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## Predicting Global Minimum in Complex Beryllium Borate System for Deep-ultraviolet Functional Optical Applications

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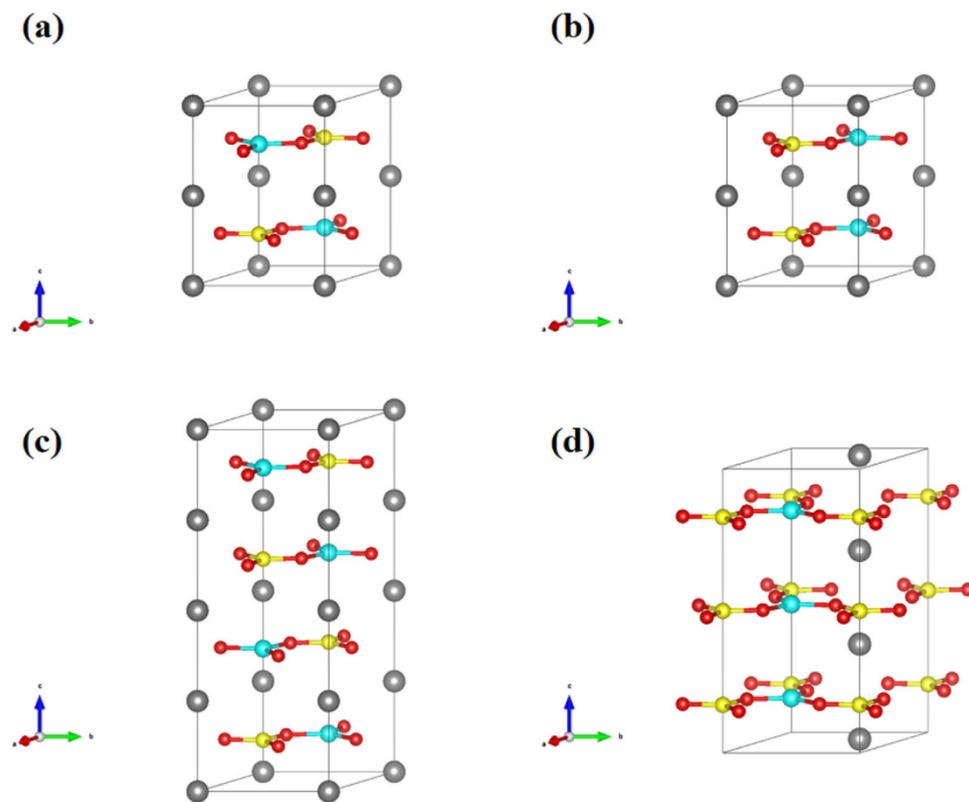
Searching for high performance materials for optical communication and laser industry in deep-ultraviolet (DUV) region has been the subject of considerable interest. Such materials by design from scratching on multi-component complex crystal systems are challenging. Here, we predict, through density function calculations and unbiased structure searching techniques, the formation of quaternary NaBeBO<sub>3</sub> compounds at ambient pressure. Among the four low-energy phases, the *P*<sub>6<sub>3</sub>/m structure exhibits a DUV cutoff edge of 20 nm shorter than α-BaB<sub>2</sub>O<sub>4</sub> (189 nm) – the best-known DUV birefringent material. While the *P*-6 structure exhibits one time second-harmonic generation efficiency of KH<sub>2</sub>PO<sub>4</sub> and possesses excellent crystal growth habit without showing any layer habit as observed in the only available DUV nonlinear optical material KBe<sub>2</sub>BO<sub>3</sub>F<sub>2</sub>, whose layer habit limits its wide industrial applications. These NaBeBO<sub>3</sub> structures are promising candidates for the next generation of DUV optical materials, and the structure prediction technique will shed light on future optical materials design.</sub>

Viable DUV (<200 nm) optical materials play a critical role in optical communication and the laser industry<sup>1–5</sup>, as they possess wide transparency range and high damage threshold<sup>6–10</sup>. Among them, birefringent or nonlinear optical (NLO) materials are utilized in polarization beam splitters, optical isolators, semiconductor photolithography and laser micromachining<sup>11–15</sup>. Only a few materials, such as α-BaB<sub>2</sub>O<sub>4</sub> (α-BBO)<sup>1,7,8</sup> and KBe<sub>2</sub>BO<sub>3</sub>F<sub>2</sub> (KBBF)<sup>16,17</sup>, can be practically used as birefringent or NLO materials in the DUV region. However, both α-BBO and KBBF do not have DUV commercial availability since α-BBO exhibits high UV cutoff edge (189 nm) and KBBF suffers from a strong layering tendency. As such, it is the subject of considerable interest to investigate DUV birefringent and NLO materials<sup>18–22</sup>. In the past few years, first principle calculations have been an efficient method to evaluate and verify the physical and chemical properties of optical materials<sup>23–25</sup>.

Theoretical search methods can be classified into three categories. The first method used to search optical crystal structure is atom/group/mixing-substitution<sup>26–28</sup>. It comes from the synthetic train of thought of the experimental scientists, and most structure searches of optical materials belong to this method. This method involves a mixing substitution wherein a hypothetical ABX<sub>n</sub> compound has A-site and B-site substitution in combination with BX<sub>n</sub> group rotation. The second method is high-throughput computational materials design<sup>29</sup> by analyzing and calculating large quantities of known candidate structures to discover useful material systems. This method requires a good descriptor that can rapidly characterize relative properties, through using this descriptor to search new materials in enormous data repositories. This method has been successfully used for mid-infrared NLO materials<sup>30</sup> and scintillators<sup>31,32</sup>.

Although the above two methods have offered some useful suggestions to experimental synthesis, they do not provide the lowest energy structures on the free energy surface for an undiscovered crystal structure, which are closely related to experimental results. Is there an efficient means to address this issue? The third method provides the suitable solution-crystal structure prediction, which aims at finding the global minimum on a potential

