe layer has an in-plane easy axis at zero bias field, so when a sufficiently large out-of-plane bias field is applied at an oblique angle in the “ yz ” plane (Fig. 1b), the static magnetization M of the “free” layer also goes out-of-plane, making the angle θ_M with the vertical axis “ z ”. In such a geometry, the Slonczewski *propagating* spin waves¹⁷ can be excited in any in-plane direction^{18–20} and, due to the influence of the i -DMI, they have the maximum nonreciprocity when propagating along the x -axis, perpendicular to the in-plane projection of the bias magnetic field. Our numerical simulations have shown that the wave numbers of SWs excited at a particular frequency ω and propagating along the positive and negative directions of the x -axis are different. The difference is proportional to the magnitude of the i -DMI parameter D . This result, well reproduced by a simple one-dimensional analytical model, can be used to establish a novel procedure for the experimental measurements of D . Micromagnetic simulations have also demonstrated that (i) a novel propagating spin-wave mode, characterized by a spiral spatial profile, can be excited at sufficiently large magnitudes of D and I , and (ii) skyrmions can be efficiently nucleated by the SHE in the SHO geometry. Similarly to optics^{21,22}, the excitation of spiral spin-waves in magnetism could be attractive for designing new information coding protocols. Recent experimental observations have demonstrated that skyrmions^{15,16,23–25} can be nucleated via conversion of domain walls in Ta/CoFeB/MgO²⁶, or by applying an

out-of-plane field in Ir/Co/Pt²⁷ and Pt/Co/MgO²⁸ multilayers. Although a single skyrmion can be nucleated by a spin-polarized scanning tunneling microscope²⁹, the control of its room temperature nucleation is still an experimental challenge. Earlier achievements have shown the possibility to solve this problem^{15,23,30}. Our results show an alternative method to control the nucleation of single skyrmions, based on the use of the SHE.

Results

Static characterization of the SHO structure and phase diagram of the SHO excitations. We have micromagnetically studied a Pt(5 nm)/CoFe(1 nm) SHO with a rectangular cross section of $1500 \times 3000 \text{ nm}^2$ (see Fig. 1a for the sketch of the device, including a Cartesian coordinate system where x and y are the in-plane axes, while z is the out-of-plane axis, Methods and Supplementary Note 1 for the detailed description of the micromagnetic framework and simulation parameters). Figure 1b shows the angle θ_M , characterizing the equilibrium orientation of the static magnetization in the SHO, as a function of the external bias magnetic field B . This field is applied at the tilting angle $\theta_B = 15^\circ$ with respect to the perpendicular of the SHO ferromagnetic layer in the y - z plane (see inset in Fig. 1b). As the bias field increases, the magnetization vector tends to align along the field direction.

Similarly to what is observed in STT oscillators based on the point-contact geometry, the type of the spin-wave mode excited by the SHE can be controlled by the direction of the bias magnetic field and the effective anisotropy. In particular, the materials with in-plane easy axis demonstrate excitation of self-localized spin-wave “bullets”, or co-existence of bullets and Slonczewski modes^{31,32}, for sufficiently large values of θ_M , and excitation of Slonczewski propagating spin-wave modes for sufficiently small values of θ_M ^{18,33}. In this study, numerical simulations showed that, for the bias field larger than 200 mT and $\theta_M < 37^\circ$, the Slonczewski propagating spin-wave modes were excited.

As it will be discussed below, the additional degree of freedom of the i -DMI can introduce qualitative differences in the spatial profile of the Slonczewski-type cylindrical mode, compared to the case when i -DMI is ignored. Hereafter, we focus on the results obtained at the bias field of 400 mT and active region (distance between the Au electrodes in Fig. 1a) of $d = 100 \text{ nm}$, however similar findings have been obtained at $d = 200 \text{ nm}$ and at larger bias fields (up to 800 mT).

