

ARTICLE

Meta-analysis of quantitative pleiotropic traits for next-generation sequencing with multivariate functional linear models

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To analyze next-generation sequencing data, multivariate functional linear models are developed for a meta-analysis of multiple studies to connect genetic variant data to multiple quantitative traits adjusting for covariates. The goal is to take the advantage of both meta-analysis and pleiotropic analysis in order to improve power and to carry out a unified association analysis of multiple studies and multiple traits of complex disorders. Three types of approximate F -distributions based on Pillai–Bartlett trace, Hotelling–Lawley trace, and Wilks’s Lambda are introduced to test for association between multiple quantitative traits and multiple genetic variants. Simulation analysis is performed to evaluate false-positive rates and power of the proposed tests. The proposed methods are applied to analyze lipid traits in eight European cohorts. It is shown that it is more advantageous to perform multivariate analysis than univariate analysis in general, and it is more advantageous to perform meta-analysis of multiple studies instead of analyzing the individual studies separately. The proposed models require individual observations. The value of the current paper can be seen at least for two reasons: (a) the proposed methods can be applied to studies that have individual genotype data; (b) the proposed methods can be used as a criterion for future work that uses summary statistics to build test statistics to meta-analyze the data.

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INTRODUCTION

Meta-analysis of multiple studies and pleiotropy analysis of multiple traits are two areas in association studies that recently have received extensive attention in the literature.^{1–10} To our knowledge, meta-analysis and pleiotropy analysis have been performed separately so far, and there are no gene-based meta-analysis methods for combining multiple studies together and for carrying out a unified pleiotropy analysis. Here, multivariate functional linear models (MFLM) are developed to connect genetic variant data to multiple quantitative traits adjusting for covariates in a meta-analysis context. The goal is to take the advantage of both meta-analysis and pleiotropy analysis in order to improve power and to carry out a unified analysis of multiple studies and multiple quantitative traits of complex disorders.

A noticeable feature of next-generation sequencing data is that dense panels of genetic variants are available via high-throughput sequencing technology, and so we face high-dimension genetic data.^{11–14} The genetic data can consist of rare variants, or common variants, or a combination of the two, where the rare variants’ minor allele frequencies (MAFs) are less than 0.01–0.05. The high dimensionality of genetic data and the presence of dense rare variants raise

huge challenges, and properly dealing with the high dimensionality and rare variants is one priority of statistical research in recent years.¹⁵

In our previous research as well as research from other groups, functional data techniques were used to reduce the dimensionality of genetic data and to build fixed effect functional regression models for association analysis of quantitative, dichotomous, and survival traits.^{10,16–29} In most cases, it was shown that the functional regression test statistics perform better than sequence kernel association test (SKAT), its optimal unified test (SKAT-O), and a combined sum test of rare and common variant effect (SKAT-C) of mixed models.^{4,16–27,30–33} Specifically, mixed model-based SKAT/SKATO/SKAT-C performs well when (a) the number of causal variants is large and (b) each causal variant contributes a small amount to the traits, as the assumption of mixed models is satisfied under these circumstances.^{7,21,34} In most cases, however, fixed models perform better since the causal variants of complex disorders can be common or rare or a combination of the two and some causal variants may have relatively large effects.^{10,16–27} If the number of causal variants is large and each causal variant contributes a small amount to the traits, it would be hard to show association as the power of a test can be

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low.³⁵ One may want to note that SKAT and SKAT-O were shown to have higher power than burden tests, which is another main method to analyze rare variants.^{4,32,36–38} Thus, fixed models can be useful in association studies of complex traits.

As functional regression models perform well in most cases, we are motivated to extend them to meta-analysis of pleiotropy traits. For individual studies, MFLM were built to perform pleiotropy analysis between multiple genetic variants and multiple quantitative traits adjusting for covariates in Wang *et al.*¹⁰ Similarly, functional linear models were developed to perform meta-analysis of a univariate quantitative trait in Fan *et al.*¹⁸ In this paper, we build MFLM to analyze multiple traits of multiple studies and introduce related approximate *F*-distributed test statistics to test for association based on multivariate analysis theory. The proposed methods are applied to analyze lipid traits in eight European cohorts. Simulation analysis is performed to evaluate the false-positive rates and power of the proposed tests.

MATERIALS AND METHODS

Consider a meta-analysis with *L* studies in a genomic region. For the *ℓ*-th study, we assume that there are *n_ℓ* individuals who are sequenced in the region at *m_ℓ* variants. For each individual, we assume there are *J* quantitative trait phenotypes, *J* ≥ 1. In this article, the research goal is to model association between the *m_ℓ* genetic variants and the *J* phenotypic traits by combining all the *L* studies as a whole. We assume that the *m_ℓ* variants are located with ordered physical positions $0 \leq t_{\ell 1} < \dots < t_{\ell m_\ell}$. To make the notation simpler, we normalized the region $[t_{\ell 1}, t_{\ell m_\ell}]$ to be $[0, 1]$. For the *i*-th individual in the *ℓ*-th study, let *y_{ℓ ij}* denote her/his *j*-th quantitative trait (*j* = 1, 2, ..., *J*), *G_{ℓ i}* = (*x_{ℓ i}(t_{ℓ 1})*, ..., *x_{ℓ i}(t_{ℓ m_ℓ)}*)' denote her/his genotypes of the *m_ℓ* variants, and *Z_{ℓ i}* = (*z_{ℓ i1}*, ..., *z_{ℓ ic_ℓ}*)' denote her/his *c_ℓ* covariates. Hereafter, ' denotes the transpose of a vector or matrix. For the genotypes, we assume that *x_{ℓ i}(t_{ℓ k})* (*k* = 0, 1, 2) is the number of minor alleles of individual *i* at the *k*-th variant.

Multivariate functional linear models

We view the *i*-th individual's genotype data as a genetic variant function (GVF) *X_{ℓ i}(t)*, *t* ∈ [0, 1] from the *ℓ*-th study. To relate the GVF to the phenotypic traits adjusting for covariates, we consider the following MFLM for *ℓ* = 1, 2, ..., *L*, *i* = 1, 2, ..., *n_ℓ*,

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \int_0^1 B_{\ell}(t) X_{\ell i}(t) dt + E_{\ell i}. \quad (1)$$

The notations used in the model (1) are defined below

$$Y_{\ell i} = \begin{pmatrix} y_{\ell i1} \\ \vdots \\ y_{\ell iJ} \end{pmatrix}, A_{\ell 0} = \begin{pmatrix} \alpha_{\ell 01} \\ \vdots \\ \alpha_{\ell 0J} \end{pmatrix}, A_{\ell} = \begin{pmatrix} \alpha_{\ell 11} & \dots & \alpha_{\ell c_{\ell 1}} \\ \vdots & \ddots & \vdots \\ \alpha_{\ell 1J} & \dots & \alpha_{\ell c_{\ell J}} \end{pmatrix},$$

$$B_{\ell}(t) = \begin{pmatrix} \beta_{\ell 1}(t) \\ \vdots \\ \beta_{\ell J}(t) \end{pmatrix}, E_{\ell i} = \begin{pmatrix} \varepsilon_{\ell i1} \\ \vdots \\ \varepsilon_{\ell iJ} \end{pmatrix},$$

where *A_{ℓ 0}* is a vector of overall means, *A_ℓ* is a *c_ℓ* × *J* matrix of regression coefficients of covariates, *B_ℓ(t)* is a vector of genetic effect functions *β_{ℓ j}(t)*, and *E_{ℓ i}* is a vector of error terms. For each pair of *ℓ* and *i*, the error vector *E_{ℓ i}* is normally distributed with a mean vector of zeros and a *J* × *J* variance-covariance matrix *Σ*. Moreover, *E_{ℓ 1}*, ..., *E_{ℓ n_ℓ}* are assumed to be independent.