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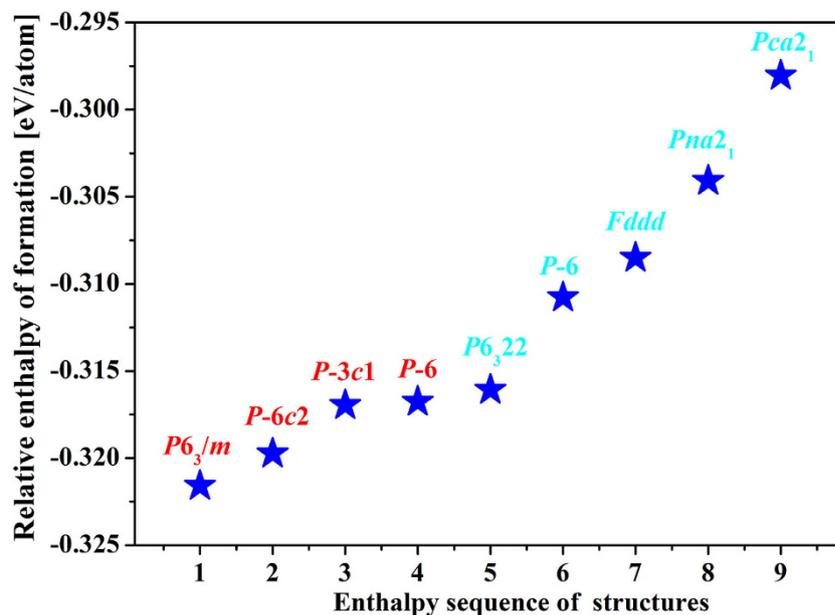
**Figure 1. Predicted structures of NaBeBO<sub>3</sub> at ambient pressure.** The gray, blue, yellow and red balls represent Na, Be, B and O atoms, respectively. (a) *P*6<sub>3</sub>/*m* structure. (b) *P*-6*c*2 structure. (c) *P*-3*c*1 structure. (d) *P*-6 structure. Structural details are given in the Supporting Information.

energy surface. Structure prediction has been widely applied in high pressure regimes<sup>33,34</sup>, material surface reconstruction<sup>35</sup> and cluster structure search<sup>36</sup>. However, owing to the complexities of optical material systems, which are always more than binary system, no functional optical material structure prediction has been reported.

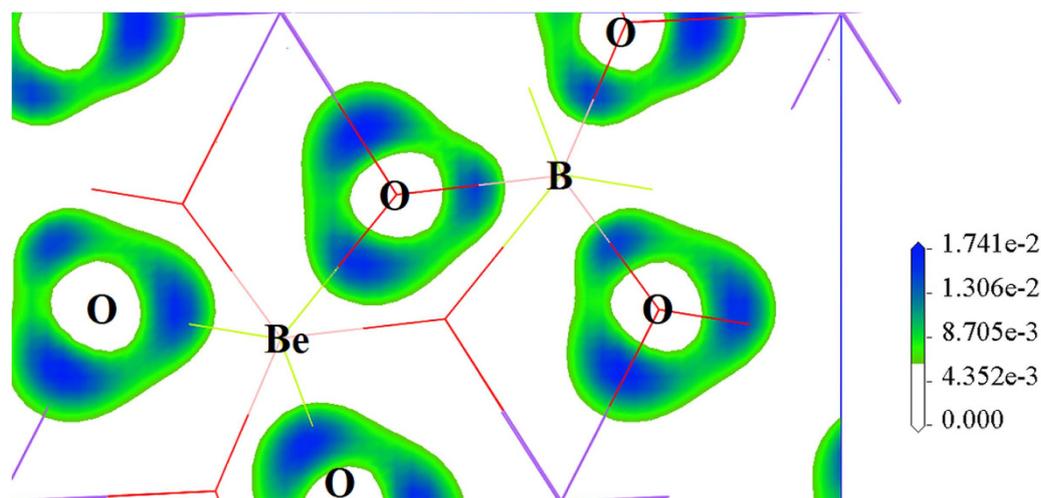
Here we first introduce a systematic global structure optimization method to develop the next generation of DUV optical materials in complex beryllium borate quaternary system that is attributable to its very short absorption edges. Through searching free energy surfaces (more than 40,000 structures) via the newly developed Artificial Bee Colony (ABC) algorithm as implemented in the CALYPSO (crystal structure analysis by particle swarm optimization) code<sup>37,38</sup>, we have extensively explored the stable phases of NaBeBO<sub>3</sub> at ambient pressure, and obtained a comprehensive set of structures for NaBeBO<sub>3</sub>. In particular, we have established for the first time the thermodynamically stable structures. In doing so, the first example of 3-fold coordinated Be atoms in borates is observed among the energetically favorable NaBeBO<sub>3</sub> structures. Equally important, the four lowest energy NaBeBO<sub>3</sub> structures possess superior linear and nonlinear optical properties, as well as good chemical stability. They are attractive candidates for the next generation of DUV birefringent or DUV NLO materials. Our studies also provide insights and a road map for exploring the design and synthetic strategies for NaBeBO<sub>3</sub>. Such research also offers a key route to structural determination of materials with specific functional optical properties.

## Results

**Crystal structures.** Structure predictions through the ABC technique in the CALYPSO code with simulation sizes up to six NaBeBO<sub>3</sub> formula units (f.u.) per simulation cell were performed twice at ambient pressure. The four structures with lowest energy were systematically studied, and the other five structures with higher energy are shown in Supplementary Fig. 1 and Supplementary Table 1. The four energetically favorable structures belong to hexagonal *P*6<sub>3</sub>/*m* (2f.u. per cell, Fig. 1a; Supplementary Table 1), hexagonal *P*-6*c*2 (2f.u. per cell, Fig. 1b; Supplementary Table 1), trigonal *P*-3*c*1 (4f.u. per cell, Fig. 1c; Supplementary Table 1) and hexagonal *P*-6 (3f.u. per cell, Fig. 1d; Supplementary Table 1) space group. Two of the energetically favored structures are non-centrosymmetric, i.e. hexagonal *P*-6*c*2 and *P*-6. In the four NaBeBO<sub>3</sub> structures, *P*6<sub>3</sub>/*m*, *P*-6*c*2, *P*-3*c*1 and *P*-6, the planar BeO<sub>3</sub> and the BO<sub>3</sub> units connect with each other through corner-sharing the O atoms to generate a (BeBO<sub>3</sub>)<sub>∞</sub> layer. This layer is perfectly parallel to the *ab* plane. One (BeBO<sub>3</sub>)<sub>∞</sub> layer links with an adjacent layer through six-coordinate Na atoms. As shown in Fig. 1(a–d), the difference of the NaBeBO<sub>3</sub> structures is the direction and position of the planar BeO<sub>3</sub> units and BO<sub>3</sub> units in the (BeBO<sub>3</sub>)<sub>∞</sub> layer. In addition, the Na–O, Be–O and B–O distances are in the range of 2.432–2.452, 1.543–1.547 and 1.384–1.386 Å, respectively. The O–B–O and O–Be–O angles are all 120° to make the planar BO<sub>3</sub> and BeO<sub>3</sub> units to be equilateral triangles. Intriguingly, to the



**Figure 2.** Relative enthalpies of formation per atom with respect to Na<sub>2</sub>O, B<sub>2</sub>O<sub>3</sub> and BeO for different NaBeBO<sub>3</sub> structures at ambient pressure.



