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Effect of step frequency on leg stiffness during running in unilateral transfemoral amputees

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Spring-like leg behavior is a general feature of mammalian bouncing gaits, such as running and hopping. Although increases in step frequency at a given running speed are known to increase the stiffness of the leg spring (k_{leg}) in non-amputees, little is known about stiffness regulation in unilateral transfemoral amputees. In this study, we investigated stiffness regulation at different step frequencies at a given running speed in unilateral transfemoral amputees. We recruited nine unilateral transfemoral amputees wearing running-specific prostheses. They were asked to perform the action of running across a range of step frequencies (± 20 , ± 15 , ± 10 , ± 5 , and 0% of their preferred step frequency) at a given speed on an instrumented treadmill. The k_{leg} values were calculated using ground reaction force data in both the affected and unaffected limbs. It was found that k_{leg} increased with increasing step frequency for the unaffected limb, but not for the affected limb. Consequently, the unilateral transfemoral amputees attained the desired step frequency in the unaffected limb, but were unable to match the three highest step frequencies using their affected limbs. These results suggest that the stiffness regulation strategy during running differs between the affected and unaffected limbs.

The spring–mass model is widely used to quantify spring-like leg functions in mammalian bouncing gaits, such as hopping and running (Fig. 1)^{1–3}. The model consists of the subject's body mass and a massless linear leg spring. In the model, the stiffness of the leg spring (leg stiffness; k_{leg}) has been shown to change depending on the demand. For example, k_{leg} is invariant over a wide range of running speeds², but is increased with step frequency at a given running speed⁴. As reported in previous studies, humans increase k_{leg} to accommodate increases in step frequencies (f_{step}) during running at a given speed^{4–6}. Further, humans offset the increased k_{leg} in the mechanical behavior of the spring–mass system by decreasing the angle swept by the leg spring (θ) at a higher f_{step}^4 . As a result, the vertical stiffness of the spring–mass system (k_{vert}) increases, the vertical displacement of the center of mass (COM) during the ground contact time (t_c) decreases, and the system bounces off the ground in less time as f_{step} is increased⁴. Because spring-like leg behavior is a general feature of mammalians bouncing gaits, an improved understanding of the frequency-dependent modulation of leg stiffness regulation will provide insight into the neuromechanical principles of legged locomotion in humans.

The use of carbon-fiber running-specific prostheses (RSPs) have allowed lower-extremity amputees to regain running ability by providing spring-like leg function in the affected limb. Stiffness regulation during running across a range of f_{step} has been examined in unilateral transtibial amputees, where k_{leg} was increased in the unaffected limb but was unchanged in the affected limb⁷. However, little is known about stiffness regulation over a wide range of f_{step} during running in unilateral transfemoral amputees (TFAs). Because f_{step} is associated with running velocity, physiological responses, and potential injury risks^{8–10}, knowledge of how unilateral TFAs adjust stance leg mechanics for increasing f_{step} at a given running velocity may help in developing effective running-gait rehabilitation and individualized specifications of RSPs. Therefore, this study investigated stiffness regulation during running at different f_{step} values at a given running speed in unilateral TFAs wearing RSPs.

A recent finding showed that an athlete with unilateral transtibial amputation was unable to match relatively lower and higher hopping frequencies as a consequence of the invariant leg spring stiffness of the affected limb during one-legged hopping¹¹. Further, in unilateral transtibial amputees, Oudenhoven *et al.* demonstrated that k_{leg} of the affected limb did not change across a range of f_{step} at a given running speed⁷. Because both the biological

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Figure 1. Spring–mass model for running. The leg spring is compressed during the first half of the stance phase and rebounds during the second half. The maximal vertical displacement of the center of mass and the leg spring compression during ground contact are represented by Δy and ΔL , respectively. Half of the angle swept by the leg spring during the ground contact is denoted by θ .



