and Rowe¹ give a list of seven formulæ which by no means exhausts the logical possibilities. In view of certain erroneous statements which have been made as to the nature and meaning of this coefficient, and of certain fallacious inferences drawn from its use, it is thought desirable to offer the following comments, based upon a preliminary examination of the problem from the biological point of view, in the hope that workers with the necessary statistical and mathematical equipment might be persuaded to give some attention to the development of this device which, it is thought, could be of considerable value in taxonomic practice.

with the necessary statistical and mathematical equipment might be persuaded to give some attention to the development of this device which, it is thought, could be of considerable value in taxonomic practice. The following points in connexion with this coefficient seem to have been overlooked : (1) It is an index expressing one mean value (root mean square deviation) as a percentage of another mean value. Accordingly, the values normally calculated may be regarded as being possibly not true values since no correction is ever made for correlation effects, and notably no correction is made for the effect of spurious correlation which arises where an index is calculated from mean values, as shown by Pearson²; nor is correction ever made for the correlation which generally exists between a mean and its standard deviation. (2) The numerator of the index is a quantity determined by many factors according to which it can be partitioned. The CV is custom-arily calculated only from such values of the standard deviation as may be to hand : at best these are sample values and it cannot be held that they accurately represent the variability of the particular group to which they refer. Accordingly, it is likely to be erroneous to compare the CV's of two groups, unless the conditions of sampling, that is to say, the sources of variance, are identical. Even when sampling conditions are similar, such comparison of CV's can be regarded as evidence of relative variability of the groups only in tespect of the particular measurements to which they refer. Com-parison on other measurements may reverse the relative positions. (3) The correlation between a mean (of a particular measurement in a particular species the CV may or may not vary with sex, age, locality, season or other factor. Again, the coefficients of different measurements in the one species may or may not vary with sex, age, locality, season or other factor. Again, the coefficients of different measurements in the one species may or may not vary with sex,

of a particular measurement made on different species, or genera. I have compiled tables of means, standard deviations and CV's, and ind it generally demonstrable that the characteristic value of the CVfor any measurement in any group cannot be predicted, but must be separately determined. This does not deny that the behaviour of this coefficient might be according to some discernible law, particularly if some alteration were made in the manner of its calculation. How-ever, this is a question of the relationship between two variables (the mean and the variance) under various conditions, and such relationship cannot be analysed by means of an index. Finally, as a matter of immediate practical importance, it is fallacious to attempt to set any general limits to the value of the CV or to draw any particular conclusions from departures from such limits. (4) Since so many factors may contribute to the size of the variance, and since the manner of that contribution cannot be predicted, it is impossible to argue to the sample from the value of the CV. But de-partures in subsequent samples, from the value of the CV established for a particular specification of sampling, might serve to indicate that the conditions of sampling had been departed from, or that certain changes in the population had occurred. However, despite these limitations to the CV it is desirable to have some measure of relative variability, and it is thought that with some modification, and with care in the specification of the conditions of use, the CV can serve this purpose. In the first place a CV should be cited, as a taxonomic feature, only where the material from which it was obtained can be precisely specified. Secondly, since the object is to permit comparisons, it would be desirable to effect some choice of conditions of sampling which can be generally reproduced ; thus it might be wise to specify the CV for the sexes separately, to specify a single locality (say, the type locality) and only a few age groups. Thirdly, it

While the CV in its present form is of very limited value it probably could be made a most useful adjunct to the usual set of statistical measures quoted in taxonomic works.

G. L. KESTEVEN Fisheries Section, Marine Biological Laboratory, Cronulla, New South Wales. Sept. 3.

¹Simpson and Rowe, "Quantitative Zoology" (McGraw-Hill, 1937). ⁴Pearson, K., Proc. Mag. Soc., **60**, 489 (1897).