Figure 1c shows a phase diagram of dynamical excitations in the SHO on the plane D -vs- I . Seven different regions can be identified: (i) uniform states (US), (ii) Slonczewski linear modes (SLM), (iii) spiral modes (SpM), (iv) skyrmions (SKY), as well as the bistability regions (v) uniform states/skyrmions (US/SKY), (vi) Slonczewski linear modes/skyrmions (SLM/SKY) and (vii) Slonczewski linear/spiral modes (SLM/SpM). At small values of the driving current, the SHO is in the US, i.e. in a region characterized by a uniform magnetic configuration. SLMs are excited at a critical current I_{th} that slightly decreases as a function of D (see Fig. 1d). The excited modes in the SLM region exhibit a two-dimensional radiation pattern that changes from the isotropic (see Supplementary Movies 1 and 2 for the SLM dynamics at $I = 4.22 \text{ mA}$ and $I = 5.28 \text{ mA}$ respectively, $B = 400 \text{ mT}$ and $D = 0.0 \text{ mJ/m}^2$) to the anisotropic cylindrical profile with the increase of the i -DMI parameter D (see Supplementary Movies 3 and 4 for the SLM at $I = 4.22 \text{ mA}$ and $I = 5.28 \text{ mA}$, respectively, $B = 400 \text{ mT}$ and $D = 1.5 \text{ mJ/m}^2$). The cylindrical profile of the spin-wave radiation evolves into a spiral-like profile for $1.5 \text{ mJ/m}^2 < D < 3.0 \text{ mJ/m}^2$, and a sufficiently large I (SpM region) (see as an example Supplementary Movie 5). The identification of the scenario leading to the radiation of these *spiral* spin-wave modes is one of the most important results of this study.

The SKY region is observed starting from D values near the critical value of $D_C = 3.16 \text{ mJ/m}^2$ ($D_C = 4\sqrt{A(K_u + (B_Z - 0.5\mu_0 M_S)M_S)/\pi}$)³⁴. The skyrmion nucleation process, driven by the SHE, occurs together with the excitation of propagating spin-waves (see for an example Supplementary Movie 6), and at the current I_{sky} (solid line between the point ‘A’ and ‘B’). The I_{sky} curve coincides with I_{th} for D values larger than 4 mJ/m^2 (point ‘A’ in Fig. 1c). This fact constitutes the second key result of this study, i.e. the prediction that a pure spin-current with in-plane polarization can be used for the nucleation of skyrmions. The regions US/SKY, SKY/SLM and SLM/SpM are the bistability regions, obtained sweeping the current back and forth and using in each simulation the final state at the previous current. In the first of these regions, we have either a uniform ground state or skyrmions, depending on the excitation history. In particular, the US is achieved when the current is not sufficiently large to obtain the SKY region. On the other hand, when the current is large enough to reach the SKY region, skyrmions are nucleated and remain stable also at zero current, therefore the SKY state is achieved in the US/SKY region. Concerning the second region SKY/SLM, a SLM is excited if the current is increased from the US/SKY region. Skyrmions and a SLM coexist if the current is decreased from the SKY region. In the last region, an SLM (SpM) is observed, if the current is increased (decreased) from SLM (SpM) region. The origin of this hysteretic behavior will be discussed in detail below. We have also investigated the role of the Oersted field, finding that it does not influence qualitatively the results of Fig. 1c (see Supplementary Note 2 for more details).

Excitation of Slonczewski linear spin-wave mode. As it was pointed out earlier, the i -DMI leads to the excitation of nonreciprocal spin-waves. It can be observed qualitatively in the Supplementary Movies 3 and 4, and by comparing the mode profile in Fig. 2a,b. The largest nonreciprocal effect induced by the i -DMI occurs in the direction perpendicular to the in-plane projection of the static magnetization \mathbf{M}_0 (x -axis), while the propagation along the in-plane projection of \mathbf{M}_0 (y -axis) is reciprocal, and is characterized by the wave number that is the same as in the case of zero D (0.03 and 0.035 nm^{-1} at $I = 4.22 \text{ mA}$ and $I = 5.28 \text{ mA}$, respectively, see Supplementary Note 2). Those results are consistent with the previous experimental measurements³⁵ and the results of the analytical theory¹². The i -DMI-induced appearance of the nonreciprocal spin-waves leads to the decrease of the threshold current (Fig. 1d), and to a “red” shift of the generation frequency for increasing values of D , at a constant current (Fig. 2c). Figure 2d summarizes the dependence of the wave numbers ($|k_x|$ and $|k_y|$) on D computed from the spatial distribution of the magnetization for $I = 4.22 \text{ mA}$ and $I = 5.28 \text{ mA}$. The difference between the $|k_x|$ and $|k_y|$ is shown in Fig. 2e, and, as it can be noticed, is independent of I . All these numerically obtained features can