COM displacement (m)

Figure 2. Time-normalized vGRF–COM displacement curves during ground contact while running at -20% to +20% of the preferred step frequency (0%). Black and gray curves indicate the unaffected and affected limb, respectively, recorded for one subject. The leg is compressed from the landing, and the vGRF is increased with COM displacement. The vGRF peaks at the midstance, and subsequently, the GRF decreases with the extension of the leg until take-off. The direction of the force–COM displacement curves is counter-clockwise in all conditions. The slopes (dotted lines) of these curves represent the vertical stiffness (k_{vert}). k_{vert} is the slope of the vGRF–COM displacement curve in the leg compression phase.

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knee and ankle joints are missing in the affected limbs, the asymmetric adjustment of spring-like leg behavior is likely to be retained in unilateral TFAs. Thus, it was hypothesized that k_{leg} of unilateral TFAs would differ between the affected and unaffected limbs over a wide f_{step} range at a given running speed.

Results

Vertical ground reaction force–center-of-mass displacement curves. Figure 2 depicts a typical example of the relationship between the vertical ground reaction force (vGRF) and center-of-mass (COM) displacement curves (recorded from one subject) during running in the range of -20% to +20% of the subject's preferred f_{step} . Both legs are compressed at touchdown, and vGRF is increased with COM displacement. The vGRF peaks at midstance, and subsequently, the vGRF decreases with the extension of the leg until take-off.

Actual step frequency. First, we determined the actual step frequency (f_{actual}), which is defined as the inverse of the time from touchdown to contralateral touchdown. On average, the unaffected limb could match the metronome frequency within 3% at all designated values of f_{step} . The affected limb could match the designated metronome frequency from -20% to +5% within the 3% criteria, but not at the three highest frequencies (+10%, +15%, and +20%), at which the actual step frequency (f_{actual}) of the affected limb was lower than the designated frequency. We found a significant main effect of f_{step} on f_{actual} , but no significant main effect of limb (Table 1). We also observed a significant interaction effect of f_{step} and limb on f_{actual} (Table 1). Simple main effects demonstrated that f_{actual} was significantly increased as f_{step} increased in both the affected and unaffected limbs; however, f_{actual} of the unaffected limb was significantly higher than the affected limb at +10%, +15%, and +20% f_{step} (Fig. 3A).

| | f _{step} | | Limb | | $f_{\rm step} 	imes { m Lin}$ | nb |
|-----------------------------|-------------------|------------|-------|------------|-------------------------------|------------|
| | F | Sig. | F | Sig. | F | Sig. |
| $f_{\rm actual}$ (Hz) | 909.92 | P = < 0.01 | 3.56 | P = 0.10 | 11.4 | P = < 0.01 |
| k_{leg} (kN/BW/m) | 8.83 | P = < 0.01 | 4.88 | P = 0.06 | 8.87 | P = < 0.01 |
| F_{peak} (N/BW) | 40.61 | P = < 0.01 | 0.90 | P = 0.37 | 14.28 | P = < 0.01 |
| $\Delta L(\mathbf{m})$ | 96.09 | P = < 0.01 | 9.14 | P = < 0.05 | 5.06 | P = < 0.01 |
| k _{vert} (kN/BW/m) | 20.04 | P = < 0.01 | 9.41 | P = < 0.05 | 6.38 | P = < 0.05 |
| Δy (m) | 62.38 | P = < 0.01 | 20.05 | P = < 0.01 | 0.94 | P = 0.49 |
| θ (deg.) | 9.29 | P = < 0.01 | 0.01 | P=0.96 | 29.91 | P = < 0.01 |
| $t_{\rm c}({\rm s})$ | 9.69 | P = < 0.01 | 1.37 | P = 0.28 | 20.4 | P = < 0.01 |

Table 1. Results of the two-way repeated measures ANOVA. *F* values and corresponding *P* values are presented for all spring-mass parameters.

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Consequently, the differences in f_{actual} between the affected and unaffected limbs was greater for higher f_{step} (especially at +10%, +15%, and +20%) than for lower f_{step} (Fig. 3A).