**Figure 3.** Isosurface of ELF for (BeBO<sub>3</sub>)<sub>∞</sub> layer in *P6<sub>3</sub>/m* structure.

best of our knowledge, it is the first time to discover the 3-fold coordinated Be atoms in borates, similar to the Be atoms in Y<sub>2</sub>BeO<sub>4</sub> (ref. 39) and Rb<sub>2</sub>Be<sub>2</sub>Si<sub>2</sub>O<sub>7</sub><sup>40</sup>.

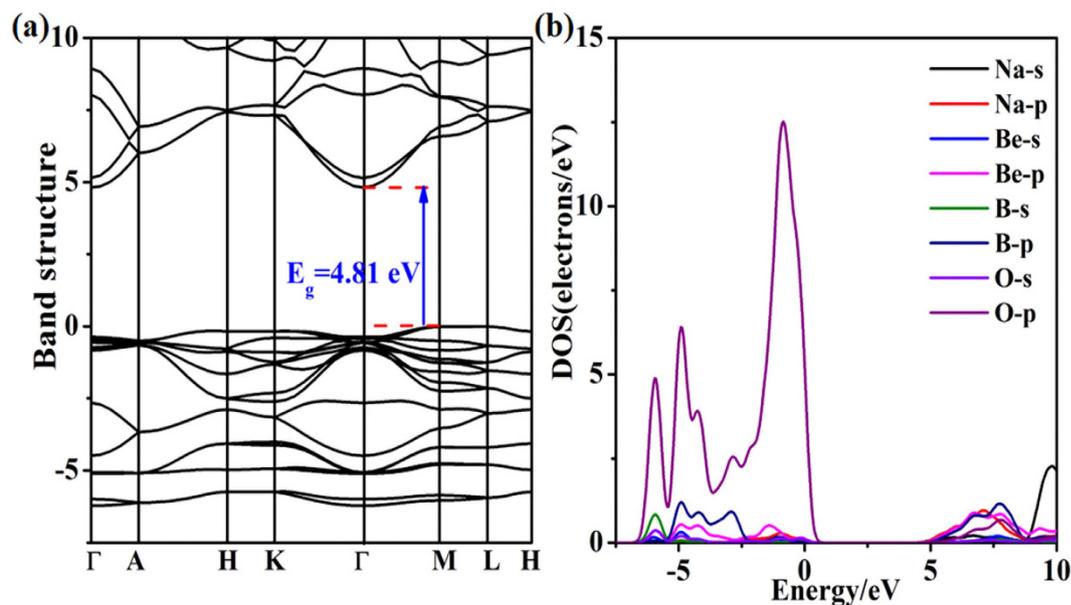
**Structural stability.** Formation enthalpies can be used to assess relative stability of crystalline compounds at low temperatures. The formation enthalpy for NaBeBO<sub>3</sub> can be defined as follows:

$$h_f(\text{NaBeBO}_3) = [2H(\text{NaBeBO}_3) - H(\text{Na}_2\text{O}) - H(\text{B}_2\text{O}_3) - 2H(\text{BeO})]/(2 \times 6),$$

where  $h_f$  is the enthalpy of formation per atom and  $H$  is the calculated enthalpy per chemical unit for each compound at ambient pressure, here, Na<sub>2</sub>O, B<sub>2</sub>O<sub>3</sub> and BeO are chosen as the reference structures attributed to their stability at ambient pressure. The formation enthalpies of the NaBeBO<sub>3</sub> phases, calculated at higher levels of accuracy, are plotted in Fig. 2. The phase with space group of *P6<sub>3</sub>/m* is the most stable structure with the formation enthalpy about -0.322 eV/atom, the remaining phases with space groups *P-6c2*, *P-3c1* and *P-6* have formation enthalpies of about 2 meV/atom, 5 meV/atom and 5 meV/atom higher than that of the *P6<sub>3</sub>/m* structure. The formation enthalpies (Supplementary Table 2) of several other reaction paths are also negative, these results indicate that the NaBeBO<sub>3</sub> structures might be experimentally synthesizable. The phonon calculations have also shown

Value atomic pair	Bond distances (Å)	Overlap populations (e)
Na-O	2.432–2.455	–0.03
B-O	1.384–1.386	0.87
Be-O	1.544–1.547	0.64

**Table 1.** Bond distances and Mulliken overlap populations for the characteristic atomic pairs in four lowest energy NaBeBO<sub>3</sub> structures.



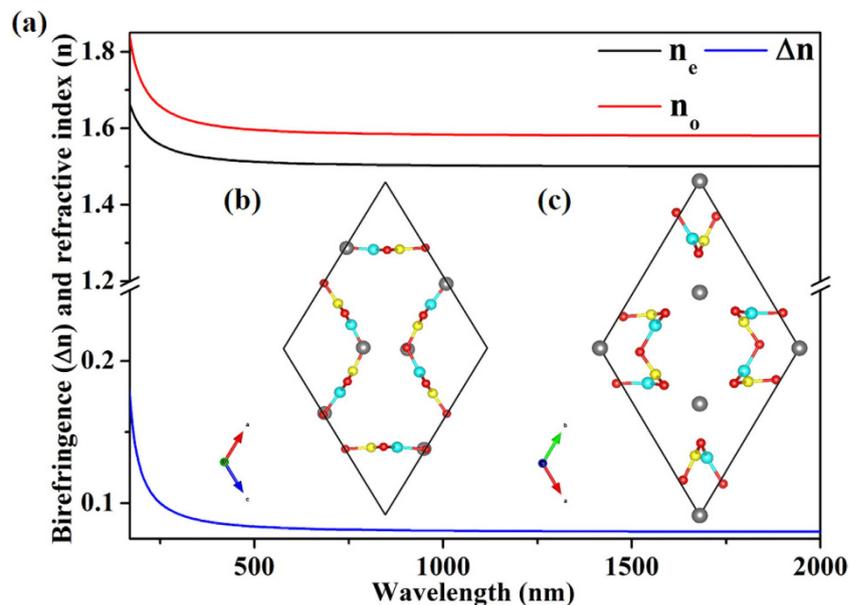
**Figure 4.** Band structure and density of states of  $P6_3/m$  structure.

that these structures are kinetically stable by reason that none of the imaginary phonon mode exists in the whole Brillouin Zone (Supplementary Fig. 2).