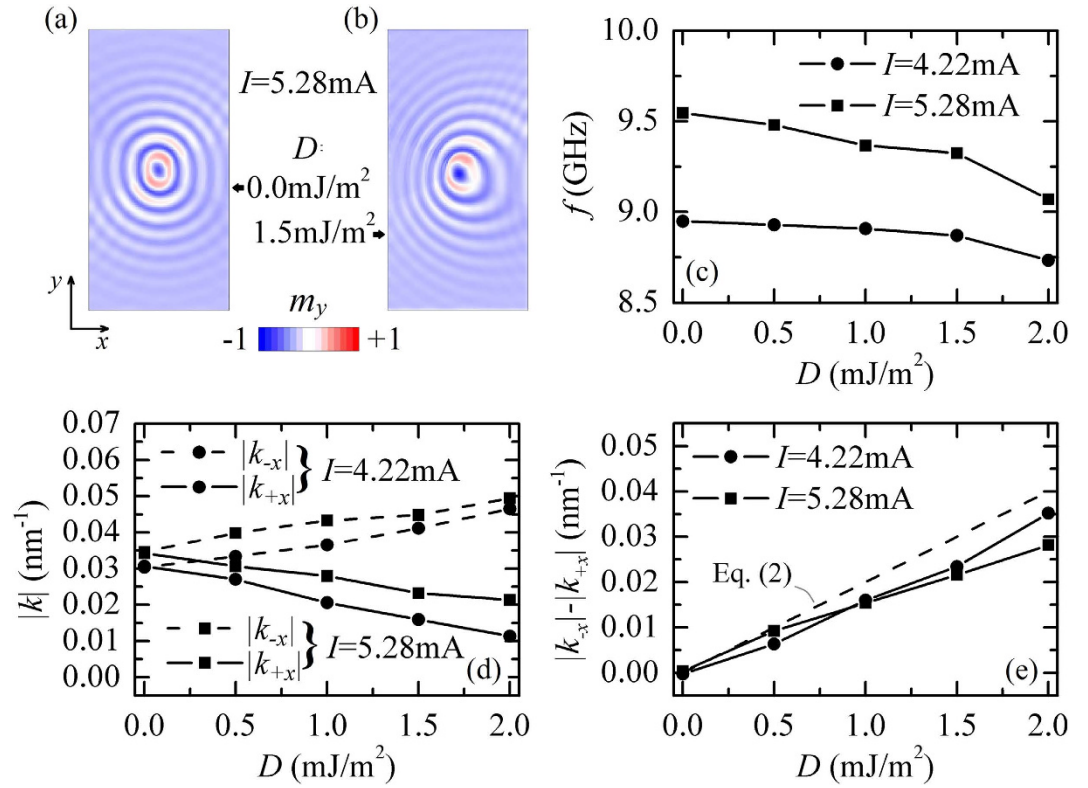


Figure 2. Non-reciprocal Slonczewski linear modes. (a,b) Example of the spatial profile of the reciprocal and nonreciprocal Slonczewski spin waves, respectively, calculated for $I = 5.28$ A and $D = 0.0$ and 1.5 mJ/m², respectively. (c) Oscillation frequency of the excited SLM as a function of D for two values of the driving current. (d) Wave numbers along the $-x$ and $+x$ directions as functions of D for two values of current; (e) Difference between the wave numbers along the positive and negative x -directions as a function D for the same two values of current (solid lines) and the same difference calculated analytically from Eq. (2) (dashed line).

be understood using a simple one-dimensional analytical model. In the framework of this model, we consider only the spin-waves propagating along the x -direction, where the spin-waves exhibit the largest nonreciprocity.

The frequency and wave vectors of the excited spin-waves are defined by the spatial quantization rule, which is determined by the spatial distribution of the spin-current J_s . In the case of a nonreciprocal spectrum, the general quantization rule can be written as $f(k_+ - k_-, J_s(x)) = 0^{36}$, or, equivalently $k_+ - k_- = \text{const} = f_1(J_s(x))$, where k_+ and k_- are the wave vectors of spin-waves propagating in opposite directions along the direction of maximum nonreciprocity and having the same frequency (for a reciprocal wave spectrum this rule is reduced to the condition $|k| = \text{const}$). The approximate spin-wave spectrum in the x -direction can be written as $\omega_k \approx \omega_0 + \omega_M \tilde{\lambda}^2 k_x^2 - \omega_M \tilde{D} k_x$ (see Methods), where ω_0 is the angular frequency of the ferromagnetic resonance in the SHO, $\tilde{D} = 2D/(\mu_0 M_S^2) \sin^2 \theta_M$, $\tilde{\lambda}^2 = \lambda^2(2\omega_H + \omega_M(1 - H_{an}/M_S) \sin^2 \theta_M)/2\omega_0$, λ is the exchange length in the material of the SHO ferromagnetic layer, and $H_{an} = 2K_u/(\mu_0 M_S)$ is the anisotropy field. From this equation, the wave vectors of counter-propagating nonreciprocal spin-waves, having the same frequency ω , can be computed as:

$$k_{\pm x} = \frac{1}{2\omega_M \tilde{\lambda}^2} (\omega_M \tilde{D} \mp \sqrt{\omega_M^2 \tilde{D}^2 + 4\omega_M \tilde{\lambda}^2 (\omega - \omega_0)}) \quad (1)$$

where k_{-x} (k_{+x}) is associated with the plus (minus) sign in the second term in the circular brackets in the equation (1). Substituting the wavenumber of equation (1) in the quantization rule, we get the condition $\sqrt{\omega_M^2 \tilde{D}^2 + 4\omega_M \tilde{\lambda}^2 (\omega - \omega_0)} = \text{const}_1$ that gives the following dependence of the generation frequency on D : $\Delta\omega = -\omega_M \tilde{D}^2 / (4\tilde{\lambda}^2)$. Thus, the generation frequency has a “red” shift with the increased D , as obtained from our micromagnetic simulations (see Fig. 2c). This effect could be easily understood by noting that the minimum spin-wave frequency in the spectrum becomes lower with the increase of D . From equation (1), it is easy to calculate the difference between the wave numbers of the excited waves:

$$k_{-x} - k_{+x} = \tilde{D} / \tilde{\lambda}^2 \quad (2)$$

and to verify that this difference is independent of the quantization constant and, therefore, of the spatial distribution of the spin-current. Hence, the condition (2) can be used for the experimental determination of the

magnitude and sign of the i -DMI parameter. Equation (2) gives a reasonable description of the simulation data, considering the same physical parameters of the SHO (Fig. 2e). Small deviation of Eq. (2) from micromagnetic results are related to the usage of approximate SW spectrum which allows us to give simple and clear qualitative explanation of the observed effect and derive explicit expression for Δk . The fact that the dependence $\Delta k(D)$ is almost the same for different I is linked to a weak nonlinear variation of the spin-wave spectrum with driving current, due to a small difference in amplitudes of the excited spin-waves. Therefore, the difference of the spin-wave numbers is mainly determined by the linear spin-wave spectrum. From an experimental point of view, a direct determination of D can be achieved by measuring the wavelength of the emitted spin-waves along the $+x$ and $-x$ direction, using the phase-resolved micro-focused Brillouin light scattering³⁷ or time-resolved Kerr microscopy³⁸. However, this method of determination of D may have practical limitations due to the fact that the wavelength of the excited spin-waves (see Fig. 2d) are in the range 0.13–0.63 μm , i.e. being comparable with the lateral resolution of the above mentioned optical techniques.

Within the above described one-dimensional model, we can also calculate the dependence of the threshold current for spin-wave excitation on D . Assuming a rectangular profile of the charge current density in the active region ($J(x) = J$ within $x = [0, d]$, and $J(x) = 0$ otherwise), one can get the following implicit expression (similar to equation (6c) in³⁹),

$$\left(\bar{k} + i \frac{\Gamma_G - \Gamma_J}{v} \right) \tan \left[\left(\bar{k} + i \frac{\Gamma_G - \Gamma_J}{v} \right) \frac{d}{2} \right] = -i \left(\bar{k} + i \frac{\Gamma_G}{v} \right) \quad (3)$$

where $\bar{k} = (k_{-x} - k_{+x})/2$ is the average wave number of excited nonreciprocal spin-waves (note, that in our notation $k_{-x} < 0$), d is the distance between the SHO golden electrodes characterizing the spatial localization of the spin-current, $v = [\omega_M^2 \bar{D}^2 + 4\omega_M(\omega - \omega_0)\tilde{\chi}^2]^{(-1/2)}$ is the spin-wave group velocity, $\Gamma_G = \alpha_G \omega$ is the spin-wave damping, $\Gamma_J = \sigma J$ is the negative damping created by the spin-current, and $\sigma = g\mu_B \alpha_H \sin \theta_M / (2eM_S t_{\text{CoFe}})$ determines the spin-Hall efficiency (g is the Landé factor, μ_B the Bohr magneton, e the electronic charge and t_{CoFe} the CoFe layer thickness). The threshold current calculated from Eq. (3) is compared with numerical results in Fig. 1d. Here we use fitting coefficient C which relates threshold current density J_{th} found from Eq. (3) with the current I_{th} : $I_{\text{th}} = C J_{\text{th}}$, which value was determined from the coincidence of calculated and micromagnetic threshold currents $I_{\text{th}} = 3.7$ mA at $D = 0.0$ mJ/m². One can see a good coincidence between the analytical and numerical results. Note that the decrease of the threshold current with D has the same nature, as a frequency “red” shift-lowering the bottom of the spin-wave spectrum with the increase of D and, consequently, the decrease of spin-wave damping $\Gamma_G = \alpha_G \omega$.