Leg stiffness, peak vGRF, and peak leg length compression. For all test subjects, the main effect of f_{step} on k_{leg} was significant, but no significant main effect for the limbs was found (Table 1). Statistical analysis revealed a significant interaction effect on k_{leg} (Table 1). As a result, the test of the simple main effect indicated an increase in k_{leg} from the lowest to highest f_{step} in the unaffected limb, but not in the affected limb. A significant difference in k_{leg} was noted between -15% and +20%, -10% and +15%, -5% and +15%, and +10% and +15% in the unaffected limb. Further, k_{leg} was significantly smaller in the affected limb than in the unaffected limb at +15% and +20% f_{step} (Fig. 3B). The peak vGRF (F_{peak}) showed significant main effects of f_{step} , but no significant main effect of the limb (Table 1). A significant interaction effect on F_{peak} was also observed (Table 1). Because of the simple main effect, f_{step} had a significant effect on F_{peak} , whereas no significant limb effect was observed on F_{peak} . However, the differences in F_{peak} between the affected and unaffected limbs was more noticeable for higher f_{step} (especially +10%, +15%, and +20%) than for lower f_{step} (Fig. 3C). There was a significant main effect of f_{step} , limbs, and interaction effects on the peak leg spring compression (ΔL ; Table 1 and Fig. 3D). A test of the simple main effects identified a decrease in ΔL over a wide f_{step} range for both limbs. Furthermore, we found that ΔL was significantly higher in the affected limb than in the unaffected limb at -15% and from -5% to +20% f_{step} .

Vertical stiffness and peak vertical COM displacement. Statistical analysis revealed significant main effects of f_{step} and the limb on vertical stiffness (k_{vert}), as well as the interaction effect (Table 1). Tests of the simple main effects identified an increase in k_{vert} from the lowest to the highest f_{step} for the unaffected limb, but no changes in that for the affected limb (Fig. 3E). k_{vert} of the affected limb was significantly smaller than that of the unaffected limb at -15% and from -5% to +20% (Fig. 3E). There was a significant main effect of f_{step} and the limb on the peak vertical displacement of COM (Δy ; Table 1). However, no significant interaction effect between f_{step} and the limb on Δy was found (Table 1). Statistical analysis revealed that Δy was significantly decreased with increasing f_{step} in both limbs. It was also found that Δy of the affected limb was significantly greater than that of the unaffected limb at all prescribed f_{step} except -20% (Fig. 3F).

Half-angle swept by the leg spring and ground contact time. Significant main effects of f_{step} were noted on the half-angle swept by the leg spring (θ), but no main effect of limb was observed on θ (Table 1). A significant interaction effect on θ was also identified (Table 1). The post hoc analysis revealed that θ was slightly increased from -20% to $+5\% f_{\text{step}}$ in the affected limb only. On the other hand, θ was significantly decreased from lower to higher f_{step} in the unaffected limb (Fig. 3G). Furthermore, we observed that θ was significantly greater in the affected limb at +15% and $+20\% f_{\text{step}}$ (Fig. 3G). We also identified a significant main effect of f_{step} on contact time (t_c ; Table 1). Additionally, a significant interaction effect between f_{step} and the limb on t_c was noted. However, no significant main effect of the limb was observed. The simple main effects showed that t_c in the affected limb increased from -20% to +5% but remained nearly constant until $+20\% f_{\text{step}}$ (Fig. 3H). On the other hand, t_c in the unaffected limb remained nearly constant when the subject ran at a relatively lower f_{step} but decreased at a relatively higher f_{step} . Compared with that of the unaffected limb, t_c of the affected limb was significantly longer at +15% and $+20\% f_{\text{step}}$ (Fig. 3H).