**Chemical bondings.** Owing to the unexpected discovery of the triangular BeO<sub>3</sub> units in NaBeBO<sub>3</sub>, a detailed bonding analysis was performed. The nature of this bonding was probed by calculating the electron localization functions (ELF) (Fig. 3; Supplementary Fig. 3), which is known to be an effective tool to distinguish different bonding interactions in solids<sup>41</sup>. In the NaBeBO<sub>3</sub> structures, the Na-O bonds are ionic, and the B-O bonds are covalent, that is in accordance with other borates. In particular, the Be atoms in the NaBeBO<sub>3</sub> structures are  $sp^2$  hybridized and form  $\sigma$  bonds with their neighboring O atoms. These Be-O bonds are reasonable that the Be-O distances (1.54–1.55 Å) are in the range of the reported Be-O  $\sigma$  bonds (1.51–1.87 Å) in Y<sub>2</sub>BeO<sub>4</sub> and Rb<sub>2</sub>Be<sub>2</sub>Si<sub>2</sub>O<sub>7</sub>. These conclusions are further substantiated by Mulliken population analysis<sup>42</sup> listed in Table 1, where the calculated overlap populations for Na-O, B-O and Be-O are 0.03, 0.87 and 0.64 e, respectively, indicating the ionic character of the Na-O bonds and the covalent nature of the B-O and Be-O bonds.

**Electronic structures.** The calculated electronic band structures (Fig. 4; Supplementary Fig. 4) for the NaBeBO<sub>3</sub> structures reveal that the phases with space groups  $P6_3/m$ ,  $P-6c2$ ,  $P-3c1$  and  $P-6$  are all indirect band gaps, which are 4.81, 4.80, 4.75 and 4.73 eV by the PBE functional and 7.32, 7.30, 7.25 and 7.24 eV by the PBE0 hybrid functional (Supplementary Fig. 5), respectively. The latter functional has been shown to be more precise for band gap calculations in borates<sup>43,44</sup>. Our calculated band gaps by the PBE0 hybrid functional are in good agreement with experimental and earlier theoretical predictions of sodium beryllium borates<sup>45</sup>.

Since the electronic transitions from occupied states to unoccupied states reveal the microcosmic origin of the optical properties, it is essential to analyze the partial density of states (PDOS) of the NaBeBO<sub>3</sub> structures in detail. The NaBeBO<sub>3</sub> structures have much similar electronic states distribution near the band gap. The top region of the valence band (VB) is mainly occupied by the 2s orbitals of the boron atoms and the 2p orbitals of the boron, beryllium and oxygen atoms. The B 2s, 2p states and the Be 2p states show a wide hybridization with O 2p states from –7 to 0 eV, indicating that the B-O and Be-O bonds, that belong to the (BeBO<sub>3</sub>)<sub>∞</sub> layers, make the main contribution to the top of the VB in the NaBeBO<sub>3</sub> structures. The bottom region of the conduction band (CB) is mainly occupied by the 2p states of Na, Be, B and O atoms. It is clear that the B-O and Be-O groups in the (BeBO<sub>3</sub>)<sub>∞</sub> layers are the main contributor to the optical properties. In addition, because of the small contribution of Na to the top of the VB and the bottom of the CB, its impact on the optical properties is negligible.



**Figure 5.** (a) Refractive indices and birefringence of  $P6_3/m$  structure. (b) The first simulated  $P6_3/m$  NaBeBO<sub>3</sub> structure. (c) The second simulated  $P6_3/m$  NaBeBO<sub>3</sub> structure. The gray, blue, yellow and red balls represent Na, Be, B and O atoms, respectively.

**Birefringent crystal material candidates.** The calculated refractive indices and birefringence of the NaBeBO<sub>3</sub> structures are shown in Fig. 5a and Supplementary Fig. 6. Because their point groups belong to hexagonal or trigonal crystal system, they are all uniaxial crystals with the birefringence values equal to  $|n_e - n_o|$ . The birefringence values of the phases with space groups  $P6_3/m$ ,  $P-6c2$ ,  $P-3c1$  and  $P-6$  are 0.0825, 0.083, 0.085 and 0.084 at 589.3 nm, respectively. Their large birefringence, which is related to their strong optical anisotropy, derives from the parallel arrangement of the  $(\text{BeBO}_3)_\infty$  layers. The calculated charge densities (Supplementary Fig. 7) show large electron density anisotropy for the  $(\text{BeBO}_3)_\infty$  layers, supporting our argument that the  $(\text{BeBO}_3)_\infty$  layers are the major contributors to the optical anisotropy.

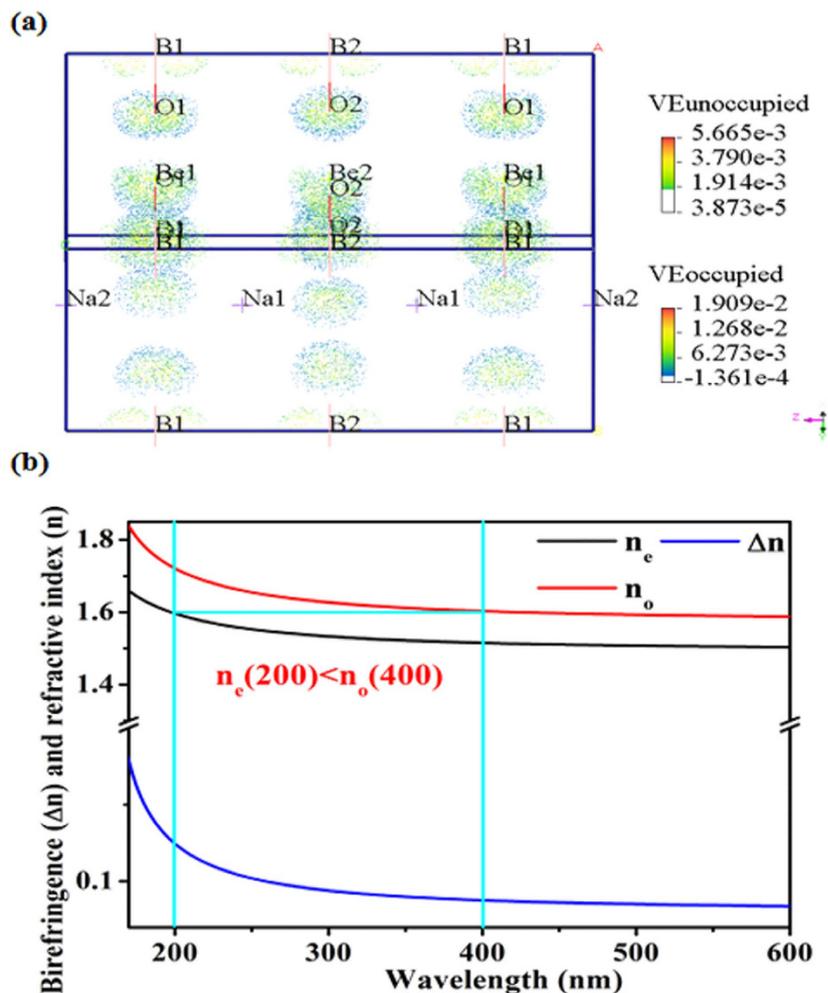
Interestingly, the NaBeBO<sub>3</sub> structures are the first kind of negative uniaxial borate crystal structure type to produce large birefringence summarized by us<sup>46</sup>, that is effectively fundamental building units in a parallel arrangement with a high number density. To further verify this conclusion, two simulated NaBeBO<sub>3</sub> structures with space group  $P6_3/m$  (Fig. 5b,c; Supplementary Table 3), that belong to the second kind of positive uniaxial borate crystal structure type to induce large birefringence, are chosen to investigate the optical anisotropy. In the two simulated NaBeBO<sub>3</sub> structures, the planar  $\text{BO}_3$  and  $\text{BeO}_3$  groups form equilateral triangle arrangements and are parallel to the b or c axis. The birefringence values ( $\Delta n = n_e - n_o$ ; Supplementary Fig. 8) of the simulated structures are 0.0850 and 0.0813 at 589.3 nm, respectively. The large birefringence values of the phases with space group  $P6_3/m$  and two other simulated  $P6_3/m$  structures well validate the two large birefringence structure type in uniaxial borates.

