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Magnetic Frustration Driven by Itinerancy in Spinel CoV₂O₄

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Localized spins and itinerant electrons rarely coexist in geometrically-frustrated spinel lattices. They exhibit a complex interplay between localized spins and itinerant electrons. In this paper, we study the origin of the unusual spin structure of the spinel CoV_2O_4 , which stands at the crossover from insulating to itinerant behavior using the first principle calculation and neutron diffraction measurement. In contrast to the expected paramagnetism, localized spins supported by enhanced exchange couplings are frustrated by the effects of delocalized electrons. This frustration produces a non-collinear spin state even without orbital orderings and may be responsible for macroscopic spin-glass behavior. Competing phases can be uncovered by external perturbations such as pressure or magnetic field, which enhances the frustration.

Geometrically frustrated systems have been attracting attention because of their unusual magnetic properties induced by the suppressed conventional long-range magnetic orderings. The spin liquid state has been widely celebrated and theoretically predicted to exist in pyrochlore lattice and spinel systems with nearest-neighbor antiferromagnetic coupling¹. One more ingredient which makes the playground of the geometrically frustrated systems wider and more interesting is the coupling between the localized spin and itinerant electron in the frustrated systems². The interplay between localized spin and itinerant electron in geometrically frustrated systems is believed to be responsible for many intriguing phenomena such as a metallic spin-liquid state³, heavy-fermion behavior⁴, anomalous transport in spin-ice systems⁵, and exotic phases^{6–8}. The effect of the interaction between localized spins and itinerant electrons has been investigated intensively on pyrochlores $A_2B_2O_7$ where A is rare-earth elements and B is transition metals and both A and B sublattices are frustrated^{3–7}. However, it has rarely been explored on another strongly frustrated system, spinel AB_2O_4 , where the magnetic ion B is only frustrated.

In the spinels, the degree of the magnetic frustration and the electronic itinerancy on sublattice *B* is a function of the distance of nearest-neighbor *B* atoms (R_{B-B}). The shorter distance due to the chemical pressure from a smaller radius of *A* site cation or the physical pressure, the stronger both the electronic itinerancy and magnetic frustration are induced⁹. On the other hand, magnetic *A* site ions can relieve the frustration via the magnetic interactions between the spins on *A* site and the localized spins on sublattice *B*. Therefore, a rich phase diagram due to the strong interplay between localized spins and itinerant electrons can be anticipated when *A* sublattice is a small magnetic ion.

In the spinel vanadates AV_2O_4 (V³⁺, S=1), the octahedral crystal field on the vanadium site with two electrons in t_{2g} levels cannot completely remove the degeneracy resulting in the non-quenched orbital angular momentum. The geometrical frustration in many spinel is relieved by lowering the crystal symmetry accompanying non-collinear spin ordering and/or orbital ordering (OO), as an example, from cubic-tetragonal structural transition, which modifies of exchange paths between spins¹⁰⁻¹⁶. Therefore, OO of partially-filled *d*-electrons on the V site has been observed in many spinel vanadates (AV_2O_4 , A = Mn, Fe, Cd, Zn, Mg). Moreover, recent studies

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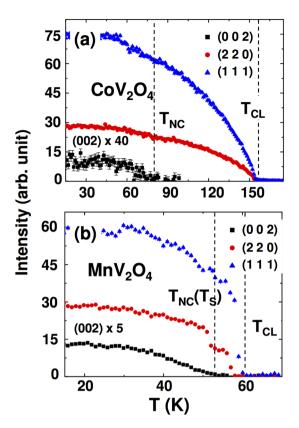


Figure 1. NC spin states in cubic CoV_2O_4 compared to tetragonal MnV_2O_4 . Temperature dependence of the (111) (triangles), (220) (circles), and (002) (squares) Bragg peak intensities for CoV_2O_4 (a) and MnV_2O_4 (b) measured by neutron diffraction at HB-3A. The peak intensities of (111) and (220) above the magnetic transition temperature are fully from the nuclear structure and were subtracted. The (002) peak is not allowed from the structural symmetry and fully originated from the magnetic scattering. The background was subtracted. All the magnetic peaks observed by our neutron diffraction are instrument resolution limited besides the peak broadening caused by the structural transition for MnV_2O_4 , and thus indicate the long range ordered magnetic moments. The strongly-reduced intensity of (002) peak in CoV_2O_4 indicates that only tiny amount of V spin orders, which is caused by enhanced itinerancy.

suggest that the spinel vanadates become itinerant when R_{V-V} falls around a threshold value of 2.94 Å, which is close to R_{V-V} when $A = \text{Co} (2.97 \text{ Å})^{17,18}$. Since it also has the smallest magnetic *A*-site cation of any known spinel vanadates, CoV_2O_4 is the ideal system to study the interplay between itinerancy and localized spins.