Discussion

We found that the unaffected limb could match the metronome frequency within 3% at all designated step frequencies. Further, we found that k_{leg} and k_{vert} of the unaffected limb were increased with higher f_{step} (Fig. 3B-E). These results are consistent with past findings suggesting that k_{leg} and k_{vert} are increased with higher f_{step} during running in non-amputees^{4–6} and in the unaffected limbs of unilateral transtibial amputees⁷. However, unilateral TFAs could not match the three fastest values of f_{step} (+10%, +15%, and +20% f_{step}) with their affected limbs, and the affected limb maintained nearly constant k_{leg} and k_{vert} values over a wide f_{step} range of. The results of this study are also consistent with those of a previous study, which showed that k_{leg} of affected limbs in unilateral transtibial amputees remained virtually constant across a range of f_{step} at a given running speed⁷. Therefore, the results support our hypothesis that the k_{leg} of unilateral TFAs would differ between the affected and unaffected limbs across a range of f_{step} at a given running speed.



Figure 3. Comparisons of (A) f_{actual} , (B) k_{leg} , (C) F_{peak} , (D) ΔL , (E) k_{vertb} , (F) Δy , (G) θ , and (H) t_c across a range of step frequencies (f_{step}). Black (unaffected leg) and gray (affected leg) circles are the means of the nine subjects. Asterisks (*, **) indicate significant differences between the unaffected legs at p < 0.05 and 0.01, respectively. Black (unaffected leg) and gray (affected leg) horizontal lines indicate significant differences at P < 0.05 (dotted lines) and 0.01 (solid lines), respectively.

In this study, increases in k_{leg} and k_{vert} of the unaffected limb at higher f_{step} were accompanied by decreases in ΔL , Δy , θ , and t_c (Fig. 3D,F,G,H). The current results agree with a past finding that, as the stiffness of the spring-mass system increases, the vertical displacement of the COM during the ground contact phase decreases, and the system facilitates bouncing off the ground in a shorter time at higher frequencies⁴. On the other hand, we found

| Subject | Sex | Age (years) | Height (m) | Total mass (kg) | Amputated limb | Time since amputation (years) | prosthetic knee | RSP model | Affected L ₀ (m) | Unaffected L ₀ (m) | Trial speed (m/s) | Preferred f _{step} (Hz) |
|---------|-----|----------------|---------------|-----------------------|-------------------|-------------------------------------|-----------------|--------------------------|--------------------------------|----------------------------------|-------------------------|-------------------------------------|
| 1 | F | 20 | 1.56 | 56.5 | Right | 5.7 | 3\$80 | Runner 1E91 (cat.3) | 0.85 | 0.84 | 2.39 | 2.88 |
| 2 | F | 21 | 1.49 | 46.7 | Right | 10.0 | 3\$80 | Sprinter 1E90 (cat.2) | 0.85 | 0.76 | 1.94 | 3.00 |
| 3 | F | 20 | 1.62 | 45.2 | Left | 3.5 | 3\$80 | Sprinter 1E90 (cat.3) | 0.85 | 0.84 | 2.14 | 2.68 |
| 4 | М | 17 | 1.77 | 86.0 | Right | 3.5 | 3\$80 | Sprinter 1E90 (cat.4) | 0.93 | 0.89 | 2.75 | 2.93 |
| 5 | М | 23 | 1.68 | 56.3 | Left | 20.0 | 3\$80 | Sprinter 1E90 (cat.3) | 0.89 | 0.84 | 2.31 | 2.73 |
| 6 | М | 34 | 1.61 | 58.7 | Left | 21.0 | 3\$80 | Runner 1E91 (cat.5) | 0.85 | 0.82 | 2.25 | 2.85 |
| 7 | М | 27 | 1.75 | 70.4 | Right | 6.2 | 3\$80 | Runner 1E91 (cat.4) | 0.96 | 0.89 | 2.86 | 2.70 |
| 8 | М | 36 | 1.61 | 59.8 | Right | 17.9 | 3\$80 | Runner 1E91 (cat.3) | 0.87 | 0.81 | 2.11 | 2.53 |
| 9 | М | 31 | 1.65 | 59.7 | Right | 3.0 | Cheetah Knee | Runner 1E91 (cat.2) | 0.88 | 0.87 | 2.00 | 2.65 |
| Mean | | 25.44 | 1.64 | 59.91 | | 10.09 | | | 0.88 | 0.84 | 2.31 | 2.77 |
| (SD) | | (6.45) | (0.08) | (11.6) | | (7.1) | | | (0.04) | (0.04) | (0.30) | (0.14) |