The UV cutoff edges of the phases with space groups  $P6_3/m$ ,  $P-6c2$ ,  $P-3c1$  and  $P-6$  are 169.4 (7.32 eV), 169.9 (7.30 eV), 171.0 (7.25 eV) and 171.2 nm (7.24 eV) respectively, which are 20, 20, 18 and 18 nm shorter than that of  $\alpha$ -BBO (189 nm). That is to say, these compounds have large birefringence and short deep UV cutoff edges, which demonstrate that they are excellent candidates for birefringent materials.

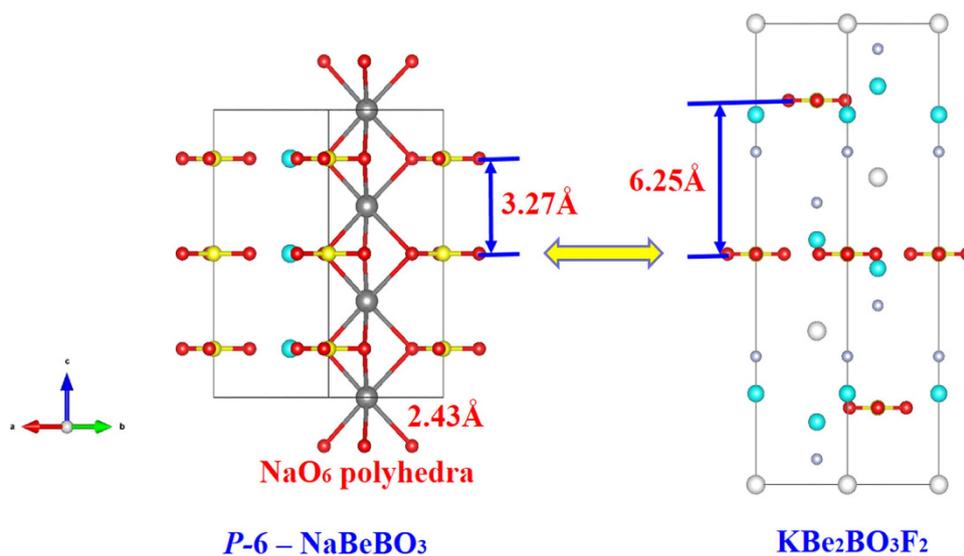
**Nonlinear optical material candidates.** The second-harmonic generation (SHG) effects are estimated owing to the absence of inversion symmetry in the phases with space groups  $P-6c2$  and the  $P-6$ . The calculated SHG coefficients are  $d_{21} = -d_{22} = d_{16} = -0.07$  pm/V for the  $P-6c2$  structure, which is only 1/5 times that of  $\text{KH}_2\text{PO}_4$  (KDP,  $d_{36} = 0.39$  pm/V). For the  $P-6$  structure, the coefficients are  $d_{11} = -d_{12} = -d_{26} = 0.07$  pm/V and  $d_{22} = -d_{21} = d_{16} = -0.40$  pm/V, the  $d_{22}$  coefficient contributes to the effective SHG coefficients ( $\Phi = 90^\circ$  for type-I phase matching), that is equivalent to that of KDP. The SHG-weighted electron densities (Fig. 6a; Supplementary Fig. 9), where only the virtual-electron attributed to its large contribution (more than 90%), indicate that the  $\text{BeO}_3$  and  $\text{BO}_3$  groups are mainly responsible for second-order NLO effects.

A marked difference in the SHG response is found in the  $P-6c2$  and the  $P-6$  structures. Their structures are similar that the  $\text{BO}_3$  and the  $\text{BeO}_3$  units in adjacent  $(\text{BeBO}_3)_\infty$  layers are almost in opposite directions, that is considered to weaken the SHG effects. Then what is the key to the notable SHG difference? The answer is the number of  $(\text{BeBO}_3)_\infty$  layers in the primitive cell, the  $P-6c2$  phase has two  $(\text{BeBO}_3)_\infty$  layers, whereas the  $P-6$  phase has three  $(\text{BeBO}_3)_\infty$  layers. As no additional layer counteracts the third layer's SHG effect, the  $P-6$  phase exhibits superior NLO properties to the  $P-6c2$  phase.

In negative uniaxial crystal, the SHG phase-matching condition can be summarized as follows:  $n_e(\lambda/2) \leq n_o(\lambda)$ , where  $n_e(\lambda/2)$  and  $n_o(\lambda)$  are the corresponding refractive index at the SHG and fundamental



**Figure 6.** (a) Occupied states and unoccupied states in the  $d_{22}$  SHG-densities of the P-6 structure in the VE process. (b) Refractive indices and birefringence of P-6 structure, and the phase-matching capabilities for P-6 at 400 nm. In negative uniaxial crystal, the  $n_e$  at 200 nm located between the  $n_e$  and  $n_o$  refractive index at 400 nm indicates the achievement of the phase-matching condition.