The frequency dependence of ac susceptibility and the divergence between the zero-field cooling and field cooling susceptibility at the cubic-tetragonal structural transition indicate a glassy spin state¹⁹⁻²¹. Although the spin-glass behavior of $Mn_{1-x}Co_xV_2O_4$ is enhanced by Co-doping⁹, CoV_2O_4 has higher magnetic ordering temperatures than those of compounds $Mn_{1-x}Co_xV_2O_4$ with x < 1. Indeed, CoV_2O_4 has higher para-collinear (T_{CL}) and collinear-non-collinear (T_{NC}) spin transition temperatures than those of any other vanadate spinels. This stands in marked contrast to the pyrochlores^{6,7}, where spin-glass phases have lower ordering temperatures with smaller A site atom doping. Bizarrely, no structural phase transition with OO has been observed for $CoV_2O_4^9$ even though the spin structure of CoV_2O_4 has been suggested to be non-collinear spin structure from the previous magnetization and neutron diffraction studies^{16,19,21,22}. This is sharply contrast to the fact that the most spinels show the structural phase transition concurrent with the orbital ordering and non-collinear spin structure as stated above. Due to these unusual magnetic behaviors, the exotic spin states in CoV_2O_4 highly demand a detailed study.

This paper clarifies the origin of the possible non-collinear (NC) spin states of CoV_2O_4 without OO and structural phase transition by using density functional theory (DFT) and spin models to interpret neutron-scattering measurements on high-quality CoV_2O_4 single crystals. Chemically-driven pressure by Co enhances the itinerancy in CoV_2O_4 . This itinerancy weakens the OO and strengthens the magnetic and structural isotropies. The frustration fostered by these isotropies²³ may be responsible for macroscopic glassy behavior in a magnetic field^{9,19}. Due to the enhanced frustration, external perturbations such as pressure or magnetic field could uncover novel magnetic phases in cubic CoV_2O_4 .

Results

NC spin states in cubic phase CoV₂O₄. To resolve the noncollinear spin structure, we performed the neutron diffraction measurements on cubic CoV_2O_4 and tetragonal MnV_2O_4 samples. Figure 1 compares the temperature dependence of the (002), (220), and (111) Bragg peaks in cubic CoV_2O_4 and tetragonal MnV_2O_4 . CoV_2O_4 and MnV_2O_4 show (111) and (220) Bragg peaks rapidly growing below 150 K and 60 K, respectively,

denoted as T_{CL} . (111) and (220) Bragg peaks are consistent with the crystal symmetry of these systems, and indicate that collinear ferrimagnetic (FIM) orderings are stabilized. Below 75 K for CoV_2O_4 , and 57 K for MnV_2O_4 denoted as T_{NO} the intensity of (002) Bragg peaks begin to increase, which is consistent with the previous neutron power diffraction study^{21,22}. The (002) peaks are forbidden by structural symmetry. Therefore, the observation of (002) peak indicates the formation of an additional antiferromagnetic (AFM) component in the *ab*-plane, thus a canted spin structure or noncollinear spin structure below $T_{NC}^{24,25}$. In case of MnV_2O_4 , T_{NC} accompanies the structural phase transition (T_S)¹⁴. However, no clear structural transition in CoV_2O_4 was observed by recent X-ray diffraction and heat capacity measurements⁹. The appearance of Bragg peak intensity at the (002) position is consistent with the recent neutron scattering measurements where it was associated with a two-in/two-out (TI/TO) structure on the V-sublattice^{25,26}. Also our DFT calculations later in the paper justify this assumption. Based on the diffraction data, it is valid to assume that the spin configuration of CoV_2O_4 is similar to the spin configurations of $\text{MnV}_2\text{O}_4^{27}$, and $\text{FeV}_2\text{O}_4^{28}$.