Expansion of Genetic Effect Function. The genetic effect functions *β_{ℓ j}(t)* of *B_ℓ(t)* are assumed to be continuous/smooth functions of the position *t*. One may expand it by B-spline or Fourier basis functions. Formally, let us expand the genetic effect functions *B_ℓ(t)* by a series of *K_β* basis functions *ψ(t)* = (*ψ₁(t)*, ..., *ψ_{K_β}(t)*)' as

$$B_{\ell}(t) = \begin{pmatrix} \beta_{\ell 11} & \dots & \beta_{\ell 1K_{\beta}} \\ \vdots & \ddots & \vdots \\ \beta_{\ell J1} & \dots & \beta_{\ell JK_{\beta}} \end{pmatrix} \psi(t) = \Omega_{\ell} \psi(t), \quad (2)$$

where *Ω_ℓ* is a *J* × *K_β* matrix of coefficients *β_{ℓ jk}*. We consider two types of basis functions: (1) the B-spline basis: *ψ_k(t)* = *B_k(t)*, *k* = 1, ..., *K_β*; and (2) the Fourier basis: *ψ₁(t)* = 1, *ψ_{2r+1}(t)* = sin(2*πr**t*), and *ψ_{2r}(t)* = cos(2*πr**t*), *r* = 1, ..., (*K_β* - 1)/2.^{39–42}

Estimation of GVF. To estimate the GVFs *X_{ℓ i}(t)* from the genotypes *G_{ℓ i}*, we use an ordinary linear square smoother.^{16–20,42,43} Let *φ_k(t)*, *k* = 1, ..., *K*, be a series of *K* basis functions, such as the B-spline basis and Fourier basis functions. Denote *φ(t)* = (*φ₁(t)*, ..., *φ_K(t)*)'. Let *Φ* denote the *m_ℓ* by *K* matrix containing the values *φ_k(t_{ℓ j})*, where *j* = 1, ..., *m_ℓ*. Using the discrete realizations *G_{ℓ i}* = (*x_{ℓ i}(t_{ℓ 1})*, ..., *x_{ℓ i}(t_{ℓ m_ℓ)}*)', we may estimate the GVF *X_{ℓ i}(t)* using an ordinary linear square smoother as follows:⁴²

$$\hat{X}_{\ell i}(t) = \phi(t)' [\Phi' \Phi]^{-1} \Phi' G_{\ell i}. \quad (3)$$

Revised MFLM. Replacing *B_ℓ(t)* by the expansion (2) and *X_{ℓ i}(t)* in the MFLM (1) by *Ŷ_{ℓ i}(t)* in (3), we have a revised multivariate linear regression model

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \Omega_{\ell} \int_0^1 \psi(t) \phi'(t) dt [\Phi' \Phi]^{-1} \Phi' G_{\ell i} + E_{\ell i}$$

$$= A_{\ell 0} + A_{\ell} Z_{\ell i} + \Omega_{\ell} W_{\ell i} + E_{\ell i}, \quad (4)$$

where *W_{ℓ i}* = $\int_0^1 \psi(t) \phi'(t) dt [\Phi' \Phi]^{-1} \Phi' G_{\ell i}$. In the above revised regression model, one needs to calculate $[\Phi' \Phi]^{-1} \Phi'$ and $\int_0^1 \psi(t) \phi'(t) dt$ to get *W_{ℓ i}*. In the statistical computing environment R, there are readily available R packages to calculate them.⁴³

Dealing with missing genotype data. If some genotype data are missing, the estimation (3) can be modified to estimate GVF *Ŷ_{ℓ i}(t)*. For instance, there is no genotype information at the first variant for the *i*-th individual, ie, we only have *G_{ℓ i}* = (*x_{ℓ i}(t_{ℓ 2})*, ..., *x_{ℓ i}(t_{ℓ m_ℓ)}*)'. Let *Φ₁* denote the *m_ℓ* - 1 by *K* matrix containing the values *φ_k(t_{ℓ j})*, where *j* = 2, ..., *m_ℓ*. Then, we may revise the estimation (3) as

$$\hat{X}_{\ell i}(t) = \phi(t) [\Phi_1' \Phi_1]^{-1} \Phi_1' (x_{\ell i}(t_{\ell 2}), \dots, x_{\ell i}(t_{\ell m_{\ell}}))' \quad (5)$$

Note that the estimation (5) only depends on the available genotype data (*x_{ℓ i}(t_{ℓ 2})*, ..., *x_{ℓ i}(t_{ℓ m_ℓ)}*)'. Hence, each individual's GVF is estimated by his/her own data. This is one advantage of functional data analysis, which can be useful in practice. Using the estimation (5), one may revise the model (4) accordingly.

Beta-smooth-only MFLM

Model (1) is a theoretical MFLM.⁴² For analysis of dense genetic data, one may use a simplified MFLM as follows

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \sum_{k=1}^{m_{\ell}} B_{\ell}(t_{\ell k}) x_{\ell i}(t_{\ell k}) + E_{\ell i}, \quad (6)$$

where *B_ℓ(t_{ℓ k})* is a vector of the genetic effects at position *t_{ℓ k}* for the *ℓ*-th study, and the other terms are the same as those in the general MFLM (1).

In model (6), *B_ℓ(t_{ℓ k})* = (*β_{ℓ 1}(t_{ℓ k})*, ..., *β_{ℓ J}(t_{ℓ k})*)' is a vector of the genetic effects at the position *t_{ℓ k}*. We assume that *B_ℓ(t)* is a vector of genetic effect functions *β_{ℓ j}(t)* of the physical position *t*. Therefore, *B_ℓ(t_{ℓ k})*, *k* = 1, 2, ..., *m_ℓ* are the values of vector *B_ℓ(t)* at the *m_ℓ* physical positions. The genetic effect functions *β_{ℓ j}(t)* are assumed to be smooth. One may expand it by B-spline or Fourier basis functions. Replacing *B_ℓ(t_{ℓ k})* by expansion (2), model (6) can be revised as

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \Omega_{\ell} \sum_{k=1}^{m_{\ell}} \psi(t_{\ell k}) x_{\ell i}(t_{\ell k}) + E_{\ell i}$$

$$= A_{\ell 0} + A_{\ell} Z_{\ell i} + \Omega_{\ell} W_{\ell i} + E_{\ell i}, \quad (7)$$

where *W_{ℓ i}* = $\sum_{k=1}^{m_{\ell}} \psi(t_{\ell k}) x_{\ell i}(t_{\ell k})$. In model (6) and its revised version (7), we use the raw genotype data *G_{ℓ i}* = (*x_{ℓ i}(t_{ℓ 1})*, ..., *x_{ℓ i}(t_{ℓ m_ℓ)}*)' directly in the analysis. The genetic effect vector *B_ℓ(t)* is assumed to be smooth or continuous. Hence, the models are called beta-smooth only.

Dealing with Missing Genotype Data. If some genotype data are missing, eg, we only have $G_{\ell i} = (? , x_{\ell i}(t_{\ell 2}), \dots, x_{\ell i}(t_{\ell m_{\ell}}))'$ and $x_{\ell i}(t_{\ell 1}) = ?$ is missing, we may revise the MFLM (6) as

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \sum_{k=2}^{m_{\ell}} B_{\ell}(t_{\ell k}) x_{\ell i}(t_{\ell k}) + E_{\ell i}. \quad (8)$$

Again, the revised MFLM (8) only depends on the available genotype data $(x_{\ell i}(t_{\ell 2}), \dots, x_{\ell i}(t_{\ell m_{\ell}}))$, and it can be revised accordingly to be a form of model (7) by expansion (2) as

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \Omega_{\ell} \sum_{k=2}^{m_{\ell}} \psi(t_{\ell k}) x_{\ell i}(t_{\ell k}) + E_{\ell i}.$$

Traditional additive effect multivariate linear models

Traditionally, an additive effect model can be used to analyze the relation between the trait and the m_{ℓ} variants in the ℓ -study as Jung *et al.*⁴⁴ and Anderson⁴⁵