The SLM in SHOs have not been observed experimentally, since the threshold current for their excitation is expected to be very large ($> 10^9$ A/cm²)²⁰, around three times larger than the current necessary to excite a “bullet” spin-wave mode in an SHO with in-plane magnetization. In the SHO of this study, we were able to reduce the critical current density of one order of magnitude ($< 4 \times 10^8$ A/cm²) thanks to the additional perpendicular interface anisotropy in the CoFe ferromagnet. This additional anisotropy allows one to achieve the positive nonlinear frequency shift, required for the SLM excitation³³, at a higher magnetization angle θ_M , which results in the higher spin-Hall efficiency, since it is proportional to $\sin \theta_M$. A further reduction of the current density can be achieved by including an additional Ta layer above the CoFe ferromagnet²⁴.

Excitation of spin-wave modes with a spiral spatial profile. Figure 3a summarizes the spin-wave frequency as a function of I computed for $D = 0.0$ mJ/m² and $D = 1.5$ mJ/m² ($d = 100$ nm). In the absence of the i -DMI, the oscillation frequency shows a monotonic increase with current, or a “blue” frequency shift, typical for the Slonczewski linear propagating spin-wave mode. A different frequency behavior is seen for $D = 1.5$ mJ/m², where the frequency tunability with current becomes non-monotonic. This behavior is robust under the variation of d , as seen from Fig. 3b where $d = 200$ nm. At sufficiently large I and D , the spin-wave is converted from the cylindrical to a spiral-like (SpM region in Fig. 1c). Figure 3c shows a spiral-type profile (the color is linked to the y -component of the magnetization).

In order to understand the origin of the spiral mode, we have performed a detailed analysis of the spatial distribution of the dynamic magnetization in the SHO ferromagnetic layer in this regime. Figure 3d–g illustrate four snapshots ($I = 6.33$ mA) which clearly reveal the physics of the spiral mode formation. In the SpM region, the SHE is able to nucleate a dynamical soliton^{40–42}. It is characterized by a central core with the magnetization pointing along the negative out-of-plane direction (opposite to the equilibrium axis of the magnetization), and by the rotation of its boundary spins through 360° (see Fig. 3d–g). The dynamical skyrmion exhibits a rotational motion (gyration) along a circular trajectory within the region of the high current density, that is typical for solitons with nonzero topological charge under the influence of spin-current⁴³ (see Supplementary Movie 7). Dynamical skyrmion plays a role of a “source” for magnetization oscillations in the outer region, and, since the source is gyrating, the radiation acquires the form of a spiral wave, as it happens in many other fields with gyrating source^{44,45}. Note, also, that once it has been excited the SpM is still stable at lower current magnitudes in the SpM/SLM region, because the excitation of the dynamical skyrmion is linked to a sub-critical Hopf bifurcation⁴². Spiral mode is strongly nonlinear because it is originated by the interaction between a dynamical skyrmion and propagating spin-waves, this is the reason of the non-monotonic behavior of the frequency of the excited mode as a function of the current.

Generation of single skyrmions and “gas” of skyrmions. The last regions of the phase diagram of Fig. 1c are related to skyrmions. For the critical D_C , the skyrmions become energetically stable³⁴ and, after the nucleation driven by the SHE (SKY region) (see Supplementary Movie 6 for the nucleation of a single skyrmion),