When the inter-vanadium distance R_{V-V} lies around the critical value (2.94 Å)²⁹, the system is expected to remain in metallic state down to very low temperatures. Therefore, the effect of the itinerant electrons should be considered in CoV₂O₄. Indeed, the ordered magnetic moment refined from the Bragg peaks is 0.47(3) μ_B/V in CoV₂O₄, which is significantly reduced from 0.95(4) μ_B/V in MnV₂O₄ due to the increased itinerancy of electrons. In addition, T_{NC} of CoV₂O₄ is higher than that of MnV₂O₄ because of a new exchange interaction originating from the itinerant electrons, which we will clarify later with the calculated band structures. An additional magnetic frustration among the localized spins may be indirectly induced by electronic itinerancy as well. Curiously, the structural phase transition associated with OO commonly observed in many vanadates is absent in CoV₂O₄, even though the TI/TO seems to emerge robustly. Since the TI/TO state originates from OO in tetragonal compounds^{27,28}, the isosymmetric TI/TO state in cubic CoV₂O₄ without any OO must have a different origin associated with its itinerancy and frustration.

Single-ion anisotropy suppressed by itinerancy. First-principles calculations were used to explore the microscopic origin for the complex NC state in cubic CoV_2O_4 . As shown in Fig. 2(a) and (c), the major magnetic anisotropy appears on the V³⁺ site with a magnitude two or three orders larger than that for the A-site (Co/Mn). Although the V³⁺ ions are surrounded by similar octahedra in both CoV_2O_4 and MnV_2O_4 , the local [111] single-ion anisotropy (SIA) of V³⁺ is significantly reduced in CoV_2O_4 (-1.2 meV) compared to that in MnV_2O_4 (-4.8 meV) due to the melting of OO by the pressure-induced itinerancy in CoV_2O_4 . Calculated by DFT, the SIA on the V sites totally disappears with an external pressure around 10 GPa in CoV_2O_4 .

While the AFM V-V interaction in a pyrochlore lattice with local [111] SIA favors the all-in/all-out (AI/AO) spin structure, the disappearance of SIA fosters strong magnetic frustration²³. OO relieves the frustration in MnV_2O_4 with structural phase transitions. However, the frustration reappears in CoV_2O_4 due to the melting of the OO and the suppression of the easy-axis anisotropy by itinerancy, as shown in Fig. 2(a,b). The recovered frustration might be responsible for the macroscopic spin-glass behavior⁹ below T_{NC} due to the competing ground states³⁰.

The SIA of *A*-site (Fig. 2c), (A = Co, Mn) is quite negligible compared to the SIA of V³⁺. While Mn²⁺ has a weak easy-plane axis because of the compressed tetragonal structure (c/a < 1), Co²⁺ does not exhibit anisotropy because of the isotropic cubic structure. The SIA of Co²⁺ is much less dependent on pressure than that of V³⁺ since Co²⁺ electronic states lie significantly below the Fermi energy (ε_F) and are thereby electronically encapsulated, as shown in Fig. 3(a). Only V³⁺ states cross ε_F . Therefore the pressure-induced itinerancy will only affect the spins on V³⁺ sites. The moment of Co ion is not affected by itinerancy.

Enhanced exchange couplings. As shown in Fig. 2 in Supplementary material, the Bragg peaks do not split or broaden with decreasing temperature below 100 K, indicating the absence of a structural transition. In agreement with this measurement, DFT calculations confirm the structural isotropy (c/a = 1) of CoV_2O_4 . As shown in Fig. 3, the $t_{2g} (d_{xy} = d_{yz} = d_{xz})$ and $e_g (d_{z^2} = d_{x^2-y^2})$ electronic levels become equally occupied and degenerate in cubic CoV_2O_4 . The structural and electronic isotropies also produce the same exchange interactions $J_{V-V}^{in} = J_{V-V}^{out} = -12$ meV between all spins on the tetrahedron as calculated from first principles, Fig. 4, where $J_{V-V}^{in} = J_{V-V}^{out}$ are in-plane and out-of-plane exchange interaction, which are not equivalent in tetragonal phase (the right panel of Fig. 3). These coupled structural, electronic, and magnetic isotropies foster frustration and the observed NC phase in Fig. 1.

Comparing the densities-of-states of CoV_2O_4 and MnV_2O_4 reveals the origin of the enhanced magnetic ordering temperatures in CoV_2O_4 . The large energy difference (~5 eV) between the occupied V and Mn *d* states weakens the exchange between Mn and V. By filling the e_g minority spin levels as indicated in Figs 2(d) and 3(a), Co significantly lowers the t_{2g} unoccupied energy level and enhances the exchange interaction between Co and V. DFT calculations reveal that the magnitude of the AFM J_{A-V} is twice as large in CoV_2O_4 (-2.5 meV) as in MnV_2O_4 (-1.2 meV). As reflected by the neutron-scattering measurements in Fig. 1, the enhanced J_{A-V} causes T_{CL} to more than double in CoV_2O_4 (150 K) compared to MnV_2O_4 (53 K).