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \begin{pmatrix} \beta_{\ell 11} & \dots & \beta_{\ell 1m_{\ell}} \\ \vdots & \dots & \vdots \\ \beta_{\ell j1} & \dots & \beta_{\ell jm_{\ell}} \end{pmatrix} G_{\ell i} + E_{\ell i} \\ = A_{\ell 0} + A_{\ell} Z_{\ell i} + \Omega_{\ell} G_{\ell i} + E_{\ell i}, \ell = 1, 2, \dots, L, i = 1, 2, \dots, n_{\ell}, \quad (9)$$

where Ω_{ℓ} is a $J \times m_{\ell}$ matrix of coefficients $\beta_{\ell jk}$, which is the additive genetic effect of variant k for the j -th trait in the ℓ -th study, and the other terms are similar to those in the MFLM (1) and (6). There is only one difference between model (6) and model (9), ie, the genetic effect coefficients $\beta_{\ell jk}$ in model (9) do not depend on the physical position $t_{\ell k}$, whereas $\beta_{\ell j}(t_{\ell k})$ in model (6) depends on the physical position $t_{\ell k}$. The genetic effect coefficients $\beta_{\ell jk}$ in model (9) are discrete, whereas $\beta_{\ell j}(t_{\ell k})$ in model (6) are the values of function $\beta_{\ell j}(t)$ at the physical positions $t_{\ell k}, k = 1, 2, \dots, m_{\ell}$.

Approximate F-distributed test statistics

Consider the revised regression models (4), (7), and the multivariate linear model (9), which model the genetic effect of the J phenotypic traits simultaneously adjusting for covariates by combining the L studies together. First, assume that the genetic effects among the L studies are different/heterogeneous. In the test of association between the m_{ℓ} genetic variants and the J quantitative traits simultaneously, the null hypothesis is $H_0 : \Omega_{\ell} = O_{\ell}, \ell = 1, \dots, L$, where O_{ℓ} is a zero $J \times K_{\beta}$ matrix $O_{J \times K_{\beta}}$ for models (4) and (7) or a zero $J \times m_{\ell}$ matrix $O_{J \times m_{\ell}}$ for model (9). We may test the null H_0 by approximate F -distribution tests based on Pillai-Bartlett trace, Hotelling-Lawley trace, and Wilks's Lambda using standard statistical approaches.^{45,46} The approximate F -distributed test statistic is denoted as heterogeneous F -approximation test statistics (Het-F).

Consider the revised models (4) and (7). If the genetic effects are homogeneous, ie, $\Omega_{\ell} = \begin{pmatrix} \beta_{11} & \dots & \beta_{1K_{\beta}} \\ \vdots & \dots & \vdots \\ \beta_{j1} & \dots & \beta_{jK_{\beta}} \end{pmatrix} = \Omega$, we may test the association

between the genetic variants and the J quantitative traits by testing a simplified null $H_0 : \Omega = O_{J \times K_{\beta}}$. The null H_0 can be tested by approximate F -distribution tests based on Pillai-Bartlett trace, Hotelling-Lawley trace, and Wilks's Lambda using standard statistical approaches. The approximate F -distributed statistic is denoted as Hom-F.

Assume that each individual of the L studies is sequenced at the same variants located at $0 \leq t_1 < \dots < t_m$ and so $m_1 = \dots = m_{\ell} = m$. In addition, assume that the genetic effects are homogenous. Let us denote

$$\Omega = \begin{pmatrix} \beta_{11} & \dots & \beta_{1m} \\ \vdots & \dots & \vdots \\ \beta_{j1} & \dots & \beta_{jm} \end{pmatrix}. \text{ Then, the model (9) is simplified as}$$

$$Y_{\ell i} = A_{\ell 0} + A_{\ell} Z_{\ell i} + \Omega G_{\ell i} + E_{\ell i}, \ell = 1, 2, \dots, L, i = 1, 2, \dots, n_{\ell}. \quad (10)$$

The null hypothesis of no association between the genetic variants and the quantitative traits is $H_0 : \Omega = O_{J \times m}$. The corresponding approximate F -distributed test statistic is denoted as Hom-F.

If there is only one study, ie, $L = 1$, the approximate F -distribution tests are equivalent to those of Wang *et al.*¹⁰ and Het-F is the same as Hom-F. If we only have one quantitative trait, ie, $J = 1$, the three approximate F -distribution tests based on Pillai-Bartlett trace, Hotelling-Lawley trace, and Wilks's Lambda are equivalent to the F -test statistics of the standard multiple linear regression. The models proposed in this article and the related approximate F -distribution tests extend the models and the F -test statistics in Fan *et al.*¹⁸

In practice, we find that the results of the three approximate F -distribution tests based on Pillai-Bartlett trace, Hotelling-Lawley trace, and Wilks's Lambda are similar to each other.¹⁰ In this article, we only report the results of approximate F -distribution tests based on Pillai-Bartlett trace.

Parameters of Functional Data Analysis

In the data analysis and simulations, we used two functions from the *fda R* package to create the basis:

```
Basis = create.bspline.basis(norder = order, nbasis = bbasis)
basis = create.fourier.basis(c(0,1), nbasis = fbasis)
```

The three parameters were taken as *order* = 4, *bbasis* = 15, *fbasis* = 25 in all data analysis and simulations. To make sure that the results are valid and stable, we tried a wide range of parameters: (1) $10 \leq K = K_{\beta} \leq 23$ for the heterogeneous genetic effect model and (2) $10 \leq K = K_{\beta} \leq 29$ for the homogeneous genetic effect model. The results are similar to each other.

RESULTS

A simulation study

To evaluate the performance of the proposed MFLM, we carried out simulation analyses for two cases: (1) the variants are all rare; (2) some variants are rare and some are common. Simulations were performed for three scenarios listed in Table 4 in Supplementary Materials.^{4,18} For scenarios 1 and 2, we used the European-like (EUR) sequence data used in Lee *et al.*³² For scenario 3, we used both the EUR and African-American-like (AA) sequence data. Specifically, the EUR sequence data were generated using COSI's calibrated best-fit models, and the generated European haplotypes mimic CEPH Utah individuals with ancestry from northern and western Europe in terms of site frequency spectrum and linkage disequilibrium (LD) pattern (Figure 4 in Schaffner *et al.*^{47,48}). Similarly, the AA sequence data mimic individuals with 20:80 mixture of Europeans and Africans, together with parameters calibrated to model realistic demographic history (including bottleneck, population expansion, and migration events). The EUR sequence data included 10 000 chromosomes covering 1 Mb regions, and the AA sequence data included 45 000 chromosomes covering 0.1 Mb regions. Genetic regions of 3 kb length were randomly selected in the simulations for type I error and power calculations.

Type I error simulations. To evaluate the type I error rates of the proposed MFLM and related tests, we generated phenotype data sets by using the model

$$Y_{\ell i} = A_{\ell} Z_{\ell i} + E_{\ell i}. \quad (11)$$

Three scenarios of covariates are given in Supplementary Table S1, in which three covariates are considered: z_1 is a dichotomous covariate taking values 0 and 1 with a probability of 0.5, z_2 and z_3 are continuous covariates from a standard normal distribution $N(0,1)$. The vector of error terms $E_{\ell i}$ in model (11) follows a normal distribution with a mean vector of 0 and a 3×3 variance-covariance matrix

$$\Sigma = \begin{pmatrix} 1.00 & 0.60 & -0.35 \\ 0.60 & 1.00 & -0.45 \\ -0.35 & -0.45 & 1.00 \end{pmatrix}$$

The 3×3 variance-covariance matrix Σ is taken from an empirical analysis of the three traits of the Trinity Students Study from Wang

*et al.*¹⁰ For scenario 1 in Supplementary Table S1, the covariate regression coefficients are given by

$$A_1 = \begin{pmatrix} 0.5 & 0.5 \\ 0.4 & 0.6 \\ 0.3 & 0.7 \end{pmatrix}, A_2 = \begin{pmatrix} 0.4 & 0.4 \\ 0.3 & 0.7 \\ 0.2 & 0.8 \end{pmatrix}, A_3 = \begin{pmatrix} 0.6 & 0.6 \\ 0.5 & 0.5 \\ 0.4 & 0.4 \end{pmatrix}.$$