**Figure 7.** The interlayer spacing of the P-6 NaBeBO<sub>3</sub> (left) and KBe<sub>2</sub>BO<sub>3</sub>F<sub>2</sub> structure (right). The NaO<sub>6</sub> polyhedra between the (BeBO<sub>3</sub>)<sub>∞</sub> layers in P-6 NaBeBO<sub>3</sub> structure are plotted in the left. The gray, blue, yellow, red, white and light gray balls represent Na, Be, B, O, K and F atoms, respectively.

wavelengths, respectively. The calculated refractive index (Fig. 6b; Supplementary Fig. 10) reveals that in the *P-6c2* and the *P-6* phases  $n_e(200\text{ nm}) < n_o(400\text{ nm})$ , indicating that these two NaBeBO<sub>3</sub> structures achieve the SHG phase-matching condition in the DUV region. The shortest SHG wavelengths for the *P-6c2* and *P-6* are all about 195 nm.

Equally important, good crystal growth habit is essential to DUV functional optical material. It is well known that KBBF is the only material to generate coherent light in the DUV region by direct SHG response, whereas its layer habit seriously impedes its commercialization. The interlayer spacing of the *P-6c2* and *P-6* phases (about 3.27 Å; Fig. 7) is 2.98 Å shorter than that of KBBF (6.25 Å). Their adjacent (BeBO<sub>3</sub>)<sub>∞</sub> layers are connected by the NaO<sub>6</sub> polyhedra (about 2.43 Å), whose interlayer binding forces far outweigh that of KBBF. This confirms the reduction of layering tendency in *P-6c2* and *P-6*.

## Discussion

By using the newly developed ABC structure searching algorithm and density functional total energy calculations, we systematically studied the possible existing phases of the NaBeBO<sub>3</sub> quaternary compound at ambient pressure. The *sp*<sup>2</sup> hybrid 3-fold coordinated Be atoms, which are never found in borates before, are discovered in four lowest energy NaBeBO<sub>3</sub> structures. More importantly, the four lowest energy NaBeBO<sub>3</sub> structures have short DUV cutoff edges about 170 nm and reduce the layer habit, and they exhibit extraordinary optical properties. The large birefringence values show that the NaBeBO<sub>3</sub> structures are excellent candidates for DUV birefringent materials. The electronic structures and the SHG-weighted electron densities clearly show that the parallel (BeBO<sub>3</sub>)<sub>∞</sub> layers are the main origin of the optical properties in these energetic favorable NaBeBO<sub>3</sub> structures. On the whole, the *P-6* phase exhibits a short UV cutoff edge of 171 nm (7.24 eV), a good SHG efficiency about one time that of KH<sub>2</sub>PO<sub>4</sub>, and is capable of being phase-matchable in the DUV region. Importantly, it mitigates the layering tendency as observed in KBBF. All these facts demonstrate that NaBeBO<sub>3</sub> with *P-6* space group is a promising DUV NLO material. In summary, this work represents a significant step forward in predicting global optimization structures of complex crystal system, and also provides a successful manner to search for the next generation of DUV functional optical materials.

## Methods

Before exploring the title compound, several known functional optical materials were predicted in the same manner. The experimental structures of KBe<sub>2</sub>BO<sub>3</sub>F<sub>2</sub><sup>47</sup>, BPO<sub>4</sub><sup>48</sup>, AgGaS<sub>2</sub><sup>49</sup>, ZnGeP<sub>2</sub> (ref. 50) were all successfully reproduced at ambient pressure through ABC technique, validating our methodology in application to functional optical materials. The results are listed in Supplementary Fig. 11 and Supplementary Table 4.

**Crystal structure prediction.** We obtain candidate structures of NaBeBO<sub>3</sub> by using swarm-intelligence CALYPSO (Crystal structure ANALysis by Particle Swarm Optimization) structure searching simulations unbiased by any prior known structure knowledge and in conjunction with first-principles density functional calculations. The artificial bee colony (ABC) algorithm, which is originally attributed to Karaboga *et al.*<sup>51</sup>, with symmetry constraint is implemented into CALYPSO software to keep the structural symmetry during structure evolution. The remarkable feature of this methodology is the capability of predicting stable structure with the only knowledge of the chemical composition.

We searched for structures of NaBeBO<sub>3</sub> with simulation cell sizes of 1–6 formula units (f.u.) at ambient pressures using the CALYPSO package<sup>52</sup>. The local structural relaxations calculations were performed in the framework of density functional theory, using the generalized gradient approximation<sup>53</sup> within the Perdew–Burke–Ernzerhof exchange functional theory<sup>54</sup>, and the frozen-core projector-augmented wave (PAW) method as implemented in the VASP code<sup>55</sup>. The adopted PAW pseudopotentials of Na, Be, B and O treat 3s<sup>1</sup>, 2s<sup>2</sup>, 2s<sup>2</sup>2p<sup>1</sup> and 2s<sup>2</sup>2p<sup>4</sup> electrons as valence. The cutoff energy 900 eV and appropriate Monkhorst–Pack *k*-meshes were chosen to ensure that all enthalpy calculations were well converged to better than 1 meV/atom. The phonon calculations have been carried out by using a supercell approach as implemented in the PHONOPY code<sup>56</sup>. More computational details can be found in the Supplementary Information.

**Properties calculation.** After ranking the enthalpy order of the NaBeBO<sub>3</sub> structures, the electronic band structure, DOS and optical property calculations of the four low enthalpy structures were performed within the framework of DFT within the generalized gradient approximation (GGA) in the scheme of Perdew–Burke–Ernzerhof<sup>54</sup>, as implemented by CASTEP code<sup>57</sup>. The norm-conserving pseudopotentials used treat 2s<sup>2</sup>2p<sup>6</sup>3s<sup>1</sup>, 2s<sup>2</sup>, 2s<sup>2</sup>2p<sup>1</sup> and 2s<sup>2</sup>2p<sup>4</sup> as valence electrons for Na, Be, B and O atoms, respectively. The cutoff energy 810 eV and Monkhorst–Pack *k* point meshes with a grid of 0.025 Å<sup>-1</sup> for Brillouin zone sampling were chosen to achieve a well-converged electronic structure and optical properties.

PBE0 hybrid functional<sup>58</sup> was used to calculate the band structures. The calculation of optical properties was scissor corrected by the calculated energy gap difference between the PBE and the PBE0, the scissor operators of the four lowest energy structures are 2.51 eV (*P6<sub>3</sub>/m*), 2.50 eV (*P-6c2*), 2.50 eV (*P-3c1*) and 2.50 eV (*P-6*). The SHG-weighted electron densities analysis<sup>59</sup> was used to analyze NLO response of the NaBeBO<sub>3</sub> structures. The theoretical methods were applied with success in a previous study to analyze the SHG coefficients of the NLO crystals<sup>60</sup>.