Surprisingly, the induced itinerancy also increases the NC ordering temperature even without OO in CoV₂O₄. As shown in Fig. 1, T_{NC} significantly increases in CoV₂O₄ (75 K) compared to MnV₂O₄ (57 K). Although it exhibits the higher NC ordering temperature, CoV₂O₄ also exhibits glassy behavior^{9,19}. While the reduced SIA and induced isotropies foster frustration²³, the enhanced exchange interaction relieves the frustration and enhances the ordering temperatures. In the series of Mn_{1-x}Co_xV₂O₄, the spin-wave gap (~2 meV) remains relatively unchanged with Co-doping (x)²⁴ despite the enhanced magnetic ordering temperatures proportional to J_{A-V} . Since the spin-wave gap is proportional to $\sqrt{D_V \times J_{A-V}}$, the increase in $|J_{A-V}|$ is compensated by the reduction in the anisotropy D_v in CoV₂O₄. By enhancing both competing effects (itinerancy-driven isotropies with reduced SIA and strengthened exchange), Co doping can foster various novel states in CoV₂O₄.

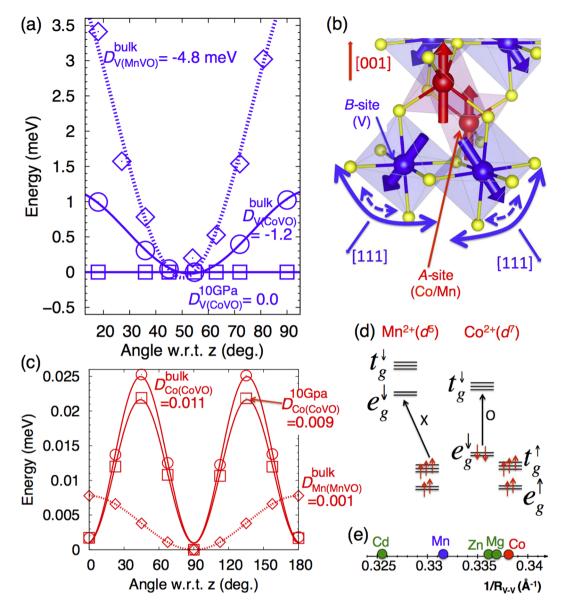


Figure 2. Reduced single-ion anisotropy (SIA) of V in CoV_2O_4 compared with that in MnV_2O_4 . (a) Total energy versus angle and associated SIA (meV) of V³⁺ in ambient (circle) and 10 GPa (square) pressure for bulk CoV_2O_4 and MnV_2O_4 (diamond). (b) NC spin configurations of V³⁺ and $\text{Co}^{2+}/\text{Mn}^{2+}$ spins pointing along local [111] and global [001] directions, respectively. The round bold (dotted) arrows close to V spins depict the rotational flexibility in CoV_2O_4 (MnV_2O_4). (c) SIA of Co^{2+} in bulk CoV_2O_4 under 10 Gpa compared to SIA of Mn^{2+} in bulk MnV_2O_4 . (d) Orbital occupation configuration of Mn^{2+} (d⁵) and Co_{2+} (d⁷). (e) R_{V-V} in CoV_2O_4 and MnV_2O_4 are compared with R_{V-V} in other vanadates from ref.²⁹.

Novel phases induced by frustration. The comparison between CoV_2O_4 and MnV_2O_4 in Fig. 4 reveals the origin of the NC states in CoV_2O_4 . The key handle to tune the magnetic couplings is the distance between the V atoms (R_{V-V} along the *x*-axis) controlled by chemical doping and external pressure. In MnV_2O_4 , the OO of the V ions relieves the magnetic frustration of the pyrochlore lattice and stabilizes the TI/TO NC spin state. The AFM Mn-V interactions increase the canting angle while maintaining this TI/TO state (Fig. 4(b)). By introducing itinerancy, Co doping promotes isotropic V-V interactions and favors the AI/AO spin state. Within the tetrahedron network, the AI/AO state has two distinct canting angles θ and π - θ compared to the one canting angle θ of the TI/ TO state, where the canting angle θ is a measure of deviation of spin from the -z axis as shown in Fig. 4(b). Guided by the DFT parameters for CoV_2O_4 , our model calculation indicates that the new two-angle state based on the AI/AO state lies within 0.1 meV/unit-cell of the TI/TO ground state. The isotropic exchange ($J_{V-V}^{in} = J_{V-V}^{out}$) fosters a new two-angle AI/AO structure that can be stabilized by a magnetic field.