For scenarios 2 and 3 in Supplementary Table S1, the covariate regression coefficients are given by

$$A_1 = \begin{pmatrix} 0.5 \\ 0.4 \\ 0.3 \end{pmatrix}, A_2 = \begin{pmatrix} 0.5 & 0.5 \\ 0.4 & 0.6 \\ 0.3 & 0.7 \end{pmatrix}, A_3 = \begin{pmatrix} 0.6 & 0.6 & 0.6 \\ 0.5 & 0.5 & 0.5 \\ 0.4 & 0.4 & 0.4 \end{pmatrix}.$$

To obtain genotype data, 3 kb subregions were randomly selected in the 1 Mb region of EUR-like data and the 0.1 Mb region of AA-like data. The ordered genotypes were these SNPs in the 3 kb subregions. Note that the trait values are not related to the genotypes, and so the null hypothesis holds. The sample sizes were 1600 (study 1), 2200 (study 2), and 3200 (study 3). The simulation settings are summarized in Supplementary Table S1. For each sample size combination, 1.2×10^6 phenotype-genotype data sets were generated to fit the

proposed models and to calculate the test statistics and related *P*-values. Then, an empirical type I error rate was calculated as the proportion of 1.2×10^6 *P*-values that were smaller than a given α level (ie, 0.05, 0.01, 0.001, and 0.0001, respectively).

Empirical power simulations. To evaluate the power of the proposed MFLM and related tests, we simulated data sets under the alternative hypothesis by randomly selecting 3 kb subregions to obtain causal variants for the phenotype values as follows. Once a 3 kb subregion was selected, a subset of p_ℓ causal variants located in the 3 kb subregion for the ℓ -th study was then randomly selected to obtain ordered genotypes $G_{\ell i} = (g_{\ell i}(t_{\ell 1}), \dots, g_{\ell i}(t_{\ell p_\ell}))'$. Then, we generated the quantitative traits by

$$Y_{\ell i} = A_\ell Z_{\ell i} + \begin{pmatrix} \beta_{\ell 11} & \dots & \beta_{\ell 1 p_\ell} \\ \beta_{\ell 21} & \dots & \beta_{\ell 2 p_\ell} \\ \beta_{\ell 31} & \dots & \beta_{\ell 3 p_\ell} \end{pmatrix} G_{\ell i} + E_{\ell i}, \ell = 1, 2, \dots, L, i = 1, 2, \dots, n_\ell,$$

where A_ℓ and $E_{\ell i}$ are the same as in the type I error model (11), and

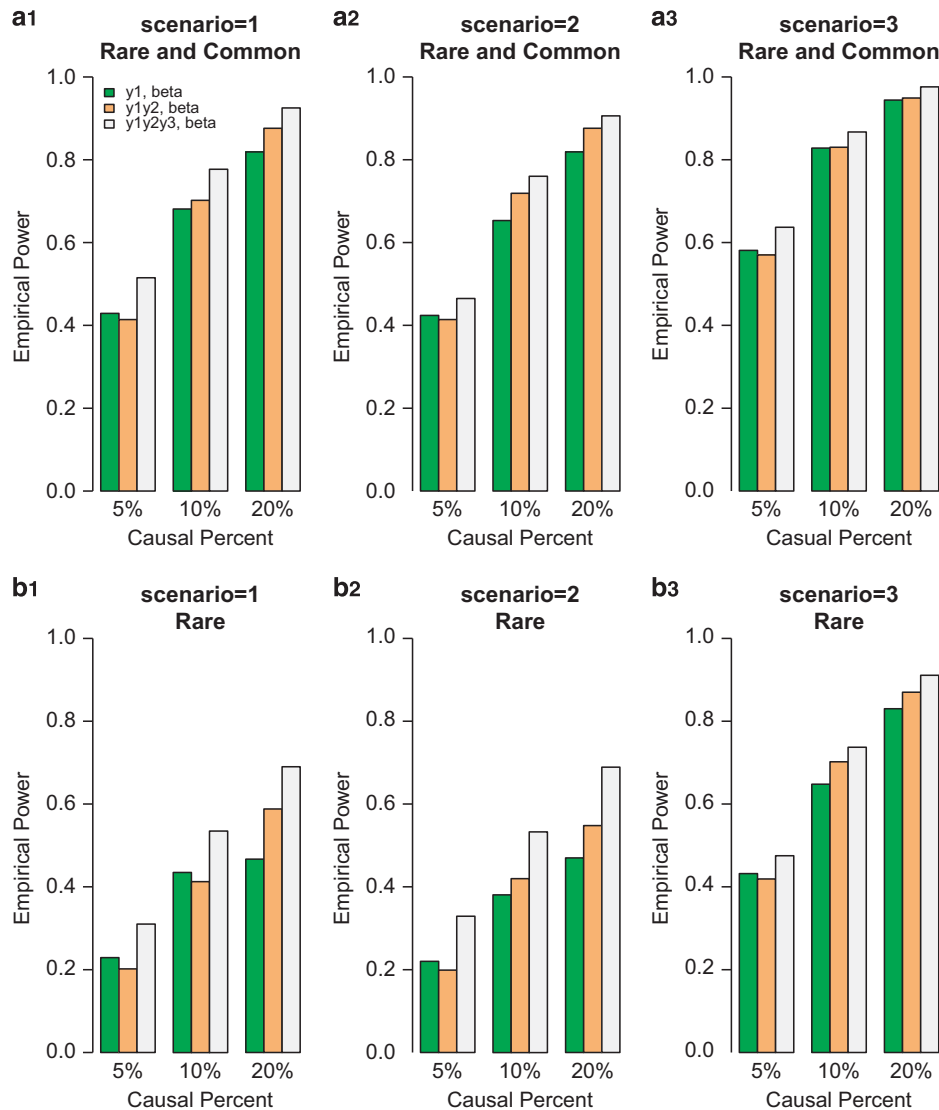


Figure 1 The empirical power of homogeneous approximate *F*-distributed Statistics (Hom-*F*) of the model (7) at $\alpha = 0.0001$, when the genetic effects were simulated as homogeneous. For each trait, 20%/80% causal variants had negative/positive effects.

the β_s are additive effect for the causal variants defined as follows. We used $|\beta_{\ell jk}| = c_{\ell j} |\log_{10}(\text{MAF}_k)|$, where MAF_k was the MAF of the k -th variant. Three genetic effect scenarios were used to perform power calculations: (1) all causal variants had positive effects; (2) 20%/80% causal variants had negative/positive effects; (3) 50%/50% causal variants had negative/positive effects. As in Fan *et al.*¹⁸ and Lee *et al.*,⁴ three different settings were considered: 5, 10, and 20% of variants in the 3 kb subregion are chosen as causal variants. When 5, 10, and 20% of the variants were causal, two parameter settings of genetic effects were considered for $c_{\ell} = (c_{\ell 1}, c_{\ell 2}, c_{\ell 3})$: (1) homogeneous and (2) heterogeneous (Supplementary Table S2). In the homogeneous case, the genetic effects are the same for the three studies, ie, $c_1 = c_2 = c_3$. In the heterogeneous case, the genetic effects are different for the three studies, ie, $c_2 = c_1 + (0.15, 0.15, 0.15)$, $c_3 = c_1 - (0.15, 0.15, 0.15)$. For each setting, 1000 data sets were simulated to calculate empirical power as the proportion of P -values, which are smaller than an $\alpha = 0.0001$ level.