## References

1. Cyranoski, D. Materials science: China's crystal cache. *Nature* **457**, 953–955 (2009).
2. Li, R. K. & Ma, Y. Y. Chemical engineering of a birefringent crystal transparent in the deep UV range. *CrystEngComm* **14**, 5421–5424 (2012).
3. Becker, P. Borate materials in nonlinear optics. *Adv. Mater.* **10**, 979–991 (1998).

4. Wang, Y. & Pan, S. L. Recent development of metal borate halides: Crystal chemistry and application in second-order NLO materials. *Coord. Chem. Rev.* doi: 10.1016/j.ccr.2015.12.008 (2016).
5. Yu, H. W., Zhang, W. G., Young, J., Rondinelli, J. M. & Halasyamani, P. S. Design and synthesis of the beryllium-free deep-ultraviolet nonlinear optical material  $\text{Ba}_3(\text{ZnB}_2\text{O}_{10})\text{PO}_4$ . *Adv. Mater.* **27**, 7380–7385 (2015).
6. Zhang, H. *et al.*  $\text{Na}_3\text{Ba}_2(\text{B}_3\text{O}_6)_2\text{F}$ : Next generation of deep-ultraviolet birefringent materials. *Cryst. Growth Des.* **15**, 523–529 (2015).
7. Appel, R., Dyer, C. D. & Lockwood, J. N. Design of a broadband UV-visible alpha-barium borate polarizer. *Appl. Opt.* **41**, 2470–2480 (2002).
8. Zhou, G. Q. *et al.* Growth and spectrum of a novel birefringent  $\alpha$ - $\text{BaB}_2\text{O}_4$  crystal. *J. Cryst. Growth* **191**, 517–519 (1998).
9. Zhao, S. G. *et al.* Beryllium-free  $\text{Li}_2\text{Sr}(\text{BO}_3)_2$  for deep-ultraviolet nonlinear optical applications. *Nat. Commun.* **5**, 4019 (2014).
10. Wang, S. C. & Ye, N.  $\text{Na}_2\text{CsBe}_6\text{B}_5\text{O}_{15}$ : An alkaline beryllium borate as deep UV nonlinear optical crystal. *J. Am. Chem. Soc.* **133**, 11458–11461 (2011).
11. Ghosh, S. *et al.* Enhancement of spin coherence using Q-factor engineering in semiconductor microdisc lasers. *Nat. Mater.* **5**, 261–264 (2006).
12. Nomura, N. *et al.* Polarimetry of illumination for 193 nm immersion lithography. *Microelectron. Eng.* **85**, 1671–1675 (2008).
13. Lin, H., Chen, L., Zhou, L. J. & Wu, L. M. Functionalization based on the substitutional flexibility: strong middle IR nonlinear optical selenides  $\text{AX}^{\text{II}}\text{X}^{\text{III}}\text{Se}_{12}$ . *J. Am. Chem. Soc.* **135**, 12914–12921 (2013).
14. Chen, C. T. *et al.* Design and synthesis of an ultraviolet-transparent nonlinear-optical crystal  $\text{Sr}_2\text{Be}_2\text{B}_2\text{O}_7$ . *Nature* **373**, 322–324 (1995).
15. Huang, H. W. *et al.*  $\text{NaSr}_3\text{Be}_3\text{B}_3\text{O}_9\text{F}_4$ : a promising deep-ultraviolet nonlinear optical material resulting from the cooperative alignment of the  $[\text{Be}_3\text{B}_3\text{O}_{12}\text{F}]^{10-}$  anionic group. *Angew. Chem. Int. Ed.* **50**, 9141–9144 (2011).
16. Chen, C. T. *et al.* Second-harmonic generation from a  $\text{KBe}_2\text{BO}_3\text{F}_2$  crystal in the deep ultraviolet. *Opt. Lett.* **27**, 637–639 (2002).
17. Xia, Y. N., Chen, C. T., Tang, D. Y. & Wu, B. C. New nonlinear-optical crystals for UV and VUV harmonic-generation. *Adv. Mater.* **7**, 79–81 (1995).
18. Yu, H. W. *et al.*  $\text{Cs}_3\text{Zn}_6\text{B}_9\text{O}_{21}$ : A new member in the KBBF family without layer habits yet exhibiting the largest second harmonic generation response. *J. Am. Chem. Soc.* **136**, 1264–1267 (2014).
19. Chung, I. *et al.* Helical polymer  $^{1/3}[\text{P}_2\text{Se}_6^{2-}]$ : strong second harmonic generation response and phase-change properties of its K and Rb salts. *J. Am. Chem. Soc.* **129**, 14996–15006 (2007).
20. Peng, Q. J. *et al.* Progress on all solid state deep-ultraviolet laser with  $\text{KBe}_2\text{BO}_3\text{F}_2$  crystal. *Rev. Laser Eng.* **36**, 1094–1097 (2008).
21. Kang, L. *et al.* Prospects for fluoride carbonate nonlinear optical crystals in the UV and deep-UV regions. *J. Phys. Chem. C* **117**, 25684–25692 (2013).
22. Tran, T. T., He, J., Rondinelli, J. M. & Halasyamani, P. S.  $\text{RbMgCO}_3\text{F}$ : A new beryllium-free deep-ultraviolet nonlinear optical material. *J. Am. Chem. Soc.* **137**, 10504–10507 (2015).
23. Zhao, S. G. *et al.* Beryllium-free  $\text{Rb}_2\text{Al}_3\text{B}_3\text{O}_{10}\text{F}$  with reinforced interlayer bonding as a deep-ultraviolet nonlinear optical crystal. *J. Am. Chem. Soc.* **137**, 2207–2210 (2015).
24. Lin, J., Lee, M. H., Liu, Z. P., Chen, C. T. & Pickard, C. J. Mechanism for linear and nonlinear optical effects in  $\beta$ - $\text{BaB}_2\text{O}_4$  crystals. *Phys. Rev. B* **60**, 13380–13389 (1999).
25. Lee, M. H., Wang, C. H. & Jan, J. H. Band-resolved analysis of nonlinear optical properties of crystalline and molecular materials. *Phys. Rev. B* **70**, 235110.1–235110.11 (2004).
26. Kang, L., Lin, Z. S., Qin, J. G. & Chen, C. T. Two novel nonlinear optical carbonates in the deep-ultraviolet region:  $\text{KBeCO}_3\text{F}$  and  $\text{RbAlCO}_3\text{F}_2$ . *Sci. Rep.* **3**, 1366–1366 (2012).
27. Kang, L. *et al.* First-principles design of a deep-ultraviolet nonlinear-optical crystal from  $\text{KBe}_2\text{BO}_3\text{F}_2$  to  $\text{NH}_4\text{Be}_2\text{BO}_3\text{F}_2$ . *Inorg. Chem.* **54**, 10533–10535 (2015).
28. Young, J., Lalkiya, P. & Rondinelli, J. M. Design of noncentrosymmetric perovskites from centric and acentric basic building units. *J. Mater. Chem. C* **4**, 4016–4027 (2016).
29. Curtarolo, S. *et al.* The high-throughput highway to computational materials design. *Nature Mater.* **12**, 191–201 (2013).
30. Kang, L. *et al.* Metal thiophosphates with good mid-infrared nonlinear optical performances: A first-principles prediction and analysis. *J. Am. Chem. Soc.* **137**, 13049–13059 (2015).
31. Ortiz, C., Eriksson, O. & Klintonberg, M. Data mining and accelerated electronic structure theory as a tool in the search for new functional materials. *Comp. Mater. Sci.* **44**, 1042–1049 (2009).
32. Klintonberg, M. *The Electronic Structure Project*; <http://gurka.fysik.uu.se/esp-fs/>
33. Miao, M. S. Caesium in high oxidation states and as a p-block element. *Nature Chem.* **5**, 846–852 (2013).
34. Ma, Y. M. *et al.* Transparent dense sodium. *Nature* **458**, 182–185 (2009).
35. Lu, S. H. *et al.* Self-assembled ultrathin nanotubes on diamond (100) surface. *Nat. Commun.* **5**, 3666 (2014).
36. Lv, J., Wang, Y. C., Zhu, L. & Ma, Y. M. Particle-swarm structure prediction on clusters. *J. Chem. Phys.* **137**, 084104 (2012).
37. Wang, Y. C., Lv, J., Zhu, L. & Ma, Y. M. Crystal structure prediction via particle swarm optimization. *Phys. Rev. B* **82**, 094116 (2010).
38. Wang, Y. C., Lv, J., Zhu, L. & Ma, Y. M. CALYPSO: a method for crystal structure prediction. *Comput. Phys. Commun.* **183**, 2063–2070 (2012).
39. Buerger, M. J. & Venkatakrishnan, V. Crystals with the warwickite structure. *Mater. Res. Bull.* **7**, 1201–1207 (1972).
40. Howie, R. A. & West, A. R. The crystal structure of  $\text{Rb}_2\text{Be}_2\text{Si}_2\text{O}_7$ . *Acta. Cryst. B*, **33**, 381–385 (1977).
41. Savin, A., Nesper, R., Wengert, S. & Fasler, T. F. ELF: The electron localization function. *Angew. Chem. Int. Ed. Engl.* **36**, 1808–1832 (1997).
42. Mulliken, R. S. Electronic population analysis on LCAO–MO molecular wave functions. I. *J. Chem. Phys.* **23**, 1833 (1955).
43. Jiang, X. X. *et al.* Development of nonlinear optical materials promoted by density functional theory simulations. *Int. J. Mod. Phys. B* **28**, 1430018 (2014).
44. Lin, Z. S. *et al.* Strategy for the optical property studies in ultraviolet nonlinear optical crystals from density functional theory. *Comp. Mater. Sci.* **60**, 99–104 (2012).
45. Jiang, X. X. *et al.* First-principles evaluation of the alkali and/or alkaline earth beryllium borates in deep ultraviolet nonlinear optical applications. *ACS Photonics* **2**, 1183–1191 (2015).
46. Bian, Q. *et al.* First principle assisted prediction of the birefringence values of functional inorganic borate materials. *J. Phys. Chem. C* **118**, 25651–25657 (2014).
47. Ye, N. & Tang, D. Hydrothermal growth of  $\text{KBe}_2\text{BO}_3\text{F}_2$  crystals. *J. Cryst. Growth* **293**, 233–235 (2006).
48. Schmidt, M. *et al.* Growth and characterization of  $\text{BPO}_4$  single crystals. *Z. Anorg. Allg. Chem.* **630**, 655–662 (2004).
49. Chahed, A., Benhelal, O., Rozale, H., Laksari, S. & Abbouni, N. Structural and electronic properties of chalcopyrite semiconductors  $\text{AgXY}_2$  (X = In, Ga; Y = S, Se, Te) under pressure. *Phys. Status Solidi B* **244**, 629–634 (2007).
50. Continenza, A. *et al.* Structural and electronic properties of narrow-gap  $\text{ABC}_2$  chalcopyrite semiconductors. *Phys. Rev. B* **46**, 10070 (1992).
51. Karaboga, D. & Akay, B. A comparative study of artificial bee colony algorithm. *Appl. Math. Comp.* **214**, 108–132 (2009).
52. Ma, Y. M., Wang, Y. C., Lv, J. & Zhu, L. CALYPSO code, <http://www.calypso.cn>.
53. Perdew, J. P. & Wang, Y. Accurate and simple analytic representation of the electron-gas correlation energy. *Phys. Rev. B* **45**, 13244 (1992).
54. Perdew, J. P., Burke, K. & Ernzerhof, M. Generalized gradient approximation made simple. *Phys. Rev. Lett.* **77**, 3865–3868 (1996).