Table 2. Subject characteristics.

invariant k_{leg} and k_{vert} of the affected limb across a range of f_{step} (Fig. 3B–E). A possible explanation for the invariant k_{leg} and k_{vert} of the affected limb with increasing f_{step} is the inability to regulate the affected limb's stiffness. A past finding demonstrated that k_{leg} of the affected limb in athletes with unilateral transtibial amputation was constant with increasing f_{step} at a given running speed⁷. According to this study, athletes with unilateral transtibial amputation was constant with increasing f_{step} at a given running speed⁷. According to this study, athletes with unilateral transtibial amputation would make the affected limb as stiff as possible to conform to the natural frequency of the RSP to the extent possible. Further, a recent finding demonstrated that an athlete with unilateral transtibial amputation could not follow relatively higher and lower hopping frequencies as a consequence of the invariant k_{vert} of the affected limb¹¹. As suggested by a previous study¹², the stiffness of the RSP including the prosthetic knee likely dictates the whole-leg stiffness during running, leading to invariant k_{leg} and k_{vert} of the affected limb across a range of f_{step} at a given speed.

Surprisingly, the subjects in our study could match the targeted f_{step} from a relatively lower f_{step} to the preferred f_{step} (0%) without changing k_{leg} and k_{vert} (Fig. 3B–E). To do so, the subjects decreased θ and t_c in these conditions (Fig. 3G,H). However, the compensatory strategy of modifying θ and t_c in the affected limb might be insufficient at relatively higher f_{step} because of the mechanical compression–decompression properties of the RSP¹³. Further, we also observed that F_{peak} did not change from the preferred f_{step} to a higher f_{step} (Fig. 3C). This may be because unilateral TFAs must maintain the minimum vGRF and the corresponding impulse to rebound from the ground under the gravitational environment. These constraints limit the magnitude of the mechanical compression–decompression properties of the RSP; therefore, the affected limb would be unable to reduce t_c any further, especially at relatively higher f_{step} . Consequently, unilateral TFAs would be unable to match the three highest f_{step} conditions (+10%, +15%, and +20% f_{step}) with their affected limbs.

As shown in Fig. 3B–E, k_{leg} and k_{vert}^{Vert} were generally lower in the affected limb than in the unaffected limb. Recent studies also demonstrated that k_{leg} and k_{vert} of the affected limb were lower than those of the unaffected limb in unilateral TFAs wearing RSPs during running^{14,15}. Further, the smaller values of k_{leg} and k_{vert} of the affected limb were mainly associated with greater ΔL and Δy , compared to the unaffected limb, but not with F_{peak} (Fig. 3C,D,F). As shown in Eqs. (2) and (3), ΔL is a function of Δy , L_0 , θ , and t_c when the foot is on the ground. Therefore, it is plausible that the higher ΔL in the affected limb than the unaffected limb may be attributed to (1) larger θ and longer t_c^{-16} (Fig. 3G,H), (2) 5% longer leg spring length (L_0) of the affected limb (Table 2), (3) mechanical properties of RSPs¹², (4) other residual structures, such as the socket–stump interface and/or larger pelvic obliquity of the frontal plane in the proximal hip joint, or any combination of these factors.