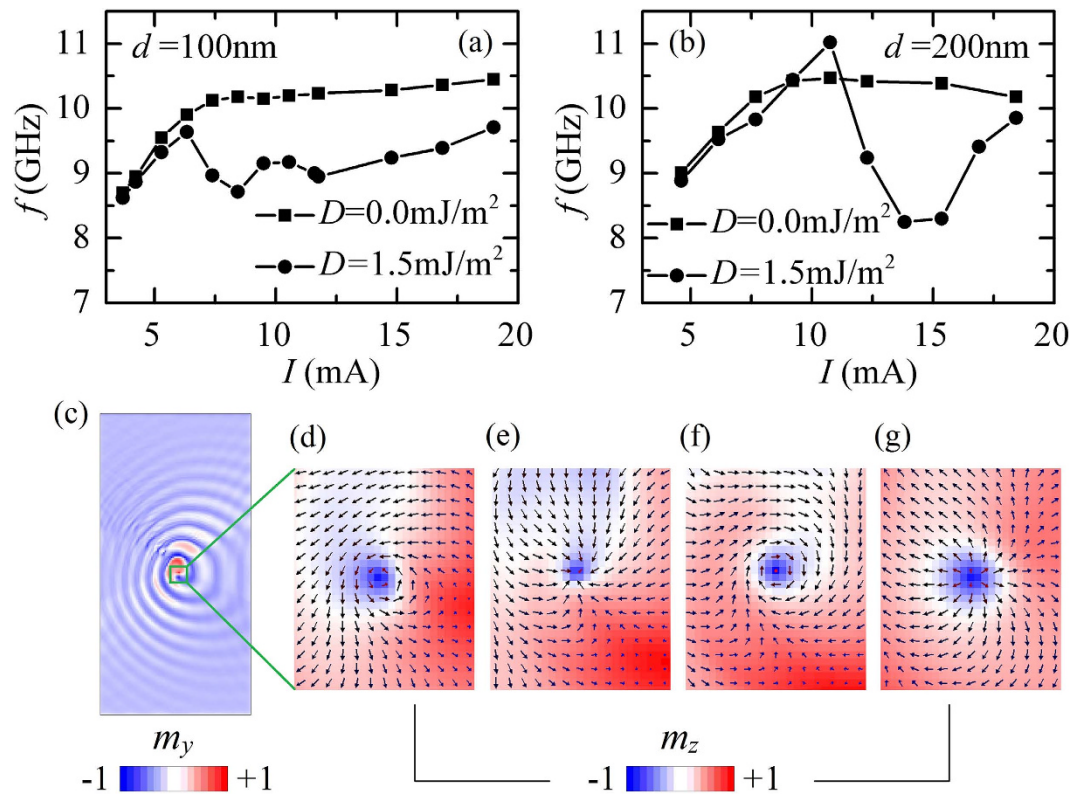


Figure 3. Excitation of a spin-wave with spiral profile. (a) Oscillation frequency of the excited mode as a function of I without and with i -DMI, for $d=100\text{nm}$. (b) Same as (a) but with $d=200\text{nm}$. (c) Example of a spatial profile of the spiral-type spin-wave for $I=6.33\text{mA}$ and $D=1.5\text{mJ/m}^2$. (d–g) Spatial distributions of the magnetization characterizing a topological-type magnetic soliton, the current-induced gyration of which causes the radiation of a spiral-type spin wave mode.

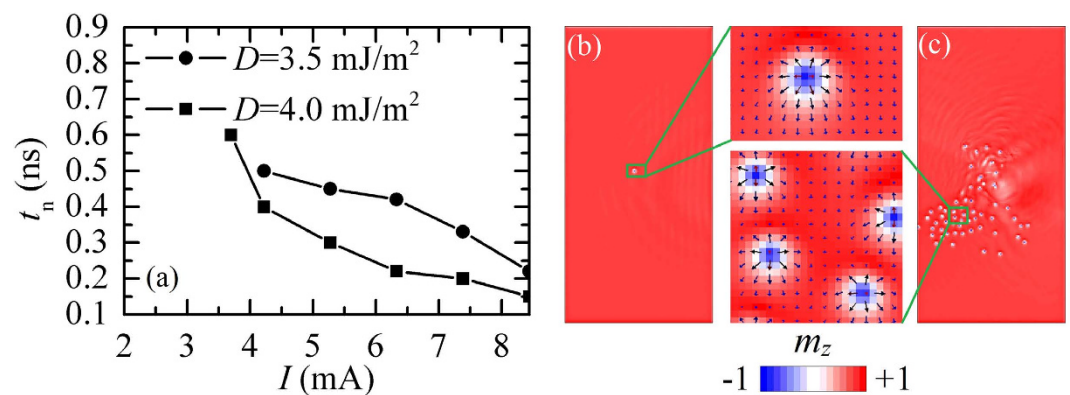


Figure 4. Skyrmion nucleation. (a) Nucleation time of a single skyrmion as a function of the current amplitude for $D=3.5$ and 4.0mJ/m^2 . (b) Snapshot of a single skyrmion and zoom of the skyrmion nucleation region. (c) Snapshot of a skyrmion gas and zoom of the region indicated by a green square in the right frame.