External pressure may also increase the degree of frustration. For high external pressure^{9,17} ~10 GPa, the enhanced itinerancy fully suppresses the local SIA ($D_v \sim 0$) of V as in Fig. 4(a) and revives the magnetic frustration of the pyrochlore lattice. Although AFM exchange between the Co and V sites then induces the observed isosymmetric TI/TO spin structure, the frustration fostered by itinerancy and the alternative states that compete with

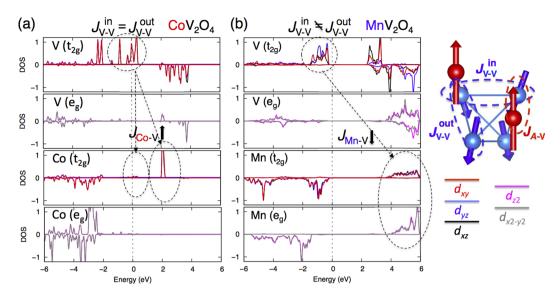


Figure 3. Origin of the enhanced magnetic ordering temperature in CoV_2O_4 . Projected density-of-states of CoV_2O_4 (**a**) compared to MnV_2O_4 (**b**) in unit of eV^{-1} . Dotted arrows denote the energy differences, Δ between V and Co/Mn for possible AFM super-exchange $(J_{A-V} \sim -t^2/\Delta)$. *t* is the hopping parameter between orbitals.

the TI/TO ground state are possibly responsible for the measured magnetic anomalies¹⁷ and spin-glass behavior⁹. Moreover, the absence of SIA ($D_v \sim 0$ and $D_A \sim 0$) at high pressure above 10 GPa (Figs 2(a) and 4(a)) preserves the rotational symmetry and may stabilize a continuum of degenerate states where the two angles (θ_1 , θ_2) rotate without energy cost as obtained in the Appendix and shown in the energy landscape of Fig. 4(d). This massive degeneracy can induce spin-glass or spin-liquid-like behavior. Since neutron scattering is limited to relatively low pressures, these novel states should be studied with synchrotron magnetic X-ray scattering.

Magnetic field measurement. Figure 4(a) provides a guide to uncover the novel states produced by the regenerated frustration. Although all other magnetic couplings (isotropic J_{V-V} , reduced D_v) foster frustration (bold red line), the remnant AFM interaction J_{Co-V} (dotted blue line in Fig. 4(a)) still relieves frustration. An external magnetic field ($\vec{H} = H\hat{z}$) can help restore frustration by weakening J_{Co-V} , thereby inducing the novel two-angle state of CoV₂O₄, as shown in Fig. 5.

To check the effect of a magnetic field on CoV_2O_4 , we carried out further elastic neutron-scattering measurements on the Co-rich single-crystal spinel $\text{Co}_{0.8}\text{Mn}_{0.2}\text{V}_2\text{O}_4$, which preserves the cubic structural and magnetic isotropies as in Fig. 4(a) but exhibits stronger scattering intensity than CoV_2O_4 due to the larger size of the single crystal. The V³⁺ AFM components in the *ab*-plane increase with the magnetic field ($H_z > 3$ T), as indicated by the increased intensity of (020) (see Fig. 5(a)). At $H_z < 3$ T, the increased intensity of (220) reflects the reorientation of the magnetic domains; at $H_z > 3$ T the (220) intensity is saturated, indicating that all magnetic domains are fully oriented and that the FIM components are constant. This is consistent with magnetization measurements on a polycrystalline sample, which provide a saturation field of ~ 2 T¹⁹. Note that the magnetic components for M_z^{Co} and M_z^{V} both contribute the magnetic scatterings at (220). Considering the Co magnetic moments saturate ferromagnetically at zero field, we assume M_z^{Co} does not change with the field. Therefore, no change of the (220) intensity at fields above 3 T indicates M_z^{V} stays almost constant at the field between 3 T and 10 T. The small change in $\Delta M_z^{\text{V}} = M^{\text{V}}(0.6\mu_B) \cos 21^{\circ}(at3\text{T}) - M^{\text{V}}(0.6\mu_B) \cos 24^{\circ}(at10\text{T}) \sim 0.01\mu_B$, which is negligible compared with ΔM_{xy}^{V} and the resolution limit of $\sim 0.1 \,\mu B$. So we can safely assume that both M_z^{V} and M_z^{Co} are constant above 3 T. Since the AFM components of V³⁺ in the *ab*-plane (M_{ab}^{N) continue to grow above 3 T, the canting angle ($\theta = \tan^{-1}[M_{ab}^{\text{V}}/M_z^{\text{V}}]$) of the V³⁺ spins must increase with the magnetic field along [001].