A better understanding of spring-like leg behavior and stiffness regulation in this population will provide insight into the underlying biomechanics and control mechanism of leg stiffness in humans and would assist in developing design parameters for spring-based prostheses for running⁴. For example, a past finding demonstrated the asymmetric k_{leg} and k_{vert} modulation of unilateral TFAs for a range of running speeds¹⁴. In our study, asymmetric k_{leg} and k_{vert} modulation is observed across a range of f_{step} at a given speed (Figure B and E). Hence, the past finding and present study both suggest that spring-like leg behavior and stiffness regulation during running differ between the affected and unaffected limbs in unilateral TFAs. In other words, unilateral TFAs wearing RSPs would adopt limb-specific control strategies to accommodate the demands of specific activities. Because increased k_{leg} and k_{vert} during running and hopping may be related to bone-related injuries such as knee osteoarthritis and stress fractures¹⁷, coaches and practitioners should consider limb-specific injury risks and control mechanisms during running in unilateral TFAs for running-gait rehabilitation and training regimes¹⁸. Additionally, the observed asymmetric k_{leg} and k_{vert} modulation could be improved by changing the prosthetic mechanical properties and configurations. Indeed, previous studies suggested that RSP stiffness¹² and prosthetic alignment¹³ could influence running performance through the regulation of stiffness in lower-extremity amputees. Although participants of the present study used their preferred RSP design and category of stiffness as well as prosthetic alignment, this may have induced the asymmetric k_{leg} and k_{vert} modulation. Therefore, the current results may contribute to providers' and patients' decision-making regarding the types and properties of the RSPs that they will employ for running.

There are certain considerations that must be acknowledged when interpreting the results of the current study. First, although we quantified the leg stiffness, which represents the overall stance leg mechanics, the natural frequency of the prosthetic foot and the stiffness of the prosthetic knee and foot were not determined in this study. As shown in Fig. 2, it seems that the use of a prosthetic knee and foot results in a large amount of energy loss (hysteresis) in the vGRF–COM displacement curves during ground contact. Therefore, as demonstrated by past findings^{7,14,19}, the stiffness of each prosthetic component should be addressed to determine stiffness regulation during running using RSPs. Second, in our study, each participant ran at different f_{step} at a given running speed, which differed depending on the participant. This is because a one-speed trial is insufficient to obtain a wide f_{step} range for all participants. Instead, we used the normalized speed (40% of the estimated maximum speed); consequently, this normalized speed was sufficiently low for all participants to obtain a wide f_{step} range. However, stiffness regulation at different f_{step} in each participant might be affected by the trial speed. Thus, caution must be used in the interpretation and generalization of these findings.

Conclusion

In summary, the results of this study suggest that (1) the affected limb of unilateral TFAs cannot modulate k_{leg} across a range of f_{step} at a given running speed, and (2) the k_{leg} regulation strategy differs between the affected and unaffected limbs. Between-limb asymmetry in the k_{leg} regulation strategy during running in unilateral TFAs may arise from their compensatory strategies and the mechanical constraints of their prosthesis properties.

Methods

Participants. In this study, we recruited nine TFAs who specialized in the 100-m sprint or long jump (Table 2). Five of the participants used the 1E91 Runner (categories 2 to 5, Ottobock, Duderstadt, Germany) and four participants used the 1E90 Sprinter (categories 2 to 4, Ottobock, Duderstadt, Germany) with rubber soles (Table 2). All of these participants belonged to track and field teams and had performed sprint training for more than five years. On average, their best recorded times in the 100-m sprint within the preceding year were 17.59 ± 2.15 s. Before the experiment, all participants (or guardians, in the case of participant 4) gave informed written consent approved by the local ethical committee. The study was ethically approved by the Institutional Review Board of our institution (Environment and Safety Headquarters, Safety Management Division, National Institute of Advanced Industrial Science and Technology) and conducted in accordance with the guidelines set out in the Declaration of Helsinki (1983).