A General Class of Confidence Interval

AMONG types of statistical inference about unknown parameters statements are possible which have a statistical truth, that is, they are random variables such that within the statistical framework adopted the probability of their being in error is known. In these statements intervals, called by Neyman confidence intervals, are assigned to the value of an unknown parameter. On generalization to more than one unknown parameter these intervals become multi-dimensional regions ; but I have pointed out¹ that the existence of

URE 521 such regions does not of itself imply in Neyman's theory the correspondence. The very the logical statement concerning the simultaneous boundary of several parameters includes a statement about the maxi-mem boundary of any selected set of these parameters, and con-sequently if the total statement is ure with probability 1 – e, the louded statement is true with probability not less than 1 – e. When the selected set confidence interval for one parameter that includes all previously known 'exact solutions' with probability 1 – e, the oblight of the selected set consists of only one parameter, this fact gives is to a general class of confidence interval for one parameter that and so new solutions with probability not less than 1 – e. When the selected set consists of only one parameter, they are the selected set consists of only one parameter, they are the selected set consists of only one parameter, they are the selected set consists of only one parameter, they are the selected set consists of only one parameter that and so new solutions with probability not less than 1 – e. When the selected set consists of only one parameter that and the selected set consists of only one parameter that and the selected set consists of only one parameter that and the selected set consistent the selected set consistent the solutions of the above sense, he seems to throw out a challenge to critics of the ord they for which the Behrens-Fisher test does not constitute a solution fits the above sense. In addition to solutions of the confidence interval type previously noted, this two-parameter distribution implies a possible solution of the new type suggested above, for which the Selected set properties are open to investiga. The added September 23. Since this letter was written. Dr. B. I. Mometrika, in which he puts forward a new solution of the confidence interval type for the 'difference between two means' problem. His sonad approximation, and promise, much more should have been we ob-the added set onterval tone terma so

Queens' College, Cambridge. Aug. 21.

Ann. Math. Stat., 10, 129 (1939). Sankhya, 7, 129 (1945). Proc. Camb. Phil. Soc., 32, 560 (1936).

Random Associations on a Lattice

GIVEN a lattice of m \times n points, suppose that each may be 'black' or 'white' with probabilities p and q = 1 - p. The probability distribution of the number of 'black-white' joins is then of interest in several branches of science^{1,1,3}. The expected number is 2pq(2mn-m-n) and the second moment about the mean is $2pq(8mn-7m-7n+4) + 4p^2q^2 (13m+13n-14mn-8)$. As m and n increase, the distribution tends to normality, and this may be proved by methods similar to those used by Bernstein⁴ in his work on Markov chains. Similar results can be obtained for the number of 'black-black' joins and also the corresponding results in three dimensions. Levene⁴ has announced results dealing with a different but similar problem. A full account will appear later. Institute of Statistics.

Institute of Statistics.

University of Oxford

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Experiment and Theory in Statistics

Experiment and Theory in Statistics Mr. D. V. LINDLEY⁴ distinguishes between the curve of best fit has the regression curve on the ground that the former gives the best estimate of the relation between the true values of the variables, while the latter gives the best estimate of the true values of one variable from the observed value of the other. He thus provides a convenient opportunity to raise a question that I have long wanted to raise, andly, whether there is any experimental evidence for this and similar deductions from statistical theory. There experimental tests are not easily devised ; for the meaning from the theory on which they are based. But the first statement seems capable of test. The true values must surely be independent of the method of examining them. Accordingly, if many different sets of observations are made on a system by many different ways, the curves of best fit from the different sets, rightly calculated, should agree significantly better than curves. List his true? Mor are the tests easy to apply. A single worker seldom accumulates the observational material to apply the test : he cannot use the observations of others, because sufficient details are scarcely ever published. The application of the tests requires organised co-operation. Until it is undertaken and the tests proved to be successful, all use of elaborate statistical theory is precined. NORMAN B. CAMPBELL Sept. 2.

Sept. 2.

1 Nature, 158, 273 (1946).