Using the spin model (Eq. 1) combined with DFT parameters (Fig. 4(a)), we confirm the increase in the canting angle with magnetic field in Fig. 5(c). The two-angle AI/AO state has an energy within 0.1 meV/unit-cell of the the one-angle TI/TO ground state in the Co-rich region. We predict that this new state is stabilized by a large magnetic field of about 140 T, as shown in Fig. 5(c),(d). Although only the one-angle TI/TO state was previously reported in vanadate compounds (AV_2O_4 , A = Zn, Mn, Fe), various competing states appear in CoV_2O_4 due to frustration. It is likely that those states can be revealed by a magnetic field or pressure.

Of course, the critical magnetic field (H_Z = 140 T) is too large for neutron scattering measurements. However, the first-order phase transition from the one-angle to the two-angle state may be captured by magnetic susceptibility measurements. Moreover, various methods can be employed to reduce the critical field. Since external pressure suppresses SIA and revives frustration as discussed in the previous section, pressure may also reduce the critical magnetic field. Contrary to the usual expectation, a magnetic field may strengthen frustration and noncollinearity in CoV₂O₄ by competing with the only exchange coupling (J_{Co-V}) that hampers frustration.

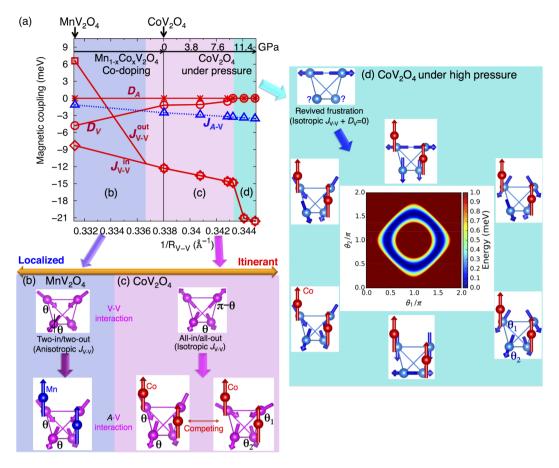


Figure 4. Evolution of magnetic couplings and competing ground states driven by Co-doping and pressure. (**a**) Change of all magnetic interactions with Co doping and external pressure (GPa) calculated by LSDA + *U* for the ground states at zero temperature. Points represent DFT results and the connecting lines are a guide for eye. J_{V-V}^{in} and J_{V-V}^{out} are expected to be degenerate at x = 0.8 (cubic) in $Mn_{1-x}Co_xV_2O_4$ from experiments^{9,24}. Bold (dotted) lines represent the exchange (*J*) and SIA (*D*) interactions. (**b**) The anisotropic J_{V-V} prefers the TI/TO state and the antiferromagnetic J_{Mn-V} also stabilizes TI/TO state in Mn-rich region. (**c**) The isotropic J_{V-V} prefers the AI/AO state but the antiferromagnetic J_{Co-V} tries to stabilizes the TI/TO state in Co-rich region. Thus, two states of the isosymmetric one-angle TI/TO state and the two-angle state that evolves from the AI/AO state compete with each other. (**d**) The energy landscape of CoV_2O_4 with the disappearance of SIA at high pressures. The massive degeneracies in the energy landscape of two angles (θ_1 and θ_2) may induce spin glass or liquid phases as explained in the text.

Discussion

It is natural to wonder if cations significantly smaller than Co^{2+} such as Be^{2+} can be substituted on the *A*-site to induce even more itinerancy and consequent frustration. However, a non-magnetic *A*-site reduces the magnetization of V so much that the system would become paramagnetic²⁹. Because strong magnetic interactions between the *A* and *B* sites is required, Co is the only candidate *A*-site cation to support localized spins with enhanced J_{Co-V} while also promoting itinerancy on the *B* site.

Compared to other vanadates (AV_2O_4) , the frustration in magnetically and structurally isotropic CoV_2O_4 explains its NC and macroscopic spin-glass properties. Since the AFM interaction between Co and V is the only factor that relieves the magnetic frustration, weakening the AFM interaction by a magnetic field or further reducing the SIA by external pressure can rekindle the frustration and reveal alternative states. Among spinel vanadates, CoV_2O_4 is uniquely located at the crossover between localized and itinerant behavior. Consequently, many exotic properties and new phases can be produced by restoring the frustration of the pyrochlore lattice.