55. Kresse, G. & Furthmüller, J. Efficient iterative schemes for *ab initio* total-energy calculations using a plane-wave basis set. *Phys. Rev. B* **54**, 11169–11186 (1996).
56. Togo, A., Oba, F. & Tanaka, I. First-principles calculations of the ferroelastic transition between rutile-type and CaCl<sub>2</sub>-type SiO<sub>2</sub> at high pressures. *Phys. Rev. B* **78**, 134106 (2008).
57. Clark, S. J. *et al.* First principles methods using CASTEP. *Z. Kristallogr.* **220**, 567–570 (2005).
58. Ernzerhof, M. & Scuseria, G. E. Assessment of the Perdew–Burke–Ernzerhof exchange–correlation functional. *J. Chem. Phys.* **110**, 5029–5036 (1999).
59. Huang, H., Lin, Z. S., Bai, L., Hu, Z. G. & Chen, C. T. *Ab initio* calculations on the borate nonlinear optical crystal BaAlBO<sub>3</sub>F<sub>2</sub>. *J. Appl. Phys.* **106**, 103107 (2009).
60. Lin, Z. S. *et al.* First-principles materials applications and design of nonlinear optical crystals. *J. Phys. D: Appl. Phys.* **47**, 253001 (2014).

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## Author Contributions

Z.Y. and S.P. designed the research. Q.B. and Z.Y. did the calculations. Q.B., Z.Y., S.P., Y.W. and C.C. analyzed the data. Q.B., Z.Y. and S.P. wrote the paper. All authors commented on the manuscript.

## Additional Information

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