Type I error simulation results. The empirical type I error rates are reported in Supplementary Table S3 when the variants are only rare

and in Supplementary Table S4 when some variants are rare and some are common. For each entry of empirical type I error rates, we generated 1.2×10^6 data sets. Results of four different $\alpha = 0.05, 0.01, 0.001$, and 0.0001 levels were reported. For the proposed approximate F -distributed test statistics of MFLM (4) and (7) and additive model (9), all empirical type I error rates are around the nominal α levels for both B-spline basis and Fourier basis (columns 5–9 of Supplementary Tables S.3 and S.4). Therefore, the approximate F -distributed test statistics of MFLM controlled type I error rates correctly for all scenarios at all significance levels. The MFLM and related approximate F -distributed test statistics can be useful in both whole-genome and whole-exome association studies.

Power results. We compared the power of F -test of univariate and the approximate F -distributed tests of bivariate and trivariate traits based on the simulated COSI sequence data. The empirical power levels of the test statistics at $\alpha = 0.0001$ level were plotted in Figures 1 and 2. In the figures, 20%/80% causal variants had negative/positive effects for each trait. In the legend of all the Figures, ‘beta’ means that the power level is from beta-smooth only model (7), and ‘add’ means that the

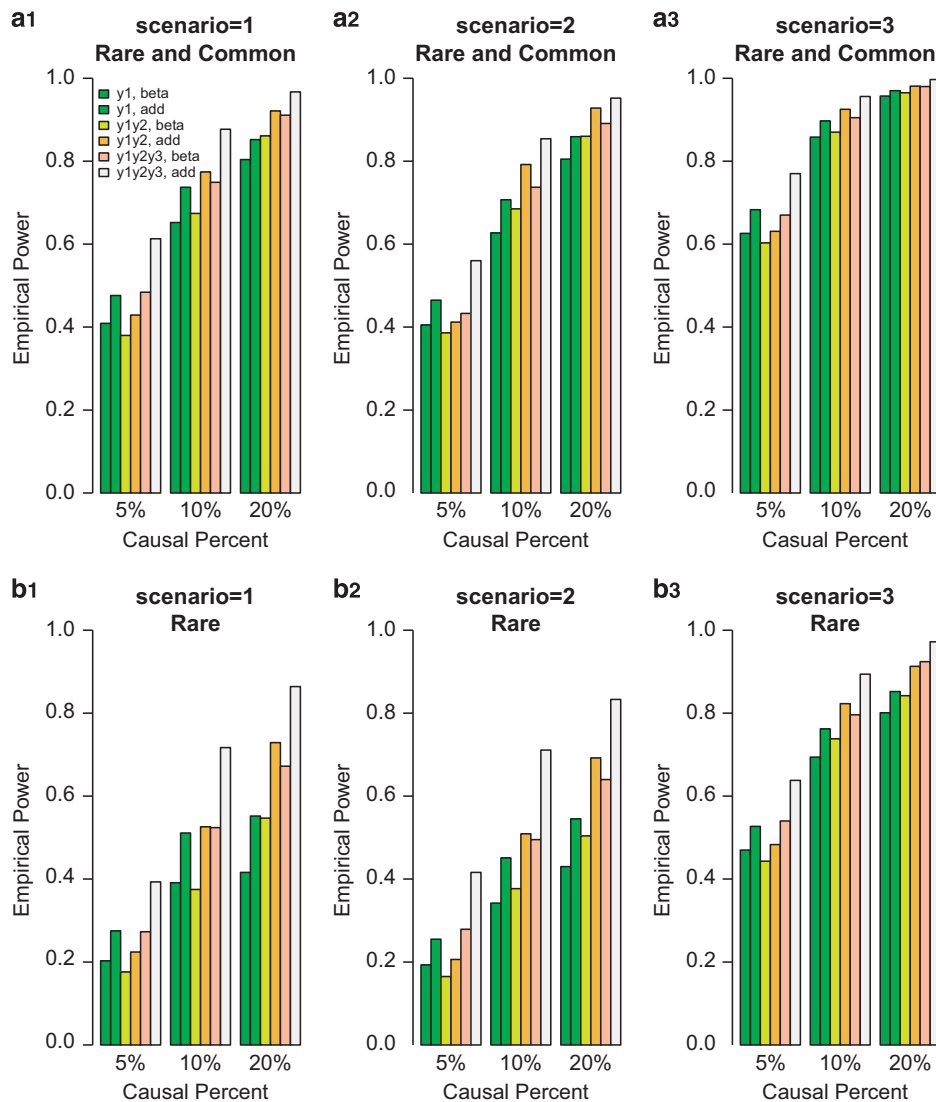


Figure 2 The empirical power of Het-F of the models (7) and (9) at $\alpha = 0.0001$, when the genetic effects were simulated as heterogeneous. For each trait, 20%/80% causal variants had negative/positive effects.

power level is from additive model (9). In Figure 1, the results of 'Hom-F' were reported when the approximate *F*-distributed statistics were constructed using the homogeneous effect model (7) when the data were generated using the homogeneous models (Supplementary Table S2). Since the genotype data are different from study to study, there are no power levels for homogeneous additive model (10) in Figure 1. In Figure 2, the results of 'Het-F' were reported that the approximate *F*-distributed statistics were constructed using heterogeneous effect models (7) and (9) when the data were generated using the heterogeneous models (Supplementary Table S2). Therefore, 'correct models' were used to analyze simulated data in Figures 1 and 2.

In general, the power levels of *F*-test of the univariate y_1 trait are the lowest, the power levels of approximate *F*-distributed tests of the bivariate (y_1, y_2) trait are in the middle, and the power levels of approximate *F*-distributed tests of the trivariate (y_1, y_2, y_3) trait are the highest for either beta-smooth only model (7) or additive model (9) in Figures 1 and 2. Therefore, it makes sense to perform multivariate analysis of pleiotropy traits.

Meta-analysis of lipid traits in eight European cohorts

Lipid traits from eight European cohorts were analyzed: five from Finland (FUSION Stage 2, D2d-2007, DPS, METSIM, and DRs EXTRA), two from Norway (HUNT and Tromso), and one from Germany (DIAGEN). The two Norwegian cohorts are combined into one study for these analyses. The genotype data were generated using

the MetaboChip, which was designed to fine map regions that have been associated with metabolic traits.⁴⁹ For each cohort, 54 741 genetic variants were genotyped.

For our analysis, we utilized the existing literature as a reference for gene selection and found that 22 gene regions were fine mapped.⁵ We used Builder Mar. 2006 (NCBI36/hg18) to determine gene positions and 5 kb was used to extend the gene region on each side of a gene. The summary of 22 genes and the number of genetic variants in each region are given in Supplementary Table S5, Supplementary Materials. Four lipid traits were analyzed: high-density lipoprotein levels, low-density lipoprotein (LDL) levels, triglycerides (TG), and total cholesterol (CHOL). The sample sizes for each trait are provided in Supplementary Table S6, Supplementary Materials. For each trait, inverse normal rank transformation was performed to make sure that normality holds. For all studies except for METSIM, age, sex, and type 2 diabetes status were used as covariates. For METSIM, age and type 2 diabetes status were used as covariates since no females were included in the study. A significance threshold of $P < 3.1 \times 10^{-6}$ was taken from Liu et al.⁵ (corresponding to 0.05/16 153 and allowing for the number of genes tested therein).