Method

Sample preparation. Single crystals of CoV_2O_4 , $Co_{0.8}Mn_{0.2}V_2O_4$ and MnV_2O_4 were grown by the traveling-solvent floating-zone (TSFZ) technique. The feed and seed rods for the crystal growth were prepared by solid state reaction. Appropriate mixtures of MnO, $CoCO_3$, and V_2O_3 were ground together and pressed into 6-mm-diameter 60-mm rods under 400 atm hydrostatic pressure, and then calcined in Ar at 1050 °C for 15 hours. The crystal growth was carried out in argon in an IR-heated image furnace (NEC) equipped with two halogen lamps and double ellipsoidal mirrors with feed and seed rods rotating in opposite directs at 25 rpm during crystal growth at a rate of 20 mm/h.

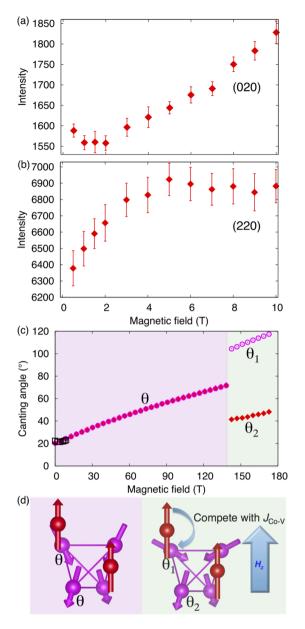


Figure 5. Prediction of novel phases driven by magnetic field in $Mn_{0.2}Co_{0.8}V_2O_4$. Experimental results for the field-dependent (020) (**a**) and (220) (**b**) Bragg peak intensities. (**c**) Field dependence of spin angle θ calculated by spin models using DFT parameters. First-order phase transition from TI/TO to AI/AO-derived state with magnetic field is indicated by the jump in θ . Black open squares are from the neutron scattering measurement up to 10 T. (**d**) One-angle state based on TI/TO (left) and two-angle state based on AI/AO (right). The latter is driven by the competition between J_{Co-V} and magnetic energy.

Neutron-scattering experiments. Single-crystal neutron diffraction was performed to determine the crystal and magnetic structures using the four-circle diffractometer (HB-3A) at the High Flux Isotope Reactor (HFIR) of the Oak Ridge National Laboratory (ORNL). A neutron wavelength of 1.003 Å was used from a bent perfect Si-331 monochromator³¹. High magnetic field single-crystal neutron diffraction experiments were performed on the cold neutron triple-axis spectrometer (CTAX) at HFIR, ORNL. The incident neutron energy was selected as 5.0 meV by a PG (002) monochromator, and the final neutron energy was also set as 5.0 meV by a PG (002) analyzer. The horizontal collimation was guide-open-80'-open. Contamination from higher-order beams was removed using a cooled Be filter. The scattering plane was set in the (H,K,0) plane and the magnetic field was applied perpendicular to the scattering plane. The nuclear and magnetic structures were refined with the program FULLPROF³². We examined more than 18 peaks of lattice and magnetic Bragg peaks to extract the precise nuclear and magnetic structural information as shown in the S2 in the Supplementary material. Due to the domain re-orientation effect, Bragg peak intensities of both (220) and (020) diffractions increase sharply in small magnetic fields, but the (220) diffraction is saturated above about 3 T. The Bragg peak intensity of the (020) diffraction, corresponding to the magnetic component of V in the *ab*-plane, inceases linearly with field.

First-principles calculations. First-principles calculations were performed using density-functional theory within the local spin-density approximation with a correction due to on-site Hubbard interaction (LSDA + *U*) as implemented in the Vienna *ab initio* simulation package (VASP-5.3)³³. We used the Liechtenstein³⁴ implementation with on-site Coulomb interaction U = 6.0 eV and on-site exchange interaction $J_H = 1.0 \text{ eV}$ to treat the localized 3d electron states in Co, Mn, and V; this choice of *U* is close to that chosen in previous work on $\text{CoV}_2\text{O}_4^{-35}$ and $\text{MnV}_2\text{O}_4^{-36,37}$. The spin-orbit interaction was included. The projector augmented wave (PAW) potentials^{38,39} explicitly include 13 valenced electrons for Mn ($3p^63d^54s^2$), 9 for Co ($3d^84s^1$), 13 for V ($3s^23p^63d^44s^1$), and 6 for oxygen ($2s^22p^4$). The wave functions were expanded in a plane-wave basis with an energy cutoff of 500 eV. To evaluate the on-site single-ion anisotropy (SIA) interaction *D*, only one cation of interest was kept while the surrounding magnetic atoms were replaced by neutral and isoelectronic Ca²⁺ and Al³⁺ cations for Co²⁺/Mn²⁺ and V³⁺, respectively. This is the same technique that was successfully used for BiFeO₃⁴⁰ and CaMn₇O₁₂⁴¹.