Tasks and experimental procedures. In this study, participants ran on an instrumented treadmill (FTMH-1244WA, Tec Gihan, Kyoto, Japan). First, as a familiarization period for instrumented treadmill running, we instructed all subjects to perform running and walking more than 5 min before the experiment²⁰. Next, each participant performed a single bout of 20-s runs to determine the preferred f_{step} for running at 40% of their maximum speed (Table 2), which was estimated by dividing 100 m by their personal best time in a 100-m sprint¹⁴. 40% of the estimated maximum speed was chosen as the running speed because this was sufficiently low for the participants to obtain a wide f_{step} range. We determined the preferred f_{step} using 14 consecutive steps in the middle of the trial. In the present study, the f_{step} was defined as the inverse of the time from touchdown to the contralateral touchdown. Because previous studies varied the f_{step} range from -30% to +30% at a given running speed⁴⁻⁷, we asked participants to run with a digital metronome beat at nine values of f_{step} : the preferred (0%), four below (-5%, -10%, -15%, and -20%), and four above the preferred f_{step} (+5%, +10%, +15%, and +20%). After a sufficient practice period at each f_{step} , participants were asked to perform a single running trial for 20 s at each targeted f_{step} (in random order), with rest periods of 1–3 min between trials to minimize the effects of fatigue. On average, the running speed in this study was 2.31 ± 0.30 m/s for 40\% of the maximum speed, and the preferred step frequency was 2.77 ± 0.14 Hz (Table 2).

Data collection and analysis. vGRF was collected by two force platforms embedded in the instrumented treadmill (sampling at 1,000 Hz). According to a previous study²¹, a fourth-order zero-lag low-pass Butterworth filter with a cut-off frequency at 25 Hz was used to filter the vGRFs. Further, a 40-N threshold for further vGRF analysis was used²²⁻²⁵. Using the vGRF, the values of f_{actual} , t_c , and F_{peak} in both the unaffected and affected limbs were determined. The representative value of stiffness was determined by averaging five consecutive steps that were within 3% of the target f_{step} . The k_{leg} (N/m) was computed as the ratio of F_{peak} to ΔL at the midstance. Thus,

$$k_{\rm leg} = F_{\rm peak} / \Delta L \tag{1}$$

with

$$\Delta L = \Delta y + L_0 (1 - \cos\theta) \tag{2}$$

where Δy was calculated by twice integrating the vertical acceleration of the COM with respect to time²⁶. The initial leg spring length (L_0) was defined as the distance from the greater trochanter to the ground in standing position. Half of the angle swept by the leg spring during the first half of stance phase (θ) was calculated as

$$\theta = \sin^{-1}(ut_c/2L_0) \tag{3}$$

where u is the average forward velocity and t_c is the ground contact time for each step. Finally, we calculated k_{vert} using the following formula:

$$k_{\rm vert} = F_{\rm peak} / \Delta y. \tag{4}$$

We calculated k_{leg} as the ratio of F_{peak} and ΔL (the ratio of F_{peak} and Δy for k_{vert}) between ground contact (initial leg compression phase) and the instant of $F_{\text{peak}}^{-11,14,27,28}$. Because body mass influences the stiffness², both k_{leg} and k_{vert} were normalized to the subject's body weight (BW), which included the prosthesis.

Statistics. A two-way repeated-measure analysis of variance (ANOVA) with two factors, f_{step} (nine levels) and limbs (two levels), was performed to compare the spring-mass parameters (f_{actual} , k_{leg} , F_{peak} , ΔL , k_{vert} , Δy , θ , and t_c) between the unaffected and affected limbs across a range of f_{step} . Mauchly's Test of Sphericity was used to ensure that the variances of the differences were comparable. If this assumption was violated, the Greenhouse–Geisser correction was applied. If a significant main effect was observed, a Bonferroni post hoc multiple comparison was performed. When the ANOVA indicated a significant interaction between the main effects, a test of the simple main effect was conducted. All statistical tests were performed at the 5% significance level using SPSS (IBM SPSS Statistics Version 19, SPSS Inc., Chicago, IL).

Data availability

The datasets generated and/or analyzed during the current study are available from the corresponding author on reasonable request.

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Author contributions

H.H. and S.H. contributed to conception and design of the work, interpretation of data and manuscript preparation. H.S., Y.N., G.H. and F.U. contributed to analysis and data acquisition.

Competing interests

The authors declare no competing interests.

Additional information

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