Using homogeneous *F*-approximation test statistics (Hom-F) based on Pillai-Bartlett trace, Table 1 reports results of three-trait and four-trait meta-analysis of lipid traits in European studies. For each combination of three to four traits, we observed association at five genes of *APOB*, *APOE*, *LDLR*, *LPL*, and *PCSK9*. For each of the five genes, we observed association for some of the traits in one-trait meta-

Table 1 Three-trait and four-trait meta-analysis of lipid traits in European studies using Hom-F based on Pillai-Bartlett trace

Traits	Gene	P-values of the Hom-F			
		Basis of Both GVF and $\beta\ell(t)$		Basis of beta-smooth only	
		B-spline basis	Fourier basis	B-spline basis	Fourier basis
LDL, TG, CHOL	<i>APOB</i>	1.29×10^{-10}	1.73×10^{-5}	9.16×10^{-10}	2.21×10^{-6}
	<i>APOE</i>	1.82×10^{-88}	5.22×10^{-90}	9.03×10^{-89}	1.31×10^{-90}
	<i>LDLR</i>	3.14×10^{-11}	2.25×10^{-9}	3.51×10^{-9}	8.49×10^{-8}
	<i>LPL</i>	1.74×10^{-7}	2.33×10^{-8}	8.71×10^{-8}	1.01×10^{-8}
	<i>PCSK9</i>	7.55×10^{-6}	4.00×10^{-7}	0.000196	2.16×10^{-6}
HDL, LDL, TG	<i>APOB</i>	6.47×10^{-10}	6.32×10^{-6}	4.89×10^{-10}	1.15×10^{-6}
	<i>APOE</i>	6.22×10^{-95}	3.11×10^{-97}	4.77×10^{-95}	2.03×10^{-96}
	<i>LDLR</i>	1.03×10^{-11}	2.16×10^{-10}	1.34×10^{-10}	4.51×10^{-9}
	<i>LPL</i>	6.31×10^{-7}	2.98×10^{-7}	3.64×10^{-7}	1.69×10^{-6}
	<i>PCSK9</i>	1.46×10^{-7}	3.62×10^{-8}	4.54×10^{-5}	1.08×10^{-6}
HDL, LDL, CHOL	<i>APOB</i>	1.01×10^{-9}	1.67×10^{-5}	5.61×10^{-10}	2.23×10^{-6}
	<i>APOE</i>	1.62×10^{-82}	1.25×10^{-83}	5.03×10^{-81}	5.94×10^{-83}
	<i>LDLR</i>	1.33×10^{-10}	6.82×10^{-10}	3.07×10^{-9}	2.24×10^{-8}
	<i>LPL</i>	2.32×10^{-7}	8.76×10^{-8}	2.24×10^{-7}	1.33×10^{-7}
	<i>PCSK9</i>	1.18×10^{-6}	3.25×10^{-8}	7.88×10^{-5}	1.57×10^{-7}
HDL, TG, CHOL	<i>APOB</i>	1.11×10^{-10}	2.93×10^{-6}	1.66×10^{-10}	4.11×10^{-7}
	<i>APOE</i>	4.59×10^{-88}	1.10×10^{-88}	2.10×10^{-87}	1.06×10^{-86}
	<i>LDLR</i>	4.67×10^{-12}	1.48×10^{-10}	7.33×10^{-11}	3.23×10^{-9}
	<i>LPL</i>	1.86×10^{-9}	6.25×10^{-11}	1.47×10^{-9}	2.33×10^{-10}
	<i>PCSK9</i>	7.62×10^{-8}	1.47×10^{-8}	1.13×10^{-5}	1.35×10^{-7}
HDL, LDL, TG, CHOL	<i>APOB</i>	2.23×10^{-10}	1.60×10^{-6}	1.67×10^{-10}	1.24×10^{-7}
	<i>APOE</i>	4.76×10^{-93}	1.64×10^{-94}	7.29×10^{-94}	8.08×10^{-94}
	<i>LDLR</i>	3.17×10^{-11}	6.89×10^{-11}	1.13×10^{-9}	5.15×10^{-9}
	<i>LPL</i>	7.41×10^{-8}	8.79×10^{-9}	7.14×10^{-8}	2.20×10^{-9}
	<i>PCSK9</i>	1.41×10^{-7}	1.51×10^{-7}	8.07×10^{-5}	4.49×10^{-7}

Abbreviations: GVF, genetic variant function; Hom-F, homogeneous *F*-approximation test statistics.

The associations that attain a threshold significance of $P < 3.1 \times 10^{-6}$ are highlighted in bold.⁵ The results of 'Basis of Both GVF and $\beta\ell(t)$ ' were based on smoothing both GVF and genetic effect functions $\beta\ell(t)$ of model (4), and the results of 'Basis of beta-smooth only' were based on smoothing $\beta\ell(t)$ only approach of model (7).

analysis by homogeneous models (Table 1 of Fan *et al.*¹⁸ presented in Supplementary Table S7 in the Supplementary Materials). The results of two-trait meta-analysis of the lipid traits are presented in Supplementary Table S8, and association is observed for each of the five genes for some of the two-trait combinations.

Using Het-F based on Pillai-Bartlett trace, Tables 2 and 3 report results of three-trait meta-analysis of the lipid traits, and results of four-trait meta-analysis of Het-F are presented in Table 4. By Het-F of MFLM (4) and (7), we observe associations for some three-trait and four-trait combinations at *APOB*, *APOE*, *CDC123*, *CDKAL1*, *CDKN2B*, *FTO*, *HMGA2*, *HNF1A*, *JAZF1*, *IDE*, *KCNQ1*, *KIF11*, *LDLR*, *LPL*, *OASL*, *PCSK9*, and *TSPAN8*. The results of two-trait meta-analysis of lipid traits are presented in Supplementary Tables S9 and S10 and association is observed for some genes and some of the two-trait combinations. Three traits (LDL, TG, and CHOL) are associated with some genes in one-trait meta-analysis by heterogeneous models (Table 2 of Fan *et al.*¹⁸ presented in Supplementary Table S11 in the Supplementary Materials). The additive effect model (9) detects some association signals, but less than the MFLM (4) and (7).

In study-based pleiotropy analysis of Wang *et al.*,¹⁰ which analyzes each data set separately, association was observed at only two genes, *APOE* and *LDLR*, in some studies (Supplementary Table S12 in the Supplementary Materials from Table 1 of Wang *et al.*¹⁰). Thus, it is more advantageous to perform meta-analysis of multiple studies.

DISCUSSION

Here we develop MFLM for meta-analysis of multiple quantitative traits adjusting for covariates. On the basis of the MFLM, approximate

F-distributed statistics of Pillai-Bartlett trace, Hotelling-Lawley trace, and Wilks's Lambda are introduced to test for association between multiple quantitative traits and multiple genetic variants. Simulation analysis is performed to show that the approximate *F*-distributed tests control the false-positive rates accurately. By evaluating power performance, it is shown that it can be advantageous to perform the proposed pleiotropy analysis instead of individual trait analysis.^{1–10,27,44} Among other merits, the MFLM can handle missing genotype data naturally.

The proposed methods were used to analyze four lipid traits in eight European cohorts. When we use the homogeneous MFLM to analyze three traits and four traits together, association is observed at five genes of *APOB*, *APOE*, *LDLR*, *LPL*, and *PCSK9*. For each of the five genes, we only observed association for some traits in one-trait meta-analysis and two-trait meta-analyses (Table 1 of Fan *et al.*¹⁸ presented in Supplementary Table S7 and Supplementary Table S8 in the Supplementary Materials). Similarly, the proposed heterogeneous MFLM detected more and stronger association signals by three-trait or four-trait analysis than one-trait or two-trait analysis.

One special feature of MFLM is that functional data analysis techniques are used to reduce the dimensionality of the next-generation sequencing data.^{39–43} The key idea is that multiple genetic variants of an individual is treated as a realization of an underlying stochastic process.⁵⁰ Therefore, the genome of an individual is viewed as a continuous stochastic function that contains both genetic position and LD information of the genetic markers. In real data analysis, one may test whether the genetic effects are heterogeneous or homogeneous, ie, to test $H_0: \Omega_1 = \dots = \Omega_L = \Omega$. If the H_0 is rejected, the genetic effects are heterogeneous; otherwise, they are homogeneous.