Microscopic spin model. Spin states in spinels can be described by the following model Hamiltonian,

$$H = -\frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j + \sum_i D_i (\hat{u}_i \cdot \mathbf{S}_i)^2$$
(1)

which contains six inequivalent sublattices. Isotropic exchange constants $J_{\text{Co}-V}$ describe nearest-neighbor interactions between the Co and V sites. $J_{\text{Co}-\text{Co}}$ and J_{V-V} describe nearest-neighbor interactions between Co-sites and V-sites, respectively. The easy-axis anisotropy is assumed to be zero for the Co-sites, while for the B-site spins, the easy-axis anisotropy D_v is along the local <111> direction. The azimuthal directions of each vanadium spin is constrained, but the canting angle θ_i , described in Fig. 4, is allowed to vary between 0 and 2π . Since θ_i may have a unique value in adjacent planes, both the two-in-two-out and all-in-all-out configurations are possible. These angles are equal to the polar angle when θ_i is between 0 and π , while the polar angles equals $2\pi - \theta_i$ and the azimuthal angle changes by π when θ_i is greater than π .

The ground state spin configuration was found by minimizing the classical energy for a given set of parameters. To avoid local minima, this was accomplished by calculating the classical energy on a grid with $\theta_i = 0$ to 2π and finding the two angles with the lowest energy. This process was repeated for values of the external magnetic field ranging from 0 to 173 T.

The inelastic neutron cross section for undamped spin waves was calculated using the 1/S formalism outlined in ref.⁴² and the appendices of ref.⁴³. For direct comparison with experimental intensities, the effects of the magnetic form factor and the instrumental resolution were included in the calculation. The coefficients for Co²⁺, and V³⁺ are from ref.⁴⁴. The resolution function was approximated as a Gaussian in energy with a full width at half-maximum of 1.5 meV. Effects from finite resolution in Q were not considered.

While DFT can provide guidance for the values of the isotropic exchange interactions, LSDA + U overestimates the experimental moment ($M_v = 0.47(4)\mu_B$) of CoV₂O₄ measured by neutron scattering. Our spin model uses the magnetic moment ($M_v = 0.5 \mu_B$), which is within the experimental uncertainty. In addition, parameters calculated with DFT were adjusted to reproduce the measured canting angle of CoV₂O₄ ($\theta = 20.8 \pm 1.7^{\circ}$) in zero field. Care was also taken to avoid a long-range spiral configuration⁴⁵ that was not observed in our neutron diffraction measurements. The final set of parameters used for CoV₂O₄ are $J_{Co-Co} = 0.5 \text{ meV}$, $J_{Co-V} = -2.5 \text{ meV}$, $J_{V-V} = -11.0 \text{ meV}$, $D_V = -2.7 \text{ meV}$, $redM_{Co} = 3.00 \mu_B$ and $redM_V = 0.5 \mu_B$.

Canting angles of the new phase with $D_v = 0.0$. At high pressures, we take $D_v = 0.0$ in Eq.(1). Then, the total energy per unit magnetic unit cell is

$$E(\alpha) = -12J_{Co-V}S_{Co}S_V\alpha - 4J_{V-V}S_V^2\alpha^2 + \text{constant}$$
⁽²⁾

where $\alpha = \cos\theta_1 + \cos\theta_2$. The total energy is at a minimum if

$$\alpha = -\frac{3J_{Co-V}S_{Co}}{2J_{V-V}S_{V}}$$
(3)

which limits the allowed combination of θ_1 and θ_2 . When $\theta_1 = \theta_2$ and $D_{Co} = D_v = 0.0$, this condition is identical to the expression for θ in ref.³⁶.

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Author Contributions

J.H.L. conceived the original idea. J.H.L. and M.S.Y. carried out first-principles calculations. S.E.H. and R.S.F. performed spin-wave simulations. J.M., H.C., T.H., and M.M. measured and analyzed neutron scattering Bragg peaks. H.D.Z. synthesized the samples. J.H.L., S.E.H., J.M., H.B.C., M.L., T.H., H.-J.L., M.S.Y., S.O., M.M., and R.S.F. discussed the results. J.H.L. and R.F. wrote the manuscript.

Additional Information

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