they remain stable even when the driving current is switched off (US/SKY region). Once the skyrmion is nucleated, it is shifted along the spin-current direction, as expected for Néel skyrmions¹⁶. For D below 4.0mJ/m^2 (point 'A' in Fig. 1c), I_{sky} and I_{th} split into different curves, and, hence, in the SKY/SLM region when the current increases from the uniform state, only the SLMs are excited. The presence of this region in the phase diagram is interesting from a fundamental point of view, as it identifies a scenario where the interaction between the spin-waves and skyrmions⁴⁶ can be studied. Figure 4a shows the nucleation time of a single skyrmion as a function of the current magnitude for two values of D (3.5 and 4.0mJ/m^2). It can be seen from Fig. 4a that a sub-nanosecond skyrmion nucleation time can be achieved (see Fig. 4b for a single skyrmion snapshot). Our results predict a new scenario for a single skyrmion nucleation driven by a pure spin-current. This method can be used as an alternative to the method based on the STT from a perpendicular spin-polarized current¹⁵, with the possible advantage of

the simpler fabrication process of the device. If current pulses are applied consecutively or if the current is not switched off, more skyrmions are nucleated up to a saturation value that marks a transition to a skyrmion gas phase⁴⁷. In detail, since the current is non-uniformly applied, the skyrmions tend to accumulate in one side of the ferromagnet until no more skyrmions can be hosted because of the skyrmion-skyrmion magnetostatic repulsion (see Fig. 4c for an example of the spatial distribution of the skyrmions). A skyrmion gas is, therefore, formed, and each skyrmion further nucleated is immediately annihilated (see Supplementary Movie 8). This result paves the way to study the magnetic properties of skyrmion gas described theoretically in⁴⁷.

Discussion

In our study, we propose an SHO device geometry that, combining SHE and *i*-DMI, offers a unique opportunity to study nonreciprocal effects of spin-wave propagation in two dimensional systems and to observe a new type of dynamical spin-wave modes having a spiral spatial profile. This novel spin-wave mode originates from the gyrotropic rotation of a dynamical skyrmion. From the technological point of view, the proposed SHO geometry could be useful for the development of novel generators of short propagating spin-waves in future magnonic signal processing devices. From the fundamental point of view, it is also very interesting, as it allows to study the interaction of spin-wave and skyrmions, as well as to control the number of the nucleated skyrmions by applying a properly designed current pulse.

Methods

Micromagnetic framework. Micromagnetic simulations were carried out by means of a *state-of-the-art* parallel micromagnetic solver, which numerically integrates the LLG equation including the Slonczewski-like torque due to SHE^{48,20}:

$$\frac{d\mathbf{m}}{d\tau} = -\mathbf{m} \times \mathbf{h}_{\text{EFF}} + \alpha_G \mathbf{m} \times \frac{d\mathbf{m}}{d\tau} - \frac{g\mu_B}{2\gamma_0 e M_S^2 t_{\text{CoFe}}} \alpha_H \mathbf{m} \times \mathbf{m} \times (\hat{z} \times \mathbf{J}) \quad (4)$$

where \mathbf{m} and \mathbf{h}_{EFF} are the normalized magnetization and the effective field of the ferromagnet. The effective field includes the standard magnetic field contributions, as well as the *i*-DMI and Oersted field (see also Supplementary Note 1). τ is the dimensionless time $\tau = \gamma_0 M_S t$, where γ_0 is the gyromagnetic ratio, and M_S is the saturation magnetization of the ferromagnet. α_G is the Gilbert damping, g is the Landé factor, μ_B is the Bohr Magneton, e is the electron charge, t_{CoFe} is the thickness of the ferromagnetic layer, α_H is the spin-Hall angle obtained from the ratio between the spin current and the electrical current. \hat{z} is the unit vector of the out-of-plane direction and \mathbf{J} is the in-plane current density injected via the heavy metal. The *i*-DMI energetic density expression, as derived considering the ultra-thin film hypothesis ($\frac{\partial \mathbf{m}}{\partial z} = 0$), is $\varepsilon_{i\text{-DMI}} = D[m_z \nabla \cdot \mathbf{m} - (\mathbf{m} \cdot \nabla)m_z]$, D being the parameter taking into account the intensity of the DMI, and m_z is the z -component of the normalized magnetization. By making the functional derivative of equation, the normalized *i*-DMI effective field is given by:

$$\mathbf{h}_{i\text{-DMI}} = -\frac{1}{\mu_0 M_S^2} \frac{\delta \varepsilon_{i\text{-DMI}}}{\delta \mathbf{m}} = -\frac{2D}{\mu_0 M_S^2} [(\nabla \cdot \mathbf{m})\hat{z} - \nabla m_z] \quad (5)$$

The boundary conditions related to the interfacial DMI are expressed by $\frac{d\mathbf{m}}{dn} = \frac{1}{\xi} (\hat{z} \times \mathbf{n}) \times \mathbf{m}$ where \mathbf{n} is the unit vector normal to the edge and $\xi = \frac{2A}{D}$ (being A the exchange constant) is a characteristic length in the presence of *i*-DMI.