Table 2 Three-trait meta-analysis of lipid traits in European studies using Het-F based on Pillai-Bartlett trace

Traits	Gene	P-values of the Het-F				
		Basis of Both GVF and $\beta\ell(t)$		Basis of beta-smooth only		Additive model (9)
		B-spline basis	Fourier basis	B-spline basis	Fourier basis	
LDL, TG, CHOL	<i>APOB</i>	1.20 × 10⁻¹⁰	2.01 × 10⁻⁸	3.92 × 10 ⁻⁶	1.39 × 10⁻⁶	2.06 × 10⁻⁷
	<i>APOE</i>	3.80 × 10⁻⁶⁹	8.84 × 10⁻⁶⁸	1.07 × 10⁻⁶³	2.62 × 10⁻⁶⁵	2.79 × 10⁻⁶⁴
	<i>CDKL1</i>	3.77 × 10 ⁻⁶	2.97 × 10⁻⁷	5.90 × 10 ⁻⁶	3.03 × 10⁻⁷	0.001498
	<i>FTO</i>	1.15 × 10⁻⁶	0.000219	0.000242	0.001061	0.001042
	<i>HNF1A</i>	1.69 × 10⁻¹⁰	1.73 × 10⁻⁷	4.00 × 10⁻⁷	3.79 × 10⁻⁸	2.02 × 10⁻⁸
	<i>LPL</i>	5.98 × 10⁻⁷	2.86 × 10⁻⁶	1.11 × 10⁻⁶	2.48 × 10⁻⁸	0.000581
	<i>OSAL</i>	1.37 × 10⁻⁶	6.14 × 10 ⁻⁵	3.08 × 10 ⁻⁵	0.000824	0.000993
	<i>TSPAN8</i>	3.31 × 10⁻⁸	5.38 × 10⁻⁹	2.30 × 10⁻⁸	2.80 × 10⁻⁹	3.06 × 10⁻⁸
	<i>PCSK9</i>	2.28 × 10⁻⁸	8.68 × 10⁻¹⁰	2.49 × 10⁻¹⁰	1.63 × 10⁻¹⁰	5.87 × 10⁻¹¹
	HDL, LDL, TG	<i>APOB</i>	7.90 × 10⁻¹³	2.40 × 10⁻¹⁰	4.29 × 10⁻⁸	7.68 × 10⁻⁹
<i>APOE</i>		5.25 × 10⁻⁷⁷	1.01 × 10⁻⁷⁵	1.97 × 10⁻⁷¹	1.16 × 10⁻⁷³	2.83 × 10⁻⁷²
<i>CDC123</i>		1.14 × 10 ⁻⁵	1.55 × 10 ⁻⁵	8.07 × 10 ⁻⁶	1.98 × 10⁻⁶	0.018755
<i>CDKL1</i>		1.37 × 10⁻⁸	4.18 × 10⁻⁹	4.90 × 10⁻⁹	3.34 × 10⁻¹⁰	2.72 × 10 ⁻⁵
<i>CDKN2B</i>		6.12 × 10⁻⁷	1.95 × 10⁻⁶	1.64 × 10⁻⁶	1.51 × 10⁻⁶	3.72 × 10 ⁻⁶
<i>FTO</i>		4.38 × 10⁻⁸	3.80 × 10 ⁻⁶	5.76 × 10 ⁻⁶	3.88 × 10 ⁻⁵	5.65 × 10 ⁻⁵
<i>HNF1A</i>		1.48 × 10⁻¹⁰	1.04 × 10⁻⁸	4.48 × 10⁻⁹	1.55 × 10⁻⁹	1.16 × 10⁻⁹
<i>JAZF1</i>		1.58 × 10⁻⁶	2.31 × 10⁻⁶	2.80 × 10⁻⁶	9.99 × 10 ⁻⁶	0.003786
<i>KIF11</i>		1.74 × 10⁻⁶	0.000153	1.31 × 10 ⁻⁵	6.83 × 10 ⁻⁶	0.000198
<i>LPL</i>		2.29 × 10⁻⁷	4.09 × 10⁻⁷	2.36 × 10⁻⁷	6.03 × 10⁻⁹	3.59 × 10 ⁻⁵
<i>OSAL</i>		1.38 × 10⁻⁹	7.99 × 10⁻⁸	4.01 × 10⁻⁸	1.20 × 10⁻⁶	6.20 × 10 ⁻⁶
<i>TSPAN8</i>		1.95 × 10⁻¹¹	1.28 × 10⁻¹²	9.49 × 10⁻¹²	6.69 × 10⁻¹³	1.43 × 10⁻¹¹
<i>PCSK9</i>		4.08 × 10⁻¹⁰	3.75 × 10⁻¹²	6.47 × 10⁻¹¹	6.24 × 10⁻¹¹	2.50 × 10⁻¹¹

Abbreviations: GVF, genetic variant function; Het-F, heterogeneous *F*-approximation test statistics. The associations that attain a threshold significance of $P < 3.1 \times 10^{-6}$ are highlighted in bold.⁵ The results of 'Basis of Both GVF and $\beta\ell(t)$ ' were based on smoothing both GVF and genetic effect functions $\beta\ell(t)$ of model (4), the results of 'Basis of beta-Smooth Only' were based on smoothing $\beta\ell(t)$ only approach of model (7), and the results of 'Additive Model (9)' were based on the additive effect model (9).

Table 3 Three-trait meta-analysis of lipid traits in European studies using Het-F based on Pillai-Bartlett trace

Traits	Gene	P-values of the Het-F					
		Basis of both GVF and $\beta\ell(t)$		Basis of beta-smooth only		Additive model (9)	
		B-spline basis	Fourier basis	B-spline basis	Fourier basis		
HDL, LDL, CHOL	<i>APOB</i>	4.23 × 10⁻¹¹	6.12 × 10⁻⁸	4.50 × 10 ⁻⁶	1.11 × 10⁻⁶	7.75 × 10⁻⁹	
	<i>APOE</i>	4.59 × 10⁻⁶⁶	3.96 × 10⁻⁶⁵	1.44 × 10⁻⁶⁰	7.92 × 10⁻⁶³	4.98 × 10⁻⁶²	
	<i>CDKL1</i>	7.85 × 10⁻⁷	2.07 × 10⁻⁸	6.30 × 10⁻⁸	5.77 × 10⁻⁹	0.000183	
	<i>FTO</i>	2.89 × 10⁻⁷	4.84 × 10 ⁻⁵	0.000331	0.000907	0.001266	
	<i>HNF1A</i>	1.91 × 10⁻¹⁰	7.11 × 10⁻⁸	7.35 × 10⁻⁸	1.07 × 10⁻⁸	3.20 × 10⁻⁸	
	<i>JAZF1</i>	2.89 × 10⁻⁶	1.02 × 10 ⁻⁵	4.42 × 10 ⁻⁶	2.91 × 10 ⁻⁶	0.053595	
	<i>LDLR</i>	5.87 × 10⁻⁷	2.07 × 10⁻⁷	8.56 × 10⁻⁸	2.87 × 10⁻⁸	6.70 × 10⁻⁸	
	<i>LPL</i>	4.56 × 10⁻⁷	2.99 × 10⁻⁷	1.71 × 10 ⁻⁵	5.70 × 10 ⁻⁶	0.017553	
	<i>OSAL</i>	2.81 × 10⁻⁹	6.62 × 10⁻⁷	8.13 × 10⁻⁷	3.67 × 10 ⁻⁵	0.000276	
	<i>TSPAN8</i>	5.79 × 10⁻¹²	1.20 × 10⁻¹³	8.15 × 10⁻¹³	6.81 × 10⁻¹⁴	1.36 × 10⁻¹²	
	<i>PCSK9</i>	5.23 × 10⁻¹⁰	1.64 × 10⁻¹¹	4.65 × 10⁻¹¹	8.36 × 10⁻¹¹	3.58 × 10⁻¹⁰	
	HDL, TG, CHOL	<i>APOB</i>	3.25 × 10⁻¹³	7.35 × 10⁻¹²	5.16 × 10⁻⁹	2.84 × 10⁻¹⁰	1.80 × 10⁻⁷
		<i>APOE</i>	1.64 × 10⁻⁶⁹	8.22 × 10⁻⁶⁸	1.21 × 10⁻⁶⁶	9.28 × 10⁻⁶⁷	1.28 × 10⁻⁶⁵
<i>CDKL1</i>		7.17 × 10⁻⁸	1.18 × 10⁻⁸	4.47 × 10⁻⁸	2.38 × 10⁻⁹	2.55 × 10 ⁻⁵	
<i>FTO</i>		2.86 × 10⁻⁸	6.38 × 10⁻⁷	2.41 × 10⁻⁶	2.03 × 10 ⁻⁵	2.91 × 10 ⁻⁵	
<i>HNF1A</i>		7.17 × 10⁻⁹	4.60 × 10⁻⁷	9.22 × 10⁻⁸	2.14 × 10⁻⁸	2.38 × 10⁻⁸	
<i>KIF11</i>		2.68 × 10⁻⁶	9.95 × 10 ⁻⁵	2.74 × 10 ⁻⁵	1.35 × 10 ⁻⁵	0.001113	
<i>LPL</i>		5.18 × 10⁻⁸	9.15 × 10⁻⁸	2.73 × 10⁻⁷	1.13 × 10 ⁻⁹	1.50 × 10 ⁻⁵	
<i>OSAL</i>		9.59 × 10⁻⁸	4.81 × 10⁻⁷	1.17 × 10⁻⁷	1.20 × 10⁻⁶	4.65 × 10 ⁻⁶	
<i>TSPAN8</i>		3.34 × 10⁻⁹	1.15 × 10⁻¹⁰	4.38 × 10⁻¹⁰	4.82 × 10⁻¹¹	7.09 × 10⁻¹⁰	
<i>PCSK9</i>		8.29 × 10⁻¹¹	2.89 × 10⁻¹¹	2.95 × 10⁻¹⁰	4.21 × 10⁻¹⁰	1.59 × 10⁻¹¹	