We have studied a bilayer system Pt(5 nm)/CoFe(1 nm) with a rectangular cross section of $1500 \times 3000 \text{ nm}^2$. The electric current was locally injected into the ferromagnet via a thick Au electrode (thickness of 150 nm) with two tips located at a distance d from each other. The charge current flowing in the Pt layer gives rise to the SHE and then, to flow of perpendicular (along the “ z ” axis) pure spin current at the Pt/CoFe interface creating an anti-damping Slonczewski-like torque in the ferromagnetic layer and excites in it persistent magnetization oscillations. For the results discussed in the main text, we have considered the following physical parameters of the SHO (Fig. 1a): saturation magnetization $M_S = 1 \times 10^6 \text{ A/m}$ ⁴⁹, exchange stiffness constant $A = 2.0 \times 10^{-11} \text{ J/m}$, interfacial perpendicular anisotropy induced at the boundary between CoFe and Pt characterized by the anisotropy constant $K_u = 5.5 \times 10^5 \text{ J/m}^3$ ⁵⁰, damping constant $\alpha_G = 0.03$ ⁵¹, and the spin-Hall angle $\alpha_H = 0.1$ ⁹. The ferromagnetic CoFe layer has an in-plane equilibrium magnetization at zero field which is directed along the y - in-plane direction due to the shape anisotropy of the ferromagnetic layer. The real spatial distributions of the density J_c of the charge current, density J_s of the spin current and the Oersted field were calculated numerically, as it is described in the Supplementary Note 1.

Derivation of analytical equations. The spin wave dispersion relation along the x -direction in the presence of *i*-DMI can be calculated analogously to ref. 12 and has the following form

$$\omega_k = \sqrt{(\omega_H + \omega_M \lambda^2 k_x^2)(\omega_H + \omega_M \lambda^2 k_x^2 + \omega_M(1 - H_{an}/M_S) \sin^2 \theta_M)} - \omega_M \tilde{D} k_x, \quad (6)$$

where $\omega_H = \gamma B_{\text{eff}}$, B_{eff} is the static effective field, $\omega_M = \gamma \mu_0 M_S$. In the range $\omega_M \lambda^2 k^2 \ll \omega_0$ it can be approximated as $\omega_k \approx \omega_0 + \omega_M \tilde{\lambda}^2 k_x^2 - \omega_M \tilde{D} k_x$, where $\omega_0 = \sqrt{\omega_H(\omega_H + \omega_M(1 - H_{an}/M_S) \sin^2 \theta_M)}$ is the angular frequency of the ferromagnetic resonance in the ferromagnetic layer, and $\tilde{\lambda}^2 = \lambda^2(2\omega_H + \omega_M(1 - H_{an}/M_S) \sin^2 \theta_M)/2\omega_0$.

Making a formal substitution $k_x \rightarrow -i(d/dx)$ in this dispersion equation, it is possible to obtain the following dynamical equation describing the spatial and temporal evolution of the spin wave complex amplitude a :

$$\frac{\partial a}{\partial t} = -i\omega a = -i \left(\omega_0 - \omega_M \tilde{\lambda}^2 \frac{\partial^2}{\partial x^2} + i\omega_M \tilde{D} \frac{\partial}{\partial x} \right) a - \alpha_G \omega a + \sigma J(x) a \quad (7)$$

The spin wave damping is accounted for by the term $\alpha_G \omega$ (spin wave ellipticity, which could modify the damping term⁵² in our case is small), while the influence of the spin current could be easily calculated from equation (4) within the framework of the perturbation theory⁵² and is given by the term $\sigma J(x)a$, with $\sigma = g\mu_B \alpha_H \sin \theta_M / (2eM_S t_{CoFe})$. Equation (3) for the threshold current can be obtained, analogously to ref. 13, by deriving general analytical solutions of equation (7) inside and outside the current-carrying region, and applying the boundary conditions of continuity for the spin wave complex amplitude a and its derivative. It is clear, that in the reciprocal case, when $k_x = -k_{+x}$, Eq. (3) is reduced to Eq. (6) from ref. 39.

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Author Contributions

A.G., R.Z., M.C., G.G. and G.F. initiated the work and designed the numerical experiments. R.V. and A.S. developed the analytical theory and performed the analytical calculations. A.L. performed the computation of the spatial distribution of the current density and the Oersted field and wrote the supplementary note 1. A.G. performed micromagnetic simulations supported by V.P., G.S., B.A. and M.C. V.P. wrote the supplementary note 2 and prepared the last version of the figures. A.G. and G.F. analyzed the data. G.F. wrote the paper with input from R.V., A.S. and R.T. All authors contributed to the general discussion of the results and commented on the manuscript.

Additional Information

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