Abbreviations: GVF, genetic variant function; Het-F, heterogeneous *F*-approximation test statistics. The associations that attain a threshold significance of $P < 3.1 \times 10^{-6}$ are highlighted in bold.⁵ The results of 'basis of both GVF and $\beta\ell(t)$ ' were based on smoothing both GVF and genetic effect functions $\beta\ell(t)$ of model (4), the results of 'basis of beta-smooth only' were based on smoothing $\beta\ell(t)$ only approach of model (7), and the results of 'additive model (9)' were based on the additive effect model (9).

Table 4 Four-trait meta-analysis of lipid traits in European studies using Het-F based on Pillai-Bartlett trace

Traits	Gene	P-values of the Het-F				
		Basis of both GVF and $\beta\ell(t)$		Basis of beta-smooth only		Additive model (9)
		B-spline basis	Fourier basis	B-spline basis	Fourier basis	
HDL, LDL, TG, CHOL	<i>APOB</i>	7.23 × 10⁻¹³	1.66 × 10⁻¹¹	7.62 × 10⁻⁸	3.28 × 10⁻⁹	5.26 × 10⁻¹⁵
	<i>APOE</i>	7.45 × 10⁻⁷⁴	3.26 × 10⁻⁷²	4.64 × 10⁻⁶⁷	1.61 × 10⁻⁶⁹	3.18 × 10⁻⁶⁸
	<i>CDC123</i>	4.12 × 10 ⁻⁵	0.000519	5.53 × 10⁻⁷	3.87 × 10⁻⁷	0.016618
	<i>CDKAL1</i>	2.37 × 10⁻⁸	2.66 × 10⁻⁹	5.03 × 10⁻⁹	8.06 × 10⁻¹⁰	0.000182
	<i>FTO</i>	1.73 × 10⁻⁹	2.29 × 10⁻⁶	2.77 × 10⁻⁶	2.88 × 10 ⁻⁵	3.83 × 10 ⁻⁶
	<i>HMGA2</i>	1.92 × 10 ⁻⁵	4.07 × 10 ⁻⁵	6.97 × 10 ⁻⁶	1.34 × 10⁻⁶	2.99 × 10⁻⁸
	<i>HNF1A</i>	4.40 × 10⁻¹⁴	9.32 × 10⁻¹⁰	2.99 × 10⁻¹⁰	5.91 × 10⁻¹²	2.05 × 10⁻¹⁰
	<i>IDE</i>	7.57 × 10 ⁻⁶	1.92 × 10⁻⁶	5.52 × 10⁻⁷	2.29 × 10⁻⁶	0.057381
	<i>KCNQ1</i>	8.64 × 10⁻⁷	2.16 × 10⁻⁷	0.000121	4.23 × 10 ⁻⁵	1.85 × 10 ⁻⁵
	<i>KIF11</i>	4.54 × 10⁻⁷	3.00 × 10 ⁻⁵	4.33 × 10 ⁻⁶	2.50 × 10⁻⁶	0.000326
	<i>LDLR</i>	6.34 × 10⁻⁷	7.06 × 10⁻⁷	3.60 × 10⁻⁷	2.02 × 10⁻⁷	3.96 × 10⁻⁷
	<i>LPL</i>	3.62 × 10⁻⁹	3.71 × 10⁻⁸	9.08 × 10⁻⁹	2.48 × 10⁻¹¹	1.11 × 10 ⁻⁵
	<i>OASL</i>	1.11 × 10 ⁻¹⁰	1.64 × 10⁻⁸	3.87 × 10⁻⁹	1.88 × 10⁻⁷	6.23 × 10⁻⁷
	<i>PCSK9</i>	7.64 × 10⁻¹⁰	3.82 × 10⁻¹¹	2.57 × 10⁻¹¹	1.37 × 10⁻¹⁰	5.53 × 10⁻¹⁰
	<i>TSPAN8</i>	8.05 × 10⁻¹³	9.58 × 10⁻¹⁵	2.03 × 10⁻¹³	6.01 × 10⁻¹⁵	3.48 × 10⁻¹³

Abbreviations: GVF, genetic variant function; Het-F, heterogeneous *F*-approximation test statistics. The associations that attain a threshold significance of $P < 3.1 \times 10^{-6}$ are highlighted in bold.⁵ The results of 'basis of Both GVF and $\beta\ell(t)$ ' were based on smoothing both GVF and genetic effect functions $\beta\ell(t)$ of model (4), the results of 'basis of beta-smooth only' were based on smoothing $\beta\ell(t)$ only approach of model (7), and the results of 'additive model (9)' were based on the additive effect model (9).

In linkage analysis, it is well known that the genetic data are treated as functions of the recombination fraction^{51,52} to order genes along a chromosome.⁵³ Thus, it is reasonable and desirable to treat genetic data as functions. In linkage analysis, one needs to estimate the recombination fractions based on pedigree data. In next-generation sequencing

data, the physical positions in terms of base pairs are available in almost all studies and one does not need to estimate them. However, in association studies, the genetic data are usually treated as discrete and the physical positions are simply ignored in most literature except in recent functional regression models.^{10,16-29} Our functional

regression models provide a way to properly utilize the physical positions in gene-based association studies.

In genetic meta-analysis, summary statistics from different studies are usually used to meta-analyze the data as individual data are not always available.^{5,54} In our case, the European cohorts individual genetic data are available for analysis. Therefore, we build our MFLM using the individual-level data. If only summary statistics of functional regression models are available from different studies, it is still an open question if those statistics can be used to meta-analyze the data. It is known that meta-analysis using individual data are advantageous over meta-analysis of summary statistics in non-genetics studies.^{55–57} It would be interesting to evaluate the pros and cons of two approaches in genetic association analysis in the future studies. Note that the functional regressions are simply ordinary regressions after revising the theoretical functional models by functional data analysis techniques, and so the strategy of usual meta-analysis would be useful.⁵⁴ It should be possible to use results from functional regression models for a meta-analysis across cohorts. However, the details are still waiting for further work.

CONFLICT OF INTEREST

The authors declare no conflict of interest.

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COMPUTER PROGRAM

The methods proposed in this paper are implemented by using procedures of the R functional data analysis (fda) package. The R codes for data analysis and simulations are available from the web site: <http://www.nichd.nih.gov/about/org/diphrr/bbb/software/fan/Pages/default.aspx>.

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